Homework assignment 2-1

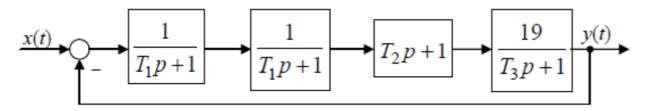
Rauf Yagfarov Variant #6

$$T_1$$
 = 3.75 sec

$$T_2$$
 = 1.5 sec

$$T_3$$
 = 0.15 sec

1) Static control system



$$W(p) = \frac{28.5 p + 19}{(0.15 p + 1) (3.75 p + 1)^2}$$

$$\Phi(p) = \frac{13.5111 \ p + 9.00741}{p^3 + 7.2 \ p^2 + 17.1378 \ p + 9.48148}$$

Maclaurin series:

$$0.95 - 0.292125 p - 0.19339 p^2 + 0.47119 p^3 - 0.67401 p^4 + O(p^5)$$

$$C_0 = 0.95$$

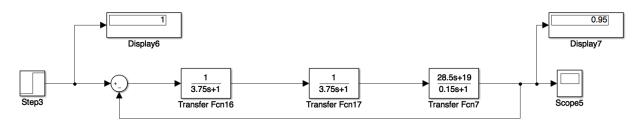
$$C_1$$
= -0.292125

$$C_2$$
= -0.19339

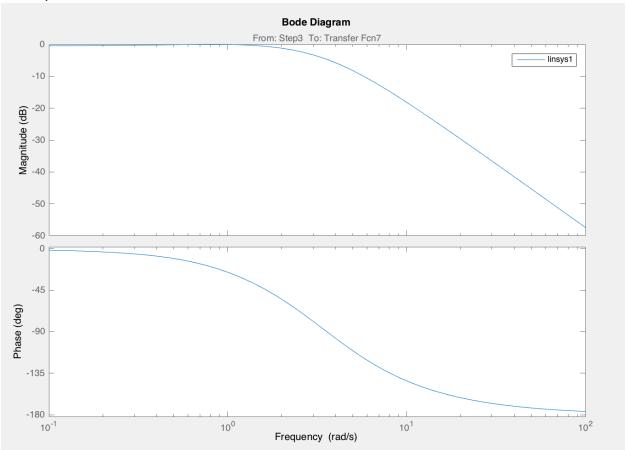
$$C_3$$
= 0.47119

$$C_4$$
= -0.67401

1.a) g(t) = 1(t)



Bode plot :

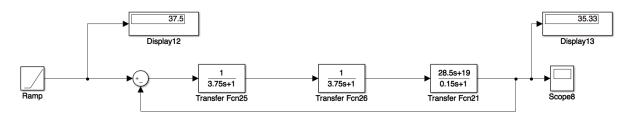


measured result:

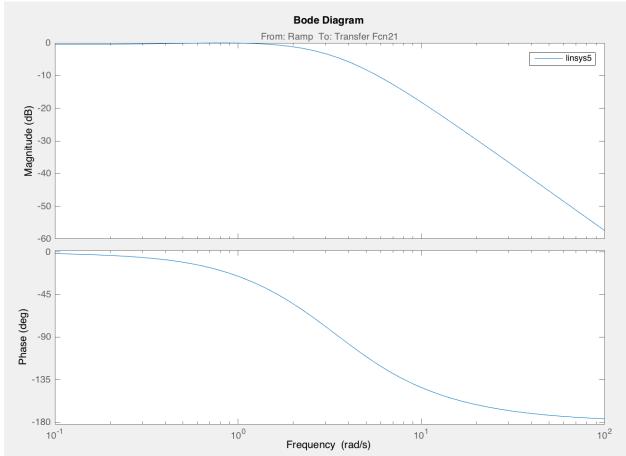
$$\epsilon$$
 = 1 - 0.95 = 0.05

$$\varepsilon = 1 - C_0 g(t) = 1 - 0.95 * 1 = 0.05$$

1.b) g(t) = t1(t)



Bode plot:

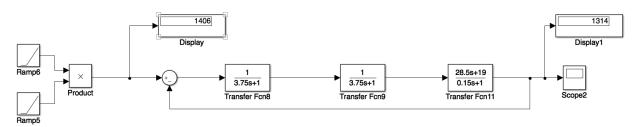


measured result:

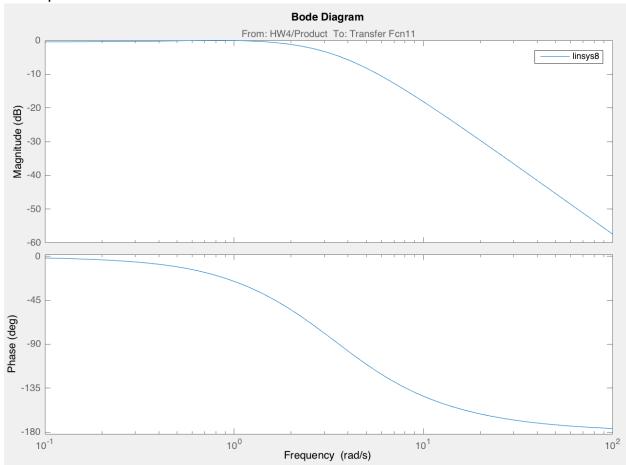
$$\varepsilon = 37.5 - 35.33 = 2.17$$

$$\epsilon$$
 =37.5-C₀ g(t)-C₁ g`(t) = 37.5 - 0.95*37.5 + 0.292125 = 2,167125

1.c) $g(t) = t^2 1(t)$



Bode plot :

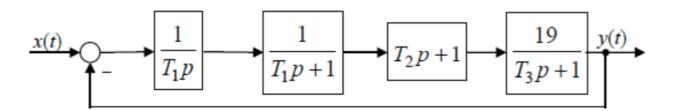


measured result:

$$\varepsilon = 1406 - 1314 = 92$$

$$\epsilon$$
 =1406 -C_0 g(t)-C_1 g`(t)-C_2 g``(t)/2 = 1406 - 0.95*1406 + 0.292125*75 + 0.19339*2/2 = 92,402765

2) Astatic of 1st order control system



W(p)=
$$\frac{19 (3 p + 1)}{(0.3 p + 1) (7.5 p + 1)^2 \left(\frac{19 (3 p + 1)}{(0.3 p + 1) (7.5 p + 1)^2} + 1\right)}$$

$$\Phi(p) = \frac{3.37778 p + 1.12593}{p^3 + 3.6 p^2 + 4.28444 p + 1.18519}$$

Maclaurin series:

$$1. - 0.197368 p - 0.43473 p^2 + 0.778799 p^3 - 0.965369 p^4 + O(p^5)$$

 $C_0 = 1$

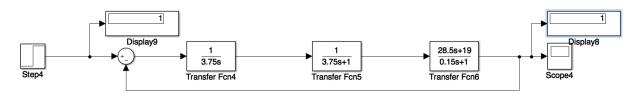
 $C_1 = -0.197368$

 C_2 = -0.43473

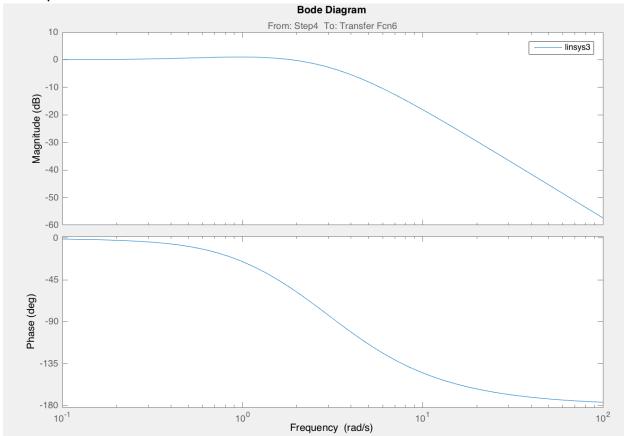
 C_3 = 0.778799

 C_4 = -0.965369

2.a) g(t) = 1(t)



Bode plot:



measured result:

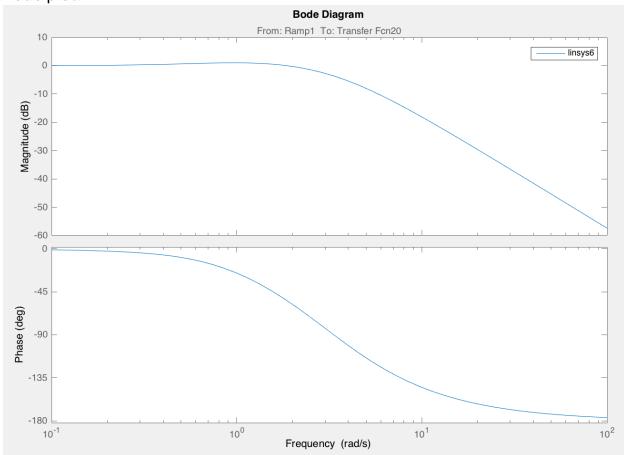
$$\varepsilon = 1 - 1 = 0$$

$$\epsilon = 1 - C_0 g(t) = 1 - 1 * 1 = 0$$

2.b) g(t) = t1(t)



Bode plot:

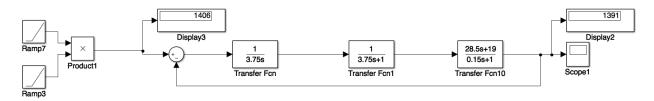


measured result:

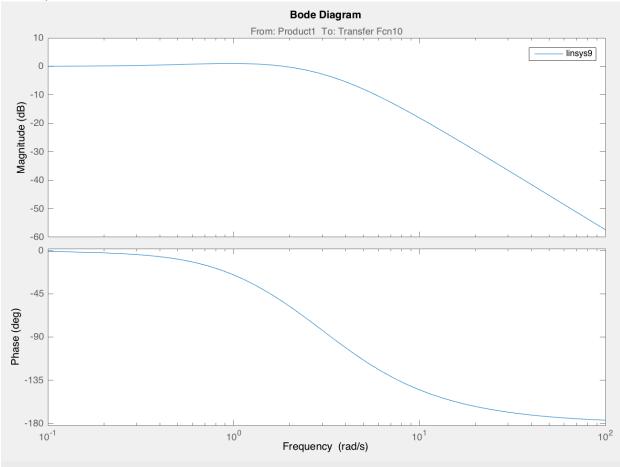
$$\varepsilon = 37.5 - 37.3 = 0.2$$

$$\varepsilon$$
 =37.5-C₀ g(t)-C₁ g`(t) = 37.5 - 1*37.5 + 0.58425 = 0

2.c) $g(t) = t^2 1(t)$



Bode plot:

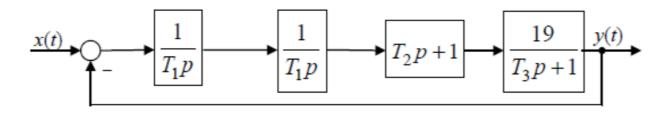


measured result:

$$\varepsilon = 1406 - 1391 = 15$$

$$\epsilon$$
 =1406 -C₀ g(t)-C₁ g`(t)-C₂g``(t)/2 = 1406 - 1*1406 + 0.197368*75 + 0.43473 = 15,23733

3) Astatic of 2nd order control system



W(p)=
$$\frac{0.0711111 (28.5 p + 19)}{(0.15 p + 1) p^2}$$

$$\Phi(p) = \frac{13.5111 \ p + 9.00741}{p^3 + 6.66667 \ p^2 + 13.5111 \ p + 9.00741}$$

Maclaurin series:

$$1. - 0.740132 p^2 + 0.999178 p^3 - 0.950972 p^4 + O(p^5)$$

$$C_0$$
= 1

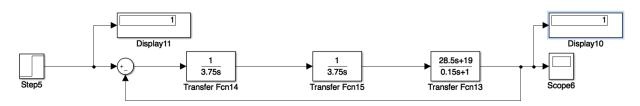
$$C_1 = 0$$

$$C_2$$
= -0.740132

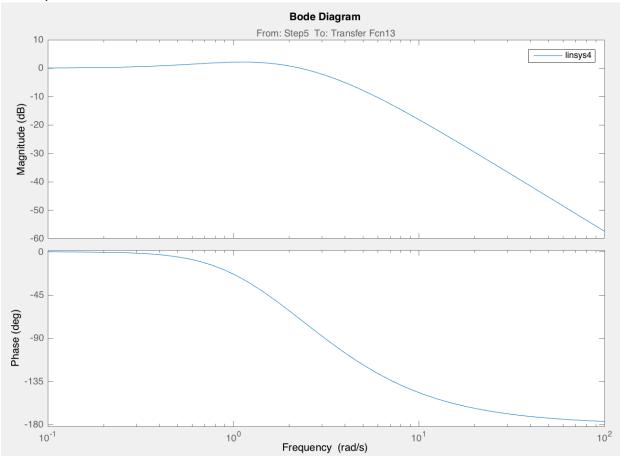
$$C_3$$
= 0.999178

$$C_4$$
= -0.95097

3.a) g(t) = 1(t)



Bode plot:



measured result:

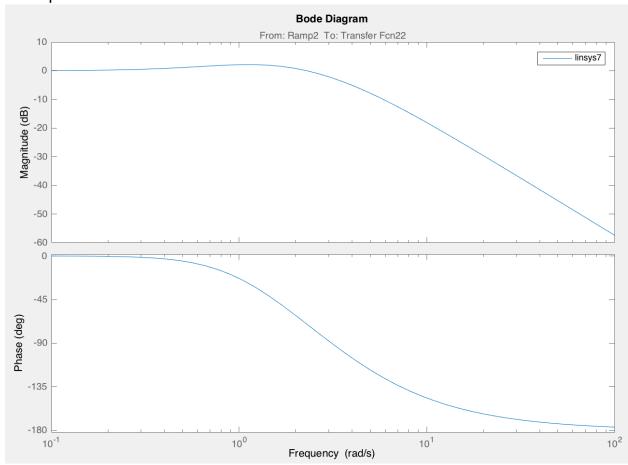
$$\varepsilon = 1 - 1 = 0$$

$$\epsilon = 1 - C_0 g(t) = 1 - 1 * 1 = 0$$

3.b) g(t) = t1(t)



Bode plot:

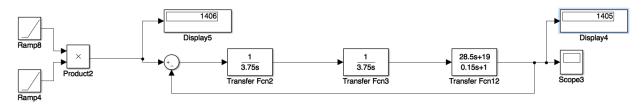


measured result:

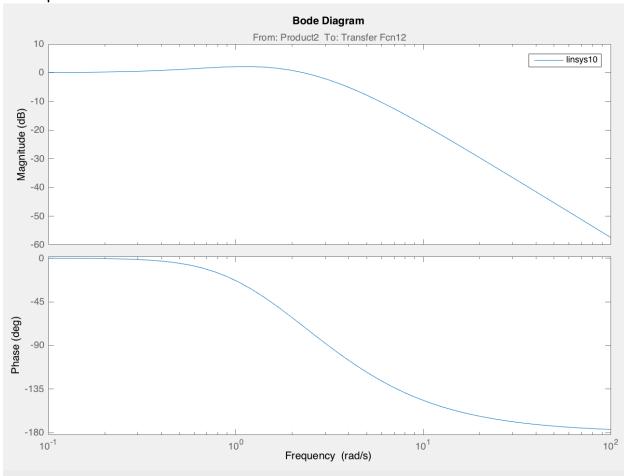
$$\varepsilon = 37.5 - 37.5 = 0$$

$$\varepsilon = 37.5 - C_0 g(t) - C_1 g'(t) = 37.5 - 1*37.5 - 0 = 0$$

3.c) $g(t) = t^2 1(t)$



Bode plot:



measured result:

$$\epsilon = 1406 - 1405 = 1$$

$$\epsilon$$
 =1406 -C₀ g(t)-C₁ g`(t)-C₂g``(t)/2 = 1406 - 1*1406 - 0 +0.740132 = 0.740132

The results of measurements and calculations

Scheme	X(t) = 1(t)		X(t) = t*1(t)		X(t) = t^2 * 1(t)	
	measured	calculated	measured	calculated	measured	calculated
static	0.05	0.05	2.17	2,167125	92	92,402765
Astatic 1st order	0	0	0.2	0	15	15,23733
Astatic 2nd order	0	0	0	0	1	0.740132