# PHP 2500 Introduction to Biostatistics

# Problem Set Six Solutions

### 1/

# **Chapter 11, #5**

The two samples are paired since we are taking repeated observations on the same subject.

 $H_0\text{: }\mu_{CF}\!-\!\!\mu_{OB}=0\quad versus\ H_0\text{: }\mu_{CF}\!-\!\!\mu_{OB}\neq0$ 

ttest cf=ob

Paired t test

Variable	Obs	Mean	Std. Err.	Std. Dev.	-	. Interval]
cf ob	14 14	4.443571 4.080714	.2589319	.9688344 1.05698	3.884183 3.470432	5.00296 4.690997
diff	14	.3628571	.1084984	.4059638	.1284606	.5972537

Ho: 
$$mean(cf - ob) = mean(diff) = 0$$

Ha: mean(diff) < 0  

$$t = 3.3444$$
  
P <  $t = 0.9974$ 

Ha: mean(diff) > 0

t = 3.3228 P > t = 0.0080

The p-value for the two sided test is .0053.

ttest after12=after24, level(90)

Therefore, we reject the null hypothesis that the difference in means is 0.

### **Chapter 11, #7**

Paired t test

Variable	Obs	Mean	Std. Err.	Std. Dev.	[90% Conf.	Interval]
after12 after24	7 7	69.85714 30.42857	15.95593 7.981697	42.21543 21.11758	38.85189 14.9187	100.8624 45.93845
diff	7	39.42857	11.86603	31.39457	16.37073	62.48641

Ho: 
$$mean(after12 - after24) = mean(diff) = 0$$

Ha:	mea	an (	diff) < 0
	t	=	3.3228
p.	< +	=	0 9920

Ha: mean(diff) 
$$\sim = 0$$
  
t = 3.3228  
P > |t| = 0.0159

Our one sided 95% CI for  $\delta = \mu_{12} - \mu_{24}$  is  $\delta \ge 16.36$ .

h

Our test of the null hypothesis yields a one-sided p-value of .0080 therefore, we reject the null hypothesis at the 5% level of significance.

3/

### **Chapter 11, #9**

а

Assuming equal variances,

ttesti 23 111 8 24 109 8, level(99)

Two-sample t test with equal variances

	0bs	Mean	Std. Err.	Std. Dev.	[99% Conf.	Interval]
х У	23 24	111 109	1.668115 1.632993	8	106.298 104.4156	115.702 113.5844
combined	47   47	109.9787	1.163542	7.97684	106.8523	113.1052
diff		2	2.334368		-4.278482	8.278482

Degrees of freedom: 45

Ho: mean(x) - mean(y) = diff = 0

The two-sided hypothesis test yields a p-value of .3961 therefore we cannot reject the null hypothesis that the two populations of women have the same mean arterial blood pressure.

b. 99% CI is (-4.28, 8.28). This interval contains the value 0 which was to be expected since we did not reject the null hypothesis that the difference in mean arterial bp between the two groups of women was 0.

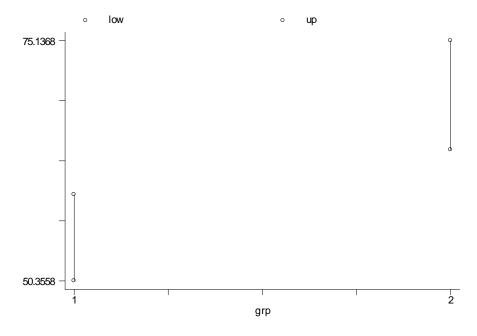
### 4/ Chapter 11, #10

a. ttesti 156 54.8 28.1 148 69.5 34.7

Two-sample t test with equal variances

	Obs	Mean	Std. Err.	Std. Dev.	[95% Conf	. Interval]
х У	156   148	54.8 69.5	2.249801 2.852322	28.1 34.7	50.35577 63.86315	59.24423 75.13685
combined	304	61.95658	1.85161	32.28392	58.31294	65.60022
diff		-14.7	3.612929		-21.8097	-7.590298

Degrees of freedom: 302



Since the Confidence interval on the difference does not contain zero, there appears to be evidence that the populations means are different. Note that it is tempting to simply notice that the two confidence intervals do not overlap and the two population means are not likely to be equal, but this is not the correct way to assess if there is a difference or not.

b. ttesti 156 54.8 28.1 148 69.5 34.7

Two-sample t test with equal variances

	0bs	Mean	Std. Err.	Std. Dev.	[95% Conf	. Interval]
x y	156   148	54.8 69.5	2.249801 2.852322	28.1 34.7	50.35577 63.86315	59.24423 75.13685
combined	304	61.95658	1.85161	32.28392	58.31294	65.60022
diff		-14.7	3.612929		-21.8097	-7.590298

Degrees of freedom: 302

Ho: 
$$mean(x) - mean(y) = diff = 0$$

The p-value for the two sided test is .0001, therefore I reject the null hypothesis that the population means are equal.

A 95% CI for the true difference in population means is (-21.8097, -7.59028)

d.

```
. ttesti 156 172.5 68.8 148 185.5 69.0
```

Two-sample t test with equal variances

-----

	Obs	Mean	Std. Err.	Std. Dev.	[95% Conf.	<pre>Interval]</pre>
х У	156 148	172.5 185.5	5.508408 5.671765	68.8 69	161.6188 174.2913	183.3812 196.7087
combined	304	178.8289	3.962633	69.09087	171.0312	186.6267
diff		-13	7.905814		-28.55746	2.557458
Degrees of	freedom:	302				

Ho: mean(x) - mean(y) = diff = 0

The p-value for this two sided test is .1011, therefore I cannot reject that the two groups of husbands have the same mean carbohydrate intake.

### 5/ Chapter 11, #13

a. summ bed80 bed86

Variable	0bs	Mean	Std. Dev.	Min	Max
bed80	51	4.686275	1.009756	3	7
bed86	51	4.235294	1.176235	2	8

b. ttest bed80= bed86, unpaired

Two-sample t test with equal variances

Variable	Obs	Mean	Std. Err.	Std. Dev.	•	<pre>Interval]</pre>
bed80   bed86	51 51	4.686275 4.235294	.1413942	1.009756 1.176235	4.402276 3.904473	4.970273 4.566116
combined	102	4.460784	.1103036	1.114011	4.241972	4.679597
diff		.4509804	.2170722		.0203153	.8816454

Degrees of freedom: 100

Ho: mean(bed80) - mean(bed86) = diff = 0

The p-value for the two sided test is .0403, therefore I would reject the null hypothesis that the mean number of beds in the two years was the same.

c.
ttest bed80= bed86

Paired t test

Variable	0bs	Mean	Std. Err.	Std. Dev.	•	. Interval]
bed80 bed86	51 51	4.686275 4.235294	.1413942 .1647059	1.009756 1.176235	4.402276 3.904473	4.970273 4.566116
diff	51   51	.4509804	.08075	.5766706	.2887892	.6131716

The p-value for the paired test is ~0, therefore I would again reject the null hypothesis that the mean number of beds was the same in each year.

d. The difference between the two tests is that the paired t-test recognizes (and takes in to account) that we have repeated observations on the same "unit". So in a sense we have controlled a great deal of variability. Treating the data as if it came from two independent populations is dangerous in that we ignore the natural pairing in the data. In this case we happen to reach the same conclusion.

```
e.
gen diff=bed80-bed86
```

ci diff

Variable	Obs.	Mean	Std. Err.	[95% Conf.	Interval]
diff	   51	.4509804	.08075	.2887892	.6131716

95% CI for the true difference is (.289, .613)

### 6/

# **Chapter 11, #15**

a.
ttest pdi, by ( trtment) unequal

Two-sample t test with unequal variances

Group	0bs	Mean	Std. Err.		[95% Conf	=
0	73 70	91.91781 97.77143	1.929775 1.755225	16.488 14.68527	88.07087 94.26985	95.76474 101.273
combined	143	94.78322	1.325531	15.85104	92.16289	97.40354
diff	 	-5.85362	2.60861		-11.0109	6963371

Satterthwaite's degrees of freedom: 140.247

The p-value for the two sided test is .0264. Therefore, we reject the null hypothesis that the mean pdi score is the same for children's in both treatment groups.

b.

```
. ttest mdi, by (trtment) unequal
```

Two-sample t test with unequal variances

Group	0bs	Mean	Std. Err.	Std. Dev.	[95% Conf	. Interval]
0	74	103.1622	1.914019	16.46501	99.34753	106.9768
	70	106.4	1.741754	14.57256	102.9253	109.8747

```
combined | 144 104.7361 1.300364 15.60437 102.1657 107.3065
______
diff | -3.237838 2.58789 -8.353798 1.878122
Satterthwaite's degrees of freedom: 141.386
          Ho: mean(0) - mean(1) = diff = 0
```

The p-value for this two sided test is .2129. Therefore, we cannot reject the null hypothesis that the mean mdi score is the same for children in both treatment groups.

These tests suggest that the type of surgical treatment will impact a child's psychomotor development but not their mental development.

### 7/ **Chapter 13, #7**

```
signtest time1= time2
```

Sign test

```
sign | observed expected
-----<del>-</del>
 positive | 9 7
negative | 5 7
zero | 0 0
    all | 14 14
```

```
One-sided tests:
```

```
Ho: median of time1 - time2 = 0 vs.
 Ha: median of time1 - time2 > 0
    Pr(#positive >= 9) =
        Binomial(n = 14, x \ge 9, p = 0.5) = 0.2120
 Ho: median of time1 - time2 = 0 vs.
 Ha: median of time1 - time2 < 0
     Pr(#negative >= 5) =
        Binomial(n = 14, x >= 5, p = 0.5) = 0.9102
Two-sided test:
 Ho: median of time1 - time2 = 0 vs.
 Ha: median of time1 - time2 ~= 0
     Pr(#positive >= 9 or #negative >= 9) =
        min(1, 2*Binomial(n = 14, x >= 9, p = 0.5)) = 0.4240
```

The p-value for the two sided test is .4240 therefore, we cannot reject the null hypothesis that the median difference in respiratory rates for the two times is equal to 0.

```
b.
signrank time1= time2
Wilcoxon signed-rank test
```

expected	sum ranks	obs	sign
52.5 52.5 0	80.5 24.5 0	9   5   0	positive negative zero
105	105	14	all

```
unadjusted variance adjustment for ties -0.12 adjustment for zeros 0.00 adjusted variance 253.63

Ho: time1 = time2 z = 1.758 Prob > |z| = 0.0787
```

If we use the Wilcoxon Sign-Rank test we find a two-sided p-value of .0787. Therefore, I would not reject the null hypothesis that the median respiratory rate at the two times is equal.

c.

Using the two-sided test, we do reach the same conclusions.

### 8/

# **Chapter 13, #8**

a.
signrank air= so2

Wilcoxon signed-rank test

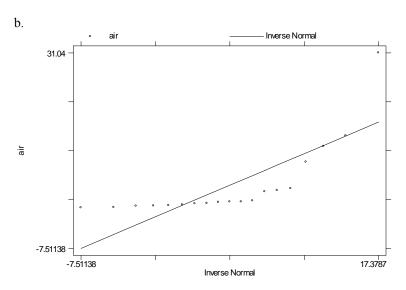
sign	obs	sum ranks	expected
positive negative zero	5   14   0	43 147 0	95 95 0
all	19	190	190

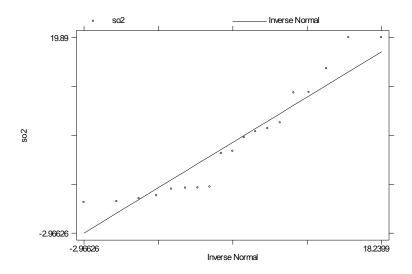
unadjusted	var	iance	617.50
adjustment	for	ties	0.00
adjustment	for	zeros	0.00
adjusted va	arian	nce	617.50

Ho: air = so2  

$$z = -2.093$$
  
Prob >  $|z| = 0.0364$ 

The p-value for the two-sided test is .0364. Therefore, I would reject the null hypothesis that the median difference is equal to zero.





Neither of the variables are normally distributed, therefore a ttest would not have been appropriate.

# 9/ Chapter 13, #11

a.
ranksum age, by(sex)

Two-sample Wilcoxon rank-sum (Mann-Whitney) test

expected	rank sum	obs	sex
224 154	221 157	16   11	0
378	378	27	combined

unadjusted variance 410.67 adjustment for ties -0.38 ------adjusted variance 410.29

Ho: age(sex==0) = age(sex==1) z = -0.148Prob > |z| = 0.8823

The p-value for the rank sum test is .8823, therefore, I cannot reject the null hypothesis that the median age is the same for males and females.

### b.

 $\rightarrow$  sex = 0

. by sex: centile age, centile(50)

-> sex = 1

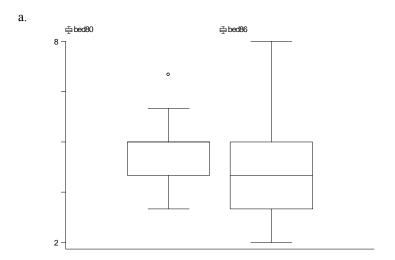
-- Binom. Interp. -Variable | Obs Percentile Centile [95% Conf. Interval]

age | 11 50 87 58.85091 141.4691

-> sex = 0						
Variable	0bs	Mean	Std. Dev.	Min	Max	
age	16	97.25	39.4656	46	175	
-> sex = 1						
Variable	0bs	Mean	Std. Dev.	Min	Max	
age	11	107.6364	66.1321	53	277	

Notice that for each sex, the median age  $\neq$  mean age which implies the data is not symmetric. Therefore, a ttest would not be appropriate.

10/ Chapter 13, #13



b.
signrank bed80= bed86

Wilcoxon signed-rank test

sign	obs	sum ranks	expected
positive negative zero	25 2 24	950 76 300	513 513 300
all	51	1326	1326
unadjusted var	riance 1	11381.50	

Ho: bed80 = bed86 z = 4.426Prob > |z| = 0.0000

The p-value is  $\sim$ 0 and thus I would reject the null hypothesis that the median number of beds is the same in both years.

```
c.
```

```
. ranksum bed, by( year)
```

Prob > |z| = 0.0188

Two-sample Wilcoxon rank-sum (Mann-Whitney) test

year	obs	rank sum	expected		
80 86	51   51	2963 2290	2626.5 2626.5		
combined	102	5253	5253		
unadjusted variance 22325.25 adjustment for ties -1817.57					
adjusted varia	ance 20	507.68			
Ho: bed(year==80) = bed(year==86) z = 2.350					

The p-value is .0188. Therefore, I would reject the null hypothesis that the median number of beds is the same in both years.

#### d

The sign rank test assumes the data is paired whereas the rank sum test assumes we have two independent populations. In this example, both tests yield the same conclusions. The sign-rank test would be the appropriate choice here since the data is actually paired (repeated measurements on the same state).

e.

Non-parametric tests yielded the same results. This is actually not surprising since from part a we see the data is approximately symmetric (which would imply the mean=median).

### 11/ Chapter 14, #9

a.

```
. cii 45 4, level(90)
```

Variable	Obs	Mean	Std. Err.		Interval]
	   45	.0888889	.0424232	.0309353	.1919756

Therefore a 90% CI for the true proportion is (.031, .192)

```
b.
H<sub>0</sub>: p=.22
H<sub>a</sub>: p≠ .22
```

bitesti 45 4 .22

Blume

d.

The p-value is .03, therefore we would reject the null hypothesis that the true proportion is the same for children in the special ed program as for all 3<sup>rd</sup> graders.

```
sampsi .22 .1, onesample power(.95) alpha(.05)
Estimated sample size for one-sample comparison of proportion
  to hypothesized value
Test Ho: p = 0.2200, where p is the proportion in the population
Assumptions:
 \begin{array}{rcl} & \text{alpha =} & 0.0500 & (\text{two-sided}) \\ & \text{power =} & 0.9500 \\ & \text{alternative p =} & 0.1000 \end{array}
Estimated required sample size:
                           119
Therefore, a sample of size 119 would be required.
```

# 12/

### Chapter 14, #11

For prepaid plan,  $p^{13/311} = .042$ For Medicaid plan,  $p^{-} = 22/310 = .071$ 

b.

```
. prtesti 311 13 310 22, level(90) count
```

x: Number of obs = 311 y: Number of obs = 310 Two-sample test of proportion

Variable	Mean	Std. Err.	z	P>   z	[90% Conf.	Interval]
х У	.0418006	.0113485 .0145836	3.68336 4.86627	0.0002 0.0000	.023134 .0469798	.0604673
diff	0291671   under Ho:	.0184789	-1.57586	0.1151	0595622	.001228

Ho: proportion(x) - proportion(y) = diff = 0

The p-value for the two sided test is .1151, therefore, I cannot reject the null hypothesis that the proportions for the two populations are identical (at the 10% significance level).

#### 13/

### Chapter 14, #12

b.

Two-sample test of proportion

x: Number of obs = 97 y: Number of obs = 161

Variable	Mean	Std. Err.		P>   z		Interval]
х У	.247   .174		5.64075 5.82368	0.0000	.1611761 .1154402	.3328239
diff	!	.0530106	1.41606	0.1568	030899	.176899

Ho: proportion(x) - proportion(y) = diff = 0

C.

The p-value for the two sided test is .1568. Therefore, I cannot reject the null hypothesis that the proportion of intravenous drug users who have a positive tuberculin skin test result are the same for those who share needles and those who do not.

d. 95% CI for the true difference in proportions is (-0.03, .18).

### 14/ Chapter 15, #8

a. tabi 1250 991\1387 1666, chi2

row	col	2	Total
1 2	+   1250   1387	991 1666	2241   3053
Total	+   2637	2657	+   5294

Pearson chi2(1) = 55.3553 Pr = 0.000

Therfore,  $\chi^2 = 55.35$ 

b.

The chi-square value we found is significantly different than 1, thus we would conclude that the behavior of college students changes from one year to the next.

c. prtesti 2637 1250 2657 991, count

Two-sample test of proportion x: Number of obs = 2637 y: Number of obs = 2657

Variable	Mean	Std. Err.	Z	P>   z	[95% Conf. I	interval]
х У	.4740235	.0097236 .0093818	48.7497 39.7553	0.0000	.4549656 .354589	.4930815 .3913651
diff	.1010465   under Ho:	.0135117	7.44011	0.0000	.0745639	.127529

Again – we would reject the null hypothesis that the proportion of students who drove while drinking is the same in the two years.

d. 95% CI for true difference in proportions is (.0745639, .127529).

### 15/ Chapter 15, #11

a.
tabi 2040 367 327\149 60 48\288 25 70\703 197 252\425 62 88\121 72 79, chi2

	col				
row	] 1	2	3	Total	
1	+   2040	367	327	2734	
2	149	60	48	257	
3	288	25	70	383	
4	703	197	252	1152	
5	425	62	88	575	
6	121	72	79	272	
Total	+   3726	783	864	5373	

Pearson chi2(10) = 209.0933 Pr = 0.000

Since our chi-square statistic is significantly different than 10, we would conclude that the results are not consistent across studies.

One problem might be that we might report a direction of effect that is the opposite of the true association.

### 16/ Chapter 15, #13

a. mcci 27 20 12 68

Cases	Controls   Exposed	Unexposed	   Total
Exposed Unexposed	27   12	20 68	47   80
Total	39	88	127

McNemar's chi2(1) = 2.00 Prob > chi2 = 0.1573 Exact McNemar significance probability = 0.2153

Proportion with factor

Cases Controls	.3700787	[95% Conf.	Interval]	
difference ratio rel. diff.	.0629921 1.205128 .0909091	0314928 .9301778 0292189	.157477 1.561351 .211037	
odds ratio	1.666667	.7759952	3.739198	(exact)

b.

Since McNemar's chi-square statistic is not significantly different than 1, we can not reject the null hypothesis of no association between retirement status and cardiac arrest.

c.
mcci 27 20 12 68

Cases		Controls Exposed	Unexposed	Total
	Exposed	27 12	20 68	47   80
	Total	39	88	127

McNemar's chi2(1) = 2.00 Prob > chi2 = 0.1573 Exact McNemar significance probability = 0.2153

Proportion with factor

Cases	.3700787			
Controls	.3070866	[95% Conf.	<pre>Interval]</pre>	
difference	.0629921	0314928	.157477	
ratio	1.205128	.9301778	1.561351	
rel. diff.	.0909091	0292189	.211037	
odds ratio	1.666667	.7759952	3.739198	(exact)

OR = 1.67

d.

95% CI for population OR is (.776, 3.739). Yes this interval contains the value 1 which was to be expected since we did not reject the null hypothesis of no association.

## 17/ Chapter 15, #15

a. mcci 2 8 2 33

Cases		Controls Exposed	Unexposed	   Total
	Exposed Unexposed	2 2	8 33	10
	Total	4	41	45

McNemar's chi2(1) = 3.60 Prob > chi2 = 0.0578 Exact McNemar significance probability = 0.1094

Proportion with factor

Cases	.222222			
Controls	.0888889	[95% Conf.	Interval]	
difference	.1333333	020997	.2876637	
ratio	2.5	.9382946	6.661021	
rel. diff.	.1463415	.0066704	.2860125	
odds ratio	4	.7982264	38.6707	(exact)

b. We see that McNemar's chi-square statistic takes on the value 3.60 which is not significantly different than 1. Therefore, we cannot reject the null hypothesis of no association (but we must do so with caution. An inference based entirely on p-values could be questionable here).

# 18/ Chapter 15, #16

cci 108 163 117 268

	Exposed	Unexposed	Total	Proportion Exposed	
Cases Controls	108 117	163 268	271   385	0.3985	
Total	225	431	   656	0.3430	
	Point e	estimate	   [95% Conf.	Interval]	
Odds ratio Attr. frac. ex. Attr. frac. pop	. 34	L <b>7697</b> 11107 59393	<b>1.080447</b>   .0744574		(exact) (exact)
- -	ch	ni2(1) =	6.32 Pr>chi	2 = 0.0119	

a.

Relative Odds for Smokers vs Non-Smokers = 1.517697

b.

95% CI for population OR:

(1.08, 2.13)

C.

Chi-Square Statistic is 6.32 which is significantly different than 1 therefore we reject the null hypothesis of no association.

# 19/ Chapter 15, #17

a.

.cci 28 251 6 273, level(99)

	Exposed	Unexposed	Total	Proportion Exposed	
Cases Controls	28	251 273	279   279	0.1004 0.0215	
Total	34	524	558	0.0609	
	Point	estimate	   [99% Conf.	Interval]	
Odds ratio Attr. frac. ex. Attr. frac. pop	.80	075697 029827 005861	1.592784   .3721686	22.07797 .954706	(exact) (exact)
=		 rhi2(1) =	15 16 Prachi	2 = 0 0001	

b.

OR = 5.076

C.

99% CI for population OR: (1.59, 22.08)

# 20/

# **Chapter 15, #18**

a.

P(abortion|0 alcohol) = 6793/33164 = .205

P(abortion|1-2 drinks) = 2068/9099 = .227

P(abortion|3-6 drinks)=776/3069 = .253

P(abortion|7-20 drinks) = 456/1527 = .299 P(abortion|21+ drinks)=98/287 = .341

b.

tabodds case alcohol [fweight=freq],or base(1)

alcohol	Odds Ratio	chi2	P>chi2	[95% Conf.	Interval]
1	1.000000				
2	1.141822	21.71	0.0000	1.079823	1.207381
3	1.313780	39.20	0.0000	1.205875	1.431340
4	1.652876	77.69	0.0000	1.476384	1.850467
5	2.012933	32.47	0.0000	1.574664	2.573183
Test of homoge	eneity (equal	odds): chi2(4	 ) = 118.91		

Pr>chi2 = 0.0000 Score test for trend of odds: chi2(1) = 152.17 Pr>chi2 = 0.0000

• Note that the relative odds for each alcohol "level" are in the column labeled Odds Ratio.

The 95% CI's are highlighted in the above table.

d.

None of the 95% OR's contain the value 1 suggesting that spontaneous abortions and alcohol use are associated. Also, all of the estimated OR's >1 and increase with increasing alcohol consumption.