Creating A Vector Map

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Aim:

In this project we want to calculate global co ordinates of any point in some given screen shots(ss) with respect to a global origin. The user will be given the ss and he can choose any point in those screenshots whose global co ordinate he is interested in.

Methodology:

I have described the whole method in another pdf named "Description of Code". There I have written how we did the project along with how the user should use the code.

Description of data:

This part is also mostly explained in the other pdf I have attached. I have also attached another excel file named "Guide Map" which contains some landmarks with co-ordinates (details of which can be found in the second pdf) and also the 9 ss from which the user can pick any location of his interest and save it by an appropriate name. The screenshots are taken from google maps at the same zoom level.

Model:

We will ask the user to take at least 2 attempts when they mark any point in any ss.

Let x_{ijk} be the x co-ordinate of the j^{th} landmark of SS "i" at k^{th} trial. α_i is the negative of the distance of ss "i" from the global origin (G) along x axis.(i is from 1 to I)

 β_j is the distance of j^{th} landmark from G along x axis.(j is from 1 to J) ϵ_{ijk} is the random error while taking the measurement of j^{th} landmark in ss "i" at k-th trial.

Now we can write the linear model as follows:

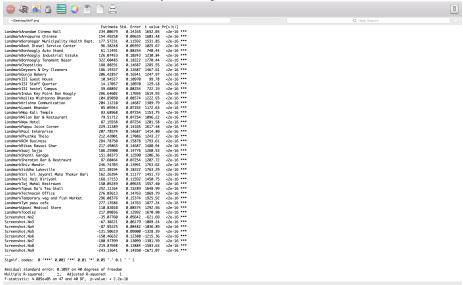
$$x_{ijk} = \alpha_i + \beta_j + \epsilon_{ijk}$$

We have information on x_{ijk} . We need to estimate β_j and α_i for all j=1 to J and i=1 to I given $\alpha_1 = 0$ since we have taken our global origin same as the origin of first ss. **Hence rank of our data matrix is (I+J-1)**. The process is exactly the same for estimating the global y co-ordinates. Since screenshots and locations have no connection between them we expect no interaction term to be present. An important thing to note here is that any two ss must have at least one area in common. Otherwise it is impossible to carry on this estimation.

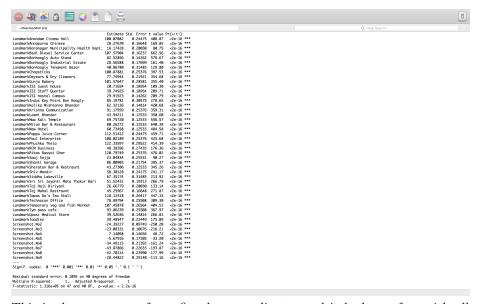
Fitting model to our pre-specified data without any user input:

In the other PDF I have explained the process. In a nutshell we will be providing to the user a data with some landmarks. These landmarks will ensure that all the 9 ss are connected and hence the user is advised to use them. So we will now fit our model on these landmarks already specified in the data. We expect our fit to be a "very" good fit here with no outliers in our residuals. Then only we can say that when there is some discrepancy in output the user had made some mistake in selecting or naming the landmarks and it is not due to our pre specified data.

First we check the summary of our plots.



This is the summary of our fitted x co-ordinates and it looks perfect with all the ss and landmarks significant and adjusted r square is 1.



This is the summary of our fitted y co-ordinates and it looks perfect with all the ss and landmarks significant and adjusted r square is 1.

Now we can check the ANOVA table.

Analysis of Variance Table

```
Response: x.coordinate
              Df Sum Sq Mean Sq F value
                                             Pr(>F)
              39 233353 5983.4 497229 < 2.2e-16 ***
Landmark
                                  445717 < 2.2e-16 ***
                 42908
Screenshot.No 8
                          5363.6
Residuals
              40
                             0.0
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
This is the ANOVA table for x co-ordinates.It looks perfect till now.
Analysis of Variance Table
Response: y.coordinate
```

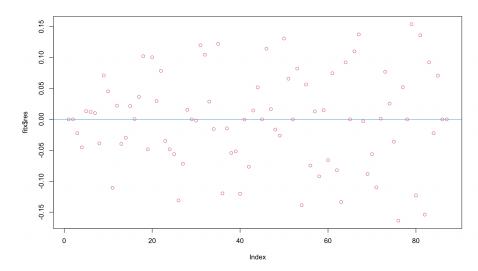
Df Sum Sq Mean Sq F value Pr(>F)
Landmark 39 213886 5484.3 152652 < 2.2e-16 ***
Screenshot.No 8 8382 1047.8 29164 < 2.2e-16 ***
Residuals 40 1 0.0

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

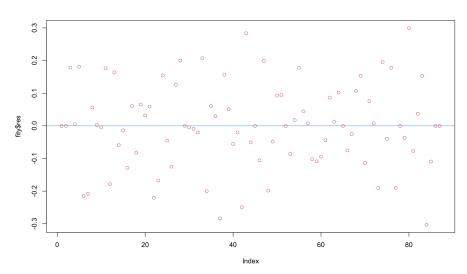
This is the ANOVA table for y co-ordinates. It looks perfect till now.

Residual Analysis:

We first check our residual plots of the fit.



This is the residual plot of our x co-ordinates which looks quite good.

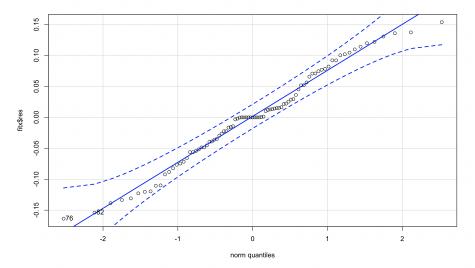


This is the residual plot of our y co-ordinates which also looks quite good. Now from the plot it seems there is no outliers in our residuals. Also there is no pattern in residuals which is also desired. Still we can try out a method to see if there are any outliers in our residuals.

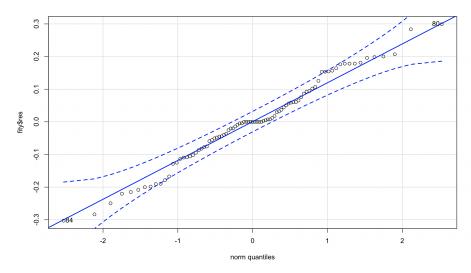
The method is as follows:

- \bullet Define Q1 as the 1^{st} quartile of our data and Q3 as 3^{rd} quartile of our data.
- Define Inter Quartile Range (IQR) as Q3-Q1
- We can call a point outlier if it lies out of the interval [Q1-1.5*IQR,Q3+1.5*IQR].

Using this method we found out that the residuals for both the fits (x and y co ordinates) there are no points outside this interval and hence we can say there are no outliers. Finally we can perform a QQ plot.



This is the qq plot for the residuals of the fit of ${\bf x}$ co-ordinates. This is quite a nice fit.



This is the qq plot for the residuals of the fit of y co-ordinates. This is also a very good fit.

We also found out a list of places which are probably influential. Some of the places connect two ss and hence is influential since if we drop them the entire map gets disconnected. So as long as the residual plots are fine we need not worry about the influential points.

<pre>[1] "ISI hostel Campus"</pre>	"Bonhoogly Auto Stand"
[3] "Laxmi Bhandar"	"Sheraton Bar & Restraunt"
<pre>[5] "Milan Bar & Restaurant"</pre>	"Bedi Diesel Service Center"
[7] "New Hotel"	"Bonhoogly Industrial Estate"
[9] "Taj Mahal Restraunt"	"Annapurna Chinese"
[11] "Upasi Medical Store"	"Taj Haji Biriyani"
[13] "Deyears & Dry Cleaners"	"foodiez"
[15] "Sri Sri Jayanti Mata Thakur Bo	ari" "Shiv Mandir"
[17] "Tym pass cafe"	"Pappu Juice Corner"
[19] "Technocon Office"	"RCM Business"
[1] "ISI hostel Campus"	"Bonhoogly Auto Stand"
[3] "Laxmi Bhandar"	"Sheraton Bar & Restraunt"
[5] "Milan Bar & Restaurant"	"Maa Kali Temple"
[7] "New Hotel"	"Bedi Diesel Service Center"
[9] "Kalika Mishtanno Bhandar"	"Bonhoogly Industrial Estate"
[11] "Taj Mahal Restraunt"	"Annapurna Chinese"
[13] "Taj Haji Biriyani"	"Baranagar Municipality Health Dept."
[15] "foodiez"	"Deyears & Dry Cleaners"
[17] "Pappu Juice Corner"	"Paul Enterprise"
[19] "Shiv Mandir"	"Anandam Cinema Hall"
[21] "Tapas Da's Tea Stall"	"Technocon Office"
[23] "RCM Business"	

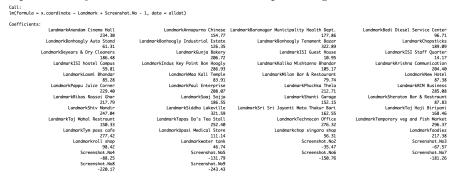
The first one is a list of the influential points found while doing the fit for x-co

ordinate and the second one is for y co-ordinate.

We also calculated the correlation between fitted and residual values for each of the estimate of x and y co-ordinates. They came out to be $7.825654*10^{-18}$ and $4.192693*10^{-17}$ respectively. So finally we can say that the residuals follow iid normal with mean 0 and are homoscedastic. This implies that our model fits perfectly for the pre-specified data. Hence we can safely say that if the user finds there is any error in estimating any of the landmarks that he chose in the ss then it is due to his mistake while choosing some landmarks. We can also give a super set of the probable mistakes that he made. All our data is stored in the alldat [] variable. So once we find out the serial number of the datas whose residuals are outliers we can check out those from our alldat [] matrix. We will do this for the residuals of both the fits for x as well as the y co-ordinate. Even if we find that estimate of only one co ordinate of a particular location has an outlier residual we will include it in our probable mistakes list. We will illustrate this in the following example.

Fitting the model when the user has given input for landmarks:

Now we know that our given data is perfect. So we will now take some user inputs and try to fit the model to our user input and given data.

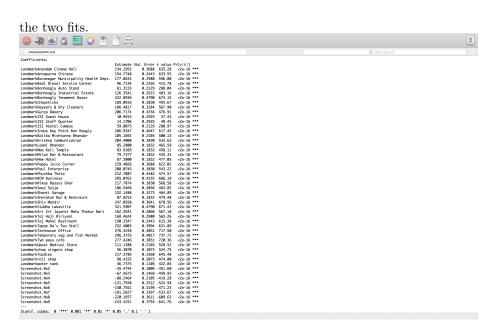


These are our estimates of global x co-ordinate.

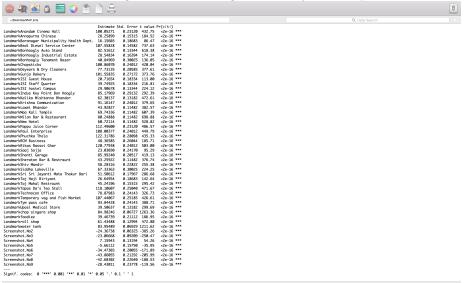
```
Cofficients:

LandmarkAnnadam Cinema Itali
La
```

These are our estimates of global y co-ordinate. We can check the summary of



This is a summary of the fitted x co ordinates. As we can see all the screenshots and landmarks are significant which is good. The adjusted r squared is 1.



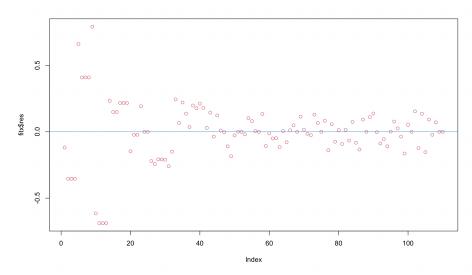
This is a summary of the fitted y co ordinates. As we can see all the screenshots and landmarks are significant which is good. The adjusted r squared is 1.

Analysis of Variance Table

```
Response: x.coordinate
              Df Sum Sq Mean Sq F value
                                             Pr(>F)
              42 258430
                                    71941 < 2.2e-16 ***
Landmark
                         6153.1
                                    71365 < 2.2e-16 ***
Screenshot.No
               8
                   48831
                          6103.9
Residuals
              60
                       5
                             0.1
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
This is the anova table for x co-ordinates which is perfect.
Response: y.coordinate
              Df Sum Sq Mean Sq F value
                                             Pr(>F)
Landmark
              42 317335
                          7555.6
                                  224788 < 2.2e-16 ***
               8
                          1390.3
                                   41362 < 2.2e-16 ***
Screenshot.No
                  11122
Residuals
              60
                       2
                             0.0
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

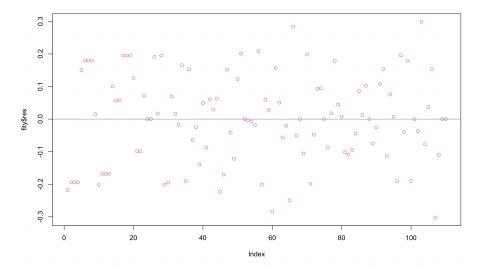
This is the anova table for y co-ordinates which is perfect.

Residual Analysis:



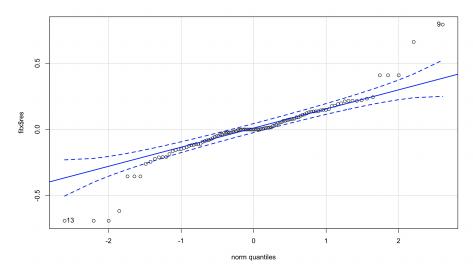
This is plot of residuals of the fitted global x co-ordinates. It seems there are some outliers unlike the last time. We checked if any of these residuals lie before 1.5*IQR of Q1 or after 1.5*IQR of Q3. We found out that all entries numbered 5,6,7,8,9,10,11,12,13 does. We checked out from alldat[] file and found out that these numbers correspond to a landmark that the user has selected in addition to

our pre existing data i.e. those in "Guide Map" namely "chop singara shop". So the user is advised to take verify the location of "chop singara shop" once again.

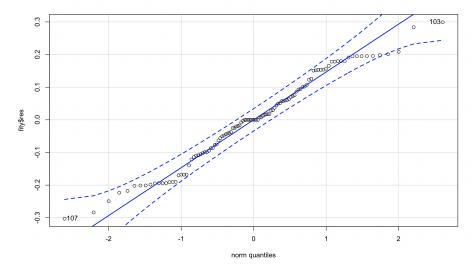


Now this is the residual plot of the estimated global y co-ordinates. This looks better. We do our IQR test and find out that there are no as such outliers in fit residuals of y co-ordinates. So our probable mistakes list here contains only "chop singara shop".

Now we do a QQ plot of our residuals.



This is a QQ plot of the x co-ordinates. For the bulk of data it looks ok but there are some deviations which is indicating some problem with user input.



This is a QQ plot of the y co-ordinates. This looks better and there are lesser deviations.

We also calculated the correlation among the fitted and residual values for both the estimates of x and y co-ordinates. The former came out to be as low as $2.562009*10^{-17}$ and the latter was $3.926711*10^{-17}$.

Success and Limitations of the project:

The limitations of the project are we considered only same zoom level and no rotation. If we include zoom level then good amount of care must be taken to estimate the errors as in those case errors may not be homoscedastic or even maybe correlated if we include rotation also .Except that the project went fine. We did include some roads also in the map which is shown in the other pdf. We have also allowed the user to click on multiple points on the map to know the names of the place. From the residual analysis we can see the fits are quite good unless the user messes up really bad. We also provided an extra data with landmarks and co ordinate i.e "Guide Map" which will always make the map connected no matter what location the user chooses so that should make it more user friendly. We have also converted the name that user gives to a landmark of his choice to lower case alphabets so that next time even if by mistake he uses any capital letters at a different place this will not cause any trouble. At the same time there is one more limitation that if he by mistake misspells any location the code will take it as a new entry. It would have been nice if we could have generated a warning message in that case.