${\tt EXTENDS}\ Integers,\ Sequences$ 

CONSTANT Data

We first define Remove(i, seq) to be the sequence obtained by removing element number i from sequence seq.

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 \begin{array}{l} Remove(i,\,seq) \; \stackrel{\triangle}{=} \\ [j \in 1 \ldots (Len(seq)-1) \mapsto \text{if} \; j < i \; \text{then} \; seq[j] \\ \qquad \qquad \qquad \text{else} \; \; seq[j+1]] \end{array}
```

VARIABLES AVar, BVar, The same as in module ABSpec

AtoB, The sequence of data messages in transit from sender to receiver.

BtoA The sequence of ack messages in transit from receiver to sender.

Messages are sent by appending them to the end of the sequence.

and received by removing them from the head of the sequence.

 $vars \triangleq \langle AVar, BVar, AtoB, BtoA \rangle$ 

$$TypeOK \triangleq \land AVar \in Data \times \{0, 1\} \\ \land BVar \in Data \times \{0, 1\} \\ \land AtoB \in Seq(Data \times \{0, 1\}) \\ \land BtoA \in Seq(\{0, 1\})$$

$$Init \triangleq \land AVar \in Data \times \{1\}$$

$$\land BVar = AVar$$

$$\land AtoB = \langle \rangle$$

$$\land BtoA = \langle \rangle$$

The action of the sender sending a data message by appending AVar to the end of the message queue AtoB. It will keep sending the same message until it receives an acknowledgment for it from the receiver.

$$ASnd \triangleq \land AtoB' = Append(AtoB, AVar) \land UNCHANGED \langle AVar, BtoA, BVar \rangle$$

The action of the sender receiving an ack message. If that ack is for the value it is sending, then it chooses another message to send and sets AVar to that message. If the ack is for the previous value it sent, it ignores the message. In either case, it removes the message from BtoA.

$$\begin{array}{ll} ARcv & \triangleq & \land BtoA \neq \langle \rangle \\ & \land \text{ if } Head(BtoA) = AVar[2] \\ & \quad \text{THEN } \exists \ d \in Data : AVar' = \langle d, \ 1 - AVar[2] \rangle \\ & \quad \text{ELSE } AVar' = AVar \\ & \land BtoA' = Tail(BtoA) \\ & \land \text{ UNCHANGED } \langle AtoB, \ BVar \rangle \end{array}$$

The action of the receiver sending an acknowledgment message for the last data item it received.

$$BSnd \triangleq \land BtoA' = Append(BtoA, BVar[2]) \land UNCHANGED \langle AVar, BVar, AtoB \rangle$$

The action of the receiver receiving a data message. It sets BVar to that message if it's not for the data item it has already received.

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BRcv \triangleq \land AtoB \neq \langle \rangle
\land \text{ IF } Head(AtoB)[2] \neq BVar[2]
\land \text{ THEN } BVar' = Head(AtoB)
\land \text{ ELSE } BVar' = BVar
\land AtoB' = Tail(AtoB)
\land \text{ UNCHANGED } \langle AVar, BtoA \rangle
```

LoseMsg is the action that removes an arbitrary message from queue AtoB or BtoA.

$$LoseMsg \triangleq \land \lor \land \exists \ i \in 1 \dots Len(AtoB) : \\ AtoB' = Remove(i, \ AtoB) \\ \land BtoA' = BtoA \\ \lor \land \exists \ i \in 1 \dots Len(BtoA) : \\ BtoA' = Remove(i, \ BtoA) \\ \land AtoB' = AtoB \\ \land \ UNCHANGED \ \langle AVar, \ BVar \rangle$$

 $Next \triangleq ASnd \lor ARcv \lor BSnd \lor BRcv \lor LoseMsq$ 

$$Spec \stackrel{\triangle}{=} Init \wedge \Box [Next]_{vars}$$

 $ABS \stackrel{\triangle}{=} \text{Instance } ABSpec$ 

THEOREM  $Spec \Rightarrow ABS!Spec$ 

FairSpec is Spec with fairness conditions added.

$$FairSpec \triangleq Spec \land SF_{vars}(ARcv) \land SF_{vars}(BRcv) \land WF_{vars}(ASnd) \land WF_{vars}(BSnd)$$

- **\\*** Modification History
- \* Last modified Sat Jun 11 19:31:09 CST 2022 by wengjialin
- \\* Last modified Wed Dec 27 13:29:51 PST 2017 by lamport
- $\backslash \ ^*$  Created  $Wed\ Mar\ 25\ 11:53:40\ PDT\ 2015$  by lamport