LeetCode題解

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https://github.com/soulmachine/leetcode

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內容簡介

本書的目標讀者是準備去北美找工作的碼農,也適用於在國內找工作的碼農,以及剛接觸 ACM 算法競賽的新手。

本書包含了 LeetCode Online Judge(http://leetcode.com/onlinejudge) 所有題目的答案,所有 代碼經過精心編寫、編碼規範良好、適合讀者反覆揣摩、模仿、甚至在紙上默寫。

全書的代碼,使用 C++ 11 的編寫,並在 LeetCode Online Judge 上測試通過。本書中的 代碼規範、跟在公司中的工程規範略有不同、為了使代碼短(方便迅速實現):

- 所有代碼都是單一文件。這是因為一般 OJ 網站,提交代碼的時候只有一個文本框,如果還是按照標準做法,比如分為頭文件.h 和源代碼.cpp,無法在網站上提交;
- Shorter is better。能遞歸則一定不用棧;能用 STL 則一定不自己實現。
- 不提倡防禦式編程。不需要檢查 malloc()/new 返回的指針是否為 nullptr; 不需要檢查 內部函數入口參數的有效性。

本手冊假定讀者已經學過《數據結構》^①、《算法》^②這兩門課,熟練掌握 C++或 Java。

GitHub 地址

本書是開源的, GitHub 地址: https://github.com/soulmachine/leetcode

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Algorithms», Robert Sedgewick, Addison-Wesley Professional, http://book.douban.com/subject/4854123/

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第1章 編程技巧

在判斷兩個浮點數 a 和 b 是否相等時,不要用 a==b,應該判斷二者之差的絕對值 fabs(a-b)是否小於某個閾值,例如 1e-9。

判斷一個整數是否是為奇數,用 x % 2 != 0,不要用 x % 2 == 1,因為 x 可能是負數。用 char 的值作為數組下標(例如,統計字符串中每個字符出現的次數),要考慮到 char 可能是負數。有的人考慮到了,先強制轉型為 unsigned int 再用作下標,這仍然是錯的。正確的做法是,先強制轉型為 unsigned char,再用作下標。這涉及 C++整型提升的規則,就不詳述了。

以下是關於 STL 使用技巧的、很多條款來自《Effective STL》這本書。

vector 和 string 優先於動態分配的數組

首先,在性能上,由於 vector 能夠保證連續內存,因此一旦分配了後,它的性能跟原始數組相當;

其次,如果用 new,意味着你要確保後面進行了 delete,一旦忘記了,就會出現 BUG, 且這樣需要都寫一行 delete,代碼不夠短;

再次, 聲明多維數組的話, 只能一個一個 new, 例如:

```
int** ary = new int*[row_num];
for(int i = 0; i < row_num; ++i)
    ary[i] = new int[col_num];</pre>
```

用 vector 的話一行代碼搞定,

vector<vector<int> > ary(row_num, vector<int>(col_num, 0));

使用 reserve 來避免不必要的重新分配

Things about binary search

The difference between using index or length.

```
// LeetCode,
// 時間複雜度 O(logn), 空間複雜度 O(1)
class solution{
```

2 第1章編程技巧

```
public:
     int findIndex(const vector<int>& vec, int target) {
          int left, right;
          left = 0; right = (int)vec.size() - 1; // right is using index
          while (left <= right) { // this line is different
              int mid = left + (right - left) / 2;
              if (vec[mid] < target)</pre>
                  left = ++mid;
              else if (vec[mid] > target)
                  right = --mid; // this line is different
              else
                  return mid;
          }
         return -1;
     }
 };
 // LeetCode,
 // 時間複雜度 O(logn), 空間複雜度 O(1)
 class solution{
 public:
     int findIndex(const vector<int>& vec, int target) {
          int left, right;
          left = 0; right = (int)vec.size(); // right is using length
          while (left < right) { // this line is different
              int mid = left + (right - left) / 2;
              if (vec[mid] < target)</pre>
                  left = ++mid;
              else if (vec[mid] > target)
                  right = mid; // this line is different
              else
                  return mid;
         return -1;
     }
 };
Hash map in c++ with custom class
 using h = std::hash<int>;
 auto hash = [](const Node& n)
                \{\text{return } ((17 * 31 + h()(n.a)) * 31 + h()(n.b)) * 31 + h()(n.c); \};
 auto equal = [](const Node& 1, const Node& r)
                 {return l.a == r.a && l.b == r.b && l.c == r.c;};
 std::unordered_map<Node, int, decltype(hash), decltype(equal)> m(8, hash, equal);
 namespace std {
 template<>
 struct hash<pair<Iterator, Iterator>> {
     size_t operator()(pair<Iterator, Iterator> const& p) const {
          return ((size_t) &(*p.first)) ^ ((size_t) &(*p.second));
```

```
};
};
```

Priority queue in c++ with custom class

Use unordered map with pair

```
namespace std
{
    template <>
        struct hash<pair<int, int>>
        {
            size_t operator()(pair<int, int> const& p) const
              {
                 return ((size_t)&(p.first) ^ (size_t)&(p.second));
              }
        };
}
class Solution {
private:
    unordered_set<pair<int, int>> m_example;
}
```

第2章線性表

這類題目考察線性表的操作,例如,數組,單鏈表,雙向鏈表等。

2.1 數組

2.1.1 Remove Duplicates from Sorted Array

描述

Given a sorted array, remove the duplicates in place such that each element appear only once and return the new length.

Do not allocate extra space for another array, you must do this in place with constant memory. For example, Given input array A = [1,1,2],

Your function should return length = 2, and A is now

1,2

分析

無

```
return index + 1;
     }
 };
代碼 2
 // LeetCode, Remove Duplicates from Sorted Array
 // 使用 STL, 時間複雜度 O(n), 空間複雜度 O(1)
 class Solution {
 public:
     int removeDuplicates(vector<int>& nums) {
         return distance(nums.begin(), unique(nums.begin(), nums.end()));
 };
代碼3
 // LeetCode, Remove Duplicates from Sorted Array
 // 使用 STL, 時間複雜度 O(n), 空間複雜度 O(1)
 class Solution {
 public:
     int removeDuplicates(vector<int>& nums) {
         return distance(nums.begin(), removeDuplicates(nums.begin(), nums.end(), nums.begin())
     }
     template<typename InIt, typename OutIt>
     OutIt removeDuplicates(InIt first, InIt last, OutIt output) {
         while (first != last) {
             *output++ = *first;
             first = upper_bound(first, last, *first);
         }
         return output;
     }
 };
```

相關題目

• Remove Duplicates from Sorted Array II, 見 §2.1.2

2.1.2 Remove Duplicates from Sorted Array II

描述

```
Follow up for "Remove Duplicates": What if duplicates are allowed at most twice? For example, Given sorted array A = [1,1,1,2,2,3],
```

6 第2章 線性表

Your function should return length = 5, and A is now

1, 1, 2, 2, 3

分析

加一個變量記錄一下元素出現的次數即可。這題因為是已經排序的數組,所以一個變量即可解決。如果是沒有排序的數組,則需要引入一個 hashmap 來記錄出現次數。

代碼1

代碼 2

下面是一個更簡潔的版本。上面的代碼略長,不過擴展性好一些,例如將occur < 2改為occur < 3、就變成了允許重複最多 3 次。

```
return index;
     }
 };
代碼3
   Variable of duplication
 // LeetCode, Remove Duplicates from Sorted Array II
 // @author
 // 時間複雜度 O(n), 空間複雜度 O(1)
 class Solution {
 public:
     int removeDuplicates(vector<int>& nums, int du) {
          int index = du:
          for (int i = du; i < (int)nums.size(); i++) {</pre>
              if (nums[index - du] != nums[i])
                  nums[index++] = nums[i];
          }
         return index;
     }
 }:
```

相關題目

• Remove Duplicates from Sorted Array, 見 §2.1.1

2.1.3 Search in Rotated Sorted Array

描述

Suppose a sorted array is rotated at some pivot unknown to you beforehand.

```
(i.e., 0 1 2 4 5 6 7 might become 4 5 6 7 0 1 2).
```

You are given a target value to search. If found in the array return its index, otherwise return -1.

You may assume no duplicate exists in the array.

分析

二分查找, 難度主要在於左右邊界的確定。

```
// LeetCode, Search in Rotated Sorted Array
// 時間複雜度 O(log n), 空間複雜度 O(1)
class Solution {
public:
    int search(const vector<int>& nums, int target) {
```

```
int first = 0, last = nums.size();
        while (first != last) {
             const int mid = first + (last - first) / 2;
             if (nums[mid] == target)
                 return mid;
             if (nums[first] <= nums[mid]) {</pre>
                 if (nums[first] <= target && target < nums[mid])</pre>
                     last = mid;
                 else
                     first = mid + 1;
             } else {
                 if (nums[mid] < target && target <= nums[last-1])</pre>
                     first = mid + 1;
                 else
                     last = mid;
             }
        }
        return -1;
    }
};
```

相關題目

• Search in Rotated Sorted Array II, 見 §2.1.4

2.1.4 Search in Rotated Sorted Array II

描述

Follow up for "Search in Rotated Sorted Array": What if duplicates are allowed?

Would this affect the run-time complexity? How and why?

Write a function to determine if a given target is in the array.

分析

允許重複元素, 則上一題中如果 A [m] >= A [1], 那麼 [1, m] 為遞增序列的假設就不能成立了, 比如

1, 3, 1, 1, 1

如果 A[m]>=A[1] 不能確定遞增, 那就把它拆分成兩個條件:

- 若 A[m]>A[1], 則區間 [1,m] 一定遞增
- 若 A [m] == A [1] 確定不了, 那就 1++, 往下看一步即可。

代碼

```
// LeetCode, Search in Rotated Sorted Array II
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    bool search(const vector<int>& nums, int target) {
        int first = 0, last = nums.size();
        while (first != last) {
            const int mid = first + (last - first) / 2;
            if (nums[mid] == target)
                return true;
            if (nums[first] < nums[mid]) {</pre>
                 if (nums[first] <= target && target < nums[mid])</pre>
                     last = mid;
                 else
                     first = mid + 1:
            } else if (nums[first] > nums[mid]) {
                 if (nums[mid] < target && target <= nums[last-1])</pre>
                     first = mid + 1;
                 else
                     last = mid;
            } else
                //skip duplicate one
                first++;
        return false;
    }
}:
```

相關題目

• Search in Rotated Sorted Array, 見 §2.1.3

2.1.5 Median of Two Sorted Arrays

描述

There are two sorted arrays A and B of size m and n respectively. Find the median of the two sorted arrays. The overall run time complexity should be $O(\log(m+n))$.

分析

這是一道非常經典的題。這題更通用的形式是,給定兩個已經排序好的數組,找到兩者所有元素中第k大的元素。

O(m+n) 的解法比較直觀,直接 merge 兩個數組,然後求第 k 大的元素。

不過我們僅僅需要第k大的元素,是不需要"排序"這麼昂貴的操作的。可以用一個計數器,記錄當前已經找到第m大的元素了。同時我們使用兩個指針pA和pB,分別指向A和B數組的第一個

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元素,使用類似於 merge sort 的原理,如果數組 A 當前元素小,那麼 pA++,同時 m++;如果數組 B 當前元素小,那麼 pB++,同時 m++。最終當 m 等於 k 的時候,就得到了我們的答案,O(k) 時間,O(1) 空間。但是,當 k 很接近 m+n 的時候,這個方法還是 O(m+n) 的。

有沒有更好的方案呢? 我們可以考慮從 k 入手。如果我們每次都能夠刪除一個一定在第 k 大元素之前的元素,那麼我們需要進行 k 次。但是如果每次我們都刪除一半呢? 由於 A 和 B 都是有序的,我們應該充分利用這裏面的信息,類似於二分查找,也是充分利用了"有序"。

假設 A 和 B 的元素個數都大於 k/2,我們將 A 的第 k/2 個元素(即 A [k/2-1])和 B 的第 k/2 個元素(即 B [k/2-1])進行比較,有以下三種情況(為了簡化這裏先假設 k 為偶數,所得到的結論對於 k 是奇數也是成立的):

- A[k/2-1] == B[k/2-1]
- A[k/2-1] > B[k/2-1]
- A[k/2-1] < B[k/2-1]

如果 A[k/2-1] **<** B[k/2-1] ,意味着 A[0] 到 A[k/2-1] 的肯定在 $A \cup B$ 的 top k 元素的範圍內,換句話説,A[k/2-1] 不可能大於 $A \cup B$ 的第 k 大元素。留給讀者證明。

因此,我們可以放心的刪除 A 數組的這 k/2 個元素。同理,當 A $\lfloor k/2-1 \rfloor$ > B $\lfloor k/2-1 \rfloor$ 時,可以刪除 B 數組的 k/2 個元素。

當 A[k/2-1] == B[k/2-1] 時, 説明找到了第 k 大的元素, 直接返回 A[k/2-1] 或 B[k/2-1] 即可。因此, 我們可以寫一個遞歸函數。那麼函數什麼時候應該終止呢?

- 當 A 或 B 是空時,直接返回 B[k-1] 或 A[k-1];
- 當 k=1 是, 返回 min(A[0], B[0]);
- 當 A [k/2-1] == B [k/2-1] 時,返回 A [k/2-1] 或 B [k/2-1]

代碼

10

```
// LeetCode, Median of Two Sorted Arrays
// 時間複雜度 D(log(m+n)), 空間複雜度 D(log(m+n))
class Solution {
public:
    double findMedianSortedArrays(const vector<int>& A, const vector<int>& B) {
        const int m = A.size();
        const int n = B.size();
        int total = m + n;
        if (total & 0x1)
            return find_kth(A.begin(), m, B.begin(), n, total / 2 + 1);
            return (find_kth(A.begin(), m, B.begin(), n, total / 2)
                    + find_kth(A.begin(), m, B.begin(), n, total / 2 + 1)) / 2.0;
    }
private:
    static int find_kth(std::vector<int>::const_iterator A, int m,
            std::vector<int>::const_iterator B, int n, int k) {
        //always assume that m is equal or smaller than n
```

```
if (m > n) return find_kth(B, n, A, m, k);
if (m == 0) return *(B + k - 1);
if (k == 1) return min(*A, *B);

//divide k into two parts
int ia = min(k / 2, m), ib = k - ia;
if (*(A + ia - 1) < *(B + ib - 1))
    return find_kth(A + ia, m - ia, B, n, k - ia);
else if (*(A + ia - 1) > *(B + ib - 1))
    return find_kth(A, m, B + ib, n - ib, k - ib);
else
    return A[ia - 1];
};
```

相關題目

無

2.1.6 Longest Consecutive Sequence

描述

Given an unsorted array of integers, find the length of the longest consecutive elements sequence. For example, Given

, The longest consecutive elements sequence is

1, 2, 3, 4

. Return its length: 4.

Your algorithm should run in O(n) complexity.

分析

如果允許 $O(n \log n)$ 的複雜度,那麼可以先排序,可是本題要求 O(n)。由於序列裏的元素是無序的,又要求 O(n),首先要想到用哈希表。

用一個哈希表 unordered_map<int, bool> used 記錄每個元素是否使用,對每個元素,以該元素為中心,往左右擴張,直到不連續為止,記錄下最長的長度。

```
// Leet Code, Longest Consecutive Sequence
// 時間複雜度 O(n), 空間複雜度 O(n)
class Solution {
```

```
public:
    int longestConsecutive(const vector<int> &nums) {
        unordered map<int, bool> used;
        for (auto i : nums) used[i] = false;
        int longest = 0;
        for (auto i : nums) {
            if (used[i]) continue;
            int length = 1;
            used[i] = true;
            for (int j = i + 1; used.find(j) != used.end(); ++j) {
                used[j] = true;
                ++length;
            }
            for (int j = i - 1; used.find(j) != used.end(); --j) {
                used[j] = true;
                ++length;
            }
            longest = max(longest, length);
        return longest;
    }
};
```

分析 2

第一直覺是個聚類的操作,應該有 union,find 的操作.連續序列可以用兩端和長度來表示. 本來用兩端就可以表示,但考慮到查詢的需求,將兩端分別暴露出來.用 unordered_map<int, int> map 來存儲.原始思路來自於 http://discuss.leetcode.com/questions/1070/longest-consecutive-sequence

```
// Leet Code, Longest Consecutive Sequence
// 時間複雜度 O(n), 空間複雜度 O(n)
// Author: @advancedxy
class Solution {
public:
    int longestConsecutive(vector<int> &nums) {
        unordered_map<int, int> map;
        int size = nums.size();
        int l = 1;
```

```
for (int i = 0; i < size; i++) {
            if (map.find(nums[i]) != map.end()) continue;
            map[nums[i]] = 1;
            if (map.find(nums[i] - 1) != map.end()) {
                1 = max(1, mergeCluster(map, nums[i] - 1, nums[i]));
            if (map.find(nums[i] + 1) != map.end()) {
                1 = max(l, mergeCluster(map, nums[i], nums[i] + 1));
        return size == 0 ? 0 : 1;
    }
private:
    int mergeCluster(unordered_map<int, int> &map, int left, int right) {
        int upper = right + map[right] - 1;
        int lower = left - map[left] + 1;
        int length = upper - lower + 1;
        map[upper] = length;
        map[lower] = length;
        return length;
    }
};
```

相關題目

無

2.1.7 Two Sum

描述

Given an array of integers, find two numbers such that they add up to a specific target number.

The function twoSum should return indices of the two numbers such that they add up to the target, where index1 must be less than index2. Please note that your returned answers (both index1 and index2) are not zero-based.

You may assume that each input would have exactly one solution.

```
Input: numbers={2, 7, 11, 15}, target=9
Output: index1=1, index2=2
```

分析

方法 1:暴力,複雜度 $O(n^2)$,會超時

方法 2: hash。用一個哈希表,存儲每個數對應的下標,複雜度 O(n).

方法 3: 先排序, 然後左右夾逼, 排序 $O(n \log n)$, 左右夾逼 O(n), 最終 $O(n \log n)$ 。 但是注意, 這題需要返回的是下標, 而不是數字本身, 因此這個方法行不通。

代碼

```
//LeetCode, Two Sum
 // 方法 2: hash。用一個哈希表,存儲每個數對應的下標
 // 時間複雜度 O(n), 空間複雜度 O(n)
 class Solution {
 public:
     vector<int> twoSum(vector<int> &nums, int target) {
         unordered_map<int, int> mapping;
         vector<int> result;
         for (int i = 0; i < nums.size(); i++) {</pre>
             mapping[nums[i]] = i;
         for (int i = 0; i < nums.size(); i++) {</pre>
             const int gap = target - nums[i];
             if (mapping.find(gap) != mapping.end() && mapping[gap] > i) {
                 result.push_back(i + 1);
                 result.push_back(mapping[gap] + 1);
                 break;
             }
         return result;
 };
代碼
 // 時間複雜度 O(n), 空間複雜度 O(n)
 class Solution {
 public:
     vector<int> twoSum(vector<int>& nums, int target) {
         unordered_map<int, int> cache;
         for (size_t i = 0; i < nums.size(); i++)</pre>
         {
             auto it = cache.find(target - nums[i]);
             if (it != cache.end())
             {
                 return vector<int>{it->second, (int)i};
             cache.emplace(nums[i], i);
         return vector<int>(); // should not go here
     }
 };
```

相關題目

- 3Sum, 見 §2.1.9
- 3Sum Closest, 見 §2.1.10
- 4Sum, 見 §2.1.11

2.1.8 Two Sum III

描述

Design and implement a TwoSum class. It should support the following operations: add and find. add - Add the number to an internal data structure. find - Find if there exists any pair of numbers which sum is equal to the value.

```
Example 1:
 add(1); add(3); add(5);
 find(4) -> true
 find(7) \rightarrow false
   Example 2:
 add(3); add(1); add(2);
 find(3) -> true
 find(6) -> false
代碼
 // 用一個 hash map, 存储每個數對應的 count
 // 時間複雜度 O(n), 空間複雜度 O(n)
 class TwoSum {
 public:
     /** Initialize your data structure here. */
     TwoSum() {
     }
     /** Add the number to an internal data structure.. */
     void add(int number) {
         m_cache[number]++;
     /** Find if there exists any pair of numbers which sum is equal to the value. */
     bool find(int value) {
         for (const auto& [k, v] : m_cache)
         {
             auto it = m_cache.find(value - k);
             if (it != m_cache.end())
                 // 例子: value: 4, k: 2. 當 k == 2 在數組中只出現一次,不能當是答案
                 if (value - k == k)
                 {
                     if (v > 1)
                         return true;
                     else
                         continue;
                 }
                 else
                     return true;
             }
```

```
}
    return false;
}
private:
    unordered_map<int, int> m_cache;
};

/**
    * Your TwoSum object will be instantiated and called as such:
    * TwoSum* obj = new TwoSum();
    * obj->add(number);
    * bool param_2 = obj->find(value);
    */
```

2.1.9 3Sum

描述

Given an array S of n integers, are there elements a, b, c in S such that a + b + c = 0? Find all unique triplets in the array which gives the sum of zero.

Note:

- Elements in a triplet (a, b, c) must be in non-descending order. (ie, $a \le b \le c$)
- The solution set must not contain duplicate triplets.

```
For example, given array S = {-1 0 1 2 -1 -4}.

A solution set is:

(-1, 0, 1)

(-1, -1, 2)
```

分析

先排序, 然後左右夾逼, 複雜度 $O(n^2)$ 。

這個方法可以推廣到 k-sum,先排序,然後做 k-2 次循環,在最內層循環左右夾逼,時間複雜 度是 $O(\max\{n\log n, n^{k-1}\})$ 。

```
// LeetCode, 3Sum
// 先排序, 然後左右夾逼, 注意跳過重複的數, 時間複雜度 O(n^2), 空間複雜度 O(1)
class Solution {
   public:
    vector<vector<int>> threeSum(vector<int>& nums) {
        vector<vector<int>> result;
        if (nums.size() < 3) return result;
        sort(nums.begin(), nums.end());
        const int target = 0;</pre>
```

```
auto last = nums.end();
        for (auto i = nums.begin(); i < last-2; ++i) {</pre>
            auto j = i+1;
            if (i > nums.begin() && *i == *(i-1)) continue;
            auto k = last-1;
            while (j < k) {
                 if (*i + *j + *k < target) {
                     while(*j == *(j - 1) && j < k) ++j;
                } else if (*i + *j + *k > target) {
                     --k:
                     while(*k == *(k + 1) && j < k) --k;
                } else {
                     result.push_back({ *i, *j, *k });
                     ++j;
                     --k;
                     while(*j == *(j - 1) && *k == *(k + 1) && j < k) ++j;
                }
            }
        return result;
    }
};
```

相關題目

- Two sum, 見 §2.1.7
- 3Sum Closest, 見 §2.1.10
- 4Sum, 見 §2.1.11

2.1.10 3Sum Closest

描述

Given an array S of n integers, find three integers in S such that the sum is closest to a given number, target. Return the sum of the three integers. You may assume that each input would have exactly one solution.

```
For example, given array S = \{-1 \ 2 \ 1 \ -4\}, and target = 1.
```

The sum that is closest to the target is 2. (-1 + 2 + 1 = 2).

分析

先排序, 然後左右夾逼, 複雜度 $O(n^2)$ 。

```
// LeetCode, 3Sum Closest
// 先排序, 然後左右夾逼, 時間複雜度 O(n^2), 空間複雜度 O(1)
```

```
class Solution {
public:
    int threeSumClosest(vector<int>& nums, int target) {
        int result = 0;
        int min_gap = INT_MAX;
        sort(nums.begin(), nums.end());
        for (auto a = nums.begin(); a != prev(nums.end(), 2); ++a) {
            auto b = next(a);
            auto c = prev(nums.end());
            while (b < c) {
                 const int sum = *a + *b + *c;
                 const int gap = abs(sum - target);
                 if (gap < min_gap) {</pre>
                     result = sum;
                     min_gap = gap;
                 }
                 if (sum < target) ++b;</pre>
            }
        }
        return result;
    }
};
```

相關題目

- Two sum, 見 §2.1.7
- 3Sum, 見 §2.1.9
- 4Sum, 見 §2.1.11

2.1.11 4Sum

描述

Given an array S of n integers, are there elements a, b, c, and d in S such that a + b + c + d = target? Find all unique quadruplets in the array which gives the sum of target.

Note:

- Elements in a quadruplet (a, b, c, d) must be in non-descending order. (ie, $a \le b \le c \le d$)
- The solution set must not contain duplicate quadruplets.

For example, given array $S = \{1 \ 0 \ -1 \ 0 \ -2 \ 2\}$, and target = 0.

A solution set is:

```
(-1, 0, 0, 1)
(-2, -1, 1, 2)
(-2, 0, 0, 2)
```

分析

先排序,然後左右夾逼,複雜度 $O(n^3)$,會超時。 可以用一個 hashmap 先緩存兩個數的和,最終複雜度 $O(n^3)$ 。這個策略也適用於 3Sum。

左右夾逼

```
// LeetCode, 4Sum
 // 先排序, 然後左右夾逼, 時間複雜度 O(n<sup>3</sup>), 空間複雜度 O(1)
 class Solution {
 public:
     vector<vector<int>> fourSum(vector<int>& nums, int target) {
         vector<vector<int>> result:
         if (nums.size() < 4) return result;
         sort(nums.begin(), nums.end());
         auto last = nums.end();
         for (auto a = nums.begin(); a < prev(last, 3); ++a) {</pre>
             for (auto b = next(a); b < prev(last, 2); ++b) {</pre>
                 auto c = next(b);
                 auto d = prev(last);
                 while (c < d) {
                     if (*a + *b + *c + *d < target) {
                     } else if (*a + *b + *c + *d > target) {
                         --d;
                     } else {
                         result.push_back({ *a, *b, *c, *d });
                         --d;
                     }
                 }
             }
         }
         sort(result.begin(), result.end());
         result.erase(unique(result.begin(), result.end()), result.end());
         return result;
     }
 };
map 做緩存
 // LeetCode, 4Sum
 // 用一個 hashmap 先緩存兩個數的和
 // 時間複雜度, 平均 O(n^2), 最壞 O(n^4), 空間複雜度 O(n^2)
 class Solution {
 public:
```

```
vector<vector<int> > fourSum(vector<int> &nums, int target) {
         vector<vector<int>> result;
         if (nums.size() < 4) return result;
         sort(nums.begin(), nums.end());
         unordered_map<int, vector<pair<int, int> > cache;
         for (size_t a = 0; a < nums.size(); ++a) {</pre>
             for (size t b = a + 1; b < nums.size(); ++b) {</pre>
                  cache[nums[a] + nums[b]].push back(pair<int, int>(a, b));
             }
         }
         for (int c = 0; c < nums.size(); ++c) {
             for (size t d = c + 1; d < nums.size(); ++d) {
                  const int key = target - nums[c] - nums[d];
                  if (cache.find(key) == cache.end()) continue;
                  const auto& vec = cache[key];
                 for (size_t k = 0; k < vec.size(); ++k) {</pre>
                      if (c <= vec[k].second)
                          continue; // 有重疊
                     result.push_back( { nums[vec[k].first],
                              nums[vec[k].second], nums[c], nums[d] });
                 }
             }
         sort(result.begin(), result.end());
         result.erase(unique(result.begin(), result.end()), result.end());
         return result;
     }
 };
multimap
 // LeetCode, 4Sum
 // 用一個 hashmap 先緩存兩個數的和
 // 時間複雜度 O(n^2), 空間複雜度 O(n^2)
 // @author 龔陸安(http://weibo.com/luangong)
 class Solution {
 public:
     vector<vector<int>> fourSum(vector<int>& nums, int target) {
         vector<vector<int>> result;
          if (nums.size() < 4) return result;
         sort(nums.begin(), nums.end());
         unordered_multimap<int, pair<int, int>> cache;
         for (int i = 0; i + 1 < nums.size(); ++i)
             for (int j = i + 1; j < nums.size(); ++j)
                  cache.insert(make_pair(nums[i] + nums[j], make_pair(i, j)));
         for (auto i = cache.begin(); i != cache.end(); ++i) {
```

```
int x = target - i->first;
             auto range = cache.equal range(x);
             for (auto j = range.first; j != range.second; ++j) {
                  auto a = i->second.first;
                  auto b = i->second.second;
                 auto c = j->second.first;
                 auto d = j->second.second;
                  if (a != c && a != d && b != c && b != d) {
                      vector<int> vec = { nums[a], nums[b], nums[c], nums[d] };
                      sort(vec.begin(), vec.end());
                     result.push_back(vec);
                 }
             }
         }
         sort(result.begin(), result.end());
         result.erase(unique(result.begin(), result.end()), result.end());
         return result;
     }
 };
方法 4
 // LeetCode, 4Sum
 // 先排序, 然後左右夾逼, 時間複雜度 O(n^3logn), 空間複雜度 O(1), 會超時
 // 跟方法 1 相比,表面上優化了,實際上更慢了,切記!
 class Solution {
 public:
     vector<vector<int>> fourSum(vector<int>& nums, int target) {
         vector<vector<int>> result;
         if (nums.size() < 4) return result;</pre>
         sort(nums.begin(), nums.end());
         auto last = nums.end();
         for (auto a = nums.begin(); a < prev(last, 3);</pre>
                 a = upper_bound(a, prev(last, 3), *a)) {
             for (auto b = next(a); b < prev(last, 2);</pre>
                     b = upper_bound(b, prev(last, 2), *b)) {
                  auto c = next(b);
                 auto d = prev(last);
                 while (c < d) {
                      if (*a + *b + *c + *d < target) {
                          c = upper_bound(c, d, *c);
                      } else if (*a + *b + *c + *d > target) {
                          d = prev(lower_bound(c, d, *d));
                      } else {
                         result.push_back({ *a, *b, *c, *d });
                          c = upper_bound(c, d, *c);
                          d = prev(lower_bound(c, d, *d));
                     }
                 }
             }
         }
```

```
return result;
};
```

相關題目

- Two sum, 見 §2.1.7
- 3Sum, 見 §2.1.9
- 3Sum Closest, 見 §2.1.10

2.1.12 4Sum II

描述

Given four lists A, B, C, D of integer values, compute how many tuples (i, j, k, l) there are such that A[i] + B[j] + C[k] + D[l] is zero.

To make problem a bit easier, all A, B, C, D have same length of N where $0 \le N \le 500$. All integers are in the range of -228 to 228 - 1 and the result is guaranteed to be at most 231 - 1.

Example:

```
Input:
A = [ 1, 2]
B = [-2,-1]
C = [-1, 2]
D = [ 0, 2]

Output:
2

Explanation:
The two tuples are:
1. (0, 0, 0, 1) -> A[0] + B[0] + C[0] + D[1] = 1 + (-2) + (-1) + 2 = 0
2. (1, 1, 0, 0) -> A[1] + B[1] + C[0] + D[0] = 2 + (-1) + (-1) + 0 = 0
```

Hash map

2.1.13 Remove Element

描述

Given an array and a value, remove all instances of that value in place and return the new length. The order of elements can be changed. It doesn't matter what you leave beyond the new length.

分析

無

代碼1

};

```
// LeetCode, Remove Element
 // 時間複雜度 O(n), 空間複雜度 O(1)
 class Solution {
 public:
     int removeElement(vector<int>& nums, int target) {
         int index = 0;
         for (int i = 0; i < nums.size(); ++i) {
             if (nums[i] != target) {
                 nums[index++] = nums[i];
             }
         return index;
 };
代碼 2
 // LeetCode, Remove Element
 // 使用 remove(), 時間複雜度 O(n), 空間複雜度 O(1)
 class Solution {
 public:
     int removeElement(vector<int>& nums, int target) {
         return distance(nums.begin(), remove(nums.begin(), nums.end(), target));
```

相關題目

• 無

2.1.14 Next Permutation

描述

Implement next permutation, which rearranges numbers into the lexicographically next greater permutation of numbers.

If such arrangement is not possible, it must rearrange it as the lowest possible order (ie, sorted in ascending order).

The replacement must be in-place, do not allocate extra memory.

Here are some examples. Inputs are in the left-hand column and its corresponding outputs are in the right-hand column.

```
1,2,3 \rightarrow 1,3,2

3,2,1 \rightarrow 1,2,3

1,1,5 \rightarrow 1,5,1
```

分析

算法過程如圖 2-1 所示 (來自 http://fisherlei.blogspot.com/2012/12/leetcode-next-permutation.html)。



- 1. From right to left, find the first digit (PartitionNumber)which violate the increase trend, in this example, 6 will be selected since 8,7,4,3,2 already in a increase trend.
- From right to left, find the first digit which large than PartitionNumber, call it changeNumber. Here the 7 will be selected.
- 3. Swap the PartitionNumber and ChangeNumber.
- 4. Reverse all the digit on the right of partition index.

图 2-1 下一個排列算法流程

```
// LeetCode, Next Permutation
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    void nextPermutation(vector<int> &nums) {
       next_permutation(nums.begin(), nums.end());
    }
    template<typename BidiIt>
    bool next_permutation(BidiIt first, BidiIt last) {
        // Get a reversed range to simplify reversed traversal.
        const auto rfirst = reverse_iterator<BidiIt>(last);
        const auto rlast = reverse_iterator<BidiIt>(first);
        // Begin from the second last element to the first element.
        auto pivot = next(rfirst);
        // Find `pivot`, which is the first element that is no less than its
        // successor.
                       'Prev' is used since 'pivort' is a 'reversed_iterator'.
        while (pivot != rlast && *pivot >= *prev(pivot))
```

```
++pivot;

// No such elemenet found, current sequence is already the largest
// permutation, then rearrange to the first permutation and return false.
if (pivot == rlast) {
    reverse(rfirst, rlast);
    return false;
}

// Scan from right to left, find the first element that is greater than
// `pivot`.
    auto change = find_if(rfirst, pivot, bind1st(less<int>(), *pivot));

swap(*change, *pivot);
    reverse(rfirst, pivot);
    return true;
};
```

相關題目

- Permutation Sequence, 見 §2.1.16
- Permutations, 見 §9.3
- Permutations II, 見 §9.4
- Combinations, 見 §9.5

2.1.15 Prev Permutation

描述

Implement previous permutation

```
1,2,3 \rightarrow 3,2,1

3,2,1 \rightarrow 3,1,2

1,1,5 \rightarrow 5,1,1
```

分析

無

```
// LeetCode, Previous Permutation
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
   void prevPermutation(vector<int> &nums) {
```

```
prev permutation(nums.begin(), nums.end());
    }
    template<typename BidiIt>
    bool prev_permutation(BidiIt first, BidiIt last) {
        const auto rfirst = reverse_iterator<BidiIt>(last);
        const auto rlast = reverse_iterator<BidiIt>(first);
        auto pivot = next(rfirst);
        while (pivot != rlast && *(pivot) <= *prev(pivot))
            pivot++;
        if (pivot == rlast) {
            reverse(rfirst, rlast);
            return false;
        }
        auto change = find_if(rfirst, pivot, bind1st(greater<int>(), *pivot));
        swap(*change, *pivot);
        reverse(rfirst, pivot);
        return true;
    }
};
```

相關題目

- Permutation Sequence, 見 §2.1.16
- Permutations, 見 §9.3
- Permutations II, 見 §9.4
- Combinations, 見 §9.5

2.1.16 Permutation Sequence

描述

The set $[1,2,3,\cdots,n]$ contains a total of n! unique permutations.

By listing and labeling all of the permutations in order, We get the following sequence (ie, for n = 3):

```
"123"
"132"
"213"
"231"
"312"
"321"
```

Given n and k, return the kth permutation sequence.

Note: Given n will be between 1 and 9 inclusive.

分析

簡單的,可以用暴力枚舉法,調用 k-1 次 next_permutation()。

暴力枚舉法把前k個排列都求出來了、比較浪費、而我們只需要第k個排列。

利用康託編碼的思路,假設有n個不重複的元素,第k個排列是 $a_1, a_2, a_3, ..., a_n$,那麼 a_1 是哪一個位置呢?

我們把 a_1 去掉,那麼剩下的排列為 $a_2, a_3, ..., a_n$,共計 n-1 個元素,n-1 個元素共有 (n-1)! 個排列,於是就可以知道 $a_1 = k/(n-1)!$ 。

同理, $a_2, a_3, ..., a_n$ 的值推導如下:

$$k_2 = k\%(n-1)!$$
 $a_2 = k_2/(n-2)!$
 \dots
 $k_{n-1} = k_{n-2}\%2!$
 $a_{n-1} = k_{n-1}/1!$
 $a_n = 0$

使用 next permutation()

```
// LeetCode, Permutation Sequence
// 使用 next_permutation(), TLE
class Solution {
public:
    string getPermutation(int n, int k) {
        string s(n, '0');
        for (int i = 0; i < n; ++i)
            s[i] += i+1;
        for (int i = 0; i < k-1; ++i)
            next_permutation(s.begin(), s.end());
        return s;
    }
    template<typename BidiIt>
    bool next_permutation(BidiIt first, BidiIt last) {
        // 代碼見上一題 Next Permutation
};
```

康託編碼

```
// LeetCode, Permutation Sequence
// 康託編碼, 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
```

```
string getPermutation(int n, int k) {
        string s(n, '0');
        string result;
        for (int i = 0; i < n; ++i)
            s[i] += i + 1;
        return kth_permutation(s, k);
    }
private:
    int factorial(int n) {
        int result = 1;
        for (int i = 1; i \le n; ++i)
            result *= i;
        return result;
    }
    // seq 已排好序, 是第一個排列
    template<typename Sequence>
    Sequence kth_permutation(const Sequence &seq, int k) {
        const int n = seq.size();
        Sequence S(seq);
        Sequence result;
        int base = factorial(n - 1);
        --k; // 康託編碼從 O 開始
        for (int i = n - 1; i > 0; k \% = base, base /= i, --i) {
            auto a = next(S.begin(), k / base);
            result.push_back(*a);
            S.erase(a);
        }
        result.push_back(S[0]); // 最後一個
        return result;
    }
};
```

相關題目

- Next Permutation, 見 §2.1.14
- Permutations, 見 §9.3
- Permutations II, 見 §9.4
- Combinations, 見 §9.5

2.1.17 Valid Sudoku

描述

Determine if a Sudoku is valid, according to: Sudoku Puzzles - The Rules http://sudoku.com.au/TheRules.aspx .

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The Sudoku board could be partially filled, where empty cells are filled with the character '.'.

5	3			7				
6			1	9	5			
	9	8					6	
8				6				3
4			8		3			1
7				2				6
	6					2	8	
			4	1	9			5
				8			7	9

图 2-2 A partially filled sudoku which is valid

分析

細節實現題。

```
// LeetCode, Valid Sudoku
// 時間複雜度 O(n^2), 空間複雜度 O(1)
class Solution {
public:
   bool isValidSudoku(const vector<vector<char>>& board) {
        bool used[9];
        for (int i = 0; i < 9; ++i) {
           fill(used, used + 9, false);
           for (int j = 0; j < 9; ++j) // 檢查行
                if (!check(board[i][j], used))
                   return false;
           fill(used, used + 9, false);
           for (int j = 0; j < 9; ++j) // 檢查列
               if (!check(board[j][i], used))
                   return false;
        }
        for (int r = 0; r < 3; ++r) // 檢查 9 個子格子
           for (int c = 0; c < 3; ++c) {
               fill(used, used + 9, false);
               for (int i = r * 3; i < r * 3 + 3; ++i)
```

相關題目

• Sudoku Solver, 見 §11.10

2.1.18 Trapping Rain Water

描述

Given n non-negative integers representing an elevation map where the width of each bar is 1, compute how much water it is able to trap after raining.

For example, Given

, return 6.



图 2-3 Trapping Rain Water

分析

對於每個柱子,找到其左右兩邊最高的柱子,該柱子能容納的面積就是 min(max_left, max_right) - height。所以,

- 1. 從左往右掃描一遍,對於每個柱子,求取左邊最大值;
- 2. 從右往左掃描一遍,對於每個柱子,求最大右值;
- 3. 再掃描一遍,把每個柱子的面積並累加。 也可以,
- 1. 掃描一遍, 找到最高的柱子, 這個柱子將數組分為兩半;
- 2. 處理左邊一半;
- 3. 處理右邊一半。

代碼1

```
// LeetCode, Trapping Rain Water
// 思路 1, 時間複雜度 O(n), 空間複雜度 O(n)
class Solution {
public:
    int trap(const vector<int>& A) {
        const int n = A.size();
        int *max_left = new int[n]();
        int *max_right = new int[n]();
        for (int i = 1; i < n; i++) {
            \max_{i=1}^{n} = \max(\max_{i=1}^{n} -1), A[i-1]);
            \max_{right[n-1-i]} = \max(\max_{right[n-i]}, A[n-i]);
        }
        int sum = 0;
        for (int i = 0; i < n; i++) {
            int height = min(max_left[i], max_right[i]);
            if (height > A[i]) {
                sum += height - A[i];
            }
        }
        delete[] max_left;
        delete[] max_right;
        return sum;
    }
};
```

```
// LeetCode, Trapping Rain Water
// 思路 2, 時間複雜度 O(n), 空間複雜度 O(1)
```

```
class Solution {
public:
    int trap(const vector<int>& A) {
        const int n = A.size();
        int max = 0; // 最高的柱子, 將數組分為兩半
        for (int i = 0; i < n; i++)
            if (A[i] > A[max]) max = i;
        int water = 0;
        for (int i = 0, peak = 0; i < max; i++)
            if (A[i] > peak) peak = A[i];
            else water += peak - A[i];
        for (int i = n - 1, top = 0; i > max; i--)
            if (A[i] > top) top = A[i];
            else water += top - A[i];
       return water;
   }
}:
```

代碼 3

第三種解法,用一個棧輔助,小於棧頂的元素壓入,大於等於棧頂就把棧裏所有小於或等於當前值的元素全部出棧處理掉。

```
// LeetCode, Trapping Rain Water
// 用一個棧輔助, 小於棧頂的元素壓入, 大於等於棧頂就把棧裏所有小於或
// 等於當前值的元素全部出棧處理掉, 計算面積, 最後把當前元素入棧
// 時間複雜度 O(n), 空間複雜度 O(n)
class Solution {
public:
   int trap(const vector<int>& A) {
       const int n = A.size();
       stack<pair<int, int>> s;
       int water = 0;
       for (int i = 0; i < n; ++i) {
          int height = 0;
          while (!s.empty()) { // 將棧裏比當前元素矮或等高的元素全部處理掉
              int bar = s.top().first;
              int pos = s.top().second;
             // bar, height, A[i] 三者夾成的凹陷
             water += (min(bar, A[i]) - height) * (i - pos - 1);
             height = bar;
              if (A[i] < bar) // 碰到了比當前元素高的, 跳出循環
                 break:
             else
                 s.pop(); // 彈出棧頂, 因為該元素處理完了, 不再需要了
          }
          s.push(make_pair(A[i], i));
```

```
return water;
};
```

相關題目

- Container With Most Water, 見 §13.6
- Largest Rectangle in Histogram, 見 §5.1.3

2.1.19 Rotate Image

描述

You are given an $n \times n$ 2D matrix representing an image.

Rotate the image by 90 degrees (clockwise).

Follow up: Could you do this in-place?

分析

首先想到, 純模擬, 從外到內一圈一圈的轉, 但這個方法太慢。 如下圖, 首先沿着副對角線翻轉一次, 然後沿着水平中線翻轉一次。



图 2-4 Rotate Image

或者、首先沿着水平中線翻轉一次、然後沿着主對角線翻轉一次。

```
// LeetCode, Rotate Image
// 思路 1, 時間複雜度 O(n^2), 空間複雜度 O(1)
class Solution {
public:
    void rotate(vector<vector<int>>& matrix) {
        const int n = matrix.size();

    for (int i = 0; i < n; ++i) // 沿着副對角線反轉
        for (int j = 0; j < n - i; ++j)
            swap(matrix[i][j], matrix[n - 1 - j][n - 1 - i]);

    for (int i = 0; i < n / 2; ++i) // 沿着水平中線反轉</pre>
```

```
for (int j = 0; j < n; ++j)
                 swap(matrix[i][j], matrix[n - 1 - i][j]);
     }
 };
代碼 2
 // LeetCode, Rotate Image
 // 思路 2. 時間複雜度 O(n^2). 空間複雜度 O(1)
 class Solution {
 public:
     void rotate(vector<vector<int>>& matrix) {
         const int n = matrix.size();
         for (int i = 0; i < n / 2; ++i) // 沿着水平中線反轉
             for (int j = 0; j < n; ++j)
                 swap(matrix[i][j], matrix[n - 1 - i][j]);
         for (int i = 0; i < n; ++i) // 沿着主對角線反轉
             for (int j = i + 1; j < n; ++j)
                 swap(matrix[i][j], matrix[j][i]);
     }
 };
```

相關題目

無

2.1.20 Plus One

描述

Given a number represented as an array of digits, plus one to the number.

分析

高精度加法。

```
// LeetCode, Plus One
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
   vector<int> plusOne(vector<int> &digits) {
       add(digits, 1);
       return digits;
    }
private:
```

```
// 0 <= digit <= 9
     void add(vector<int> &digits, int digit) {
         int c = digit; // carry, 進位
         for (auto it = digits.rbegin(); it != digits.rend(); ++it) {
             *it += c;
             c = *it / 10;
             *it %= 10;
         if (c > 0) digits.insert(digits.begin(), 1);
     }
 };
代碼 2
 // LeetCode, Plus One
 // 時間複雜度 O(n), 空間複雜度 O(1)
 class Solution {
 public:
     vector<int> plusOne(vector<int> &digits) {
         add(digits, 1);
         return digits;
     }
 private:
     // 0 <= digit <= 9
     void add(vector<int> &digits, int digit) {
         int c = digit; // carry, 進位
         for_each(digits.rbegin(), digits.rend(), [&c](int &d){
             d += c;
             c = d / 10;
             d \% = 10;
         });
         if (c > 0) digits.insert(digits.begin(), 1);
     }
 };
```

相關題目

無

2.1.21 Climbing Stairs

描述

You are climbing a stair case. It takes n steps to reach to the top.

Each time you can either climb 1 or 2 steps. In how many distinct ways can you climb to the top?

分析

設 f(n) 表示爬 n 階樓梯的不同方法數, 為了爬到第 n 階樓梯, 有兩個選擇:

- 從第 n-1 階前進 1 步;
- 從第 n-1 階前進 2 步;

因此, 有 f(n) = f(n-1) + f(n-2)。

這是一個斐波那契數列。

方法 1, 遞歸, 太慢; 方法 2, 迭代。

方法 3,數學公式。 斐波那契數列的通項公式為 $a_n = \frac{1}{\sqrt{5}} \left[\left(\frac{1+\sqrt{5}}{2} \right)^n - \left(\frac{1-\sqrt{5}}{2} \right)^n \right]$ 。

迭代

```
// LeetCode, Climbing Stairs
// 迭代, 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    int climbStairs(int n) {
        int prev = 0;
        int cur = 1;
        for(int i = 1; i <= n; ++i){
            int tmp = cur;
            cur += prev;
            prev = tmp;
        }
        return cur;
    }
};</pre>
```

數學公式

```
// LeetCode, Climbing Stairs
// 數學公式, 時間複雜度 O(1), 空間複雜度 O(1)
class Solution {
   public:
   int climbStairs(int n) {
      const double s = sqrt(5);
      return floor((pow((1+s)/2, n+1) + pow((1-s)/2, n+1))/s + 0.5);
   }
};
```

相關題目

• Decode Ways, 見 §14.12

2.1.22 Gray Code

描述

The gray code is a binary numeral system where two successive values differ in only one bit.

Given a non-negative integer n representing the total number of bits in the code, print the sequence of gray code. A gray code sequence must begin with 0.

For example, given n = 2, return [0,1,3,2]. Its gray code sequence is:

- 00 0
- 01 1
- 11 3
- 10 2

Note:

- For a given n, a gray code sequence is not uniquely defined.
- For example, [0,2,3,1] is also a valid gray code sequence according to the above definition.
- For now, the judge is able to judge based on one instance of gray code sequence. Sorry about that.

分析

格雷碼 (Gray Code) 的定義請參考 http://en.wikipedia.org/wiki/Gray_code

自然二進制碼轉換為格雷碼: $g_0 = b_0, g_i = b_i \oplus b_{i-1}$

保留自然二進制碼的最高位作為格雷碼的最高位,格雷碼次高位為二進制碼的高位與次高位異或,其餘各位與次高位的求法類似。例如,將自然二進制碼1001,轉換為格雷碼的過程是:保留最高位;然後將第1位的1和第2位的0異或,得到1,作為格雷碼的第2位;將第2位的0和第3位的0異或,得到0,作為格雷碼的第3位;將第3位的0和第4位的1異或,得到1,作為格雷碼的第4位,最終,格雷碼為1101。

格雷碼轉換為自然二進制碼: $b_0 = q_0, b_i = q_i \oplus b_{i-1}$

保留格雷碼的最高位作為自然二進制碼的最高位,次高位為自然二進制高位與格雷碼次高位異或,其餘各位與次高位的求法類似。例如,將格雷碼 1000 轉換為自然二進制碼的過程是:保留最高位 1,作為自然二進制碼的最高位;然後將自然二進制碼的第 1 位 1 和格雷碼的第 2 位 0 異或,得到 1,作為自然二進制碼的第 2 位;將自然二進制碼的第 2 位 1 和格雷碼的第 3 位 0 異或,得到 1,作為自然二進制碼的第 3 位;將自然二進制碼的第 3 位 1 和格雷碼的第 4 位 0 異或,得到 1,作為自然二進制碼的第 4 位 0 異或,得到 1,作為自然二進制碼的第 4 位 0 最終,自然二進制碼為 1111。

格雷碼有數學公式,整數 n 的格雷碼是 $n \oplus (n/2)$ 。

這題要求生成 n 比特的所有格雷碼。

方法 1, 最簡單的方法,利用數學公式,對從 $0 \sim 2^n - 1$ 的所有整數,轉化為格雷碼。方法 2. n 比特的格雷碼,可以遞歸地從 n-1 比特的格雷碼生成。如圖 82-5 所示。



图 2-5 The first few steps of the reflect-and-prefix method.

數學公式

```
// LeetCode, Gray Code
// 數學公式, 時間複雜度 O(2<sup>n</sup>), 空間複雜度 O(1)
class Solution {
public:
    vector<int> grayCode(int n) {
        vector<int> result;
        const size_t size = 1 << n; // 2^n</pre>
        result.reserve(size);
        for (size_t i = 0; i < size; ++i)
            result.push_back(binary_to_gray(i));
        return result;
    }
private:
    static unsigned int binary_to_gray(unsigned int n) {
        return n ^ (n >> 1);
};
```

Reflect-and-prefix method

```
// LeetCode, Gray Code
// reflect-and-prefix method
// 時間複雜度 O(2<sup>n</sup>), 空間複雜度 O(1)
class Solution {
public:
    vector<int> grayCode(int n) {
        vector<int> result;
        result.reserve(1<<n);
        result.push_back(0);
        for (int i = 0; i < n; i++) {
            const int highest_bit = 1 << i;</pre>
            for (int j = result.size() - 1; j >= 0; j--) // 要反着遍歷, 才能對稱
                result.push_back(highest_bit | result[j]);
        }
```

```
return result;
};
```

相關題目

• 無

2.1.23 Set Matrix Zeroes

描述

Given a $m \times n$ matrix, if an element is 0, set its entire row and column to 0. Do it in place.

Follow up: Did you use extra space?

A straight forward solution using O(mn) space is probably a bad idea.

A simple improvement uses O(m+n) space, but still not the best solution.

Could you devise a constant space solution?

分析

O(m+n) 空間的方法很簡單,設置兩個 bool 數組,記錄每行和每列是否存在 0。想要常數空間,可以複用第一行和第一列。

```
// LeetCode, Set Matrix Zeroes
// 時間複雜度 O(m*n), 空間複雜度 O(m+n)
class Solution {
public:
    void setZeroes(vector<vector<int> > &matrix) {
       const size_t m = matrix.size();
       const size_t n = matrix[0].size();
       vector<bool> row(m, false); // 標記該行是否存在 0
       vector<bool> col(n, false); // 標記該列是否存在 0
       for (size_t i = 0; i < m; ++i) {
           for (size_t j = 0; j < n; ++j) {
               if (matrix[i][j] == 0) {
                   row[i] = col[j] = true;
               }
           }
       for (size_t i = 0; i < m; ++i) {
           if (row[i])
               fill(&matrix[i][0], &matrix[i][0] + n, 0);
       }
```

```
for (size_t j = 0; j < n; ++j) {
             if (col[j]) {
                 for (size t i = 0; i < m; ++i) {
                     matrix[i][j] = 0;
             }
         }
     }
 };
代碼 2
 // LeetCode, Set Matrix Zeroes
 // 時間複雜度 O(m*n), 空間複雜度 O(1)
 class Solution {
 public:
     void setZeroes(vector<vector<int> > &matrix) {
         const size_t m = matrix.size();
         const size_t n = matrix[0].size();
         bool row_has_zero = false; // 第一行是否存在 0
         bool col_has_zero = false; // 第一列是否存在 0
         for (size_t i = 0; i < n; i++)
             if (matrix[0][i] == 0) {
                 row_has_zero = true;
                 break;
             }
         for (size_t i = 0; i < m; i++)
             if (matrix[i][0] == 0) {
                 col_has_zero = true;
                 break;
             }
         for (size_t i = 1; i < m; i++)
             for (size_t j = 1; j < n; j++)
                 if (matrix[i][j] == 0) {
                     matrix[0][j] = 0;
                     matrix[i][0] = 0;
                 }
         for (size_t i = 1; i < m; i++)
             for (size_t j = 1; j < n; j++)
                 if (matrix[i][0] == 0 || matrix[0][j] == 0)
                     matrix[i][j] = 0;
         if (row_has_zero)
             for (size_t i = 0; i < n; i++)
                 matrix[0][i] = 0;
         if (col_has_zero)
             for (size_t i = 0; i < m; i++)
                 matrix[i][0] = 0;
     }
 };
```

相關題目

無

2.1.24 Gas Station

描述

There are N gas stations along a circular route, where the amount of gas at station i is gas [i].

You have a car with an unlimited gas tank and it costs cost[i] of gas to travel from station i to its next station (i+1). You begin the journey with an empty tank at one of the gas stations.

Return the starting gas station's index if you can travel around the circuit once, otherwise return -1.

Note: The solution is guaranteed to be unique.

分析

首先想到的是 $O(N^2)$ 的解法,對每個點進行模擬。

O(N) 的解法是,設置兩個變量,sum 判斷當前的指針的有效性;total 則判斷整個數組是否有解,有就返回通過 sum 得到的下標,沒有則返回-1。

代碼

```
// LeetCode, Gas Station
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    int canCompleteCircuit(vector<int> &gas, vector<int> &cost) {
        int total = 0;
        int j = -1;
        for (int i = 0, sum = 0; i < gas.size(); ++i) {
            sum += gas[i] - cost[i];
            total += gas[i] - cost[i];
            if (sum < 0) {
                j = i;
                sum = 0;
            }
        }
        return total >= 0 ? j + 1 : -1;
    }
};
```

相關題目

• 無

數組 43 2.1

Candy 2.1.25

描述

There are N children standing in a line. Each child is assigned a rating value.

You are giving candies to these children subjected to the following requirements:

- Each child must have at least one candy.
- Children with a higher rating get more candies than their neighbors.

What is the minimum candies you must give?

分析

無

迭代版

```
// LeetCode, Candy
// 時間複雜度 O(n), 空間複雜度 O(n)
class Solution {
public:
    int candy(vector<int> &ratings) {
       const int n = ratings.size();
       vector<int> increment(n);
       // 左右各掃描一遍
       for (int i = 1, inc = 1; i < n; i++) {
            if (ratings[i] > ratings[i - 1])
               increment[i] = max(inc++, increment[i]);
           else
               inc = 1;
       }
       for (int i = n - 2, inc = 1; i \ge 0; i--) {
            if (ratings[i] > ratings[i + 1])
               increment[i] = max(inc++, increment[i]);
           else
               inc = 1;
       // 初始值為 n, 因為每個小朋友至少一顆糖
       return accumulate(&increment[0], &increment[0]+n, n);
    }
};
```

遞歸版

```
// LeetCode, Candy
// 備忘錄法, 時間複雜度 O(n), 空間複雜度 O(n)
// @author fancymouse (http://weibo.com/u/1928162822)
```

```
class Solution {
public:
    int candy(const vector<int>& ratings) {
        vector<int> f(ratings.size());
        int sum = 0;
        for (int i = 0; i < ratings.size(); ++i)</pre>
            sum += solve(ratings, f, i);
        return sum;
    }
    int solve(const vector<int>& ratings, vector<int>& f, int i) {
        if (f[i] == 0) {
            f[i] = 1;
            if (i > 0 && ratings[i] > ratings[i - 1])
                f[i] = max(f[i], solve(ratings, f, i - 1) + 1);
            if (i < ratings.size() - 1 && ratings[i] > ratings[i + 1])
                f[i] = max(f[i], solve(ratings, f, i + 1) + 1);
        return f[i];
    }
};
```

相關題目

• 無

2.1.26 Counting Bits

描述

Given a non negative integer number num. For every numbers i in the range $0 \le i \le num$ calculate the number of 1's in their binary representation and return them as an array.

```
Example 1:
Input: 2
Output: [0,1,1]

Example 2:
Input: 5
Output: [0,1,1,2,1,2]
```

Follow up:

- It is very easy to come up with a solution with run time O(n*sizeof(integer)). But can you do it in linear time O(n)/possibly in a single pass?
- Space complexity should be O(n).
- Can you do it like a boss? Do it without using any builtin function like __builtin_popcount in c++ or in any other language.

Pop Count

```
// 時間複雜度 O(nk), 空間複雜度 O(n)
// 思路:利用 PopCount 暴力地數每一個數字的 bit 1 的總數
class Solution {
public:
   vector<int> countBits(int num) {
       vector<int> result(num+1, 0);
       for (int i = 0; i <= num; i++)
           result[i] = PopCount(i);
       return result;
   }
private:
   int PopCount(int x)
   {
       int count;
       for (count = 0; x != 0; ++count)
           x &= x - 1; // 消除最後的的 bit 1
       return count;
   }
};
```

Approach #2 DP + Most Significant Bit [Accepted]

Intuition

Use previous count results to generate the count for a new integer.

Algorithm

Suppose we have an integer:

$$x = (1001011101)_2 = (605)_{10}$$

and we already calculated and stored all the results of 0 to x-1.

Then we know that x is differ by one bit with a number we already calculated:

$$x' = (1011101)_2 = (93)_{10}$$

They are different only in the most significant bit.

Let's exam the range [0,3] in the binary form:

- $(0) = (0)_2$
- $(1) = (1)_2$
- $(2) = (10)_2$
- $(3) = (11)_2$

One can see that the binary form of 2 and 3 can be generated by adding 1 bit in front of 0 and 1. Thus, they are different only by 1 regarding pop count.

Similarly, we can generate the results for [4,7] using [0,3] as blueprints.

In general, we have the following transition function for popcount P(x):

$$P(x+b) = P(x) + 1, b = 2^m > x$$

With this transition function, we can then apply Dynamic Programming to generate all the pop counts starting from 0.

图 2-6 counting bits

動劃 + Most Significant Bit

```
// 時間複雜度 O(n), 空間複雜度 O(n)
// 思路:當前的數字的 bit 總數, 跟前一個的 2 次方差數字的 bit 總數有關係
class Solution {
public:
    vector<int> countBits(int num) {
        vector<int> result(num+1, 0);
        int i = 0;
        int b = 1; // 這是 2 次方總數
        while (b <= num)
        {
```

Approach #3 DP + Least Significant Bit [Accepted]

Intuition

We can have different transition functions, as long as x' is smaller than x and their pop counts have a function.

Algorithm

Following the same principle of the previous approach, we can also have a transition function by playing with the least significant bit.

Let look at the relation between x and x' = x/2

```
x = (1001011101)_2 = (605)_{10}

x' = (100101110)_2 = (302)_{10}
```

We can see that x' is differ than x by one bit, because x' can be considered as the result of removing the least significant bit of x.

Thus, we have the following transition function of pop count P(x):

```
P(x) = P(x/2) + (x \mod 2)
```

图 2-7 counting bits 2

動劃 + Least Significant Bit

```
// 時間複雜度 O(n), 空間複雜度 O(n)
class Solution {
public:
    vector<int> countBits(int num) {
        vector<int> result(num+1, 0);

        for (int i = 1; i <= num; i++)
            result[i] = result[i >> 1] + (i & 1);

        return result;
    }
};
```

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動劃 + Last Set Bit

```
// 時間複雜度 O(n), 空間複雜度 O(n)
class Solution {
public:
   vector<int> countBits(int num) {
       vector<int> result(num+1, 0);
       // i & (i - 1) 會把最右 (Least Significant Bit) 除去
       for (int i = 1; i <= num; i++)
           result[i] = result[i & (i - 1)] + 1;
       return result;
   }
};
```

2.1.27 Single Number

描述

Given an array of integers, every element appears twice except for one. Find that single one.

Note: Your algorithm should have a linear runtime complexity. Could you implement it without using extra memory?

分析

異或 (XOR),不僅能處理兩次的情況,只要出現偶數次,都可以清零。

```
// LeetCode, Single Number
 // 時間複雜度 O(n), 空間複雜度 O(1)
 class Solution {
 public:
     int singleNumber(vector<int>& nums) {
         int x = 0;
         for (auto i : nums) {
             x ^= i;
         return x;
     }
 };
代碼 2
```

```
// LeetCode, Single Number
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
```

```
int singleNumber(vector<int>& nums) {
    return accumulate(nums.begin(), nums.end(), 0, bit_xor<int>());
};
```

相關題目

• Single Number II, 見 §2.1.28

2.1.28 Single Number II

描述

Given an array of integers, every element appears three times except for one. Find that single one.

Note: Your algorithm should have a linear runtime complexity. Could you implement it without using extra memory?

分析

本題和上一題 Single Number,考察的是位運算。

方法 1: 創建一個長度為 sizeof(int) 的數組 count[sizeof(int)], count[i] 表示在在 i 位出現的 1 的次數。如果 count[i] 是 3 的整數倍,則忽略;否則就把該位取出來組成答案。

方法 2: 用 one 記錄到當前處理的元素為止,二進制 1 出現 "1 次" (mod 3 之後的 1) 的有哪些二進制位;用 two 記錄到當前計算的變量為止,二進制 1 出現 "2 次" (mod 3 之後的 2) 的有哪些二進制位。當 one 和 two 中的某一位同時為 1 時表示該二進制位上 1 出現了 3 次,此時需要清零。即用二進制模擬三進制運算。最終 one 記錄的是最終結果。

```
// LeetCode, Single Number II
// 方法 1, 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
   int singleNumber(vector<int>& nums) {
       const int W = sizeof(int) * 8; // 一個整數的 bit 數, 即整數字長
       int count[W]; // count[i] 表示在在i位出現的1的次數
       fill_n(&count[0], W, 0);
       for (int i = 0; i < nums.size(); i++) {
           for (int j = 0; j < W; j++) {
               count[j] += (nums[i] >> j) & 1;
               count[j] %= 3;
           }
       }
       int result = 0;
       for (int i = 0; i < W; i++) {
           result += (count[i] << i);
```

```
return result;
     }
 };
代碼 2
 // LeetCode, Single Number II
 // 方法 2. 時間複雜度 O(n), 空間複雜度 O(1)
 class Solution {
 public:
     int singleNumber(vector<int>& nums) {
         int one = 0, two = 0, three = 0;
         for (auto i : nums) {
             two |= (one & i);
             one = i;
             three = ~(one & two);
             one &= three;
             two &= three;
         }
         return one;
     }
 };
```

相關題目

• Single Number, 見 §2.1.27

2.1.29 Duplicate Zeros

描述

Given a fixed length array arr of integers, duplicate each occurrence of zero, shifting the remaining elements to the right.

Note that elements beyond the length of the original array are not written.

Do the above modifications to the input array in place, do not return anything from your function.

Example 1:

```
Input: [1,0,2,3,0,4,5,0]
Output: null
Explanation: After calling your function, the input array is modified to: [1,0,0,2,3,0,0,4]
    Example 2:
Input: [1,2,3]
Output: null
Explanation: After calling your function, the input array is modified to: [1,2,3]
```

分析

Space Complexity O(1). Find the new last, loop from back and handle the edge case of the last zero without duplicate.

```
// LeetCode, Duplicate Zeros
 // 時間複雜度 O(n), 空間複雜度 O(1)
 class solution{
 public:
     void duplicateZeros(vector<int>& arr) {
         int N = arr.size();
         if (N < 2) return;
         // count for new last
         int last = 0;
         for (int i = 0; i < N && last < N; i++, last++) {
             if (arr[last] == 0)
                 i++:
             if (i == N) \{ // handle if the last zero need to duplicate
                 arr[i-1] = arr[last];
                 last--;
                 N--;
             }
         }
         for (int i = last - 1, right = N - 1; i >= 0 && right >= 0; i--, right--) {
             if (arr[i] == 0) {
                 arr[right--] = 0;
                 arr[right] = 0;
             }
             else
                 arr[right] = arr[i];
         }
     }
 };
代碼
 // LeetCode, Duplicate Zeros
 // 時間複雜度 O(n), 空間複雜度 O(n)
 class solution{
 public:
     void duplicateZeros(vector<int>& arr) {
         int N = arr.size();
         if (N < 2) return;
         // count for zeros
         int count = 0;
         for (const auto& a : arr) if (a == 0) count++;
```

相關題目

• 無

2.1.30 Subarray Sum Equals K

描述

Given an array of integers and an integer k, you need to find the total number of continuous subarrays whose sum equals to k.

```
Example 1:
Input: nums = [1,1,1], k = 2
Output: 2
```

分析

The idea behind this approach is as follows: If the cumulative sum(represented by sum[i]sum[i] for sum upto i-th index) upto two indices is the same, the sum of the elements lying in between those indices is zero. Extending the same thought further, if the cumulative sum upto two indices, say ii and jj is at a difference of kk i.e. if sum[i] - sum[j] = ksum[i] - sum[j] = k, the sum of elements lying between indices ii and jj is kk.

Based on these thoughts, we make use of a hashmap mapmap which is used to store the cumulative sum upto all the indices possible along with the number of times the same sum occurs. We store the data in the form: (sum_i, no. of occurences of sum_i)(sum i ,no.ofoccurencesofsum i). We traverse over the array numsnums and keep on finding the cumulative sum. Every time we encounter a new sum, we make a new entry in the hashmap corresponding to that sum. If the same sum occurs again, we increment the count corresponding to that sum in the hashmap. Further, for every sum encountered, we also determine the number of times the sum sum-ksum-k has occured already, since it will determine the number of times a subarray with sum kk has occured upto the current index. We increment the countcount by the same amount.

代碼

```
// LeetCode, Duplicate Zeros
// 時間複雜度 O(n), 空間複雜度 O(n)
class solution{
public:
   int subarraySum(vector<int>& nums, int k) {
       // 用 hash map 去存放累加總數和出現的次數
       // 設 sum[i] 為累加總數由 0 到 i
       // 若 sum[j] - sum[i] = k, 那麼由 i 到 j 之間便會有一個 k 總的子列
       unordered_map<int, int> cache; // key: cumulative sum, value: count
       cache[0] = 1; // 一定有 sum = 0
       int sum = 0;
       int count = 0;
       for (const auto& n : nums)
           sum += n;
           auto it = cache.find(sum - k);
           if (it != cache.end())
               count += it->second;
           cache[sum]++; // 加到 hash map
       }
       return count;
   }
};
```

相關題目

無

2.1.31 Candy Crush

描述

This question is about implementing a basic elimination algorithm for Candy Crush.

Given a 2D integer array board representing the grid of candy, different positive integers board[i][j] represent different types of candies. A value of board[i][j] = 0 represents that the cell at position (i, j) is empty. The given board represents the state of the game following the player's move. Now, you need to restore the board to a stable state by crushing candies according to the following rules:

• If three or more candies of the same type are adjacent vertically or horizontally, "crush" them all at the same time - these positions become empty.

 After crushing all candies simultaneously, if an empty space on the board has candies on top of itself, then these candies will drop until they hit a candy or bottom at the same time. (No new candies will drop outside the top boundary.)

- After the above steps, there may exist more candies that can be crushed. If so, you need to repeat the
 above steps.
- If there does not exist more candies that can be crushed (ie. the board is stable), then return the current board.

You need to perform the above rules until the board becomes stable, then return the current board. Example:

Input: [[110,5,112,113,114],[210,211,5,213,214],[310,311,3,313,314],[410,411,412,5,414] ,[5,1,512,3,3],[610,4,1,613,614],[710,1,2,713,714],[810,1,2,1,1],[1,1,2,2,2],[4,1,4,4,1014]]

Output: [[0,0,0,0,0],[0,0,0,0,0],[110,0,0,0,114],[210,0,0,0,214],[310,0,0,113,314], [410,0,0,213,414],[610,211,112,313,614],[710,311,412,613,714],[810,411,512,713,1014]]



图 2-8 candy crush

分析

```
// LeetCode, Candy Crush
// 時間複雜度 O(n), 空間複雜度 O(n)
class solution{
public:
    vector<vector<int>>> candyCrush(vector<vector<int>>& board) {
```

```
int M = board.size();
        int N = board[0].size();
        bool isNeedScan = true;
        while (isNeedScan)
            // check row by row
            HandleRowByRow(board, M, N);
            // check col by col
            HandleColByCol(board, M, N);
            // dropping action
            isNeedScan = DoDropAction(board, M, N);
        return board;
    }
private:
    void PrintBoard(vector<vector<int>>& board)
        for (const auto& r : board)
        {
            for (const auto& c : r)
                cout << c << "\t";
            cout << endl;</pre>
    }
    bool DoDropAction(vector<vector<int>>& board, int M, int N)
        bool isDoDrop = false;
        // do dropping col by col
        for (int j = 0; j < N; j++)
            int lowestNeg = M-1;
            while (lowestNeg >= 0 && board[lowestNeg][j] >= 0) lowestNeg--;
            if (lowestNeg >= 0) isDoDrop = true;
            // update next positive position
            int nextPositive = lowestNeg;
            while (nextPositive >= 0)
            {
                while (nextPositive >= 0 && board[nextPositive][j] < 0) nextPositive--;
                // move the data
                for (; nextPositive >= 0 && board[nextPositive][j] >= 0; nextPositive--)
                    board[lowestNeg--][j] = board[nextPositive][j];
            for (; lowestNeg >= 0; lowestNeg--)
                board[lowestNeg][j] = 0;
        }
        return isDoDrop;
    }
    void HandleRowByRow(vector<vector<int>>& board, int M, int N)
```

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```
{
        for (int i = 0; i < M; i++)
            for (int j = 0; j + 2 < N; j++)
                int cur = abs(board[i][j]);
                bool found = false;
                while (j + 2 < N \&\& cur == abs(board[i][j+1]) \&\& cur == abs(board[i][j+2]))
                    found = true;
                    board[i][j] = -cur;
                    j++;
                }
                if (found)
                    board[i][j] = -cur;
                    board[i][++j] = -cur;
                }
            }
        }
    }
    void HandleColByCol(vector<vector<int>>& board, int M, int N)
        for (int j = 0; j < N; j++)
            for (int i = 0; i + 2 < M; i++)
                int cur = abs(board[i][j]);
                bool found = false;
                while (i + 2 < M && cur == abs(board[i+1][j]) && cur == abs(board[i+2][j]))
                    found = true;
                    board[i][j] = -cur;
                    i++;
                }
                if (found)
                    board[i][j] = -cur;
                    board[++i][j] = -cur;
                }
            }
        }
    }
};
```

相關題目

• Candy Crush II, 見 §11.13

2.1.32 Intersection of Two Arrays

描述

```
Given two arrays, write a function to compute their intersection.

Example 1:

Input: nums1 = [1,2,2,1], nums2 = [2,2]

Output: [2]

Example 2:

Input: nums1 = [4,9,5], nums2 = [9,4,9,8,4]

Output: [9,4]
```

Note:

- Each element in the result must be unique.
- The result can be in any order.

分析

- Use std method
- 2. Use hash map
- 3. Sort then merge

代碼 - STD method

```
// LeetCode
// 時間複雜度 O(nlogn), 空間複雜度 O(n)
class solution{
public:
    vector<int> intersection(vector<int>& nums1, vector<int>& nums2) {
        // 先順序
        sort(nums1.begin(), nums1.end());
        sort(nums2.begin(), nums2.end());
        vector<int> result(nums1.size() + nums2.size());
        // 利用 std
        vector<int>::iterator it = set_intersection(nums1.begin(), nums1.end()
                                                   , nums2.begin(), nums2.end()
                                                   , result.begin());
        // 删去多餘的空間
        result.resize(it - result.begin());
        result.erase(unique(result.begin(), result.end()), result.end());
```

```
return result;
     }
 };
代碼 - Hash map
 // LeetCode
 // 時間複雜度 O(n), 空間複雜度 O(n)
 class solution{
 public:
     vector<int> intersection(vector<int>& nums1, vector<int>& nums2) {
         // 使用 hash map
         unordered_set<int> map1(nums1.begin(), nums1.end());
         unordered_set<int> map2(nums2.begin(), nums2.end());
         vector<int> result; result.reserve(map1.size() + map2.size());
         for (const auto& e1 : map1) {
             // 在兩個 hash map 中出現, 便是答案
             auto it = map2.find(e1);
             if (it != map2.end()) result.push_back(e1);
         return result;
     }
 };
代碼 - Merge vector
 // LeetCode
 // 時間複雜度 O(nlogn), 空間複雜度 O(n)
 class solution{
 public:
     vector<int> intersection(vector<int>& nums1, vector<int>& nums2) {
         // 朱順序
         sort(nums1.begin(), nums1.end());
         sort(nums2.begin(), nums2.end());
         vector<int> result; result.reserve(nums1.size() + nums2.size());
         // merge 兩支 vector
         for (int p1 = 0, p2 = 0; p1 < nums1.size() && p2 < nums2.size()) {
             if (nums1[p1] < nums2[p2])
                 p1++;
             else if (nums1[p1] > nums2[p2])
                 p2++;
             else {
                 result.push_back(nums1[p1]);
                 p1++;
                 p2++;
             }
         }
         // 除去重覆
         result.erase(unique(result.begin(), result.end()), result.end());
```

```
return result;
};
```

2.1.33 Find the Duplicate Number

描述

Given an array nums containing n + 1 integers where each integer is between 1 and n (inclusive), prove that at least one duplicate number must exist. Assume that there is only one duplicate number, find the duplicate one.

```
Example 1:
 Input: [1,3,4,2,2]
 Output: 2
   Example 2:
 Input: [3,1,3,4,2]
 Output: 3
分析
   Nil
代碼 - Cycle - bucket sort
 // LeetCode
 // 時間複雜度 O(nlogn), 空間複雜度 O(n)
 class solution{
 public:
     int findDuplicate(vector<int>& nums) {
         // 這個跟 cycle linked list 差不多
         // 重覆的 element 會形成 cycle
         int fast = nums[0];
         int slow = nums[0];
         do {
             fast = nums[nums[fast]];
             slow = nums[slow];
         } while (fast != slow);
         int slow2 = nums[0];
         while (slow2 != slow) {
             slow2 = nums[slow2];
             slow = nums[slow];
```

return slow2;

```
};
```

2.1.34 Find K-th Smallest Pair Distance

描述

Given an integer array, return the k-th smallest distance among all the pairs. The distance of a pair (A, B) is defined as the absolute difference between A and B.

```
Example 1:
```

```
Input: nums = [1,3,1]  
k = 1  
Output: 0  
Explanation: Here are all the pairs:  
(1,3) \rightarrow 2  
(1,1) \rightarrow 0  
(3,1) \rightarrow 2  
Then the 1st smallest distance pair is (1,1), and its distance is 0.

• 2 \le len(nums) \le 10000.

• 0 \le nums[i] \le 1000000.

• 1 \le k \le len(nums) * (len(nums) - 1) / 2.
```

分析

估一個 distance 值,數一數有多少個 distance 值係細過此一估值。然後以二分法原則去調整估值的大細。

```
// LeetCode
// 時間複雜度 O(nlogn), 空間複雜度 O(n)
class Solution {
public:
    int smallestDistancePair(vector<int>& nums, int k) {
        if (nums.size() == 0) return 0;
        sort(nums.begin(), nums.end());

    int lo = 0;
    int hi = nums[nums.size() - 1] - nums[0];
    while (lo < hi) {
        int mi = lo + (hi - lo) / 2; // 得出估值
        int count = 0, left = 0;
        for (int right = 0; right < nums.size(); ++right) {
            while (nums[right] - nums[left] > mi) left++;
            count += right - left;
```

```
}
//count = number of pairs with distance <= mi
if (count >= k) hi = mi; // 二分法來調整估值大細
else lo = mi + 1;
}
return lo;
}
};
```

2.1.35 Find Pivot Index

描述

Given an array of integers nums, write a method that returns the "pivot" index of this array.

We define the pivot index as the index where the sum of all the numbers to the left of the index is equal to the sum of all the numbers to the right of the index.

If no such index exists, we should return -1. If there are multiple pivot indexes, you should return the left-most pivot index.

```
Example 1:

Input: nums = [1,7,3,6,5,6]

Output: 3

Explanation:

The sum of the numbers to the left of index 3 (nums[3] = 6) is equal to the sum of numbers to Also, 3 is the first index where this occurs.

Example 2:

Input: nums = [1,2,3]

Output: -1

Explanation:

There is no index that satisfies the conditions in the problem statement.
```

分析

先計算總數,往右走,每走一步都會跟左邊總加值對比。

```
// LeetCode
// 時間複雜度 O(), 空間複雜度 O()
class Solution {
public:
    int pivotIndex(vector<int>& nums) {
        int sum = 0, leftsum = 0;
        for (int x: nums) sum += x;
        for (int i = 0; i < nums.size(); ++i) {
            if (leftsum == sum - leftsum - nums[i]) return i;
            leftsum += nums[i];</pre>
```

```
}
    return -1;
}
```

2.1.36 Largest Number At Least Twice of Others

描述

In a given integer array nums, there is always exactly one largest element.

Find whether the largest element in the array is at least twice as much as every other number in the array.

If it is, return the index of the largest element, otherwise return -1.

```
Example 1:
```

```
Input: nums = [3, 6, 1, 0]
Output: 1
Explanation: 6 is the largest integer, and for every other number in the array x, 6 is more than twice as big as x. The index of value 6 is 1, so we return 1.

Example 2:
Input: nums = [1, 2, 3, 4]
Output: -1
Explanation: 4 isn't at least as big as twice the value of 3, so we return -1.

Note:
```

- nums will have a length in the range [1, 50].
- Every nums[i] will be an integer in the range [0, 99].

分析

first pass 先求得最大值, second pass 找尋第二大的一倍數值, 若過大, 回值-1

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```
maxIndex = i;
}

for (int i = 0; i < N; i++) {
    if (firstMax > nums[i])
        if (firstMax < 2 * nums[i]) return -1;
}

return maxIndex;
}
</pre>
```

2.1.37 Array Partition I

描述

Given an array of 2n integers, your task is to group these integers into n pairs of integer, say (a1, b1), (a2, b2), ..., (an, bn) which makes sum of min(ai, bi) for all i from 1 to n as large as possible.

```
Example 1:
```

```
Input: [1,4,3,2]
Output: 4
Explanation: n is 2, and the maximum sum of pairs is 4 = min(1, 2) + min(3, 4).
Note:
```

- n is a positive integer, which is in the range of [1, 10000].
- All the integers in the array will be in the range of [-10000, 10000].

分析

Nil

```
// LeetCode
// 時間複雜度 O(n), 空間複雜度 O(n)
class Solution {
public:
    int arrayPairSum(vector<int>& nums) {
        vector<int> arr(20001, 0);
        int shift = 10000;
        for (const int& num : nums)
            arr[num + shift]++;
        int d = 0, sum = 0;
        for (int i = -10000; i <= 10000; i++)
        {
            sum += (arr[i + shift] + 1 - d) / 2 * i;
            d = (2 + arr[i + shift] - d) % 2; // 在前邊加 2, 用來防止負數的出現。
```

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```
return sum;
     }
 };
代碼
 // LeetCode
 // 時間複雜度 O(nlogn), 空間複雜度 O(1)
 class Solution {
 public:
      int arrayPairSum(vector<int>& nums) {
          sort(nums.begin(), nums.end());
          int sum = 0;
          for (int i = 0; i < nums.size(); i += 2)
              sum += nums[i];
         return sum;
     }
 };
2.1.38
        Rotate Array
描述
   Given an array, rotate the array to the right by k steps, where k is non-negative.
   Example 1:
 Input: nums = [1,2,3,4,5,6,7], k = 3
 Output: [5,6,7,1,2,3,4]
 Explanation:
 rotate 1 steps to the right: [7,1,2,3,4,5,6]
 rotate 2 steps to the right: [6,7,1,2,3,4,5]
 rotate 3 steps to the right: [5,6,7,1,2,3,4]
   Example 2:
 Input: nums = [-1,-100,3,99], k = 2
 Output: [3,99,-1,-100]
 Explanation:
 rotate 1 steps to the right: [99,-1,-100,3]
 rotate 2 steps to the right: [3,99,-1,-100]
額外的空間
 // LeetCode
 // 時間複雜度 O(n), 空間複雜度 O(n)
 class Solution {
 public:
```

void rotate(vector<int>& nums, int k) {
 vector<int> a(nums.size());

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```
for (int i = 0; i < nums.size(); i++)</pre>
             a[(i + k) \% nums.size()] = nums[i];
        nums = a;
    }
};
```

循環取代法

Look at the following example to clarify the process:

```
nums: [1, 2, 3, 4, 5, 6]
k: 2
```



图 2-9 cyclic replacements

```
// LeetCode
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    void rotate(vector<int>& nums, int k) {
        k = k % nums.size();
        int count = 0;
        for (int start = 0; count < nums.size(); start++) {</pre>
            int current = start;
            int prev = nums[start];
            do {
                int next = (current + k) % nums.size();
                int temp = nums[next];
                nums[next] = prev;
                prev = temp;
                current = next;
                count++;
            } while (start != current);
        }
    }
};
```

reverse

```
Original List
                                : 1 2 3 4 5 6 7
                                : 7 6 5 4 3 2 1
After reversing all numbers
```

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```
After reversing first k numbers : 5 6 7 4 3 2 1
After revering last n-k numbers : 5 6 7 1 2 3 4 --> Result
// LeetCode
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    void rotate(vector<int>& nums, int k) {
        k %= nums.size();
        reverse(nums, 0, nums.size() - 1);
        reverse(nums, 0, k - 1);
        reverse(nums, k, nums.size() - 1);
    }
private:
    void reverse(vector<int>& nums, int start, int end) {
        while (start < end) {
            int temp = nums[start];
            nums[start] = nums[end];
            nums[end] = temp;
            start++;
            end--;
        }
    }
};
```

2.1.39 Reverse Words in a String

描述

```
Given an input string, reverse the string word by word.
```

```
Example 1:
```

```
Input: "the sky is blue"
Output: "blue is sky the"

Example 2:
Input: " hello world! "
Output: "world! hello"
Explanation: Your reversed string should not contain leading or trailing spaces.
    Example 3:
Input: "a good example"
```

Note:

Output: "example good a"

- A word is defined as a sequence of non-space characters.
- Input string may contain leading or trailing spaces. However, your reversed string should not contain leading or trailing spaces.

Explanation: You need to reduce multiple spaces between two words to a single space in the rev

You need to reduce multiple spaces between two words to a single space in the reversed string.

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分析

Reverse

```
// LeetCode
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
   string reverseWords(string s) {
       if (s.size() == 0) return s;
       // 整段 reverse
       MyReverse(s.begin(), s.end());
       // 每個字 reverse
       auto cur = s.begin();
       auto next = cur;
       while (next < s.end())
       {
           // 尋找字的開端
           cur = find_if(cur, s.end(), [&](const char& c) { return (c != ' '); });
           // 尋找空白的開端
           next = find if(cur, s.end(), [&](const char& c) { return (c == ' '); });
           MyReverse(cur, next);
           cur = next;
       }
       // 對應的 std 方法
       // s.erase(s.find_last_not_of(' ')+1); // 移除領先空格
       // s.erase(0, s.find_first_not_of(' ')); // 移除尾隨空格
       s.erase(InPlaceRemoveSpace(s.begin(), s.end());
       return s;
   }
private:
   template <class RandIT>
       RandIT InPlaceRemoveSpace(RandIT first, RandIT last)
       bool isFirst = true;
       // 移除領先空格, 尾隨空格, 中間多餘空格
       auto cur = first;
       while (first < last)
       {
           // 找尋下一個字
           first = find_if(first, last, [&](const char& c) { return (c != ' '); });
           if (first >= last) break;
           if (!isFirst) *cur++ = ' '; // 只有當不是第一個文字, 會加入空格
           while (first < last && *first != ' ') *cur++ = *first++; // 補上文字, 直至空格出現
           if (first >= last) break;
```

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```
isFirst = false;
        }
        return cur;
    }
    template <class RandIT>
        void MyReverse(RandIT first, RandIT last)
    {
        last--;
        while (first < last)
            // 進行 swap
            auto tmp = *last;
            *last-- = *first;
            *first++ = tmp;
        }
    }
};
```

2.1.40 Happy Number

描述

Write an algorithm to determine if a number n is "happy".

A happy number is a number defined by the following process: Starting with any positive integer, replace the number by the sum of the squares of its digits, and repeat the process until the number equals 1 (where it will stay), or it loops endlessly in a cycle which does not include 1. Those numbers for which this process ends in 1 are happy numbers.

Return True if n is a happy number, and False if not.

Example:

```
Input: 19
Output: true
Explanation:
1^2 + 9^2 = 82
8^2 + 2^2 = 68
6^2 + 8^2 = 100
1^2 + 0^2 + 0^2 = 1
```

2.1 數組

利用循環特性



Based on our exploration so far, we'd expect continually following links to end in one of three ways. 1. It eventually gets to 1. 2. It eventually gets stuck in a cycle. 3. It keeps going higher and higher, up towards infinity.

That 3rd option sounds really annoying to detect and handle. How would we even know that it is going to continue going up, rather than eventually going back down, possibly to 1? Luckily, it turns out we don't need to worry about it. Think carefully about what the largest next number we could get for each number of digits is.

Digits	Largest	Next
1	9	81
2	99	162
3	999	243
4	9999	324
13	99999999999	1053

图 2-10 Why have loop

```
// LeetCode
// 時間複雜度 O(n), 空間複雜度 O(n)
class Solution {
public:
    bool isHappy(int n) {
        unordered_set<int> seen;

        // 由例子中可以看到, 若果計不到 1 , 便會重覆
        // 並且不會愈計愈大, 所以可以用這個方法
        while (n != 1 && seen.find(n) == seen.end())
         {
             seen.insert(n);
             n = GetNext(n);
        }

        return n == 1;
    }
private:
```

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```
int GetNext(int n)
         int result = 0;
         while (n)
             int d = n \% 10;
             result += d * d;
             n /= 10;
         return result;
     }
 };
快慢雙指針法
 // LeetCode
 // 時間複雜度 O(logN), 空間複雜度 O(1)
 class Solution {
 public:
     bool isHappy(int n) {
         int slow = n;
         int fast = GetNext(slow);
         while (fast != 1 && fast != slow)
             slow = GetNext(slow);
             fast = GetNext(GetNext(fast));
         }
         return fast == 1;
     }
 private:
     int GetNext(int n)
         int result = 0;
         while (n)
         {
             int d = n \% 10;
             result += d * d;
             n /= 10;
         return result;
     }
 };
數學規則
 // LeetCode
 // 時間複雜度 O(logN), 空間複雜度 O(1)
 class Solution {
```

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```
public:
   bool isHappy(int n) {
        // 通過觀察, 只有以下路徑會循環
        // 4 -> 16 -> 37 -> 58 -> 89 -> 145 -> 42 -> 20 -> 4
       while (n != 1 && n != 4)
           n = GetNext(n);
       return n == 1;
   }
private:
    int GetNext(int n)
    {
        int result = 0;
        while (n)
            int d = n \% 10;
           result += d * d;
           n /= 10;
       return result;
   }
};
```

2.1.41 Isomorphic Strings

描述

Given two strings s and t, determine if they are isomorphic.

Two strings are isomorphic if the characters in s can be replaced to get t.

All occurrences of a character must be replaced with another character while preserving the order of characters. No two characters may map to the same character but a character may map to itself.

```
Example 1:
Input: s = "egg", t = "add"
Output: true

Example 2:
Input: s = "foo", t = "bar"
Output: false

Example 3:
Input: s = "paper", t = "title"
Output: true

字母 hash

// LeetCode
// 時間複雜度 O(n), 空間複雜度 O(n)
class Solution {
```

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```
public:
    bool isIsomorphic(string s, string t) {
        vector<char> v1(256, 0);
        vector<char> v2(256, 0);

        for (size_t i = 0; i < s.size(); i++)
        {
             if (v1[s[i]] != 0 && v1[s[i]] != t[i]) return false;
             if (v2[t[i]] != 0 && v2[t[i]] != s[i]) return false;

             v1[s[i]] = t[i];
             v2[t[i]] = s[i];
         }

        return true;
    }
};</pre>
```

2.1.42 Group Shifted Strings

描述

Given a string, we can "shift" each of its letter to its successive letter, for example: "abc" -> "bcd". We can keep "shifting" which forms the sequence:

```
"abc" -> "bcd" -> ... -> "xyz"
```

Given a list of non-empty strings which contains only lowercase alphabets, group all strings that belong to the same shifting sequence.

```
Example:
Input: ["abc", "bcd", "acef", "xyz", "az", "ba", "a", "z"],
Output:
[
    ["abc","bcd","xyz"],
    ["az","ba"],
    ["acef"],
    ["a","z"]
]
```

暴力 shift

```
// LeetCode
// 時間複雜度 O(n), 空間複雜度 O(n)
class Solution {
public:
    vector<vector<string>> groupStrings(vector<string>& strings) {
        unordered_map<string, vector<string>> hashMap;
        for(auto &str : strings) {
            string temp = str;
            convertStringToKey(temp);
        }
}
```

2.1 數組 73

```
hashMap[temp].push_back(str);
          }
          vector<vector<string>> answer;
          for(auto it = hashMap.begin(); it != hashMap.end(); ++it) {
              answer.push_back(it->second);
          return answer;
      }
 private:
     void convertStringToKey(string &str) {
          while(str[0] != 'a') {
              for(int i = 0; i < str.size(); ++i) {</pre>
                  str[i] += 1;
                  if(str[i] > 'z') {
                      str[i] = 'a';
                  }
              }
          }
     }
 };
Counting shift
 // LeetCode
 // 時間複雜度 O(n), 空間複雜度 O(n)
 class Solution {
 public:
      vector<vector<string>> groupStrings(vector<string>& strings) {
          unordered_map<string, vector<string>> hashMap;
          for(auto &str : strings) {
              string temp = str;
              convertStringToKey(temp);
              hashMap[temp].push_back(str);
          }
          vector<vector<string>> answer;
          for(auto it = hashMap.begin(); it != hashMap.end(); ++it) {
              answer.push_back(it->second);
          return answer;
      }
 private:
     void convertStringToKey(string &str) {
          if (str.size() == 0) return;
          if (str[0] != 'a')
          {
              int diffFromA = str[0] - 'a';
              for (size_t i = 0; i < str.size(); ++i)</pre>
                  if ((str[i] - 'a') < diffFromA)</pre>
```

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第 3 章 鏈表

3.1 單鏈表

```
單鏈表節點的定義如下:
// 單鏈表節點
struct ListNode {
   int val;
   ListNode *next;
   ListNode(int x): val(x), next(nullptr) { }
};
```

3.1.1 Add Two Numbers

描述

You are given two linked lists representing two non-negative numbers. The digits are stored in reverse order and each of their nodes contain a single digit. Add the two numbers and return it as a linked list.

```
Input: (2 -> 4 -> 3) + (5 -> 6 -> 4)
Output: 7 -> 0 -> 8
```

分析

跟 Add Binary (見 §4.5) 很類似

```
// LeetCode, Add Two Numbers
// 跟 Add Binary 很類似
// 時間複雜度 O(m+n), 空間複雜度 O(1)
class Solution {
public:
    ListNode *addTwoNumbers(ListNode *11, ListNode *12) {
        ListNode dummy(-1); // 頭節點
        int carry = 0;
        ListNode *prev = &dummy;
        for (ListNode *pa = 11, *pb = 12;
```

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```
pa != nullptr || pb != nullptr;
    pa = pa == nullptr ? nullptr : pa->next,
    pb = pb == nullptr ? nullptr : pb->next,
    prev = prev->next) {
        const int ai = pa == nullptr ? 0 : pa->val;
        const int bi = pb == nullptr ? 0 : pb->val;
        const int value = (ai + bi + carry) % 10;
        carry = (ai + bi + carry) / 10;
        prev->next = new ListNode(value); // 尾插法
    }
    if (carry > 0)
        prev->next = new ListNode(carry);
    return dummy.next;
}
```

相關題目

• Add Binary, 見 §4.5

3.1.2 Reverse Linked List II

描述

Reverse a linked list from position m to n. Do it in-place and in one-pass.

```
For example: Given 1->2->3->4->5->nullptr, m=2 and n=4, return 1->4->3->2->5->nullptr.
```

Note: Given m, n satisfy the following condition: $1 \le m \le n \le length$ of list.

分析

這題非常繁瑣,有很多邊界檢查, 15 分鐘內做到 bug free 很有難度!

```
// LeetCode, Reverse Linked List II
// 迭代版, 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    ListNode *reverseBetween(ListNode *head, int m, int n) {
        ListNode dummy(-1);
        dummy.next = head;

    ListNode *prev = &dummy;
    for (int i = 0; i < m-1; ++i)
        prev = prev->next;
    ListNode* const head2 = prev;
```

```
prev = head2->next;
    ListNode *cur = prev->next;
    for (int i = m; i < n; ++i) {
        prev->next = cur->next;
        cur->next = head2->next;
        head2->next = cur; // 頭插法
        cur = prev->next;
    }
    return dummy.next;
}
```

相關題目

• 無

3.1.3 Partition List

描述

Given a linked list and a value x, partition it such that all nodes less than x come before nodes greater than or equal to x.

You should preserve the original relative order of the nodes in each of the two partitions.

For example, Given 1->4->3->2->5->2 and x = 3, return 1->2->2->3->4->5.

分析

無

```
// LeetCode, Partition List
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    ListNode* partition(ListNode* head, int x) {
        ListNode left_dummy(-1); // 頭結點
        ListNode right_dummy(-1); // 頭結點

        auto left_cur = &left_dummy;
        auto right_cur = &right_dummy;

        for (ListNode *cur = head; cur; cur = cur->next) {
            if (cur->val < x) {
                left_cur = cur;
                left_cur = cur
```

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```
right_cur->next = cur;
right_cur = cur;
}
}
left_cur->next = right_dummy.next;
right_cur->next = nullptr;
return left_dummy.next;
}
};
```

相關題目

• 無

3.1.4 Remove Duplicates from Sorted List

描述

Given a sorted linked list, delete all duplicates such that each element appear only once.

For example,

Given 1->1->2, return 1->2.

Given 1->1->2->3, return 1->2->3.

分析

無

遞歸版

```
// LeetCode, Remove Duplicates from Sorted List
// 遞歸版, 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    ListNode *deleteDuplicates(ListNode *head) {
        if (!head) return head;
        ListNode dummy(head->val + 1); // 值只要跟 head 不同即可
        dummy.next = head;

        recur(&dummy, head);
        return dummy.next;
    }
private:
    static void recur(ListNode *prev, ListNode *cur) {
        if (cur == nullptr) return;
        if (prev->val == cur->val) { // 刪除 head
```

```
prev->next = cur->next;
             delete cur;
             recur(prev, prev->next);
         } else {
             recur(prev->next, cur->next);
     }
 };
迭代版
 // LeetCode, Remove Duplicates from Sorted List
 // 迭代版, 時間複雜度 O(n), 空間複雜度 O(1)
 class Solution {
 public:
     ListNode *deleteDuplicates(ListNode *head) {
         if (head == nullptr) return nullptr;
         for (ListNode *prev = head, *cur = head->next; cur; cur = prev->next) {
             if (prev->val == cur->val) {
                 prev->next = cur->next;
                 delete cur;
             } else {
                 prev = cur;
         return head;
     }
 };
```

相關題目

• Remove Duplicates from Sorted List II, 見 §3.1.5

3.1.5 Remove Duplicates from Sorted List II

描述

Given a sorted linked list, delete all nodes that have duplicate numbers, leaving only distinct numbers from the original list.

```
For example,
Given 1->2->3->4->4->5, return 1->2->5.
Given 1->1->1->2->3, return 2->3.
```

分析

無

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遞歸版

```
// LeetCode, Remove Duplicates from Sorted List II
 // 遞歸版, 時間複雜度 O(n), 空間複雜度 O(1)
 class Solution {
 public:
     ListNode *deleteDuplicates(ListNode *head) {
         if (!head || !head->next) return head;
         ListNode *p = head->next;
         if (head->val == p->val) {
             while (p && head->val == p->val) {
                 ListNode *tmp = p;
                 p = p->next;
                 delete tmp;
             }
             delete head;
             return deleteDuplicates(p);
         } else {
             head->next = deleteDuplicates(head->next);
             return head;
     }
 }:
迭代版
 // LeetCode, Remove Duplicates from Sorted List II
 // 迭代版, 時間複雜度 O(n), 空間複雜度 O(1)
 class Solution {
 public:
     ListNode *deleteDuplicates(ListNode *head) {
         if (head == nullptr) return head;
         ListNode dummy(INT_MIN); // 頭結點
         dummy.next = head;
         ListNode *prev = &dummy, *cur = head;
         while (cur != nullptr) {
             bool duplicated = false;
             while (cur->next != nullptr && cur->val == cur->next->val) {
                 duplicated = true;
                 ListNode *temp = cur;
                 cur = cur->next;
                 delete temp;
             if (duplicated) { // 刪除重複的最後一個元素
                 ListNode *temp = cur;
                 cur = cur->next;
                 delete temp;
                 continue;
             }
             prev->next = cur;
             prev = prev->next;
```

```
cur = cur->next;
          }
          prev->next = cur;
          return dummy.next;
 };
迭代版
 // LeetCode, Remove Duplicates from Sorted List II
  // 迭代版, 時間複雜度 O(n), 空間複雜度 O(1)
 class Solution {
 public:
      ListNode *deleteDuplicates(ListNode *head) {
          if (head == nullptr) return head;
          ListNode dummy(INT_MIN); dummy.next = head;
         ListNode *prev = &dummy;
         ListNode *cur = head;
         ListNode *next = cur != nullptr ? cur->next : nullptr;
          while (next != nullptr) {
              bool duplicated = false;
              while (next && cur->val == next->val) {
                  duplicated = true;
                  prev->next = next;
                  delete cur;
                  cur = next;
                  next = cur != nullptr ? cur->next : nullptr;
              if (duplicated) {
                  prev->next = next;
                  delete cur;
              }
              else
                  prev = cur;
              cur = next;
              next = cur != nullptr ? cur->next : nullptr;
         return dummy.next;
     }
 };
```

相關題目

• Remove Duplicates from Sorted List, 見 §3.1.4

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3.1.6 Rotate List

描述

Given a list, rotate the list to the right by k places, where k is non-negative.

For example: Given 1-2-3-4-5-nullptr and k = 2, return 4-5-1-2-3-nullptr.

分析

先遍歷一遍,得出鏈表長度 len,注意 k 可能大於 len,因此令 k% = len。將尾節點 next 指針指向首節點,形成一個環,接着往後跑 len - k 步,從這裏斷開,就是要求的結果了。

代碼

```
// LeetCode, Remove Rotate List
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
   ListNode *rotateRight(ListNode *head, int k) {
        if (head == nullptr || k == 0) return head;
       int len = 1;
       ListNode* p = head;
       while (p->next) { // 求長度
           len++;
           p = p->next;
       k = len - k \% len;
       p->next = head; // 首尾相連
       for(int step = 0; step < k; step++) {</pre>
           p = p->next; //接着往後跑
       head = p->next; // 新的首節點
       p->next = nullptr; // 斷開環
       return head;
    }
};
```

相關題目

• 無

3.1.7 Rotate List II

描述

Given a list, rotate the list to the left by k places, where k is non-negative.

For example: Given 1->2->3->4->5->nullptr and k = 2, return 4->5->1->2->3->nullptr.

分析

先遍歷一遍,得出鏈表長度 len,注意 k 可能大於 len,因此令 k% = len。將尾節點 next 指針指向首節點,形成一個環,接着往後跑 len - k 步,從這裏斷開,就是要求的結果了。

代碼

```
// LeetCode, Remove Rotate List
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
   ListNode *rotateRight(ListNode *head, int k) {
        if (head == nullptr || k == 0) return head;
       int len = 1;
       ListNode* p = head;
       while (p->next) { // 求長度
           len++;
           p = p->next;
       k = k % len; // This is the only difference
       p->next = head; // 首尾相連
       for(int step = 0; step < k; step++) {</pre>
           p = p->next; //接着往後跑
       head = p->next; // 新的首節點
       p->next = nullptr; // 斷開環
       return head;
    }
};
```

相關題目

無

3.1.8 Remove Nth Node From End of List

描述

Given a linked list, remove the n^{th} node from the end of list and return its head.

For example, Given linked list: 1->2->3->4->5, and n=2.

After removing the second node from the end, the linked list becomes 1->2->3->5.

Note:

Given n will always be valid.

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• Try to do this in one pass.

分析

設兩個指針 p,q, 讓 q 先走 n 步, 然後 p 和 q 一起走, 直到 q 走到尾節點, 刪除 p->next 即可。

代碼

```
// LeetCode, Remove Nth Node From End of List
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    ListNode *removeNthFromEnd(ListNode *head, int n) {
        ListNode dummy{-1, head};
        ListNode *p = &dummy, *q = &dummy;
        for (int i = 0; i < n; i++) // q 先走 n 步
            q = q-\text{next};
        while(q->next) { // 一起走
            p = p->next;
            q = q->next;
        ListNode *tmp = p->next;
        p->next = p->next->next;
        delete tmp;
        return dummy.next;
    }
};
```

相關題目

• 無

3.1.9 Swap Nodes in Pairs

描述

Given a linked list, swap every two adjacent nodes and return its head.

For example, Given 1->2->3->4, you should return the list as 2->1->4->3.

Your algorithm should use only constant space. You may <u>not</u> modify the values in the list, only nodes itself can be changed.

分析

無

代碼

```
// LeetCode, Swap Nodes in Pairs
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    ListNode *swapPairs(ListNode *head) {
       if (head == nullptr || head->next == nullptr) return head;
       ListNode dummy(-1);
       dummy.next = head;
       for(ListNode *prev = &dummy, *cur = prev->next, *next = cur->next;
               prev = cur, cur = cur->next, next = cur ? cur->next: nullptr) {
           prev->next = next;
           cur->next = next->next;
           next->next = cur;
       return dummy.next;
   }
};
  下面這種寫法更簡潔,但題目規定了不允許這樣做。
// LeetCode, Swap Nodes in Pairs
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
   ListNode* swapPairs(ListNode* head) {
       ListNode* p = head;
       while (p && p->next) \{
           swap(p->val, p->next->val);
           p = p->next->next;
       return head;
   }
};
```

相關題目

• Reverse Nodes in k-Group, 見 §3.1.10

3.1.10 Reverse Nodes in k-Group

描述

Given a linked list, reverse the nodes of a linked list k at a time and return its modified list.

If the number of nodes is not a multiple of k then left-out nodes in the end should remain as it is.

You may not alter the values in the nodes, only nodes itself may be changed.

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```
Only constant memory is allowed.
   For example, Given this linked list: 1->2->3->4->5
   For k = 2, you should return: 2->1->4->3->5
   For k = 3, you should return: 3->2->1->4->5
分析
    無
遞歸版
 // LeetCode, Reverse Nodes in k-Group
 // 遞歸版, 時間複雜度 O(n), 空間複雜度 O(1)
 class Solution {
 public:
     ListNode *reverseKGroup(ListNode *head, int k) {
          if (head == nullptr || head->next == nullptr || k < 2)
              return head;
          ListNode *next_group = head;
          for (int i = 0; i < k; ++i) {
              if (next_group)
                  next_group = next_group->next;
              else
                  return head;
          // next_group is the head of next group
          // new_next_group is the new head of next group after reversion
         ListNode *new_next_group = reverseKGroup(next_group, k);
         ListNode *prev = new_next_group, *cur = head;
          while (cur != next_group) {
              ListNode *next = cur->next;
             cur->next = prev;
             prev = cur;
             cur = next;
          return prev; // prev will be the new head of this group
 };
迭代版
 // LeetCode, Reverse Nodes in k-Group
 // 迭代版, 時間複雜度 O(n), 空間複雜度 O(1)
```

class Solution {

ListNode dummy(-1);
dummy.next = head;

ListNode *reverseKGroup(ListNode *head, int k) {

if (head == nullptr || head->next == nullptr || k < 2) return head;

public:

```
for(ListNode *prev = &dummy, *end = head; end; end = prev->next) {
           for (int i = 1; i < k && end; i++)
               end = end->next;
           if (end == nullptr) break; // 不足 k 個
           prev = reverse(prev, prev->next, end);
       }
       return dummy.next;
    }
    // prev 是 first 前一個元素, [begin, end] 閉區間, 保證三者都不為 null
    // 返回反轉後的倒數第1個元素
   ListNode* reverse(ListNode *prev, ListNode *begin, ListNode *end) {
       ListNode *end_next = end->next;
       for (ListNode *p = begin, *cur = p->next, *next = cur->next;
               cur != end_next;
               p = cur, cur = next, next = next ? next->next : nullptr) {
           cur->next = p;
       begin->next = end_next;
       prev->next = end;
       return begin;
   }
};
```

相關題目

• Swap Nodes in Pairs, 見 §3.1.9

3.1.11 Copy List with Random Pointer

描述

A linked list is given such that each node contains an additional random pointer which could point to any node in the list or null.

Return a deep copy of the list.

分析

無

```
// LeetCode, Copy List with Random Pointer
// 兩遍掃描, 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
```

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```
public:
    RandomListNode *copyRandomList(RandomListNode *head) {
        for (RandomListNode* cur = head; cur != nullptr; ) {
            RandomListNode* node = new RandomListNode(cur->label);
            node->next = cur->next;
            cur->next = node;
            cur = node->next;
        }
        for (RandomListNode* cur = head; cur != nullptr; ) {
            if (cur->random != NULL)
                cur->next->random = cur->random->next;
            cur = cur->next->next;
        }
        // 分拆兩個單鏈表
        RandomListNode dummy(-1);
        for (RandomListNode* cur = head, *new_cur = &dummy;
                cur != nullptr; ) {
            new_cur->next = cur->next;
            new_cur = new_cur->next;
            cur->next = cur->next->next;
            cur = cur->next;
        return dummy.next;
    }
};
```

相關題目

• 無

3.1.12 Linked List Cycle

描述

Given a linked list, determine if it has a cycle in it.

Follow up: Can you solve it without using extra space?

分析

最容易想到的方法是,用一個哈希表 unordered_map<int, bool> visited, 記錄每個元素是 否被訪問過,一旦出現某個元素被重複訪問,説明存在環。空間複雜度 O(n),時間複雜度 O(N)。

最好的方法是時間複雜度 O(n),空間複雜度 O(1) 的。設置兩個指針,一個快一個慢,快的指針每次走兩步,慢的指針每次走一步,如果快指針和慢指針相遇,則説明有環。參考 http://leet-code.com/2010/09/detecting-loop-in-singly-linked-list.html

代碼

```
//LeetCode, Linked List Cycle
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    bool hasCycle(ListNode *head) {
        // 設置兩個指針, 一個快一個慢
        ListNode *slow = head, *fast = head;
        while (fast && fast->next) {
            slow = slow->next;
            fast = fast->next->next;
            if (slow == fast) return true;
        }
        return false;
    }
};
```

相關題目

• Linked List Cycle II, 見 §3.1.13

3.1.13 Linked List Cycle II

描述

Given a linked list, return the node where the cycle begins. If there is no cycle, return null. Follow up: Can you solve it without using extra space?

分析

當 fast 與 slow 相遇時, slow 肯定沒有遍歷完鏈表, 而 fast 已經在環內循環了 n 圈 $(1 \le n)$ 。 假 設 slow 走了 s 步, 則 fast 走了 2s 步 (fast 步數還等於 s 加上在環上多轉的 n 圈), 設環長為 r, 則:

$$2s = s + nr$$
$$s = nr$$

設整個鏈表長 L, 環入口點與相遇點距離為 a, 起點到環入口點的距離為 x, 則

$$x + a = nr = (n-1)r + r = (n-1)r + L - x$$

 $x = (n-1)r + (L-x-a)$

L-x-a 為相遇點到環入口點的距離,由此可知,從鏈表頭到環入口點等於n-1 圈內環+相遇點到環入口點,於是我們可以從 head 開始另設一個指針 slow2,兩個慢指針每次前進一步,它倆一定會在環入口點相遇。

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代碼

```
//LeetCode, Linked List Cycle II
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    ListNode *detectCycle(ListNode *head) {
        ListNode *slow = head, *fast = head;
        while (fast && fast->next) {
            slow = slow->next;
            fast = fast->next->next;
            if (slow == fast) {
                ListNode *slow2 = head;
                while (slow2 != slow) {
                    slow2 = slow2->next;
                    slow = slow->next;
                }
                return slow2;
            }
        return nullptr;
    }
};
```

相關題目

• Linked List Cycle, 見 §3.1.12

3.1.14 Reorder List

描述

```
Given a singly linked list L: L_0 \to L_1 \to \cdots \to L_{n-1} \to L_n, reorder it to: L_0 \to L_n \to L_1 \to L_{n-1} \to L_2 \to L_{n-2} \to \cdots
```

You must do this in-place without altering the nodes' values.

For example, Given {1,2,3,4}, reorder it to {1,4,2,3}.

分析

題目規定要 in-place, 也就是説只能使用 O(1) 的空間。

可以找到中間節點,斷開,把後半截單鏈表 reverse 一下,再合併兩個單鏈表。

```
// LeetCode, Reorder List
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
```

```
public:
    void reorderList(ListNode *head) {
        if (head == nullptr || head->next == nullptr) return;
        ListNode *slow = head, *fast = head, *prev = nullptr;
        while (fast && fast->next) {
            prev = slow;
            slow = slow->next;
            fast = fast->next->next;
        prev->next = nullptr; // cut at middle
        slow = reverse(slow);
        // merge two lists
        ListNode *curr = head;
        while (curr->next) {
            ListNode *tmp = curr->next;
            curr->next = slow;
            slow = slow->next;
            curr->next->next = tmp;
            curr = tmp;
        }
        curr->next = slow;
    }
    ListNode* reverse(ListNode *head) {
        if (head == nullptr || head->next == nullptr) return head;
        ListNode *prev = head;
        for (ListNode *curr = head->next, *next = curr->next; curr;
            prev = curr, curr = next, next = next ? next->next : nullptr) {
                curr->next = prev;
        head->next = nullptr;
        return prev;
    }
};
```

相關題目

無

3.1.15 Palindrome Linked List

描述

Given a singly linked list, determine if it is a palindrome.

For example, Given 1->2, return false. Given 1->2->1, return true; Given 1->0->1, return true;

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分析

Cut in middle, reverse, compare for difference, recover, return result

```
// LeetCode, Palindrome List
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    bool isPalindrome(ListNode* head) {
        if (!head || head->next == nullptr) return true;
        // go to half
        ListNode *slow, *fast; slow = fast = head;
        while (fast->next && fast->next->next) {
            slow = slow->next:
            fast = fast->next->next;
        fast = slow->next;
        slow->next = nullptr; // cut
        // reverse half
        ListNode *head2 = reverseList(fast);
        // check if not equal
        bool result = true;
        for (ListNode *11 = head, *12 = head2;
            11 && 12;
            11 = 11 - \text{next}, 12 = 12 - \text{next})  {
            if (11->val != 12->val) {
                result = false:
                break;
            }
        }
        // recover
        slow->next = reverseList(head2);
        // return result
        return result;
    }
private:
    ListNode* reverseList(ListNode* head) {
        if (!head || head->next == nullptr) return head;
        ListNode *prev, *cur;
        prev = head; cur = prev->next;
        while (cur) {
            ListNode *next = cur->next;
            cur->next = prev;
            prev = cur;
            cur = next;
```

```
}
head->next = nullptr;

return prev;
}
```

3.1.16 Add Two Numbers II

描述

You are given two **non-empty** linked lists representing two non-negative integers. The most significant digit comes first and each of their nodes contain a single digit. Add the two numbers and return it as a linked list.

You may assume the two numbers do not contain any leading zero, except the number 0 itself.

```
Input: (7 -> 2 -> 4 -> 3) + (5 -> 6 -> 4)

Output: 7 -> 8 -> 0 -> 7
```

分析

跟 Add Binary (見 §4.5) 很類似

```
// LeetCode, Add Two Numbers II
// 跟 Add Binary 很類似
// 時間複雜度 O(m+n), 空間複雜度 O(1)
class Solution {
public:
    ListNode* addTwoNumbers(ListNode* 11, ListNode* 12) {
       // 換成雙向容器 (string)
       // 由尾至頭推進, 使用插頭法
       // convert to string
       string s1 = ListToStr(l1);
       string s2 = ListToStr(12);
       int carry = 0;
       ListNode dummy(-1, nullptr);
       // add stirng and create list
       for (auto r1 = s1.rbegin(), r2 = s2.rbegin();
            r1 != s1.rend() || r2 != s2.rend();
            r1 = r1 != s1.rend() ? next(r1) : r1, r2 = r2 != s2.rend() ? next(r2) : r2)
            int v1 = r1 != s1.rend() ? *r1 - '0' : 0;
            int v2 = r2 != s2.rend() ? *r2 - '0' : 0;
            int sum = v1 + v2 + carry;
           dummy.next = new ListNode(sum % 10, dummy.next); // 插頭法
```

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```
carry = sum / 10;
        }
        if (carry > 0)
            dummy.next = new ListNode(carry, dummy.next);
        // reverse the list
        return dummy.next;
    }
private:
    string ListToStr(ListNode *head)
        string result;
        while (head)
            result += '0' + head->val;
            head = head->next;
        return result;
    }
};
```

相關題目

• Add Two Numbers, 見 §3.1.1

3.1.17 Insert into a Cyclic Sorted List

描述

Given a node from a Circular Linked List which is sorted in ascending order, write a function to insert a value insertVal into the list such that it remains a sorted circular list. The given node can be a reference to any single node in the list, and may not be necessarily the smallest value in the circular list.

If there are multiple suitable places for insertion, you may choose any place to insert the new value. After the insertion, the circular list should remain sorted.

If the list is empty (i.e., given node is null), you should create a new single circular list and return the reference to that single node. Otherwise, you should return the original given node.

```
Example 1:
```

```
Input: head = [3,4,1], insertVal = 2
Output: [3,4,1,2]
Explanation: In the figure above, there is a sorted circular list of three elements. You are g
```



图 3-1 before insert



图 3-2 before insert

分析

Nil

```
// LeetCode
// 時間複雜度 O(logn), 空間複雜度 O(n)
class Solution {
public:
    Node* insert(Node* head, int insertVal) {
        // edge case [1,1,1], target: 0
        // edge case [2,3,5,1], target: 0
        if (head == nullptr) {
            head = new Node(insertVal);
            head->next = head;
        }
        else {
            Node *cur = head->next;
            Node *prev = head;
            Node *pivot = nullptr;
            while (!(cur->val >= insertVal && prev->val < insertVal)) {</pre>
                if (prev->val > cur->val)
                    pivot = prev; // 找出邊界, case [2,3,5,1], target: 0
                prev = cur;
                cur = cur->next;
```

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相關題目

• 無

3.1.18 LRU Cache

描述

Design and implement a data structure for Least Recently Used (LRU) cache. It should support the following operations: get and set.

get(key) - Get the value (will always be positive) of the key if the key exists in the cache, otherwise return -1.

set (key, value) - Set or insert the value if the key is not already present. When the cache reached its capacity, it should invalidate the least recently used item before inserting a new item.

分析

為了使查找、插入和刪除都有較高的性能,我們使用一個雙向鏈表(std::list)和一個哈希表(std::unordered_map),因為:

- 哈希表保存每個節點的地址,可以基本保證在 O(1) 時間內查找節點
- 雙向鏈表插入和刪除效率高,單向鏈表插入和刪除時,還要查找節點的前驅節點 具體實現細節:
- 越靠近鏈表頭部、表示節點上次訪問距離現在時間最短、尾部的節點表示最近訪問最少
- 訪問節點時,如果節點存在,把該節點交換到鏈表頭部,同時更新 hash 表中該節點的地址
- 插入節點時,如果 cache 的 size 達到了上限 capacity,則刪除尾部節點,同時要在 hash 表中刪除對應的項;新節點插入鏈表頭部

代碼

```
// LeetCode, LRU Cache
// 時間複雜度 O(logn), 空間複雜度 O(n)
class LRUCache{
private:
   struct CacheNode {
       int kev;
       int value;
       CacheNode(int k, int v) :key(k), value(v){}
   };
public:
   LRUCache(int capacity) {
       this->capacity = capacity;
   }
   int get(int key) {
       if (cacheMap.find(key) == cacheMap.end()) return -1;
       // 把當前訪問的節點移到鏈表頭部, 並且更新 map 中該節點的地址
       cacheList.splice(cacheList.begin(), cacheList, cacheMap[key]);
       cacheMap[key] = cacheList.begin();
       return cacheMap[key]->value;
   }
   void set(int key, int value) {
       if (this->capacity == 0) return;
       if (cacheMap.find(key) == cacheMap.end()) {
           if (cacheList.size() == capacity) { //刪除鏈表尾部節點(最少訪問的節點)
               cacheMap.erase(cacheList.back().key);
               cacheList.pop_back();
           }
           // 插入新節點到鏈表頭部,並且在 map 中增加該節點
           cacheList.push_front(CacheNode(key, value));
           cacheMap[key] = cacheList.begin();
       } else {
           //更新節點的值,把當前訪問的節點移到鏈表頭部,並且更新 map 中該節點的地址
           cacheMap[key]->value = value;
           cacheList.splice(cacheList.begin(), cacheList, cacheMap[key]);
           cacheMap[key] = cacheList.begin();
       }
   }
private:
   list<CacheNode> cacheList;
   unordered_map<int, list<CacheNode>::iterator> cacheMap;
   int capacity;
};
```

相關題目

無

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3.2 雙鏈表

```
雙鏈表節點的定義如下:
// 雙鏈表節點
class Node {
public:
    int val;
    Node* prev;
    Node* child;
};
```

3.2.1 Flatten a Multilevel Doubly Linked List

描述

You are given a doubly linked list which in addition to the next and previous pointers, it could have a child pointer, which may or may not point to a separate doubly linked list. These child lists may have one or more children of their own, and so on, to produce a multilevel data structure, as shown in the example below.

Flatten the list so that all the nodes appear in a single-level, doubly linked list. You are given the head of the first level of the list.



图 3-3 candy crush

3.2 雙鏈表 99

分析

Nil

遞歸版

```
// LeetCode
 // 時間複雜度 O(n), 空間複雜度 O(1)
 class Solution {
 public:
     Node* flatten(Node* head) {
          for (Node *cur = head; cur; ) {
              if (cur->child == nullptr)
                  cur = cur->next;
              else {
                  cur->next = flatten_(cur->child, cur->next);
                  cur->next->prev = cur;
                  cur->child = nullptr;
              }
          }
         return head;
     }
 private:
     Node *flatten_(Node* head, Node *tail) {
         Node *cur = head;
          while (cur->next) {
              if (cur->child == nullptr)
                  cur = cur->next;
              else {
                  Node *next = cur->next;
                  cur->next = flatten_(cur->child, next);
                  cur->next->prev = cur;
                  cur->child = nullptr;
                  cur = next;
              }
          }
          cur->next = tail;
          if (tail)
              tail->prev = cur;
         return head;
     }
 };
Stack
 // LeetCode
 // 時間複雜度 O(n), 空間複雜度 O(1)
 class Solution {
 public:
     Node* flatten(Node* head) {
          if (head == nullptr) return head;
```

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```
stack<Node*> cache;
        Node *prev = nullptr;
        cache.push(head);
        while (!cache.empty()) {
            Node *cur = cache.top();
            cache.pop();
            if (prev)
                prev->next = cur;
            cur->prev = prev;
            if (cur->next) cache.push(cur->next);
            if (cur->child) cache.push(cur->child);
            cur->child = nullptr;
            prev = cur;
        return head;
    }
};
```

相關題目

• Nil

4.1 Valid Palindrome

描述

Given a string, determine if it is a palindrome, considering only alphanumeric characters and ignoring cases.

For example,

```
"A man, a plan, a canal: Panama" is a palindrome.
```

"race a car" is not a palindrome.

Note: Have you consider that the string might be empty? This is a good question to ask during an interview.

For the purpose of this problem, we define empty string as valid palindrome.

分析

無

代碼

```
// Leet Code, Valid Palindrome
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    bool isPalindrome(string s) {
        transform(s.begin(), s.end(), s.begin(), ::tolower);
        auto left = s.begin(), right = prev(s.end());
        while (left < right) {
            if (!::isalnum(*left)) ++left;
            else if (!::isalnum(*right)) --right;
            else if (*left != *right) return false;
            else { left++, right--; }
        }
        return true;
    }
};</pre>
```

相關題目

• Palindrome Number, 見 §16.2

4.2 Valid Palindrome II

描述

Given a non-empty string s, you may delete at most one character. Judge whether you can make it a palindrome.

```
Example 1:
Input: "aba"
Output: True
Example 2:
Input: "abca"
Output: True
Explanation: You could delete the character 'c'.
```

Note: The string will only contain lowercase characters a-z. The maximum length of the string is 50000.

DFS

```
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
   bool validPalindrome(string s) {
       // errorSkip 為最大可容忍的錯誤次數
       return validP(s, 0, s.size() - 1, 1);
private:
   bool validP(const string& s, int 1, int r, int errorSkip)
       while (l < r)
       {
           if (s[1] == s[r])
           {
               1++;
               r--;
           }
           else if (errorSkip > 0)
               errorSkip--;
               // status extend 把左右可以容忍的錯誤可能性都試一試
               return validP(s, 1, r-1, errorSkip)
                   || validP(s, l+1, r, errorSkip);
           }
           else
               return false;
       return true;
```

```
};
左右探步
 // 時間複雜度 O(n), 空間複雜度 O(1)
 class Solution {
 public:
     bool validPalindrome(string s) {
         int m = s.size();
         if(m<=2) return true;</pre>
         int L,R;
         L = 0;
         R = m-1;
         while (L \le R)
             if (s[L] == s[R])
             {
                 ++L;--R;
             }
             else
             {
                 // 移除左邊
                 int LL = L+1, LR = R;
                 while (LL <= LR && s[LL] == s[LR]) {++LL;--LR;}
                 if (LL >= LR) return true;
                 // 移除右邊
                 int RL = L, RR = R-1;
                 while (RL <= RR && s[RL] == s[RR]) {++RL;--RR;}
                 if (RL >= RR) return true;
                 // 若兩個方向都不是 Palindrome
                 return false;
             }
         }
         return true;
     }
 };
```

4.3 Implement strStr()

描述

Implement strStr().

Returns a pointer to the first occurrence of needle in haystack, or null if needle is not part of haystack.

分析

暴力算法的複雜度是 O(m*n),代碼如下。更高效的的算法有 KMP 算法、Boyer-Mooer 算法和 Rabin-Karp 算法。面試中暴力算法足夠了,一定要寫得沒有 BUG。

暴力匹配

next[0] = j;

```
// LeetCode, Implement strStr()
 // 暴力解法, 時間複雜度 O(N*M), 空間複雜度 O(1)
 class Solution {
 public:
     int strStr(const string& haystack, const string& needle) {
         if (needle.empty()) return 0;
         const int N = haystack.size() - needle.size() + 1;
         for (int i = 0; i < N; i++) {
             int j = i;
             int k = 0;
             while (j < haystack.size() && k < needle.size() && haystack[j] == needle[k]) {</pre>
                 k++:
             if (k == needle.size()) return i;
         }
         return -1;
     }
 };
KMP
 // LeetCode, Implement strStr()
 // KMP, 時間複雜度 O(N+M), 空間複雜度 O(M)
 class Solution {
 public:
     int strStr(const string& haystack, const string& needle) {
         return kmp(haystack.c_str(), needle.c_str());
     }
 private:
     /*
      * Obrief 計算部分匹配表,即 next 數組.
      * @param[in] pattern 模式串
      * @param[out] next next 數組
      * @return 無
      */
     static void compute_prefix(const char *pattern, int next[]) {
         int i;
         int j = -1;
         const int m = strlen(pattern);
```

```
for (i = 1; i < m; i++) {
            while (j > -1 \&\& pattern[j + 1] != pattern[i]) j = next[j];
            if (pattern[i] == pattern[j + 1]) j++;
           next[i] = j;
       }
    }
     * @brief KMP 算法.
     * Oparam[in] text 文本
     * @param[in] pattern 模式串
     * Oreturn 成功則返回第一次匹配的位置,失敗則返回-1
    static int kmp(const char *text, const char *pattern) {
        int i;
        int j = -1;
        const int n = strlen(text);
        const int m = strlen(pattern);
        if (n == 0 \&\& m == 0) return 0; /* "","" */
        if (m == 0) return 0; /* "a","" */
        int *next = (int*)malloc(sizeof(int) * m);
        compute_prefix(pattern, next);
        for (i = 0; i < n; i++) {
            while (j > -1 \&\& pattern[j + 1] != text[i]) j = next[j];
            if (text[i] == pattern[j + 1]) j++;
            if (j == m - 1) {
                free(next);
                return i-j;
            }
        }
        free(next);
        return -1;
   }
};
```

相關題目

• String to Integer (atoi), 見 §4.4

4.4 String to Integer (atoi)

描述

Implement atoi to convert a string to an integer.

Hint: Carefully consider all possible input cases. If you want a challenge, please do not see below and

ask yourself what are the possible input cases.

Notes: It is intended for this problem to be specified vaguely (ie, no given input specs). You are responsible to gather all the input requirements up front.

Requirements for atoi:

The function first discards as many whitespace characters as necessary until the first non-whitespace character is found. Then, starting from this character, takes an optional initial plus or minus sign followed by as many numerical digits as possible, and interprets them as a numerical value.

The string can contain additional characters after those that form the integral number, which are ignored and have no effect on the behavior of this function.

If the first sequence of non-whitespace characters in str is not a valid integral number, or if no such sequence exists because either str is empty or it contains only whitespace characters, no conversion is performed.

If no valid conversion could be performed, a zero value is returned. If the correct value is out of the range of representable values, INT_MAX (2147483647) or INT_MIN (-2147483648) is returned.

分析

細節題。注意幾個測試用例:

- 1. 不規則輸入, 但是有效, "-3924x8fc", "+413",
- 2. 無效格式, "++c", "++1"
- 3. 溢出數據、"2147483648"

代碼

```
// LeetCode, String to Integer (atoi)
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    int myAtoi(const string &str) {
        int num = 0;
        int sign = 1;
        const int n = str.length();
        int i = 0;
        while (str[i] == ' ' && i < n) i++;
        if (i == n) return 0;
        if (str[i] == '+') {
            i++;
        } else if (str[i] == '-') {
            sign = -1;
            i++;
        }
```

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```
for (; i < n; i++) {
             if (str[i] < '0' || str[i] > '9')
             if (num > INT_MAX / 10 ||
                              (num == INT_MAX / 10 \&\&
                                      (str[i] - '0') > INT_MAX % 10)) {
                  return sign == -1 ? INT_MIN : INT_MAX;
             }
             num = num * 10 + str[i] - '0';
         return num * sign;
     }
 };
相關題目
```

• Implement strStr(), 見 §4.3

4.5 Add Binary

描述

Given two binary strings, return their sum (also a binary string).

For example,

```
a = "11"
b = "1"
```

Return "100".

分析

無

代碼

```
//LeetCode, Add Binary
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    string addBinary(string a, string b) {
        string result;
        const size_t n = a.size() > b.size() ? a.size() : b.size();
        reverse(a.begin(), a.end());
        reverse(b.begin(), b.end());
        int carry = 0;
        for (size_t i = 0; i < n; i++) {
            const int ai = i < a.size() ? a[i] - '0' : 0;</pre>
            const int bi = i < b.size() ? b[i] - '0' : 0;</pre>
            const int val = (ai + bi + carry) % 2;
```

```
carry = (ai + bi + carry) / 2;
    result.insert(result.begin(), val + '0');
}
if (carry == 1) {
    result.insert(result.begin(), '1');
}
return result;
}
};
```

相關題目

• Add Two Numbers, 見 §3.1.1

4.6 Longest Palindromic Substring

描述

Given a string S, find the longest palindromic substring in S. You may assume that the maximum length of S is 1000, and there exists one unique longest palindromic substring.

分析

最長迴文子串,非常經典的題。

思路一:暴力枚舉,以每個元素為中間元素,同時從左右出發,複雜度 $O(n^2)$ 。

思路二: 記憶化搜索, 複雜度 $O(n^2)$ 。 設 f[i][j] 表示 [i,j] 之間的最長迴文子串, 遞推方程如下:

$$f[i][j] = if (i == j) S[i]$$

$$if (S[i] == S[j] && f[i+1][j-1] == S[i+1][j-1]) S[i][j]$$

$$else max(f[i+1][j-1], f[i][j-1], f[i+1][j])$$

思路三:動規,複雜度 $O(n^2)$ 。設狀態為 $\mathbf{f(i,j)}$,表示區間 [i,j] 是否為迴文串,則狀態轉移方程為

$$f(i,j) = \begin{cases} true &, i = j \\ S[i] = S[j] &, j = i+1 \\ S[i] = S[j] \text{ and } f(i+1,j-1) &, j > i+1 \end{cases}$$

思路四: Manacher's Algorithm, 複雜度 O(n)。詳細解釋見 http://leetcode.com/2011/11/longest-palindromic-substring-part-ii.html。

備忘錄法

```
// LeetCode, Longest Palindromic Substring
// 備忘錄法, 會超時
// 時間複雜度 O(n^2), 空間複雜度 O(n^2)
typedef string::const_iterator Iterator;
```

```
namespace std {
 template<>
 struct hash<pair<Iterator, Iterator>> {
     size_t operator()(pair<Iterator, Iterator> const& p) const {
         return ((size_t) &(*p.first)) ^ ((size_t) &(*p.second));
 };
 class Solution {
 public:
     string longestPalindrome(string const& s) {
         cache.clear();
         return cachedLongestPalindrome(s.begin(), s.end());
     }
 private:
     unordered_map<pair<Iterator, Iterator>, string> cache;
     string longestPalindrome(Iterator first, Iterator last) {
         size_t length = distance(first, last);
         if (length < 2) return string(first, last);</pre>
         auto s = cachedLongestPalindrome(next(first), prev(last));
         if (s.length() == length - 2 && *first == *prev(last))
             return string(first, last);
         auto s1 = cachedLongestPalindrome(next(first), last);
         auto s2 = cachedLongestPalindrome(first, prev(last));
         // return max(s, s1, s2)
         if (s.size() > s1.size()) return s.size() > s2.size() ? s : s2;
         else return s1.size() > s2.size() ? s1 : s2;
     }
     string cachedLongestPalindrome(Iterator first, Iterator last) {
         auto key = make_pair(first, last);
         auto pos = cache.find(key);
         if (pos != cache.end()) return pos->second;
         else return cache[key] = longestPalindrome(first, last);
     }
 };
動規
 // LeetCode, Longest Palindromic Substring
 // 動規, 時間複雜度 O(n^2), 空間複雜度 O(n^2)
 class Solution {
 public:
```

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```
string longestPalindrome(const string& s) {
         const int n = s.size();
         bool f[n][n];
         fill_n(&f[0][0], n * n, false);
         // 用 vector 會超時
         //vector<vector<bool> > f(n, vector<bool>(n, false));
         size t max len = 1, start = 0; // 最長迴文子串的長度, 起點
         for (size_t i = 0; i < s.size(); i++) {
             f[i][i] = true;
             for (size_t j = 0; j < i; j++) { // [j, i]
                 f[j][i] = (s[j] == s[i] && (i - j < 2 || f[j + 1][i - 1]));
                 if (f[j][i] \&\& max_len < (i - j + 1)) {
                     max_len = i - j + 1;
                     start = j;
                 }
             }
         }
         return s.substr(start, max_len);
     }
 };
Manacher's Algorithm
 // LeetCode, Longest Palindromic Substring
 // Manacher's Algorithm
 // 時間複雜度 O(n), 空間複雜度 O(n)
 class Solution {
 public:
     // Transform S into T.
     // For example, S = "abba", T = "^#a#b#b#a#$".
     // ^ and $ signs are sentinels appended to each end to avoid bounds checking
     string preProcess(const string& s) {
         int n = s.length();
         if (n == 0) return "^$";
         string ret = "^";
         for (int i = 0; i < n; i++) ret += "#" + s.substr(i, 1);
         ret += "#$":
         return ret;
     }
     string longestPalindrome(string s) {
         string T = preProcess(s);
         const int n = T.length();
         // 以 T[i] 為中心,向左/右擴張的長度,不包含 T[i] 自己,
         // 因此 P[i] 是源字符串中迴文串的長度
         int P[n];
         int C = 0, R = 0;
         for (int i = 1; i < n - 1; i++) {
```

```
int i mirror = 2 * C - i; // equals to i' = C - (i-C)
            P[i] = (R > i) ? min(R - i, P[i mirror]) : 0;
            // Attempt to expand palindrome centered at i
            while (T[i + 1 + P[i]] == T[i - 1 - P[i]])
                P[i]++;
            // If palindrome centered at i expand past R,
            // adjust center based on expanded palindrome.
            if (i + P[i] > R) {
                C = i;
                R = i + P[i];
            }
        }
        // Find the maximum element in P.
        int max_len = 0;
        int center_index = 0;
        for (int i = 1; i < n - 1; i++) {
            if (P[i] > max_len) {
                max_len = P[i];
                center_index = i;
            }
        }
        return s.substr((center_index - 1 - max_len) / 2, max_len);
    }
};
```

相關題目

無

4.7 Regular Expression Matching

描述

Implement regular expression matching with support for '.' and '*'.

'.' Matches any single character. '*' Matches zero or more of the preceding element.

The matching should cover the entire input string (not partial).

The function prototype should be:

```
bool isMatch(const char *s, const char *p)
   Some examples:
isMatch("aa","a") → false
isMatch("aa","aa") → true
isMatch("aaa","aa") → false
isMatch("aa", "a*") → true
isMatch("aa", ".*") → true
```

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```
isMatch("ab", ".*") \rightarrow true isMatch("aab", "c*a*b") \rightarrow true
```

分析

這是一道很有挑戰的題。

遞歸版

```
// LeetCode, Regular Expression Matching
// 遞歸版,時間複雜度 O(n),空間複雜度 O(1)
class Solution {
public:
    bool isMatch(const string& s, const string& p) {
        return isMatch(s.c_str(), p.c_str());
    }
private:
    bool isMatch(const char *s, const char *p) {
        if (*p == '\0') return *s == '\0';
        // next char is not '*', then must match current character
        if (*(p + 1) != '*') {
            if (*p == *s || (*p == '.' && *s != '\0'))
                return isMatch(s + 1, p + 1);
            else
                return false;
        } else { // next char is '*'
            while (*p == *s \mid | (*p == '.' && *s != '\0')) {
                if (isMatch(s, p + 2))
                    return true;
                s++;
            }
            return isMatch(s, p + 2);
        }
    }
};
```

迭代版

相關題目

• Wildcard Matching, 見 §4.8

4.8 Wildcard Matching

描述

Implement wildcard pattern matching with support for '?' and '*'.

'?' Matches any single character. '*' Matches any sequence of characters (including the empty sequence).

The matching should cover the entire input string (not partial).

The function prototype should be:

isMatch("aab", "c*a*b") → false

```
bool isMatch(const char *s, const char *p)
   Some examples:
isMatch("aa","a") → false
isMatch("aa","aa") → true
isMatch("aaa","aa") → false
isMatch("aa", "*") → true
isMatch("aa", "a*") → true
isMatch("ab", "?*") → true
```

分析

跟上一題很類似。

主要是'*'的匹配問題。p每遇到一個'*',就保留住當前'*'的座標和s的座標,然後s從前往後掃描,如果不成功,則s++,重新掃描。

遞歸版

```
// LeetCode, Wildcard Matching
// 遞歸版, 會超時, 用於幫助理解題意
// 時間複雜度 O(n!*m!), 空間複雜度 O(n)
class Solution {
public:
    bool isMatch(const string& s, const string& p) {
       return isMatch(s.c_str(), p.c_str());
    }
private:
   bool isMatch(const char *s, const char *p) {
       if (*p == '*') {
           while (*p == '*') ++p; //skip continuous '*'
           if (*p == '\0') return true;
           while (*s != '\0' && !isMatch(s, p)) ++s;
           return *s != '\0';
       else if (*p == '\0' || *s == '\0') return *p == *s;
       else if (*p == *s || *p == '?') return isMatch(++s, ++p);
       else return false;
    }
};
```

迭代版

```
// LeetCode, Wildcard Matching
// 迭代版, 時間複雜度 O(n*m), 空間複雜度 O(1)
class Solution {
public:
    bool isMatch(const string& s, const string& p) {
        return isMatch(s.c_str(), p.c_str());
    }
private:
   bool isMatch(const char *s, const char *p) {
        bool star = false;
        const char *str, *ptr;
        for (str = s, ptr = p; *str != '\0'; str++, ptr++) {
            switch (*ptr) {
            case '?':
                break;
            case '*':
                star = true;
                s = str, p = ptr;
                while (*p == '*') p++; //skip continuous '*'
                if (*p == '\0') return true;
                str = s - 1;
                ptr = p - 1;
                break;
            default:
                if (*str != *ptr) {
                    // 如果前面沒有'*', 則匹配不成功
                    if (!star) return false;
                    s++;
                    str = s - 1;
                    ptr = p - 1;
                }
            }
        while (*ptr == '*') ptr++;
        return (*ptr == '\0');
   }
};
```

相關題目

• Regular Expression Matching, 見 §4.7

4.9 Longest Common Prefix

描述

Write a function to find the longest common prefix string amongst an array of strings.

分析

從位置 0 開始、對每一個位置比較所有字符串、直到遇到一個不匹配。

縱向掃描

```
// LeetCode, Longest Common Prefix
 // 縱向掃描, 從位置 O 開始, 對每一個位置比較所有字符串, 直到遇到一個不匹配
 // 時間複雜度 O(n1+n2+...)
 // @author 周倩 (http://weibo.com/zhouditty)
 class Solution {
 public:
     string longestCommonPrefix(vector<string> &strs) {
         if (strs.empty()) return "";
         for (int idx = 0; idx < strs[0].size(); ++idx) { // 縱向掃描
            for (int i = 1; i < strs.size(); ++i) {</pre>
                if (strs[i][idx] != strs[0][idx]) return strs[0].substr(0,idx);
            }
         return strs[0];
     }
 };
橫向掃描
 // LeetCode, Longest Common Prefix
 // 横向掃描, 每個字符串與第0個字符串, 從左到右比較, 直到遇到一個不匹配,
 // 然後繼續下一個字符串
 // 時間複雜度 O(n1+n2+...)
 class Solution {
 public:
     string longestCommonPrefix(vector<string> &strs) {
         if (strs.empty()) return "";
         int right_most = strs[0].size() - 1;
         for (size_t i = 1; i < strs.size(); i++)</pre>
            for (int j = 0; j <= right_most; j++)</pre>
                if (strs[i][j]!= strs[0][j]) // 不會越界, 請參考 string::[] 的文檔
                    right_most = j - 1;
         return strs[0].substr(0, right_most + 1);
     }
 };
```

相關題目

• 無

4.10 Valid Number

描述

Validate if a given string is numeric.

Some examples:

```
"0" => true
" 0.1 " => true
"abc" => false
"1 a" => false
"2e10" => true
```

Note: It is intended for the problem statement to be ambiguous. You should gather all requirements up front before implementing one.

分析

細節實現題。

本題的功能與標準庫中的 strtod() 功能類似。

有限自動機

```
// LeetCode, Valid Number
// @author 龔陸安 (http://weibo.com/luangong)
// finite automata, 時間複雜度 O(n), 空間複雜度 O(n)
class Solution {
public:
   bool isNumber(const string& s) {
        enum InputType {
            INVALID,
                       // 0
            SPACE.
                       // 1
                       // 2
            SIGN,
           DIGIT,
                       // 3
                       // 4
            DOT.
            EXPONENT.
                       // 5
           NUM_INPUTS // 6
        };
        const int transitionTable[][NUM INPUTS] = {
               -1, 0, 3, 1, 2, -1, // next states for state 0
               -1, 8, -1, 1, 4, 5,
                                     // next states for state 1
               -1, -1, -1, 4, -1, -1,
                                       // next states for state 2
                                        // next states for state 3
               -1, -1, -1, 1, 2, -1,
                                       // next states for state 4
               -1, 8, -1, 4, -1, 5,
                                        // next states for state 5
               -1, -1, 6, 7, -1, -1,
               -1, -1, -1, 7, -1, -1,
                                         // next states for state 6
                                       // next states for state 7
               -1, 8, -1, 7, -1, -1,
               -1, 8, -1, -1, -1, -1,
                                       // next states for state 8
               };
        int state = 0;
```

4.10 Valid Number 117

```
for (auto ch : s) {
             InputType inputType = INVALID;
             if (isspace(ch))
                  inputType = SPACE;
             else if (ch == '+' || ch == '-')
                  inputType = SIGN;
             else if (isdigit(ch))
                  inputType = DIGIT;
             else if (ch == '.')
                  inputType = DOT;
             else if (ch == 'e' || ch == 'E')
                  inputType = EXPONENT;
             // Get next state from current state and input symbol
             state = transitionTable[state][inputType];
             // Invalid input
             if (state == -1) return false;
         // If the current state belongs to one of the accepting (final) states,
         // then the number is valid
         return state == 1 || state == 4 || state == 7 || state == 8;
     }
 };
使用 strtod()
 // LeetCode, Valid Number
 // @author 連城 (http://weibo.com/lianchengzju)
 // 偷懶, 直接用 strtod(), 時間複雜度 O(n)
 class Solution {
 public:
     bool isNumber (const string& s) {
         return isNumber(s.c_str());
     }
 private:
     bool isNumber (char const* s) {
         char* endptr;
         strtod (s, &endptr);
         if (endptr == s) return false;
         for (; *endptr; ++endptr)
             if (!isspace (*endptr)) return false;
         return true;
     }
 };
```

相關題目

• 無

4.11 Integer to Roman

描述

Given an integer, convert it to a roman numeral.

Input is guaranteed to be within the range from 1 to 3999.

分析

無

代碼

```
// LeetCode, Integer to Roman
// 時間複雜度 O(num), 空間複雜度 O(1)
class Solution {
public:
    string intToRoman(int num) {
        const int radix[] = {1000, 900, 500, 400, 100, 90,
                50, 40, 10, 9, 5, 4, 1};
        const string symbol[] = {"M", "CM", "D", "CD", "C", "XC",
                "L", "XL", "X", "IX", "V", "IV", "I"};
        string roman;
        for (size_t i = 0; num > 0; ++i) {
            int count = num / radix[i];
            num %= radix[i];
            for (; count > 0; --count) roman += symbol[i];
        return roman;
    }
};
```

相關題目

• Roman to Integer, 見 §4.12

4.12 Roman to Integer

描述

Given a roman numeral, convert it to an integer.

Input is guaranteed to be within the range from 1 to 3999.

4.13 Count and Say 119

分析

從前往後掃描、用一個臨時變量記錄分段數字。

如果當前比前一個大, 説明這一段的值應該是當前這個值減去上一個值。比如 IV = 5 - 1; 否則, 將當前值加入到結果中, 然後開始下一段記錄。比如 VI = 5 + 1, II=1+1

代碼

```
// LeetCode, Roman to Integer
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    inline int map(const char c) {
        switch (c) {
        case 'I': return 1;
        case 'V': return 5;
        case 'X': return 10;
        case 'L': return 50;
        case 'C': return 100;
        case 'D': return 500;
        case 'M': return 1000;
        default: return 0;
        }
    }
    int romanToInt(const string& s) {
        int result = 0;
        for (size_t i = 0; i < s.size(); i++) {
            if (i > 0 \&\& map(s[i]) > map(s[i - 1]))  {
                result += (map(s[i]) - 2 * map(s[i - 1]));
            } else {
                result += map(s[i]);
        return result;
};
```

相關題目

• Integer to Roman, 見 §4.11

4.13 Count and Say

描述

The count-and-say sequence is the sequence of integers beginning as follows:

```
1, 11, 21, 1211, 111221, ...

1 is read off as "one 1" or 11.
```

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```
11 is read off as "two 1s" or 21.21 is read off as "one 2", then "one 1" or 1211.Given an integer n, generate the nth sequence.
```

Note: The sequence of integers will be represented as a string.

分析

模擬。

代碼

```
// LeetCode, Count and Say
// @author 連城 (http://weibo.com/lianchengzju)
// 時間複雜度 O(n^2), 空間複雜度 O(n)
class Solution {
public:
    string countAndSay(int n) {
        string s("1");
        while (--n)
            s = getNext(s);
        return s;
    }
    string getNext(const string &s) {
        stringstream ss;
        for (auto i = s.begin(); i != s.end(); ) {
            auto j = find_if(i, s.end(), bind1st(not_equal_to<char>(), *i));
            ss << distance(i, j) << *i;
            i = j;
        }
        return ss.str();
    }
};
```

相關題目

• 無

4.14 Anagrams

描述

Given an array of strings, return all groups of strings that are anagrams.

Note: All inputs will be in lower-case.

4.15 Simplify Path 121

分析

Anagram (迴文構詞法) 是指打亂字母順序從而得到新的單詞,比如 "dormitory" 打亂字母順序會變成 "dirty room", "tea" 會變成"eat"。

迴文構詞法有一個特點:單詞裏的字母的種類和數目沒有改變,只是改變了字母的排列順序。因此、將幾個單詞按照字母順序排序後,若它們相等、則它們屬於同一組 anagrams。

代碼

```
// LeetCode, Anagrams
// 時間複雜度 O(n), 空間複雜度 O(n)
class Solution {
public:
    vector<string> anagrams(vector<string> &strs) {
        unordered_map<string, vector<string> > group;
        for (const auto &s : strs) {
            string key = s;
            sort(key.begin(), key.end());
            group[key].push_back(s);
        }
        vector<string> result;
        for (auto it = group.cbegin(); it != group.cend(); it++) {
            if (it->second.size() > 1)
                result.insert(result.end(), it->second.begin(), it->second.end());
        return result;
    }
};
```

相關題目

無

4.15 Simplify Path

描述

Given an absolute path for a file (Unix-style), simplify it.

For example,

```
path = "/home/", => "/home"
path = "/a/./b/../../c/", => "/c"
```

Corner Cases:

- Did you consider the case where path = "/../"? In this case, you should return "/".
- Another corner case is the path might contain multiple slashes '/' together, such as "/home//foo/".
 In this case, you should ignore redundant slashes and return "/home/foo".

分析

很有實際價值的題目。

代碼

```
// LeetCode, Simplify Path
// 時間複雜度 O(n), 空間複雜度 O(n)
class Solution {
public:
    string simplifyPath(const string& path) {
        vector<string> dirs; // 當做棧
        for (auto i = path.begin(); i != path.end();) {
            ++i;
            auto j = find(i, path.end(), '/');
            auto dir = string(i, j);
            if (!dir.empty() && dir != ".") {// 當有連續 '///' 時, dir 為空
                if (dir == "..") {
                    if (!dirs.empty())
                        dirs.pop_back();
                } else
                    dirs.push_back(dir);
            }
            i = j;
        }
        stringstream out;
        if (dirs.empty()) {
           out << "/";
        } else {
            for (auto dir : dirs)
                out << '/' << dir;
        }
       return out.str();
   }
};
```

相關題目

• 無

4.16 Length of Last Word

描述

Given a string s consists of upper/lower-case alphabets and empty space characters ' ', return the length of last word in the string.

If the last word does not exist, return 0.

Note: A word is defined as a character sequence consists of non-space characters only.

For example, Given s = "Hello World", return 5.

分析

細節實現題。

用 STL

```
// LeetCode, Length of Last Word
// 偷懒, 用 STL
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    int lengthOfLastWord(const string& s) {
        auto first = find_if(s.rbegin(), s.rend(), ::isalpha);
        auto last = find_if_not(first, s.rend(), ::isalpha);
        return distance(first, last);
    }
};
```

順序掃描

```
// LeetCode, Length of Last Word
// 順序掃描, 記錄每個 word 的長度
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    int lengthOfLastWord(const string& s) {
       return lengthOfLastWord(s.c_str());
    }
private:
    int lengthOfLastWord(const char *s) {
       int len = 0:
       while (*s) {
           if (*s++ != ' ')
               ++len;
           else if (*s && *s != ' ')
               len = 0;
       return len;
```

```
};
```

相關題目

• 無

4.17 Longest Happy Prefix

描述

A string is called a happy prefix if is a non-empty prefix which is also a suffix (excluding itself). Given a string s. Return the longest happy prefix of s. Return an empty string if no such prefix exists.

```
Example 1:
Input: s = "level"
Output: "1"
Explanation: s contains 4 prefix excluding itself ("1", "le", "lev", "leve")
, and suffix ("l", "el", "vel", "evel").
The largest prefix which is also suffix is given by "l".
Example 2:
Input: s = "ababab"
Output: "abab"
Explanation: "abab" is the largest prefix which is also suffix.
They can overlap in the original string.
Example 3:
Input: s = "leetcodeleet"
Output: "leet"
Example 4:
Input: s = "a"
Output: ""
  Constraints: 1 \le \text{s.length} \le 10^5 \text{ s contains only lowercase English letters.}
```

分析

細節實現題。

順序掃描

```
// LeetCode, Longest happy prefix
// try all possible match
// 時間複雜度 O(n^2), 空間複雜度 O(1)
class Solution {
public:
    string longestPrefix(string s) {
        int N = (int)s.length();
        if (N < 2) return "";</pre>
```

4.18 Decode String 125

for (int i = 1; i < N; i++) {

```
int j = i;
             int k = 0;
             while (k < N && j < N && s[k++] == s[j++]);
             if (j == N) return s.substr(i, N - i);
         return "";
     }
 };
Rolling Hash
 // LeetCode, Longest happy prefix
 // rolling hashing
 // 時間複雜度 O(n), 空間複雜度 O(1)
 class Solution {
 public:
     string longestPrefix(string s) {
         int times = 2;
         int64_t prefixHash = 0;
         int64_t suffixHash = 0;
          int64_t multiplier = 1;
         int64_t len = 0;
          int64_t mod = 1000000007; //use some large prime as a modulo to avoid overflow errors,
          int N = s.length();
         for (int i = 0; i < N - 1; i++) {
             prefixHash = (prefixHash * times + s[i]) % mod;
             suffixHash = (multiplier * s[N - 1 - i] + suffixHash) % mod;
             if (prefixHash == suffixHash)
                  len = i + 1;
             multiplier = multiplier * times % mod;
         return s.substr(0, len);
 };
```

相關題目

• 無

4.18 Decode String

描述

Given an encoded string, return its decoded string.

The encoding rule is: k[encoded_string], where the encoded_string inside the square brackets is being repeated exactly k times. Note that k is guaranteed to be a positive integer.

You may assume that the input string is always valid; No extra white spaces, square brackets are well-formed, etc.

Furthermore, you may assume that the original data does not contain any digits and that digits are only for those repeat numbers, k. For example, there won't be input like 3a or 2[4].

分析

Nil

遞歸版

```
// LeetCode
// 時間複雜度 D(), 空間複雜度 D()
class Solution {
public:
    string decodeString(string s) {
        return decodeString(s.begin(), s.end());
    }
private:
    template <class BidirecIT>
        string decodeString(BidirecIT first, BidirecIT end)
        if (first == end) return "";
        string result;
        while (first != end)
        {
            if (isdigit(*first))
                // 取得所有數字
                auto cur = first;
                while (cur != end) { if (*cur == '[') break; cur++; }
                int num = stol(string(first, cur));
                first = cur;
                // 取得接下來的字串
                auto first2 = next(first);
                auto end2 = first2;
                int curLeft = 1; // 現在 [ 的數目
                while (end2 != end && curLeft > 0)
                {
                    if (*end2 == '[')
                       curLeft++;
                    else if (*end2 == ']')
                        curLeft--;
                    end2++;
                }
                string result2 = decodeString(first2, prev(end2));
                string result3;
                // 重覆地放入
```

```
for (int i = 0; i < num; i++)
                    result3 += result2;
                result += result3;
                first = end2;
            }
            else
            {
                // 取得所有字母
                auto cur = first;
                while (cur != end) { if (*cur >= '0' && *cur <= '9') break; cur++; }
                result += string(first, cur);
                first = cur;
            }
        }
        return result;
    }
};
```

相關題目

無

4.19 Unique Word Abbreviation

描述

An abbreviation of a word follows the form <first letter><number><last letter>. Below are some examples of word abbreviations:

Additionally for any string s of size less than or equal to 2 their abbreviation is the same s

Find whether its abbreviation is unique in the dictionary. A word's abbreviation is called unique if any of the following conditions is met:

There is no word in dictionary such that their abbreviation is equal to the abbreviation of word.

Else, for all words in dictionary such that their abbreviation is equal to the abbreviation of word those
words are equal to word.

普通數數法

```
// 時間複雜度 O(n), 空間複雜度 O(2*n)
 class ValidWordAbbr {
 public:
     ValidWordAbbr(vector<string>& dictionary) {
         for (const string& s : dictionary)
         {
             m_words[s]++;
             m_abbrs[ToAbbr(s)]++;
     }
     bool isUnique(string word) {
         auto it = m_abbrs.find(ToAbbr(word));
         auto it2 = m_words.find(word);
         // 若簡寫沒有出現過
         if (it == m_abbrs.end()) return true;
         // 若文字相同, 和所有簡寫都來自同一個字源
         else if (it2 != m_words.end() && it->second == it2->second) return true;
         // 若簡寫相同, 和簡寫來自不同文字
         else return false;
     }
 private:
     string ToAbbr(string inStr)
     {
         int N = inStr.size();
         if (N <= 2) return inStr;
         return inStr.front() + to_string(N-2) + inStr.back();
     }
 private:
     unordered_map<string, int> m_words;
     unordered_map<string, int> m_abbrs;
 };
改良版
 // 時間複雜度 O(n), 空間複雜度 O(n)
 // 用 bool 來記低同一個簡寫有沒有多過一個文字的來源
 class ValidWordAbbr {
 public:
     ValidWordAbbr(vector<string>& D) {
         for (auto& w : D) {
             Add(w);
     }
     bool isUnique(string w) {
         string abbrev;
```

```
Abbrev(w, abbrev);
       if (!dict.count(abbrev)) return true;
       auto& [s,good] = dict[abbrev];
       // 當 good 為 false, 我們可以肯定此短寫來自超過一個文字
       // 那麼投入來的文字, 必定不會是唯一
       return good && s == w;
   }
private:
   void Abbrev(const string& w, string& abbrev) {
       if (w.length() > 2){
           abbrev = w[0] + to_string(int(w.length()-2)) + w.back();
       } else {
           abbrev = w;
   }
   void Add(string& w) {
       string abbrev;
       Abbrev(w, abbrev);
       if (!dict.count(abbrev)) {
           // 第一個文字出現時, good 必定為 true
           // good 為 true 時,代表文字一致
           dict[abbrev] = {w,true};
           return;
       }
       auto& [s,good] = dict[abbrev];
       // 若果新加入的文字和之前的不同, good 為 false
       if (good && s != w) good = false;
   }
private:
   unordered_map<string, pair<string,bool>> dict;
};
```

第 5 章 棧和隊列

5.1 棧

5.1.1 Valid Parentheses

描述

Given a string containing just the characters '(', ')', '{', '}', '[' and ']', determine if the input string is valid.

The brackets must close in the correct order, "()" and "()[]" are all valid but "(]" and "([)]" are not.

分析

無

代碼

```
// LeetCode, Valid Parentheses
// 時間複雜度 O(n), 空間複雜度 O(n)
class Solution {
public:
   bool isValid (string const& s) {
        string left = "([{";
        string right = ")]}";
        stack<char> stk;
        for (auto c : s) {
            if (left.find(c) != string::npos) {
                stk.push (c);
            } else {
                if (stk.empty () || stk.top () != left[right.find (c)])
                    return false;
                else
                    stk.pop ();
           }
       }
```

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```
return stk.empty();
};
```

相關題目

- Generate Parentheses, 見 §11.9
- Longest Valid Parentheses, 見 §5.1.2

5.1.2 Longest Valid Parentheses

描述

Given a string containing just the characters '(' and ')', find the length of the longest valid (well-formed) parentheses substring.

```
For "(()", the longest valid parentheses substring is "()", which has length = 2.
```

Another example is ")()())", where the longest valid parentheses substring is "()()", which has length = 4.

分析

無

使用棒

```
// LeetCode, Longest Valid Parenthese
// 使用棧, 時間複雜度 O(n), 空間複雜度 O(n)
class Solution {
public:
    int longestValidParentheses(const string& s) {
        int max_len = 0, last = -1; // the position of the last ')'
        stack<int> lefts; // keep track of the positions of non-matching '('s
        for (int i = 0; i < s.size(); ++i) {
            if (s[i] =='(') {
                lefts.push(i);
            } else {
                if (lefts.empty()) {
                    // no matching left
                    last = i;
                } else {
                    // find a matching pair
                    lefts.pop();
                    if (lefts.empty()) {
                        max_len = max(max_len, i-last);
                    } else {
                        max_len = max(max_len, i-lefts.top());
```

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```
}
                 }
             }
         }
         return max_len;
     }
 };
Dynamic Programming, One Pass
 // LeetCode, Longest Valid Parenthese
 // 時間複雜度 O(n), 空間複雜度 O(n)
 // @author 一隻傑森 (http://weibo.com/wjson)
 class Solution {
 public:
     int longestValidParentheses(const string& s) {
         vector<int> f(s.size(), 0);
         int ret = 0;
         for (int i = s.size() - 2; i >= 0; --i) {
             int match = i + f[i + 1] + 1;
             // case: "((...))"
             if (s[i] == '(' && match < s.size() && s[match] == ')') {
                 f[i] = f[i + 1] + 2;
                 // if a valid sequence exist afterwards "((...))()"
                 if (match + 1 < s.size()) f[i] += f[match + 1];</pre>
             ret = max(ret, f[i]);
         return ret;
     }
 };
兩遍掃描
 // LeetCode, Longest Valid Parenthese
 // 兩遍掃描, 時間複雜度 O(n), 空間複雜度 O(1)
 // @author 曹鵬 (http://weibo.com/cpcs)
 class Solution {
 public:
     int longestValidParentheses(const string& s) {
         int answer = 0, depth = 0, start = -1;
         for (int i = 0; i < s.size(); ++i) {
             if (s[i] == '(') {
                 ++depth;
             } else {
                 --depth;
                 if (depth < 0) {
                     start = i;
                     depth = 0;
                 } else if (depth == 0) {
                     answer = max(answer, i - start);
```

}

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```
}
        }
        depth = 0;
        start = s.size();
        for (int i = s.size() - 1; i >= 0; --i) {
            if (s[i] == ')') {
                 ++depth;
            } else {
                --depth;
                if (depth < 0) {
                     start = i;
                     depth = 0;
                } else if (depth == 0) {
                     answer = max(answer, start - i);
            }
        return answer;
    }
};
```

相關題目

- Valid Parentheses, 見 §5.1.1
- Generate Parentheses, 見 §11.9

5.1.3 Largest Rectangle in Histogram

描述

Given n non-negative integers representing the histogram's bar height where the width of each bar is 1, find the area of largest rectangle in the histogram.



图 5-1 Above is a histogram where width of each bar is 1, given height = [2,1,5,6,2,3].

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图 5-2 The largest rectangle is shown in the shaded area, which has area = 10 unit.

For example, Given height = [2,1,5,6,2,3], return 10.

分析

簡單的,類似於 Container With Most Water($\S13.6$),對每個柱子,左右擴展,直到碰到比自己矮的,計算這個矩形的面積,用一個變量記錄最大的面積,複雜度 $O(n^2)$,會超時。

如圖 $\S5-2$ 所示,從左到右處理直方,當 i=4 時,小於當前棧頂(即直方 3),對於直方 3,無論 後面還是前面的直方,都不可能得到比目前棧頂元素更高的高度了,處理掉直方 3(計算從直方 3 到 直方 4 之間的矩形的面積,然後從棧裏彈出);對於直方 2 也是如此;直到碰到比直方 4 更矮的直方 1。

這就意味着,可以維護一個遞增的棧,每次比較棧頂與當前元素。如果當前元素大於棧頂元素, 則入棧,否則合併現有棧,直至棧頂元素小於當前元素。結尾時入棧元素 0,重複合併一次。

代碼

```
// LeetCode, Largest Rectangle in Histogram
// 時間複雜度 O(n), 空間複雜度 O(n)
class Solution {
public:
    int largestRectangleArea(vector<int> &height) {
        stack<int> s;
        height.push_back(0);
        int result = 0;
        for (int i = 0; i < height.size(); ) {</pre>
            if (s.empty() || height[i] > height[s.top()])
                s.push(i++);
            else {
                int tmp = s.top();
                s.pop();
                result = max(result,
                        height[tmp] * (s.empty() ? i : i - s.top() - 1));
            }
```

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```
return result;
     }
 };
遞歸版
 // LeetCode, Largest Rectangle in Histogram
 // 時間複雜度 O(nlogn ~ n^2), 空間複雜度 O(n)
 // 會超時
 class Solution {
 public:
     int largestRectangleArea(vector<int>& heights) {
         if (heights.size() == 0) return 0;
         return DFS(heights, 0, heights.size()-1);
     }
 private:
     int DFS(vector<int>& heights, int first, int last) {
         if (first > last) return 0;
         int minIndex = first;
         for (int i = first; i <= last; i++) {
             if (heights[minIndex] > heights[i])
                 minIndex = i;
         }
         return max(heights[minIndex] * (last - first + 1)
                    , max(DFS(heights, first, minIndex-1)
                          , DFS(heights, minIndex+1, last)));
     }
 };
遞歸版 - segment tree
 // LeetCode, Largest Rectangle in Histogram
 // 時間複雜度 O(nlogn), 空間複雜度 O(n)
 // 把尋找 min index 的時間減少為 log n
 class SegTreeNode {
 public:
     int start;
     int end;
     int min;
     SegTreeNode *left;
     SegTreeNode *right;
     SegTreeNode(int start, int end) {
         this->start = start;
         this->end = end;
         left = right = NULL;
 };
```

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```
class Solution {
public:
    int largestRectangleArea(vector<int>& heights) {
        if (heights.size() == 0) return 0;
        // first build a segment tree
        SegTreeNode *root = buildSegmentTree(heights, 0, heights.size() - 1);
        // next calculate the maximum area recursively
        return calculateMax(heights, root, 0, heights.size() - 1);
    int calculateMax(vector<int>& heights, SegTreeNode* root, int start, int end) {
        if (start > end) {
            return -1;
        if (start == end) {
            return heights[start];
        int minIndex = query(root, heights, start, end);
        int leftMax = calculateMax(heights, root, start, minIndex - 1);
        int rightMax = calculateMax(heights, root, minIndex + 1, end);
        int minMax = heights[minIndex] * (end - start + 1);
        return max( max(leftMax, rightMax), minMax );
    }
    SegTreeNode *buildSegmentTree(vector<int>& heights, int start, int end) {
        if (start > end) return NULL;
        SegTreeNode *root = new SegTreeNode(start, end);
        if (start == end) {
            root->min = start;
            return root;
        } else {
            int middle = (start + end) / 2;
            root->left = buildSegmentTree(heights, start, middle);
            root->right = buildSegmentTree(heights, middle + 1, end);
            root->min = heights[root->left->min] < heights[root->right->min]
                        ? root->left->min : root->right->min;
            return root;
        }
    }
    int query(SegTreeNode *root, vector<int>& heights, int start, int end) {
        if (root == NULL || end < root->start || start > root->end) return -1;
        if (start <= root->start && end >= root->end) {
            return root->min:
        }
        int leftMin = query(root->left, heights, start, end);
        int rightMin = query(root->right, heights, start, end);
        if (leftMin == -1) return rightMin;
        if (rightMin == -1) return leftMin;
        return heights[leftMin] < heights[rightMin] ? leftMin : rightMin;</pre>
};
```

5.1 棧

相關題目

- Trapping Rain Water, 見 §2.1.18
- Container With Most Water, 見 §13.6

5.1.4 Evaluate Reverse Polish Notation

描述

Evaluate the value of an arithmetic expression in Reverse Polish Notation.

Valid operators are +, -, *, /. Each operand may be an integer or another expression.

Some examples:

```
["2", "1", "+", "3", "*"] -> ((2 + 1) * 3) -> 9
["4", "13", "5", "/", "+"] -> (4 + (13 / 5)) -> 6
```

分析

無

```
// LeetCode, Evaluate Reverse Polish Notation
// 遞歸, 時間複雜度 O(n), 空間複雜度 O(logn)
class Solution {
public:
    int evalRPN(vector<string> &tokens) {
        int x, y;
        auto token = tokens.back(); tokens.pop_back();
        if (is_operator(token)) {
            y = evalRPN(tokens);
            x = evalRPN(tokens);
            if (token[0] == '+')
                                       x += y;
            else if (token[0] == '-') x -= y;
            else if (token[0] == '*') x *= y;
            else
                                       x /= y;
        } else {
            size_t i;
            x = stoi(token, \&i);
        return x;
    }
private:
    bool is_operator(const string &op) {
        return op.size() == 1 && string("+-*/").find(op) != string::npos;
    }
};
```

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迭代版

```
// LeetCode, Max Points on a Line
// 迭代, 時間複雜度 O(n), 空間複雜度 O(logn)
class Solution {
public:
    int evalRPN(vector<string> &tokens) {
        stack<string> s;
        for (auto token: tokens) {
            if (!is_operator(token)) {
                s.push(token);
            } else {
                int y = stoi(s.top());
                s.pop();
                int x = stoi(s.top());
                s.pop();
                if (token[0] == '+')
                else if (token[0] == '-')
                                           x -= y;
                else if (token[0] == '*')
                                           x *= y;
                                           x /= y;
                s.push(to_string(x));
            }
        }
        return stoi(s.top());
    }
private:
    bool is_operator(const string &op) {
        return op.size() == 1 && string("+-*/").find(op) != string::npos;
    }
};
```

相關題目

• 無

5.2 隊列

5.2.1 Sliding Window Maximum

描述

Given an array nums, there is a sliding window of size k which is moving from the very left of the array to the very right. You can only see the k numbers in the window. Each time the sliding window moves right by one position. Return the max sliding window.

```
Follow up: Could you solve it in linear time?
Example:
Input: nums = [1,3,-1,-3,5,3,6,7], and k = 3
Output: [3,3,5,5,6,7]
Explanation:
```

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Window position									Max
[1	3	-1]	-3	5	3	6	7		3
1	[3	-1	-3]	5	3	6	7		3
1	3	[-1	-3	5]	3	6	7		5
1	3	-1	[-3	5	3]	6	7		5
1	3	-1	-3	[5	3	6]	7		6
1	3	-1	-3	5	[3	6	7]		7

分析

以 deque 來追踪視窗內的指標、移除老去的指標、移除數值太細的元素指標

Code

```
// LeetCode
// 迭代, 時間複雜度 O(n), 空間複雜度 O(n)
class Solution {
public:
    vector<int> maxSlidingWindow(vector<int>& nums, int k) {
        int N = nums.size();
        if (N < k) return vector<int>();
        vector<int> result; result.reserve(N-k+1);
        deque<int> indexList;
        // 預準首 K 項
        for (size_t i = 0; i < k; i++)
            while (!indexList.empty() && nums[indexList.back()] < nums[i])</pre>
                indexList.pop_back();
            indexList.push_back(i);
        result.push_back(nums[indexList.front()]);
        // 完成剩下的元素
        for (size_t i = k; i < nums.size(); i++)</pre>
        {
            // 移除老去的元素
            while (!indexList.empty() && indexList.front() < i-k+1)</pre>
                indexList.pop_front();
            // 移除數值太細的元素
            while (!indexList.empty() && nums[indexList.back()] < nums[i])</pre>
                indexList.pop_back();
            indexList.push_back(i);
            result.push_back(nums[indexList.front()]);
        }
        return result;
```

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```
};
```

相關題目

• 無

5.2.2 Meeting Rooms II

描述

Given an array of meeting time intervals consisting of start and end times [[s1,e1],[s2,e2],...] (si < ei), find the minimum number of conference rooms required.

Example 1

```
Input: [[0, 30],[5, 10],[15, 20]]
Output: 2
    Example 2
Input: [[7,10],[2,4]]
Output: 1
```

分析

Nil

Priority Queue

```
// LeetCode
// 迭代, 時間複雜度 O(nlogn), 空間複雜度 O(n)
class Solution {
public:
    int minMeetingRooms(vector<vector<int>>& intervals) {
       // 順序所以時間段落
       sort(intervals.begin(), intervals.end()
             , [&](const auto& first, const auto& second)
                  return first[0] < second[0];</pre>
              });
       // 利用 priority queue 找出最快完結的時間段落
       auto Compare = [](const auto& first, const auto& second)
                         { return first.second > second.second; };
       priority_queue<pair<int, int>, vector<pair<int, int>>, decltype(Compare)>
                         pq(Compare);
       int maxUsed = 0;
       for (const auto& interval : intervals)
       {
           // 移除用完的房間
```

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```
while (!pq.empty() && interval[0] >= pq.top().second)
                 pq.pop();
             // 加入新的時間段落
             pq.push(make_pair(interval[0], interval[1]));
             // 更新同一時間的最大房間用量
             maxUsed = max(maxUsed, (int)pq.size());
         }
         return maxUsed;
     }
 };
Start End Vector
 // LeetCode
 // 迭代, 時間複雜度 O(nlogn), 空間複雜度 O(n)
 class Solution {
 public:
     int minMeetingRooms(vector<vector<int>>& intervals) {
         // 使用兩支 vector 一支為 startTime, 一支為 endTime
         vector<int> startTime, endTime;
         startTime.reserve(intervals.size());
         endTime.reserve(intervals.size());
         for (const auto& interval : intervals)
         {
             startTime.push_back(interval[0]);
             endTime.push_back(interval[1]);
         // 由細至大
         sort(startTime.begin(), startTime.end());
         sort(endTime.begin(), endTime.end());
         // 計算房間多少
         int curRm = 0;
         int maxRm = 0;
         int ei = 0;
         for (int si = 0; si < (int)startTime.size(); si++)</pre>
             while (startTime[si] >= endTime[ei])
             {
                 ei++;
                 curRm--;
             curRm++;
             maxRm = max(maxRm, curRm);
         return maxRm;
     }
 }:
```

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相關題目

無

5.3 Implement Queue using Stack

5.3.1 描述

Implement the following operations of a queue using stacks.

- push(x) Push element x to the back of queue.
- pop() Removes the element from in front of queue.
- peek() Get the front element.
- empty() Return whether the queue is empty.

Example:

```
MyQueue queue = new MyQueue();
queue.push(1);
queue.push(2);
queue.peek(); // returns 1
queue.pop(); // returns 1
queue.empty(); // returns false
```

Note:

- You must use only standard operations of a stack which means only push to top, peek/pop from top, size, and is empty operations are valid.
- Depending on your language, stack may not be supported natively. You may simulate a stack by using
 a list or deque (double-ended queue), as long as you use only standard operations of a stack.
- You may assume that all operations are valid (for example, no pop or peek operations will be called on an empty queue).

5.3.2 分析

```
push: O(1), pop: O(1)
```

5.3.3 代碼

```
// LeetCode
// 時間複雜度 D(), 空間複雜度 D()
class MyQueue {
public:
    /** Initialize your data structure here. */
    MyQueue() {
}
```

```
/** Push element x to the back of queue. */
    void push(int x) {
        if (m_data_001.empty())
            m_front = x;
        m_data_001.push(x);
    }
    /** Removes the element from in front of queue and returns that element. */
    int pop() {
        if (m_data_002.empty())
            while (!m_data_001.empty())
                m_data_002.push(m_data_001.top());
                m_data_001.pop();
        int tmp = m_data_002.top();
        m_data_002.pop();
        return tmp;
    /** Get the front element. */
    int peek() {
        if (!m_data_002.empty())
            return m_data_002.top();
        return m_front;
    /** Returns whether the queue is empty. */
    bool empty() {
        return m_data_001.empty() && m_data_002.empty();
    }
private:
    stack<int> m_data_001;
    stack<int> m_data_002;
    int m_front;
};
/**
 * Your MyQueue object will be instantiated and called as such:
 * MyQueue* obj = new MyQueue();
 * obj->push(x);
 * int param_2 = obj->pop();
 * int param_3 = obj->peek();
 * bool param_4 = obj->empty();
```

5.4 Implement Stack using Queues

5.4.1 描述

Implement the following operations of a stack using queues.

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- push(x) Push element x onto stack.
- pop() Removes the element on top of the stack.
- top() Get the top element.
- empty() Return whether the stack is empty.

Example:

```
MyStack stack = new MyStack();
stack.push(1);
stack.push(2);
stack.top(); // returns 2
stack.pop(); // returns 2
stack.empty(); // returns false
```

- You must use only standard operations of a queue which means only push to back, peek/pop from front, size, and is empty operations are valid.
- Depending on your language, queue may not be supported natively. You may simulate a queue by using a list or deque (double-ended queue), as long as you use only standard operations of a queue.
- You may assume that all operations are valid (for example, no pop or top operations will be called on an empty stack).

5.4.2 分析

```
push: O(n), pop: O(1)
```

5.4.3 代碼

```
// LeetCode
// 時間複雜度 D(), 空間複雜度 D()
class MyStack {
public:
    /** Initialize your data structure here. */
    MyStack() {
    }
    /** Push element x onto stack. */
    void push(int x) {
        m_data.push(x);
        size_t sz = m_data.size();
        while (sz > 1)
            m_data.push(m_data.front());
            m_data.pop();
            sz--;
    }
```

```
/** Removes the element on top of the stack and returns that element. */
    int pop() {
        int tmp = m_data.front();
        m_data.pop();
        return tmp;
    }
    /** Get the top element. */
    int top() {
        return m_data.front();
    /** Returns whether the stack is empty. */
    bool empty() {
       return m_data.empty();
    }
private:
    queue<int> m_data;
};
 * Your MyStack object will be instantiated and called as such:
* MyStack* obj = new MyStack();
* obj->push(x);
* int param_2 = obj->pop();
 * int param_3 = obj->top();
 * bool param_4 = obj->empty();
```

第6章

```
LeetCode 上二叉樹的節點定義如下:

// 樹的節點
struct TreeNode {
    int val;
    TreeNode *left;
    TreeNode *right;
    TreeNode(int x): val(x), left(nullptr), right(nullptr) { }
};
6.1 二叉樹的遍歷
```

樹的遍歷有兩類:深度優先遍歷和寬度優先遍歷。深度優先遍歷又可分為兩種:先根(次序)遍歷和後根(次序)遍歷。

樹的先根遍歷是:先訪問樹的根結點,然後依次先根遍歷根的各棵子樹。樹的先跟遍歷的結果 與對應二叉樹(孩子兄弟表示法)的先序遍歷的結果相同。

樹的後根遍歷是: 先依次後根遍歷樹根的各棵子樹, 然後訪問根結點。樹的後跟遍歷的結果與 對應二叉樹的中序遍歷的結果相同。

二叉樹的先根遍歷有: **先序遍歷**(root->left->right), root->right->left; 後根遍歷有: **後序遍歷**(left->right->root), right->left->root; 二叉樹還有個一般的樹沒有的遍歷次序, **中序遍歷**(left->root->right)。

6.1.1 Binary Tree Preorder Traversal

描述

Given a binary tree, return the preorder traversal of its nodes' values.

For example: Given binary tree {1,#,2,3},



return

1, 2, 3

Note: Recursive solution is trivial, could you do it iteratively?

分析

用棧或者 Morris 遍歷。

棧

```
// LeetCode, Binary Tree Preorder Traversal
 // 使用棧, 時間複雜度 O(n), 空間複雜度 O(n)
 class Solution {
 public:
     vector<int> preorderTraversal(TreeNode *root) {
         vector<int> result;
         stack<const TreeNode *> s;
         if (root != nullptr) s.push(root);
         while (!s.empty()) {
             const TreeNode *p = s.top();
             s.pop();
             result.push_back(p->val);
             if (p->right != nullptr) s.push(p->right);
             if (p->left != nullptr) s.push(p->left);
         return result;
     }
 };
Morris 先序遍歷
 // LeetCode, Binary Tree Preorder Traversal
 // Morris 先序遍歷, 時間複雜度 O(n), 空間複雜度 O(1)
 class Solution {
 public:
     vector<int> preorderTraversal(TreeNode *root) {
         vector<int> result;
         TreeNode *cur = root, *prev = nullptr;
         while (cur != nullptr) {
             if (cur->left == nullptr) {
                 result.push_back(cur->val);
                 prev = cur; /* cur 剛剛被訪問過 */
                 cur = cur->right;
             } else {
                 /* 查找前驅 */
                 TreeNode *node = cur->left;
                 while (node->right != nullptr && node->right != cur)
                     node = node->right;
```

if (node->right == nullptr) { /* 還沒線索化, 則建立線索 */

相關題目

- Binary Tree Inorder Traversal, 見 §6.1.2
- Binary Tree Postorder Traversal, 見 §6.1.3
- Recover Binary Search Tree, 見 §6.1.8

6.1.2 Binary Tree Inorder Traversal

描述

Given a binary tree, return the inorder traversal of its nodes' values.

For example: Given binary tree {1,#,2,3},



return

1, 3, 2

Note: Recursive solution is trivial, could you do it iteratively?

分析

用棧或者 Morris 遍歷。

榁

```
// LeetCode, Binary Tree Inorder Traversal
 // 使用棧, 時間複雜度 O(n), 空間複雜度 O(n)
 class Solution {
 public:
     vector<int> inorderTraversal(TreeNode *root) {
         vector<int> result;
         stack<const TreeNode *> s:
         const TreeNode *p = root;
         while (!s.empty() || p != nullptr) {
             if (p != nullptr) {
                 s.push(p);
                 p = p \rightarrow left;
             } else {
                 p = s.top();
                 s.pop();
                 result.push_back(p->val);
                 p = p->right;
             }
         return result;
     }
 };
Morris 中序遍歷
 // LeetCode, Binary Tree Inorder Traversal
 // Morris 中序遍歷, 時間複雜度 O(n), 空間複雜度 O(1)
 class Solution {
 public:
     vector<int> inorderTraversal(TreeNode *root) {
         vector<int> result;
         TreeNode *cur = root, *prev = nullptr;
         while (cur != nullptr) {
             if (cur->left == nullptr) {
                 result.push_back(cur->val);
                 prev = cur;
                 cur = cur->right;
             } else {
                 /* 查找前驅 */
                 TreeNode *node = cur->left;
                 while (node->right != nullptr && node->right != cur)
                     node = node->right;
                 if (node->right == nullptr) { /* 還沒線索化, 則建立線索 */
                     node->right = cur;
                     /* prev = cur; 不能有這句, cur 還沒有被訪問 */
                     cur = cur->left;
                 } else {
                            /* 已經線索化,則訪問節點,並刪除線索 */
```

result.push_back(cur->val);

相關題目

- Binary Tree Preorder Traversal, 見 §6.1.1
- Binary Tree Postorder Traversal, 見 §6.1.3
- Recover Binary Search Tree, 見 §6.1.8

6.1.3 Binary Tree Postorder Traversal

描述

Given a binary tree, return the postorder traversal of its nodes' values.

```
For example: Given binary tree {1,#,2,3},
```

return

3, 2, 1

Note: Recursive solution is trivial, could you do it iteratively?

分析

用棧或者 Morris 遍歷。

槔

```
// LeetCode, Binary Tree Postorder Traversal
// 使用棧,時間複雜度 O(n),空間複雜度 O(n)
class Solution {
public:
    vector<int> postorderTraversal(TreeNode *root) {
    vector<int> result;
    stack<const TreeNode *> s;
```

```
/* p, 正在訪問的結點, q, 剛剛訪問過的結點*/
         const TreeNode *p = root, *q = nullptr;
         do {
             while (p != nullptr) { /* 往左下走*/
                 s.push(p);
                 p = p \rightarrow left;
             q = nullptr;
             while (!s.empty()) {
                 p = s.top();
                 s.pop();
                 /* 右孩子不存在或已被訪問, 訪問之*/
                 if (p->right == q) {
                    result.push_back(p->val);
                    q = p; /* 保存剛訪問過的結點*/
                 } else {
                    /* 當前結點不能訪問, 需第二次進棧*/
                     s.push(p);
                     /* 先處理右子樹*/
                    p = p->right;
                    break;
                 }
         } while (!s.empty());
         return result;
     }
 };
Morris 後序遍歷
 // LeetCode, Binary Tree Postorder Traversal
 // Morris 後序遍歷, 時間複雜度 O(n), 空間複雜度 O(1)
 class Solution {
 public:
     vector<int> postorderTraversal(TreeNode *root) {
         vector<int> result;
         TreeNode dummy(-1);
         TreeNode *cur, *prev = nullptr;
         std::function < void(const TreeNode*)> visit =
             [&result](const TreeNode *node){
             result.push_back(node->val);
         };
         dummy.left = root;
         cur = &dummy;
         while (cur != nullptr) {
             if (cur->left == nullptr) {
                prev = cur; /* 必須要有 */
                 cur = cur->right;
             } else {
```

```
TreeNode *node = cur->left;
               while (node->right != nullptr && node->right != cur)
                   node = node->right;
               if (node->right == nullptr) { /* 還沒線索化, 則建立線索 */
                   node->right = cur;
                   prev = cur; /* 必須要有 */
                   cur = cur->left;
               } else { /* 已經線索化,則訪問節點,並刪除線索 */
                   visit_reverse(cur->left, prev, visit);
                   prev->right = nullptr;
                   prev = cur; /* 必須要有 */
                   cur = cur->right;
               }
           }
       }
       return result;
private:
   // 逆轉路徑
    static void reverse(TreeNode *from, TreeNode *to) {
       TreeNode *x = from, *y = from->right, *z;
       if (from == to) return;
       while (x != to) {
           z = y->right;
           y->right = x;
           x = y;
           y = z;
       }
   }
    // 訪問逆轉後的路徑上的所有結點
    static void visit_reverse(TreeNode* from, TreeNode *to,
                    std::function< void(const TreeNode*) >& visit) {
       TreeNode *p = to;
       reverse(from, to);
       while (true) {
           visit(p);
           if (p == from)
               break;
           p = p->right;
       reverse(to, from);
    }
};
```

相關題目

• Binary Tree Preorder Traversal, 見 §6.1.1

- Binary Tree Inorder Traversal, 見 §6.1.2
- Recover Binary Search Tree, 見 §6.1.8

6.1.4 Binary Tree Level Order Traversal

描述

Given a binary tree, return the level order traversal of its nodes' values. (ie, from left to right, level by level).

```
For example: Given binary tree {3,9,20,#,#,15,7},

3
/ \
9 20
/ \
15 7

return its level order traversal as:

[
[3],
[9,20],
[15,7]
]
```

分析

無

```
// LeetCode, Binary Tree Level Order Traversal
// 遞歸版, 時間複雜度 O(n), 空間複雜度 O(n)
class Solution {
public:
    vector<vector<int> > levelOrder(TreeNode *root) {
        vector<vector<int>> result;
        traverse(root, 1, result);
        return result;
    }
   void traverse(TreeNode *root, size_t level, vector<vector<int>> &result) {
        if (!root) return;
        if (level > result.size())
            result.push_back(vector<int>());
        result[level-1].push_back(root->val);
        traverse(root->left, level+1, result);
        traverse(root->right, level+1, result);
```

```
};
```

迭代版

```
// LeetCode, Binary Tree Level Order Traversal
// 迭代版, 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    vector<vector<int> > levelOrder(TreeNode *root) {
        vector<vector<int> > result;
        queue<TreeNode*> current, next;
        if(root == nullptr) {
            return result;
        } else {
            current.push(root);
        while (!current.empty()) {
            vector<int> level; // elments in one level
            while (!current.empty()) {
                TreeNode* node = current.front();
                current.pop();
                level.push_back(node->val);
                if (node->left != nullptr) next.push(node->left);
                if (node->right != nullptr) next.push(node->right);
            result.push_back(level);
            swap(next, current);
        return result;
    }
};
```

相關題目

- Binary Tree Level Order Traversal II, 見 §6.1.5
- Binary Tree Zigzag Level Order Traversal, 見 §6.1.6

6.1.5 Binary Tree Level Order Traversal II

描述

Given a binary tree, return the bottom-up level order traversal of its nodes' values. (ie, from left to right, level by level from leaf to root).

For example: Given binary tree {3,9,20,#,#,15,7},

```
3
     /\
   9 20
     15
return its bottom-up level order traversal as:
  Γ
    [15,7]
    [9,20],
    [3],
 ٦
分析
   在上一題 (見 §6.1.4) 的基礎上, reverse() 一下即可。
遞歸版
  // LeetCode, Binary Tree Level Order Traversal II
 // 遞歸版, 時間複雜度 O(n), 空間複雜度 O(n)
 class Solution {
 public:
     vector<vector<int> > levelOrderBottom(TreeNode *root) {
         vector<vector<int>> result;
         traverse(root, 1, result);
         std::reverse(result.begin(), result.end()); // 比上一題多此一行
         return result;
     }
     void traverse(TreeNode *root, size_t level, vector<vector<int>> &result) {
         if (!root) return;
          if (level > result.size())
             result.push_back(vector<int>());
         result[level-1].push_back(root->val);
         traverse(root->left, level+1, result);
         traverse(root->right, level+1, result);
     }
 };
迭代版
  // LeetCode, Binary Tree Level Order Traversal II
 // 迭代版, 時間複雜度 O(n), 空間複雜度 O(1)
 class Solution {
 public:
     vector<vector<int> > levelOrderBottom(TreeNode *root) {
         vector<vector<int> > result;
         if(root == nullptr) return result;
```

```
queue<TreeNode*> current, next;
        vector<int> level; // elments in level level
        current.push(root);
        while (!current.empty()) {
            while (!current.empty()) {
                TreeNode* node = current.front();
                current.pop();
                level.push_back(node->val);
                if (node->left != nullptr) next.push(node->left);
                if (node->right != nullptr) next.push(node->right);
            result.push_back(level);
            level.clear();
            swap(next, current);
        reverse(result.begin(), result.end()); // 比上一題多此一行
        return result;
    }
};
```

相關題目

- Binary Tree Level Order Traversal, 見 §6.1.4
- Binary Tree Zigzag Level Order Traversal, 見 §6.1.6

6.1.6 Binary Tree Zigzag Level Order Traversal

描述

Given a binary tree, return the zigzag level order traversal of its nodes' values. (ie, from left to right, then right to left for the next level and alternate between).

```
For example: Given binary tree 3,9,20,#,#,15,7,
3
/ \
```

```
/\
9 20
/\
15 7
```

return its zigzag level order traversal as:

```
[
[3],
[20,9],
[15,7]
```

分析

廣度優先遍歷、用一個 bool 記錄是從左到右還是從右到左、每一層結束就翻轉一下。

禠歸版

```
// LeetCode, Binary Tree Zigzag Level Order Traversal
 // 遞歸版, 時間複雜度 O(n), 空間複雜度 O(n)
 class Solution {
 public:
     vector<vector<int> > zigzagLevelOrder(TreeNode *root) {
         vector<vector<int>> result:
         traverse(root, 1, result, true);
         return result:
     }
     void traverse(TreeNode *root, size_t level, vector<vector<int>> &result,
             bool left_to_right) {
         if (!root) return:
         if (level > result.size())
             result.push_back(vector<int>());
         if (left_to_right)
             result[level-1].push_back(root->val);
         else
             result[level-1].insert(result[level-1].begin(), root->val);
         traverse(root->left, level+1, result, !left_to_right);
         traverse(root->right, level+1, result, !left_to_right);
     }
 };
迭代版
 // LeetCode, Binary Tree Zigzag Level Order Traversal
 // 廣度優先遍歷. 用一個 bool 記錄是從左到右還是從右到左, 每一層結束就翻轉一下。
 // 迭代版, 時間複雜度 O(n), 空間複雜度 O(n)
 class Solution {
 public:
     vector<vector<int> > zigzagLevelOrder(TreeNode *root) {
         vector<vector<int> > result;
         queue<TreeNode*> current, next;
         bool left_to_right = true;
         if(root == nullptr) {
             return result;
         } else {
             current.push(root);
         while (!current.empty()) {
```

```
vector<int> level; // elments in one level
while (!current.empty()) {
    TreeNode* node = current.front();
    current.pop();
    level.push_back(node->val);
    if (node->left != nullptr) next.push(node->left);
    if (node->right != nullptr) next.push(node->right);
    }
    if (!left_to_right) reverse(level.begin(), level.end());
    result.push_back(level);
    left_to_right = !left_to_right;
    swap(next, current);
}
return result;
}
```

相關題目

- Binary Tree Level Order Traversal, 見 §6.1.4
- Binary Tree Level Order Traversal II, 見 §6.1.5

6.1.7 Binary Tree Right side View

描述

Given a binary tree, imagine yourself standing on the right side of it, return the values of the nodes you can see ordered from top to bottom.

For example: Given binary tree 3,9,20,#,#,15,7,



return as:

[3,20,7]

分析

雙 queue BFS zigzag travel, 只選最右

```
// LeetCode, Binary Tree Zigzag Level Order Traversal
// 遞歸版,時間複雜度 O(n),空間複雜度 O(n)
class Solution {
```

```
public:
    vector<int> rightSideView(TreeNode* root) {
        if (root == nullptr) return vector<int>();
        vector<int> result;
        // 雙 queue BFS zigzag travel
        queue<TreeNode*> cur, next;
        cur.push(root);
        while (!cur.empty())
            while (!cur.empty())
                TreeNode *p = cur.front();
                cur.pop();
                if (cur.size() == 0) // 只選最右
                    result.push_back(p->val);
                if (p->left) next.push(p->left);
                if (p->right) next.push(p->right);
            }
            swap(cur, next);
        }
        return result;
    }
};
```

相關題目

- Binary Tree Level Order Traversal, 見 §6.1.4
- Binary Tree Level Order Traversal II, 見 §6.1.5

6.1.8 Recover Binary Search Tree

描述

Two elements of a binary search tree (BST) are swapped by mistake.

Recover the tree without changing its structure.

Note: A solution using O(n) space is pretty straight forward. Could you devise a constant space solution?

分析

O(n) 空間的解法是,開一個指針數組,中序遍歷,將節點指針依次存放到數組裏,然後尋找兩處逆向的位置,先從前往後找第一個逆序的位置,然後從後往前找第二個逆序的位置,交換這兩個指針的值。

中序遍歷一般需要用到棧,空間也是O(n)的,如何才能不使用棧? Morris 中序遍歷。

代碼

```
// LeetCode, Recover Binary Search Tree
// Morris 中序遍歷, 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    void recoverTree(TreeNode* root) {
        pair<TreeNode*, TreeNode*> broken;
        TreeNode* prev = nullptr;
        TreeNode* cur = root;
        while (cur != nullptr) {
            if (cur->left == nullptr) {
                detect(broken, prev, cur);
                prev = cur;
                cur = cur->right;
            } else {
                auto node = cur->left;
                while (node->right != nullptr && node->right != cur)
                   node = node->right;
                if (node->right == nullptr) {
                   node->right = cur;
                    //prev = cur; 不能有這句!因為 cur 還沒有被訪問
                   cur = cur->left;
                } else {
                   detect(broken, prev, cur);
                   node->right = nullptr;
                   prev = cur;
                   cur = cur->right;
                }
           }
        }
        swap(broken.first->val, broken.second->val);
    }
    void detect(pair<TreeNode*, TreeNode*>& broken, TreeNode* prev,
            TreeNode* current) {
        if (prev != nullptr && prev->val > current->val) {
            if (broken.first == nullptr) {
                broken.first = prev;
            } //不能用 else, 例如 {0,1}, 會導致最後 swap 時 second 為 nullptr,
              //會 Runtime Error
           broken.second = current;
       }
   }
};
```

相關題目

• Binary Tree Inorder Traversal, 見 §6.1.2

6.1.9 Same Tree

描述

Given two binary trees, write a function to check if they are equal or not.

Two binary trees are considered equal if they are structurally identical and the nodes have the same value.

分析

無

遞歸版

```
搋歸版
```

// LeetCode, Same Tree

```
// 遞歸版, 時間複雜度 O(n), 空間複雜度 O(logn)
 class Solution {
 public:
     bool isSameTree(TreeNode *p, TreeNode *q) {
         if (!p && !q) return true;
                                     // 終止條件
         if (!p || !q) return false; // 剪枝
                                     // 三方合併
         return p->val == q->val
                 && isSameTree(p->left, q->left)
                 && isSameTree(p->right, q->right);
     }
 };
迭代版
 // LeetCode, Same Tree
 // 迭代版, 時間複雜度 O(n), 空間複雜度 O(logn)
 class Solution {
 public:
     bool isSameTree(TreeNode *p, TreeNode *q) {
         stack<TreeNode*> s;
         s.push(p);
         s.push(q);
         while(!s.empty()) {
             p = s.top(); s.pop();
             q = s.top(); s.pop();
             if (!p && !q) continue;
             if (!p || !q) return false;
```

```
if (p->val != q->val) return false;
    s.push(p->left);
    s.push(q->left);
    s.push(p->right);
    s.push(q->right);
    }
    return true;
}
```

相關題目

• Symmetric Tree, 見 §6.1.12

6.1.10 Count Univalue Subtrees

描述

Given a binary tree, count the number of uni-value subtrees.

A Uni-value subtree means all nodes of the subtree have the same value.

Example:

Output: 4

分析

無

Pass Parent Values

```
// LeetCode
// 迭代版, 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    int countUnivalSubtrees(TreeNode* root) {
        if (root == nullptr) return 0;
        int count = 0;
        DFS(root, count, root->val - 1);
```

```
return count;
     }
 private:
     bool DFS(TreeNode *root, int& count, int parVal) {
         if (root == nullptr) return true;
         int leftCount, rightCount; leftCount = rightCount = 0;
         bool isLeftUni = DFS(root->left, leftCount, root->val);
         bool isRightUni = DFS(root->right, rightCount, root->val);
         count += leftCount + rightCount;
         if (!isLeftUni || !isRightUni) return false;
         count++;
         return root->val == parVal;
     }
 };
遞歸版
 // LeetCode
 // 迭代版, 時間複雜度 O(n), 空間複雜度 O(logn)
 class Solution {
 public:
     int countUnivalSubtrees(TreeNode* root) {
         if (root == nullptr) return 0;
         int uniCount = 0;
         bool uniTrue = false:
         countUnivalSubtrees(root, uniCount, uniTrue);
         return uniCount;
     }
 private:
     void countUnivalSubtrees(TreeNode *root, int& uniCount, bool& uniTrue) {
         if (root == nullptr) {
             uniCount = 0;
             uniTrue = false;
         else if (root->left == nullptr && root->right == nullptr) {
             uniCount = 1;
             uniTrue = true;
         else {
              int uniLeft, uniRight; uniLeft = uniRight = 0;
             bool isUniLeft, isUniRight; isUniLeft = isUniRight = false;
             countUnivalSubtrees(root->left, uniLeft, isUniLeft);
             countUnivalSubtrees(root->right, uniRight, isUniRight);
             // 三方比較
```

相關題目

• Same Tree, 見 §6.1.9

6.1.11 Lowest Common Ancestor of Binary Tree

描述

Given a binary tree, find the lowest common ancestor (LCA) of two given nodes in the tree.

According to the definition of LCA on Wikipedia: "The lowest common ancestor is defined between two nodes p and q as the lowest node in T that has both p and q as descendants (where we allow a node to be a descendant of itself)."

Given the following binary tree: root = [3,5,1,6,2,0,8,null,null,7,4]



图 6-1 Loest common ancestor

```
Example 1: Input: root = [3,5,1,6,2,0,8,null,null,7,4], p = 5, q = 1 Output: 3 Explanation: The LCA of nodes 5 and 1 is 3.
```

```
Example 2:
```

```
Input: root = [3,5,1,6,2,0,8,null,null,7,4], p = 5, q = 4
Output: 5
Explanation: The LCA of nodes 5 and 4 is 5
, since a node can be a descendant of itself according to the LCA definition.
```

分析

無

遞歸版

```
// LeetCode
// 遞歸版, 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    TreeNode* lowestCommonAncestor(TreeNode* root, TreeNode* p, TreeNode* q) {
        if (root == nullptr) return root;
        if (root == p || root == q) return root;

        TreeNode *left = lowestCommonAncestor(root->left, p, q);
        TreeNode *right = lowestCommonAncestor(root->right, p, q);

        if (left && right) return root;
        else if (!left) return right;
        else return left;
    }
};
```

相關題目

• Same Tree, 見 §6.1.9

6.1.12 Symmetric Tree

描述

Given two binary trees, write a function to check if they are equal or not.

Two binary trees are considered equal if they are structurally identical and the nodes have the same value.

分析

無

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搋歸版

```
// LeetCode, Symmetric Tree
 // 遞歸版, 時間複雜度 O(n), 空間複雜度 O(logn)
 class Solution {
 public:
     bool isSymmetric(TreeNode *root) {
         if (root == nullptr) return true;
         return isSymmetric(root->left, root->right);
     }
     bool isSymmetric(TreeNode *p, TreeNode *q) {
                                                          // 終止條件
         if (p == nullptr && q == nullptr) return true;
         if (p == nullptr || q == nullptr) return false; // 終止條件
         return p->val == q->val
                                     // 三方合併
                 && isSymmetric(p->left, q->right)
                 && isSymmetric(p->right, q->left);
     }
 };
迭代版
 // LeetCode, Symmetric Tree
 // 迭代版, 時間複雜度 O(n), 空間複雜度 O(logn)
 class Solution {
 public:
     bool isSymmetric (TreeNode* root) {
         if (!root) return true;
         stack<TreeNode*> s;
         s.push(root->left);
         s.push(root->right);
         while (!s.empty ()) {
             auto p = s.top(); s.pop();
             auto q = s.top (); s.pop();
             if (!p && !q) continue;
             if (!p || !q) return false;
             if (p->val != q->val) return false;
             s.push(p->left);
             s.push(q->right);
             s.push(p->right);
             s.push(q->left);
         }
         return true;
     }
 };
```

相關題目

• Same Tree, 見 §6.1.9

6.1.13 Balanced Binary Tree

描述

Given a binary tree, determine if it is height-balanced.

For this problem, a height-balanced binary tree is defined as a binary tree in which the depth of the two subtrees of every node never differ by more than 1.

分析

無

代碼

```
// LeetCode, Balanced Binary Tree
// 時間複雜度 O(n), 空間複雜度 O(logn)
class Solution {
public:
   bool isBalanced (TreeNode* root) {
        return balancedHeight (root) >= 0;
   }
     * Returns the height of `root` if `root` is a balanced tree,
     * otherwise, returns `-1`.
     */
    int balancedHeight (TreeNode* root) {
        if (root == nullptr) return 0; // 終止條件
        int left = balancedHeight (root->left);
        int right = balancedHeight (root->right);
        if (left < 0 || right < 0 || abs(left - right) > 1) return -1; // 剪枝
        return max(left, right) + 1; // 三方合併
   }
};
```

相關題目

無

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6.1.14 Flatten Binary Tree to Linked List

描述

Given a binary tree, flatten it to a linked list in-place.

For example, Given



The flattened tree should look like:



分析

無

```
// LeetCode, Flatten Binary Tree to Linked List
// 遞歸版 1, 時間複雜度 O(n), 空間複雜度 O(logn)
class Solution {
public:
   void flatten(TreeNode *root) {
       if (root == nullptr) return; // 終止條件
       flatten(root->left);
       flatten(root->right);
       if (nullptr == root->left) return;
       // 三方合併, 將左子樹所形成的鏈表插入到 root 和 root->right 之間
       TreeNode *p = root->left;
       while(p->right) p = p->right; //尋找左鏈表最後一個節點
       p->right = root->right;
       root->right = root->left;
       root->left = nullptr;
   }
};
```

```
// LeetCode, Flatten Binary Tree to Linked List
 // 遞歸版 2
 // @author 王順達(http://weibo.com/u/1234984145)
 // 時間複雜度 O(n), 空間複雜度 O(logn)
  class Solution {
 public:
     void flatten(TreeNode *root) {
         flatten(root, NULL);
     }
 private:
     // 把 root 所代表樹變成鏈表後, tail 跟在該鏈表後面
     TreeNode *flatten(TreeNode *root, TreeNode *tail) {
         if (NULL == root) return tail;
         root->right = flatten(root->left, flatten(root->right, tail));
         root->left = NULL;
         return root;
 };
迭代版
 // LeetCode, Flatten Binary Tree to Linked List
 // 迭代版, 時間複雜度 O(n), 空間複雜度 O(logn)
 class Solution {
 public:
     void flatten(TreeNode* root) {
         if (root == nullptr) return;
         stack<TreeNode*> s;
         s.push(root);
         while (!s.empty()) {
             auto p = s.top();
             s.pop();
             if (p->right)
                 s.push(p->right);
             if (p->left)
                 s.push(p->left);
             p->left = nullptr;
             if (!s.empty())
                 p->right = s.top();
         }
     }
 };
```

相關題目

無

6.1.15 Populating Next Right Pointers in Each Node II

描述

Follow up for problem "Populating Next Right Pointers in Each Node".

What if the given tree could be any binary tree? Would your previous solution still work?

Note: You may only use constant extra space.

For example, Given the following binary tree,



After calling your function, the tree should look like:

```
1 -> NULL
/ \
2 -> 3 -> NULL
/ \
4-> 5 -> 7 -> NULL
```

分析

要處理一個節點,可能需要最右邊的兄弟節點,首先想到用廣搜。但廣搜不是常數空間的,本題要求常數空間。

注意, 這題的代碼原封不動, 也可以解決 Populating Next Right Pointers in Each Node I.

6.1 二叉樹的遍歷 171

```
if (curr->right != nullptr){
                 prev->next = curr->right;
                 prev = prev->next;
             }
         connect(dummy.next);
     }
 };
迭代版
 // LeetCode, Populating Next Right Pointers in Each Node II
 // 時間複雜度 O(n), 空間複雜度 O(1)
 class Solution {
 public:
     void connect(TreeLinkNode *root) {
         while (root) {
             TreeLinkNode * next = nullptr; // the first node of next level
             TreeLinkNode * prev = nullptr; // previous node on the same level
             for (; root; root = root->next) {
                  if (!next) next = root->left ? root->left : root->right;
                  if (root->left) {
                      if (prev) prev->next = root->left;
                      prev = root->left;
                  if (root->right) {
                      if (prev) prev->next = root->right;
                      prev = root->right;
             }
             root = next; // turn to next level
         }
     }
 };
```

相關題目

• Populating Next Right Pointers in Each Node, 見 §6.4.6

6.1.16 Find Duplicate Subtrees

描述

Given a binary tree, return all duplicate subtrees. For each kind of duplicate subtrees, you only need to return the root node of any one of them.

Two trees are duplicate if they have the same structure with same node values.

Example 1:

```
1
2 3
/ / \
4 2 4
/
```

The following are two duplicate subtrees:

```
2
/
4
4
```

}

遞歸版

```
// 時間複雜度 O(n^2), 空間複雜度 O(n^2)
 class Solution {
 public:
     vector<TreeNode*> findDuplicateSubtrees(TreeNode* root) {
         unordered_map<string, int> cache;
         vector<TreeNode*> result;
         DFS(root, cache, result);
         return result;
     }
 private:
     string DFS(TreeNode *root, unordered_map<string, int>& cache, vector<TreeNode*>& result)
         if (!root) return "#";
         string serial = to_string(root->val) + "," + DFS(root->left, cache, result)
             + "," + DFS(root->right, cache, result);
         cache[serial]++;
         if (cache[serial] == 2)
             result.push_back(root);
         return serial;
     }
 };
遞歸版
 // 時間複雜度 O(n), 空間複雜度 O(n)
 class Solution {
 public:
     vector<TreeNode*> findDuplicateSubtrees(TreeNode* root) {
         unordered_map<size_t, int> cache;
         vector<TreeNode*> result;
         DFS(root, cache, result);
         return result;
```

6.2 二叉樹的構建 173

6.2 二叉樹的構建

6.2.1 Construct Binary Tree from Preorder and Inorder Traversal

描述

Given preorder and inorder traversal of a tree, construct the binary tree.

Note: You may assume that duplicates do not exist in the tree.

分析

```
1
                11 12
 Preorder: 1 2 4 8 5 9 10 3 6 7 11 12
            8 4 2 9 5 10 1 6 3 11 7 12
 Inorder:
 Postorder: 8 4 9 10 5 2 6 11 12 7 3 1
代碼
 // LeetCode, Construct Binary Tree from Preorder and Inorder Traversal
 // 遞歸, 時間複雜度 O(n), 空間複雜度 O(\logn)
 class Solution {
 public:
     TreeNode* buildTree(vector<int>& preorder, vector<int>& inorder) {
         return buildTree(begin(preorder), end(preorder),
                 begin(inorder), end(inorder));
     }
     template<typename InputIterator>
```

相關題目

• Construct Binary Tree from Inorder and Postorder Traversal, 見 §6.2.2

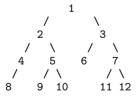
6.2.2 Construct Binary Tree from Inorder and Postorder Traversal

描述

Given inorder and postorder traversal of a tree, construct the binary tree.

Note: You may assume that duplicates do not exist in the tree.

分析



Preorder: 1 2 4 8 5 9 10 3 6 7 11 12 Inorder: 8 4 2 9 5 10 1 6 3 11 7 12 Postorder: 8 4 9 10 5 2 6 11 12 7 3 1

代碼

```
// LeetCode, Construct Binary Tree from Inorder and Postorder Traversal // 遞歸, 時間複雜度 O(n), 空間複雜度 O(logn) class Solution { public:
```

6.2 二叉樹的構建 175

```
TreeNode* buildTree(vector<int>& inorder, vector<int>& postorder) {
        return buildTree(begin(inorder), end(inorder),
                begin(postorder), end(postorder));
    }
    template<typename BidiIt>
    TreeNode* buildTree(BidiIt in_first, BidiIt in_last,
            BidiIt post first, BidiIt post last) {
        if (in_first ==in_last) return nullptr;
        if (post_first == post_last) return nullptr;
        const auto val = *prev(post_last);
        TreeNode* root = new TreeNode(val);
        auto inRootPos = find(in_first, in_last, val);
        auto leftSize = distance(in_first, inRootPos);
        auto postLeftLast = next(post_first, leftSize);
        root->left = buildTree(in first, inRootPos, post first, postLeftLast);
        root->right = buildTree(next(inRootPos), in_last, postLeftLast, prev(post_last));
        return root;
    }
};
```

相關題目

• Construct Binary Tree from Preorder and Inorder Traversal, 見 §6.2.1

6.2.3 Serialize and Deserialize Binary Tree

描述

Serialization is the process of converting a data structure or object into a sequence of bits so that it can be stored in a file or memory buffer, or transmitted across a network connection link to be reconstructed later in the same or another computer environment.

Design an algorithm to serialize and deserialize a binary tree. There is no restriction on how your serialization/deserialization algorithm should work. You just need to ensure that a binary tree can be serialized to a string and this string can be deserialized to the original tree structure.

Example:

You may serialize the following tree:



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```
as "[1,2,3,null,null,4,5]"
```

分析

無

遞歸版

```
// LeetCode
// 時間複雜度 O(n), 空間複雜度 O(n)
class Solution {
public:
    // Encodes a tree to a single string.
    string serialize(TreeNode* root) {
        string result;
        serialize(root, result);
        return result;
    }
    // Decodes your encoded data to tree.
    TreeNode* deserialize(string data) {
        list<string> parts = SplitParts(data, ',');
        return deserialize(parts);
    }
private:
    void serialize(TreeNode *root, string& result) {
        if (root == nullptr)
            result += "null,";
        else {
            result += to_string(root->val) + ",";
            serialize(root->left, result);
            serialize(root->right, result);
    }
    TreeNode *deserialize(list<string>& parts) {
        if (parts.front() == "null") {
            parts.pop_front();
            return nullptr;
        else {
            TreeNode *root = new TreeNode(StringToInt(parts.front()));
            parts.pop_front();
            root->left = deserialize(parts);
            root->right = deserialize(parts);
            return root;
        }
    list<string> SplitParts(const string& str, char deli) {
        list<string> result;
```

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```
for (auto i = str.begin(); i < str.end();) {</pre>
              auto j = find(i, str.end(), deli);
              result.push_back(string(i, j));
              i = next(j);
          return result;
      }
      int StringToInt(string num) {
          if (num.size() == 0) return 0;
          if (num[0] == '-')
              return -1 * stoi(num.substr(1));
              return stoi(num);
      }
 };
迭代 - BFS with queue
  // LeetCode
  // 時間複雜度 O(n), 空間複雜度 O(n)
  class Solution {
 public:
      // Encodes a tree to a single string.
      string serialize(TreeNode* root) {
          stringstream result;
          if (root == nullptr) return result.str();
          queue<TreeNode*> cur;
          cur.push(root);
          while (!cur.empty()) {
              TreeNode *p = cur.front();
              cur.pop();
              if (p == nullptr) {
                  result << "null,";
                  continue;
              else
                  result << p->val << ",";
              cur.push(p->left);
              cur.push(p->right);
          return result.str();
      }
      // Decodes your encoded data to tree.
      TreeNode* deserialize(string data) {
          if (data.size() == 0) return nullptr;
          auto i = find(data.begin(), data.end(), ',');
```

```
queue<TreeNode*> cur;
        // 製造 root
        TreeNode *root = new TreeNode(StringToInt(string(data.begin(), i)));
        i = next(i);
        cur.push(root);
        while (!cur.empty()) {
            TreeNode *p = cur.front();
            cur.pop();
            // 取兩個值, 一個為左, 一個為右
            // 左
            if (i >= data.end()) continue;
            auto j = find(i, data.end(), ',');
            string nextStr = string(i, j);
            if (nextStr != "null")
                p->left = new TreeNode(StringToInt(nextStr));
            i = next(j);
            // 右
            if (i >= data.end()) continue;
            j = find(i, data.end(), ',');
            nextStr = string(i, j);
            if (nextStr != "null")
                p->right = new TreeNode(StringToInt(nextStr));
            i = next(j);
            // 處理下一層
            if (p->left) cur.push(p->left);
            if (p->right) cur.push(p->right);
        }
        return root;
private:
    int StringToInt(string num) {
        if (num.size() == 0) return 0;
        if (num[0] == '-')
            return -1 * stoi(num.substr(1));
        else
            return stoi(num);
    }
};
```

相關題目

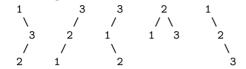
• Construct Binary Tree from Inorder and Postorder Traversal, 見 §6.2.2

6.3 二叉查找樹

6.3.1 Unique Binary Search Trees

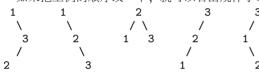
描述

Given n, how many structurally unique BST's (binary search trees) that store values 1...n? For example, Given n = 3, there are a total of 5 unique BST's.



分析

如果把上例的順序改一下,就可以看出規律了。



比如,以1為根的樹的個數,等於左子樹的個數乘以右子樹的個數,左子樹是0個元素的樹,右子樹是2個元素的樹。以2為根的樹的個數,等於左子樹的個數乘以右子樹的個數,左子樹是1個元素的樹,右子樹也是1個元素的樹。依此類推。

當數組為 1,2,3,...,n 時,基於以下原則的構建的 BST 樹具有唯一性: 以 i 為根節點的樹,其左子樹由 [1,i-1] 構成,其右子樹由 [i+1,n] 構成。

定義 f(i) 為以 [1,i] 能產生的 Unique Binary Search Tree 的數目,則如果數組為空,毫無疑問,只有一種 BST,即空樹,f(0)=1。如果數組僅有一個元素 1,只有一種 BST,單個節點,f(1)=1。如果數組任有一個元素 1 ,以第二十二三年三代

如果數組有兩個元素 1.2、 那麼有如下兩種可能



$$f(2) = f(0) * f(1)$$
 , 1 為根的情況
+ $f(1) * f(0)$, 2 為根的情況

再看一看 3 個元素的數組,可以發現 BST 的取值方式如下:

$$f(3) = f(0) * f(2)$$
 , 1 為根的情況
+ $f(1) * f(1)$, 2 為根的情況
+ $f(2) * f(0)$, 3 為根的情況

所以, 由此觀察, 可以得出 f 的遞推公式為

$$f(i) = \sum_{k=1}^{i} f(k-1) \times f(i-k)$$

至此, 問題劃歸為一維動態規劃。

代碼

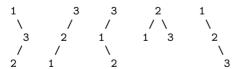
相關題目

• Unique Binary Search Trees II, 見 §6.3.2

6.3.2 Unique Binary Search Trees II

描述

Given n, generate all structurally unique BST's (binary search trees) that store values 1...n. For example, Given n=3, your program should return all 5 unique BST's shown below.



分析

見前面一題。

代碼

```
// LeetCode, Unique Binary Search Trees II
// 時間複雜度 TODO, 空間複雜度 TODO
class Solution {
public:
    vector<TreeNode *> generateTrees(int n) {
        if (n == 0) return generate(1, 0);
        return generate(1, n);
    }
private:
    vector<TreeNode *> generate(int start, int end) {
        vector<TreeNode*> subTree;
        if (start > end) {
            subTree.push_back(nullptr);
            return subTree;
        }
        for (int k = start; k \le end; k++) {
            vector<TreeNode*> leftSubs = generate(start, k - 1);
            vector<TreeNode*> rightSubs = generate(k + 1, end);
            for (auto i : leftSubs) {
                for (auto j : rightSubs) {
                    TreeNode *node = new TreeNode(k);
                    node->left = i;
                    node->right = j;
                    subTree.push_back(node);
                }
            }
        return subTree;
    }
};
```

相關題目

• Unique Binary Search Trees, 見 §6.3.1

6.3.3 Validate Binary Search Tree

描述

Given a binary tree, determine if it is a valid binary search tree (BST).

Assume a BST is defined as follows:

- The left subtree of a node contains only nodes with keys less than the node's key.
- The right subtree of a node contains only nodes with keys greater than the node's key.
- Both the left and right subtrees must also be binary search trees.

分析

代碼

相關題目

• Validate Binary Search Tree, 見 §6.3.3

6.3.4 Convert Sorted Array to Binary Search Tree

描述

Given an array where elements are sorted in ascending order, convert it to a height balanced BST.

分析

二分法。

代碼

```
if (length <= 0) return nullptr; // 終止條件

// 三方合併
auto mid = first + length / 2;
TreeNode* root = new TreeNode (*mid);
root->left = sortedArrayToBST(first, mid);
root->right = sortedArrayToBST(mid + 1, last);
return root;
}
};
```

相關題目

• Convert Sorted List to Binary Search Tree, 見 §6.3.5

6.3.5 Convert Sorted List to Binary Search Tree

描述

Given a singly linked list where elements are sorted in ascending order, convert it to a height balanced BST.

分析

這題與上一題類似,但是單鏈表不能隨機訪問,而自頂向下的二分法必須需要 RandomAccessIterator,因此前面的方法不適用本題。

存在一種自底向上 (bottom-up) 的方法,見 http://leetcode.com/2010/11/convert-sorted-list-to-balanced-binary.html

分治法, 自頂向下

```
分治法,類似於 Convert Sorted Array to Binary Search Tree,自頂向下,複雜度 O(n \log n)。

// LeetCode,Convert Sorted List to Binary Search Tree

// 分治法,類似於 Convert Sorted Array to Binary Search Tree,

// 自頂向下,時間複雜度 O(n^2),空間複雜度 O(\log n)

class Solution {

public:

    TreeNode* sortedListToBST (ListNode* head) {

        return sortedListToBST (head, listLength (head));
    }

TreeNode* sortedListToBST (ListNode* head, int len) {

        if (len == 0) return nullptr;

        if (len == 1) return new TreeNode (head->val);
```

```
TreeNode* root = new TreeNode (nth node (head, len / 2 + 1)->val);
         root->left = sortedListToBST (head, len / 2);
         root->right = sortedListToBST (nth node (head, len / 2 + 2),
                 (len - 1) / 2);
         return root;
     }
     int listLength (ListNode* node) {
         int n = 0;
         while(node) {
             ++n;
             node = node->next;
         }
         return n;
     }
     ListNode* nth_node (ListNode* node, int n) {
         while (--n)
             node = node->next;
         return node;
     }
 };
自底向上
 // LeetCode, Convert Sorted List to Binary Search Tree
 // bottom-up, 時間複雜度 O(n), 空間複雜度 O(logn)
 class Solution {
 public:
     TreeNode *sortedListToBST(ListNode *head) {
         int len = 0;
         ListNode *p = head;
         while (p) {
             len++;
             p = p->next;
         return sortedListToBST(head, 0, len - 1);
     }
 private:
     TreeNode* sortedListToBST(ListNode*& list, int start, int end) {
         if (start > end) return nullptr;
         int mid = start + (end - start) / 2;
         TreeNode *leftChild = sortedListToBST(list, start, mid - 1);
         TreeNode *parent = new TreeNode(list->val);
         parent->left = leftChild;
         list = list->next;
         parent->right = sortedListToBST(list, mid + 1, end);
```

```
return parent;
};
```

相關題目

• Convert Sorted Array to Binary Search Tree, 見 §6.3.4

6.3.6 Inorder Successor in BST

描述

Given a binary search tree and a node in it, find the in-order successor of that node in the BST. The successor of a node p is the node with the smallest key greater than p.val.

分析

Using Inorder travel

代碼

```
// LeetCode
// 時間複雜度 D(). 空間複雜度 D()
class Solution {
public:
    TreeNode* inorderSuccessor(TreeNode* root, TreeNode* p) {
        if (root == nullptr) return root;
        return DFS(root, p);
    }
private:
    TreeNode *m_prev;
    TreeNode *DFS(TreeNode *root, TreeNode *p)
        if (root == nullptr) return root;
        TreeNode *ansLeft = DFS(root->left, p);
        if (ansLeft != nullptr) return ansLeft;
        if (m_prev == p) return root;
        m_prev = root;
        return DFS(root->right, p);
    }
};
```

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代碼

```
// LeetCode
// 時間複雜度 0(), 空間複雜度 0()
class Solution {
public:
    TreeNode* inorderSuccessor(TreeNode* root, TreeNode* p) {
        if (!root) return root;
        stack<TreeNode*> cache;
        TreeNode *cur = root;
        TreeNode *prev = nullptr;
        while (!cache.empty() || cur != nullptr)
            if (cur != nullptr)
            {
                cache.push(cur);
                cur = cur->left;
            }
            else
            {
                if (prev == p)
                {
                    return cache.top();
                }
                else
                    cur = cache.top();
                    cache.pop();
                    prev = cur;
                    cur = cur->right;
                }
            }
        }
        return nullptr;
    }
};
```

6.3.7 Binary Search Tree Iterator

描述

Implement an iterator over a binary search tree (BST). Your iterator will be initialized with the root node of a BST.

Calling next() will return the next smallest number in the BST.

Example:



```
BSTIterator iterator = new BSTIterator(root);
iterator.next();    // return 3
iterator.next();    // return 7
iterator.hasNext();    // return true
iterator.next();    // return false
```

图 6-2 Binary Search Tree Iterator

分析

Using inorder

代碼

```
/**
 * Definition for a binary tree node.
 * struct TreeNode {
       int val;
       TreeNode *left;
       TreeNode *right;
       TreeNode() : val(0), left(nullptr), right(nullptr) {}
       TreeNode(int x) : val(x), left(nullptr), right(nullptr) {}
       TreeNode(int x, TreeNode *left, TreeNode *right) : val(x), left(left), right(right) {}
 * };
 */
class BSTIterator {
public:
    BSTIterator(TreeNode* root) {
        m_root = root;
        // 移到最左
        while (m_root != nullptr)
            m_cache.push(m_root);
            m_root = m_root->left;
        }
    }
    /** Oreturn the next smallest number */
    int next() {
        if (!m_cache.empty())
```

```
{
            m_root = m_cache.top();
            m_cache.pop();
        int val = m_root->val;
        m_root = m_root->right;
        // 移到最左
        while (m_root != nullptr)
            m_cache.push(m_root);
            m_root = m_root->left;
        return val;
    }
    /** Creturn whether we have a next smallest number */
    bool hasNext() {
        return !m_cache.empty();
    }
private:
    TreeNode *m_root;
    stack<TreeNode *> m_cache;
};
```

6.3.8 Search in a Binary Search Tree

描述

Given the root node of a binary search tree (BST) and a value. You need to find the node in the BST that the node's value equals the given value. Return the subtree rooted with that node. If such node doesn't exist, you should return NULL.

For Example:

Given the tree:



And the value to search: 2

You should return thie subtree:



代碼

```
class Solution {
public:
    TreeNode* searchBST(TreeNode* root, int val) {
        if (root == nullptr) return nullptr;

        if (root->val == val) return root;

        if (root->val > val)
            return searchBST(root->left, val);
        else
            return searchBST(root->right, val);
    }
};
```

6.3.9 Insert into a Binary Search Tree

描述

Given the root node of a binary search tree (BST) and a value to be inserted into the tree, insert the value into the BST. Return the root node of the BST after the insertion. It is guaranteed that the new value does not exist in the original BST.

Note that there may exist multiple valid ways for the insertion, as long as the tree remains a BST after insertion. You can return any of them.

For example:

Given the tree:



And the value to insert: 5

You can return this binary search tree:



This tree is also valid:



搋歸版

```
class Solution {
 public:
      TreeNode* insertIntoBST(TreeNode* root, int val) {
          if (root == nullptr) {
                                          // return a new node if root is null
              return new TreeNode(val);
          if (root->val < val) {</pre>
                                           // insert to the right subtree if val > root->val
              root->right = insertIntoBST(root->right, val);
          } else {
                                           // insert to the left subtree if val <= root->val
              root->left = insertIntoBST(root->left, val);
          return root;
     }
 };
迭代版
 class Solution {
 public:
      TreeNode* insertIntoBST(TreeNode* root, int val) {
          TreeNode *node = root;
          while (node != nullptr)
              if (node->val < val)
                  if (node->right == nullptr)
                      node->right = new TreeNode(val);
                      return root;
                  }
                  else
                      node = node->right;
              }
              else
              {
                  if (node->left == nullptr)
                      node->left = new TreeNode(val);
                      return root;
                  }
                  else
                      node = node->left;
              }
          }
          return new TreeNode(val);
     }
 };
```

6.3.10 Delete Node in a BST

描述

Given a root node reference of a BST and a key, delete the node with the given key in the BST. Return the root node reference (possibly updated) of the BST.

Basically, the deletion can be divided into two stages:

- · Search for a node to remove.
- If the node is found, delete the node.

For Example:

```
root = [5,3,6,2,4,null,7]
key = 3

5
/\
3 6
/\
2 4 7
```

Given key to delete is 3. So we find the node with value 3 and delete it.

One valid answer is [5,4,6,2,null,null,7], shown in the following BST.



Another valid answer is [5,2,6,null,4,null,7].



代碼

```
class Solution {
public:
    TreeNode* deleteNode(TreeNode* root, int key) {
        // return null if root is null
        if (!root) {
            return root;
        }

        // delete current node if root is the target node
        if (root->val == key) {
```

```
// replace root with root->right if root->left is null
            if (!root->left) {
                return root->right;
            }
            // replace root with root->left if root->right is null
            if (!root->right) {
                return root->left;
            // replace root with its successor if root has two children
            TreeNode* p = findSuccessor(root);
            root->val = p->val;
            root->right = deleteNode(root->right, p->val);
            return root;
        }
        if (root->val < key) {
            // find target in right subtree if root->val < key
            root->right = deleteNode(root->right, key);
        } else {
            // find target in left subtree if root->val > key
            root->left = deleteNode(root->left, key);
        return root;
    }
private:
    /**
     * findSuccesor - Helper function for finding successor
     * In BST, succesor of root is the leftmost child in root's right subtree
    TreeNode* findSuccessor(TreeNode* root) {
        TreeNode* cur = root->right;
        while (cur && cur->left) {
            cur = cur->left;
        return cur;
    }
};
```

6.3.11 Kth Largest Element in a Stream

描述

Design a class to find the kth largest element in a stream. Note that it is the kth largest element in the sorted order, not the kth distinct element.

Your KthLargest class will have a constructor which accepts an integer k and an integer array nums, which contains initial elements from the stream. For each call to the method KthLargest.add, return the element representing the kth largest element in the stream.

```
Example:
 int k = 3;
 int[] arr = [4,5,8,2];
 KthLargest kthLargest = new KthLargest(3, arr);
                      // returns 4
 kthLargest.add(3);
 kthLargest.add(5);
                       // returns 5
 kthLargest.add(10); // returns 5
 kthLargest.add(9);
                       // returns 8
 kthLargest.add(4);
                       // returns 8
   You may assume that nums' length \leq k-1 and k \leq 1
Priority Queue
 // LeetCode
 // 時間複雜度 O(), 空間複雜度 O()
 namespace std {
      struct SmallerThanInt {
          bool operator()(const int& first, const int& second) {
              return first > second;
      };
 }
 class KthLargest {
 public:
     KthLargest(int k, vector<int>& nums) {
          m k = k;
          for (const int& n : nums)
              if (m_data.size() < m_k)</pre>
                  m_data.push(n);
              else
              {
                  if (n > m_data.top())
                      m_data.pop();
                      m_data.push(n);
                  }
              }
          }
     }
      int add(int val) {
          if (m_data.size() == m_k && val < m_data.top()) return m_data.top();</pre>
          if (m_data.size() < m_k)
              m_data.push(val);
          else
          {
              if (val > m_data.top())
                  m_data.pop();
```

```
m data.push(val);
             }
         }
         return m_data.top();
     }
 private:
     priority queue<int, vector<int>, SmallerThanInt> m data;
     int m_k;
 };
 /**
  * Your KthLargest object will be instantiated and called as such:
  * KthLargest* obj = new KthLargest(k, nums);
  * int param_1 = obj->add(val);
BST method
 // LeetCode
 // 時間複雜度 D(). 空間複雜度 D()
 struct Node {
     Node* left;
     Node* right;
     int val:
     int cnt:
     Node(int v, int c) : left(NULL), right(NULL), val(v), cnt(c) {}
 };
 class KthLargest {
 private:
     Node* insertNode(Node* root, int num) {
         if (!root) {
             return new Node(num, 1);
                                            // return a new node if root is null
         if (root->val < num) { // insert to the right subtree if val > root->val
             root->right = insertNode(root->right, num);
         } else { // insert to the left subtree if val <= root->val
             root->left = insertNode(root->left, num);
         root->cnt++;
         return root;
     }
     int searchKth(Node* root, int k) {
         // m = the size of right subtree
         int m = root->right ? (root->right)->cnt : 0;
         // root is the m+1 largest node in the BST
         if (k == m + 1) {
             return root->val;
         if (k \le m) {
             // find kth largest in the right subtree
             return searchKth(root->right, k);
```

```
} else {
              // find (k-m-1)th largest in the left subtree
              return searchKth(root->left, k - m - 1);
     }
     Node* root;
     int m_k;
 public:
     KthLargest(int k, vector<int> nums) {
          root = NULL;
          for (int i = 0; i < nums.size(); ++i) {</pre>
              root = insertNode(root, nums[i]);
         m k = k;
     }
     int add(int val) {
         root = insertNode(root, val);
          return searchKth(root, m_k);
 };
 /**
  * Your KthLargest object will be instantiated and called as such:
  * KthLargest obj = new KthLargest(k, nums);
  * int param_1 = obj.add(val);
Remake Heap - fastest
 // LeetCode
 // 時間複雜度 D(), 空間複雜度 D()
 class KthLargest {
 public:
     KthLargest(int k, vector<int>& nums) {
          m_k = k;
         m_data.resize(m_k, INT_MIN);
         m_index = 0;
         for (const auto& n : nums)
              if (m_index < m_k)</pre>
                  PushHeap(m_data.begin(), m_index++, 0, n);
              else
                  if (m_data.front() < n)</pre>
                      AdjustHeap(m_data.begin(), 0, m_k, n);
              }
          }
     }
     int add(int val) {
          if (m_index == m_k && m_data.front() > val) return m_data.front();
```

```
if (m index < m k)
            PushHeap(m data.begin(), m index++, 0, val);
        else
            AdjustHeap(m_data.begin(), 0, m_k, val);
        return m_data.front();
    }
private:
    template <class RandIT, class Dist, class T>
        void PushHeap(RandIT first, Dist holeIndex, Dist topIndex, T data)
        Dist parentIndex = (holeIndex - 1) / 2;
        while (holeIndex > topIndex && *next(first, parentIndex) > data)
            *next(first, holeIndex) = *next(first, parentIndex);
            holeIndex = parentIndex;
            parentIndex = (holeIndex - 1) / 2;
        *next(first, holeIndex) = data;
    }
    template <class RandIT, class Dist, class T>
        void AdjustHeap(RandIT first, Dist holeIndex, Dist Len, T data)
    {
        Dist topIndex = holeIndex;
        Dist childIndex = (holeIndex + 1) * 2;
        while (childIndex < Len)
        {
            if (*next(first, childIndex) > *next(first, childIndex-1))
                childIndex--;
            *next(first, holeIndex) = *next(first, childIndex);
            holeIndex = childIndex;
            childIndex = (holeIndex + 1) * 2;
        if (childIndex == Len)
            *next(first, holeIndex) = *next(first, childIndex-1);
            holeIndex = childIndex-1;
        PushHeap(first, holeIndex, topIndex, data);
    }
private:
    vector<int> m_data;
    int m_k;
    int m_index;
};
/**
 * Your KthLargest object will be instantiated and called as such:
 * KthLargest* obj = new KthLargest(k, nums);
 * int param_1 = obj->add(val);
 */
```

6.3.12 Lowest Common Ancestor of a Binary Search Tree

描述

Given a binary search tree (BST), find the lowest common ancestor (LCA) of two given nodes in the BST.

According to the definition of LCA on Wikipedia: "The lowest common ancestor is defined between two nodes p and q as the lowest node in T that has both p and q as descendants (where we allow a node to be a descendant of itself)."

Given binary search tree: root = [6,2,8,0,4,7,9,null,null,3,5]

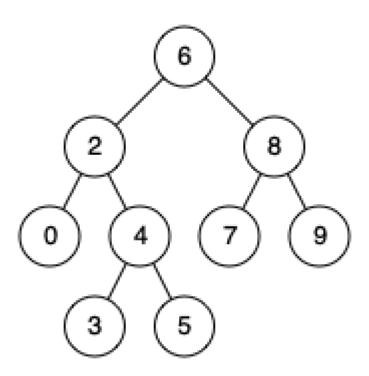


图 6-3 Lowest Common Ancestor of a BST

Example 1:

Input: root = [6,2,8,0,4,7,9,null,null,3,5], p = 2, q = 8

Output: 6

Explanation: The LCA of nodes 2 and 8 is 6.

Example 2:

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```
Input: root = [6,2,8,0,4,7,9,null,null,3,5], p = 2, q = 4
Output: 2
Explanation: The LCA of nodes 2 and 4 is 2, since a node can be a descendant of itself according Note:
```

- All of the nodes' values will be unique.
- p and q are different and both values will exist in the BST.

Code

```
class Solution {
public:
    TreeNode* lowestCommonAncestor(TreeNode* root, TreeNode* p, TreeNode* q) {
        while(root != NULL)
            //If both nodes less than that of parent => move left
            if(root->val > p->val and root->val > q->val)
                root = root->left;
            //If both nodes greater than that of parent => move right
            else if(root->val < p->val and root->val < q->val)
                root = root->right;
            //If paths diverge then return node
            else
                return root;
        }
        return root;
    }
};
```

6.3.13 Contains Duplicate II

描述

Given an array of integers and an integer k, find out whether there are two distinct indices i and j in the array such that nums[i] = nums[j] and the absolute difference between i and j is at most k.

```
Example 1:
Input: nums = [1,2,3,1], k = 3
Output: true
    Example 2:
Input: nums = [1,0,1,1], k = 1
Output: true
    Example 3:
Input: nums = [1,2,3,1,2,3], k = 2
Output: false
```

Hash map

```
// 時間複雜度 O(n), 空間複雜度 O(min(k,n))
class Solution {
public:
    bool containsNearbyDuplicate(vector<int>& nums, int k) {
        if (nums.size() == 0) return false;
        if (k == 0) return false;
        unordered_set<int> cache;
        for (size_t i = 0; i < nums.size(); i++)</pre>
        {
            if (cache.find(nums[i]) != cache.end()) return true;
            if (cache.size() >= k)
                cache.erase(nums[i-k]);
            cache.insert(nums[i]);
        }
        return false;
    }
}:
```

6.3.14 Contains Duplicate III

描述

Given an array of integers, find out whether there are two distinct indices i and j in the array such that the absolute difference between nums[i] and nums[j] is at most t and the absolute difference between i and j is at most k.

```
Example 1:
 Input: nums = [1,2,3,1], k = 3, t = 0
 Output: true
   Example 2:
 Input: nums = [1,0,1,1], k = 1, t = 2
 Output: true
   Example 3:
 Input: nums = [1,5,9,1,5,9], k = 2, t = 3
 Output: false
暴力方法
 // 時間複雜度 O(n*min(k,n)), 空間複雜度 O(min(k,n))
 class Solution {
 public:
     bool containsNearbyAlmostDuplicate(vector<int>& nums, int k, int t) {
         for (int i = 0; i < nums.size(); i++)
         {
```

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```
// abs difference 會有機會大過 int32 t, 所以要用 int64 t
             // 例子: [-1,2147483647], k = 1, t = 2147483647
             for (int j = max(i - k, 0); j < i; j++)
                  if (abs((int64 t)nums[i] - (int64 t)nums[j]) <= (int64 t)t) return true;
         }
         return false;
     }
 };
BST method
 // 時間複雜度 O(nlog(min(k,n))), 空間複雜度 O(min(k,n))
 class Solution {
 public:
     bool containsNearbyAlmostDuplicate(vector<int>& nums, int k, int t) {
         set<int> cache;
         for (int i = 0; i < nums.size(); i++)</pre>
             if (!cache.empty())
                 // 尋找當下數值的 successor
                  auto s = GetCeiling(cache, cache.begin(), nums[i]);
                  if (s != cache.end() && *s <= nums[i] + t) return true;</pre>
                  // 尋找當下數值的 predecessor
                 auto g = GetFloor(cache, cache.begin(), nums[i]);
                  if (g != cache.end() && nums[i] <= *g + t) return true;</pre>
             }
             cache.insert(nums[i]);
             if (cache.size() > k)
                 cache.erase(nums[i - k]);
         return false;
     }
 private:
     template <class BTS, class BidIT, class T>
         BidIT GetCeiling(BTS& tree, BidIT first, T val)
     {
         return tree.lower_bound(val);
     template <class BTS, class BidIT, class T>
         BidIT GetFloor(BTS& tree, BidIT first, T val)
         BidIT tmp = tree.upper_bound(val);
         if (tmp == tree.begin())
             return tree.end();
         else
             return prev(tmp);
     }
 };
```

6.4 二叉樹的遞歸 201

Bucket

```
// 時間複雜度 O(n), 空間複雜度 O(min(k,n))
class Solution {
public:
   bool containsNearbyAlmostDuplicate(vector<int>& nums, int k, int t) {
        if (t < 0) return false;
        unordered map<int64 t, int64 t> d;
        int64 t w = (int64 t)t + 1;
        for (int i = 0; i < nums.size(); i++)</pre>
            int64_t id = GetId(nums[i], w);
            // 若果同一個 bucket 有多過一個數值, 代表找到答案
            if (d.find(id) != d.end())
               return true;
            // 檢查前一個 bucket
            if (d.find(id-1) != d.end() && abs(nums[i] - d[id-1]) < w)
                return true;
            // 檢查後一個 bucket
            if (d.find(id+1) != d.end() \&\& abs(nums[i] - d[id+1]) < w)
               return true;
            d[id] = (int64_t)nums[i];
            if (i >= k) d.erase(GetId(nums[i-k], w));
        }
       return false;
   }
private:
    // ^{-3} / 5 = 0 and but we need ^{-3} / 5 = -1.
    int64_t GetId(int64_t x, int64_t w)
        return x < 0? (x + 1) / w - 1 : x / w;
};
```

6.4 二叉樹的遞歸

二叉樹是一個遞歸的數據結構、因此是一個用來考察遞歸思維能力的絕佳數據結構。

遞歸一定是深搜(見§11.16.5節 "深搜與遞歸的區別"),由於在二叉樹上,遞歸的味道更濃些,因此本節用"二叉樹的遞歸"作為標題,而不是"二叉樹的深搜",儘管本節所有的算法都屬於深搜。

二叉樹的先序、中序、後序遍歷都可以看做是 DFS,此外還有其他順序的深度優先遍歷,共有 3! = 6 種。其他 3 種順序是 root->r->l,r->root->l,r->l->root。

6.4.1 Minimum Depth of Binary Tree

描述

Given a binary tree, find its minimum depth.

The minimum depth is the number of nodes along the shortest path from the root node down to the nearest leaf node.

分析

無

遞歸版

```
// LeetCode, Minimum Depth of Binary Tree
 // 遞歸版, 時間複雜度 O(n), 空間複雜度 O(logn)
 class Solution {
 public:
     int minDepth(const TreeNode *root) {
         return minDepth(root, false);
     }
 private:
     static int minDepth(const TreeNode *root, bool hasbrother) {
         if (!root) return hasbrother ? INT_MAX : 0;
         return 1 + min(minDepth(root->left, root->right != NULL),
                 minDepth(root->right, root->left != NULL));
     }
 };
迭代版
 // LeetCode, Minimum Depth of Binary Tree
 // 迭代版, 時間複雜度 O(n), 空間複雜度 O(logn)
 class Solution {
 public:
     int minDepth(TreeNode* root) {
         if (root == nullptr)
             return 0;
         int result = INT_MAX;
         stack<pair<TreeNode*, int>> s;
         s.push(make_pair(root, 1));
         while (!s.empty()) {
             auto node = s.top().first;
             auto depth = s.top().second;
             s.pop();
             if (node->left == nullptr && node->right == nullptr)
                 result = min(result, depth);
             if (node->left && result > depth) // 深度控制, 剪枝
```

s.push(make_pair(node->left, depth + 1));

6.4 二叉樹的遞歸 203

相關題目

• Maximum Depth of Binary Tree, 見 §6.4.2

6.4.2 Maximum Depth of Binary Tree

描述

Given a binary tree, find its maximum depth.

The maximum depth is the number of nodes along the longest path from the root node down to the farthest leaf node.

分析

無

代碼

```
// LeetCode, Maximum Depth of Binary Tree
// 時間複雜度 O(n), 空間複雜度 O(logn)
class Solution {
public:
    int maxDepth(TreeNode *root) {
        if (root == nullptr) return 0;
        return max(maxDepth(root->left), maxDepth(root->right)) + 1;
    }
};
```

相關題目

• Minimum Depth of Binary Tree, 見 §6.4.1

6.4.3 Path Sum

描述

Given a binary tree and a sum, determine if the tree has a root-to-leaf path such that adding up all the values along the path equals the given sum.

For example: Given the below binary tree and sum = 22,



return true, as there exist a root-to-leaf path 5->4->11->2 which sum is 22.

分析

題目只要求返回 true 或者 false, 因此不需要記錄路徑。

由於只需要求出一個結果,因此,當左、右任意一棵子樹求到了滿意結果,都可以及時 return。 由於題目沒有説節點的數據一定是正整數,必須要走到葉子節點才能判斷,因此中途沒法剪枝, 只能進行樸素深搜。

代碼

相關題目

• Path Sum II, 見 §6.4.4

6.4 二叉樹的遞歸 205

6.4.4 Path Sum II

描述

Given a binary tree and a sum, find all root-to-leaf paths where each path's sum equals the given sum. For example: Given the below binary tree and sum = 22,

```
5
/\
4 8
//\
11 13 4
/\\
7 2 5 1

return
[
[5,4,11,2],
[5,8,4,5]
]
```

分析

跟上一題相比,本題是求路徑本身。且要求出所有結果,左子樹求到了滿意結果,不能 return,要接着求右子樹。

代碼

```
// LeetCode, Path Sum II
// 時間複雜度 O(n), 空間複雜度 O(logn)
class Solution {
public:
    vector<vector<int> > pathSum(TreeNode *root, int sum) {
        vector<vector<int> > result;
        vector<int> cur; // 中間結果
       pathSum(root, sum, cur, result);
       return result;
    }
private:
   void pathSum(TreeNode *root, int gap, vector<int> &cur,
            vector<vector<int> > &result) {
        if (root == nullptr) return;
        cur.push_back(root->val);
        if (root->left == nullptr && root->right == nullptr) { // leaf
            if (gap == root->val)
                result.push_back(cur);
        pathSum(root->left, gap - root->val, cur, result);
       pathSum(root->right, gap - root->val, cur, result);
```

```
cur.pop_back();
};
```

相關題目

• Path Sum, 見 §6.4.3

6.4.5 Binary Tree Maximum Path Sum

描述

Given a binary tree, find the maximum path sum.

The path may start and end at any node in the tree. For example: Given the below binary tree,



Return 6.

分析

這題很難,路徑可以從任意節點開始,到任意節點結束。

可以利用"最大連續子序列和"問題的思路,見第 §14.4 節。如果說 Array 只有一個方向的話,那麼 Binary Tree 其實只是左、右兩個方向而已,我們需要比較兩個方向上的值。

不過,Array 可以從頭到尾遍歷,那麼 Binary Tree 怎麼辦呢,我們可以採用 Binary Tree 最常用的 dfs 來進行遍歷。先算出左右子樹的結果 L 和 R,如果 L 大於 0,那麼對後續結果是有利的,我們加上 L,如果 R 大於 0,對後續結果也是有利的,繼續加上 R。

代碼

```
// LeetCode, Binary Tree Maximum Path Sum
// 時間複雜度 O(n), 空間複雜度 O(logn)
class Solution {
public:
    int maxPathSum(TreeNode *root) {
        max_sum = INT_MIN;
        dfs(root);
        return max_sum;
    }
private:
    int max_sum;
    int dfs(const TreeNode *root) {
        if (root == nullptr) return 0;
        int 1 = dfs(root->left);
```

6.4 二叉樹的遞歸 207

```
int r = dfs(root->right);
int sum = root->val;
if (1 > 0) sum += 1;
if (r > 0) sum += r;
max_sum = max(max_sum, sum);
return max(r, 1) > 0 ? max(r, 1) + root->val : root->val;
};
```

注意,最後 return 的時候,只返回一個方向上的值,為什麼? 這是因為在遞歸中,只能向父節點返回,不可能存在 L->root->R 的路徑,只可能是 L->root 或 R->root。

相關題目

• Maximum Subarray, 見 §14.4

6.4.6 Populating Next Right Pointers in Each Node

描述

```
Given a binary tree
struct TreeLinkNode {
  int val;
  TreeLinkNode *left, *right, *next;
  TreeLinkNode(int x) : val(x), left(NULL), right(NULL), next(NULL) {}
};
```

Populate each next pointer to point to its next right node. If there is no next right node, the next pointer should be set to NULL.

Initially, all next pointers are set to NULL.

Note:

- · You may only use constant extra space.
- You may assume that it is a perfect binary tree (ie, all leaves are at the same level, and every parent has two children).

For example, Given the following perfect binary tree,



After calling your function, the tree should look like:

```
1 -> NULL
/ \
2 -> 3 -> NULL
/ \ / \
4->5->6->7 -> NULL
```

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分析

無

代碼

```
// LeetCode, Populating Next Right Pointers in Each Node
// 時間複雜度 O(n), 空間複雜度 O(logn)
class Solution {
public:
    void connect(TreeLinkNode *root) {
        connect(root, NULL);
    }
private:
    void connect(TreeLinkNode *root, TreeLinkNode *sibling) {
        if (root == nullptr)
            return;
        else
            root->next = sibling;
        connect(root->left, root->right);
        if (sibling)
            connect(root->right, sibling->left);
        else
            connect(root->right, nullptr);
    }
};
```

相關題目

• Populating Next Right Pointers in Each Node II, 見 §6.1.15

6.4.7 Sum Root to Leaf Numbers

描述

Given a binary tree containing digits from 0-9 only, each root-to-leaf path could represent a number.

An example is the root-to-leaf path 1->2->3 which represents the number 123.

Find the total sum of all root-to-leaf numbers.

For example,



The root-to-leaf path 1->2 represents the number 12. The root-to-leaf path 1->3 represents the number 13.

Return the sum = 12 + 13 = 25.

6.4 二叉樹的遞歸 209

分析

無

代碼

```
// LeetCode, Decode Ways
// 時間複雜度 O(n), 空間複雜度 O(logn)
class Solution {
public:
    int sumNumbers(TreeNode *root) {
        return dfs(root, 0);
    }
private:
    int dfs(TreeNode *root, int sum) {
        if (root == nullptr) return 0;
        if (root->left == nullptr && root->right == nullptr)
            return sum * 10 + root->val;
        return dfs(root->left, sum * 10 + root->val) +
                dfs(root->right, sum * 10 + root->val);
    }
};
```

相關題目

無

6.4.8 Convert Binary Search Tree To Double link list

描述

Convert a Binary Search Tree to a sorted Circular Doubly-Linked List in place.

You can think of the left and right pointers as synonymous to the predecessor and successor pointers in a doubly-linked list. For a circular doubly linked list, the predecessor of the first element is the last element, and the successor of the last element is the first element.

We want to do the transformation in place. After the transformation, the left pointer of the tree node should point to its predecessor, and the right pointer should point to its successor. You should return the pointer to the smallest element of the linked list.

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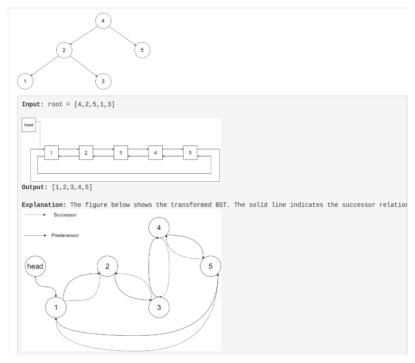


图 6-4 Convert Binary Search Tree

分析

無

```
// LeetCode, Decode Ways
// 時間複雜度 O(n), 空間複雜度 O(logn)
/*
// Definition for a Node.
class Node {
  public:
    int val;
    Node* left;
    Node* right;

    Node() {}

    Node(int _val) {
      val = _val;
      left = NULL;
      right = NULL;
    }
}
```

6.4 二叉樹的遞歸 211

```
Node(int _val, Node* _left, Node* _right) {
        val = _val;
        left = _left;
        right = _right;
    }
};
*/
class Solution {
public:
    Node* treeToDoublyList(Node* root) {
        if (root == nullptr) return root;
        m_last = m_first = nullptr;
        DFS(root);
        m_first->left = m_last;
        m_last->right = m_first;
        return m_first;
    }
private:
    void DFS(Node *node)
        if (node == nullptr) return;
        DFS(node->left);
        if (m_last)
            m_last->right = node;
            node->left = m_last;
        }
        else
        {
            m_first = node;
            node->left = nullptr;
        m_last = node;
        DFS(node->right);
    }
private:
    Node *m_last;
    Node *m_first;
};
```

第 7 章 排序

7.1 Merge Two Sorted Arrays

描述

Given two sorted integer arrays A and B, merge B into A as one sorted array.

Note: You may assume that A has enough space to hold additional elements from B. The number of elements initialized in A and B are m and n respectively.

分析

無

代碼

```
//LeetCode, Merge Sorted Array
// 時間複雜度 O(m+n), 空間複雜度 O(1)
class Solution {
public:
    void merge(vector<int>& A, int m, vector<int>& B, int n) {
        int ia = m - 1, ib = n - 1, icur = m + n - 1;
        while(ia >= 0 && ib >= 0) {
            A[icur--] = A[ia] >= B[ib] ? A[ia--] : B[ib--];
        }
        while(ib >= 0) {
            A[icur--] = B[ib--];
        }
    }
};
```

相關題目

- Merge Two Sorted Lists, 見 §7.1
- Merge k Sorted Lists, 見 §7.3

7.2 Merge Two Sorted Lists

描述

Merge two sorted linked lists and return it as a new list. The new list should be made by splicing together the nodes of the first two lists.

分析

無

代碼

```
//LeetCode, Merge Two Sorted Lists
// 時間複雜度 O(min(m,n)), 空間複雜度 O(1)
class Solution {
public:
   ListNode *mergeTwoLists(ListNode *11, ListNode *12) {
        if (l1 == nullptr) return l2;
        if (12 == nullptr) return 11;
       ListNode dummy(-1);
       ListNode *p = &dummy;
        for (; 11 != nullptr && 12 != nullptr; p = p->next) {
            if (11->val > 12->val) { p->next = 12; 12 = 12->next; }
            else { p->next = l1; l1 = l1->next; }
        p->next = 11 != nullptr ? 11 : 12;
        return dummy.next;
   }
};
```

相關題目

- Merge Sorted Array §7.1
- Merge k Sorted Lists, 見 §7.3

7.3 Merge k Sorted Lists

描述

Merge k sorted linked lists and return it as one sorted list. Analyze and describe its complexity.

分析

可以複用 Merge Two Sorted Lists (見 §7.2) 的函數

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代碼

```
//LeetCode, Merge k Sorted Lists
// 時間複雜度 O(n1+n2+...), 空間複雜度 O(1)
class Solution {
public:
    ListNode * mergeTwo(ListNode * 11, ListNode * 12){
        if(!11) return 12;
        if(!12) return 11;
        ListNode dummy(-1);
        ListNode * p = &dummy;
        for(; 11 && 12; p = p->next){
            if(11-val > 12-val){
                p->next = 12; 12 = 12->next;
            }
            else{
                p->next = 11; 11 = 11->next;
            }
        p->next = 11 ? 11 : 12;
        return dummy.next;
    }
    ListNode* mergeKLists(vector<ListNode*>& lists) {
        if(lists.size() == 0) return nullptr;
        // multi pass
        deque<ListNode *> dq(lists.begin(), lists.end());
        while(dq.size() > 1){
            ListNode * first = dq.front(); dq.pop_front();
            ListNode * second = dq.front(); dq.pop_front();
            dq.push_back(mergeTwo(first,second));
        return dq.front();
    }
};
```

相關題目

- Merge Sorted Array §7.1
- Merge Two Sorted Lists, 見 §7.2

7.4 Insertion Sort List

描述

Sort a linked list using insertion sort.

7.5 Sort List 215

分析

無

代碼

```
// LeetCode, Insertion Sort List
// 時間複雜度 O(n^2), 空間複雜度 O(1)
class Solution {
public:
    ListNode *insertionSortList(ListNode *head) {
        ListNode dummy(INT_MIN);
        //dummy.next = head;
        for (ListNode *cur = head; cur != nullptr;) {
            auto pos = findInsertPos(&dummy, cur->val);
            ListNode *tmp = cur->next;
            cur->next = pos->next;
            pos->next = cur;
            cur = tmp;
        return dummy.next;
    }
    ListNode* findInsertPos(ListNode *head, int x) {
        ListNode *pre = nullptr;
        for (ListNode *cur = head; cur != nullptr && cur->val <= x;</pre>
            pre = cur, cur = cur->next)
        return pre;
    }
};
```

相關題目

• Sort List, 見 §7.5

7.5 Sort List

描述

Sort a linked list in O(nlogn) time using constant space complexity.

分析

常數空間且 O(nlogn), 單鏈表適合用歸併排序, 雙向鏈表適合用快速排序。本題可以複用 "Merge Two Sorted Lists" 的代碼。

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代碼

```
// LeetCode, Sort List
// 歸併排序, 時間複雜度 O(nlogn), 空間複雜度 O(1)
class Solution {
public:
   ListNode *sortList(ListNode *head) {
        if (head == NULL | | head->next == NULL)return head;
        // 快慢指針找到中間節點
       ListNode *fast = head, *slow = head;
        while (fast->next != NULL && fast->next->next != NULL) {
           fast = fast->next->next;
           slow = slow->next;
        }
        // 斷開
        fast = slow;
        slow = slow->next;
       fast->next = NULL;
       ListNode *l1 = sortList(head); // 前半段排序
       ListNode *12 = sortList(slow); // 後半段排序
       return mergeTwoLists(11, 12);
   }
    // Merge Two Sorted Lists
   ListNode *mergeTwoLists(ListNode *11, ListNode *12) {
        ListNode dummy(-1);
        for (ListNode* p = &dummy; 11 != nullptr || 12 != nullptr; p = p->next) {
            int val1 = l1 == nullptr ? INT_MAX : l1->val;
            int val2 = 12 == nullptr ? INT_MAX : 12->val;
            if (val1 <= val2) {
                p->next = 11;
                11 = 11->next;
            } else {
                p->next = 12;
                12 = 12 - \text{next};
        }
       return dummy.next;
   }
};
```

相關題目

• Insertion Sort List, 見 §7.4

7.6 Merge sort Array 217

7.6 Merge sort Array

描述

分析

無

Code

```
// 時間複雜度 O(nlogn), 空間複雜度 O(1)
class Solution {
public:
    vector<int> sortArray(vector<int>& nums) {
        mergeSort(nums.begin(), nums.end());
        return nums;
private:
    template <class RandIT>
        void mergeSort(RandIT first, RandIT last)
    {
        int len = distance(first, last);
        if (len < 2) return;
        auto mid = next(first, len / 2);
        mergeSort(first, mid);
        mergeSort(mid, last);
        merge(first, mid, last);
    }
    template <class RandIT>
        void merge(RandIT first, RandIT mid, RandIT last)
    {
        vector<int> tmpVec(mid, last);
        auto ai = prev(mid);
        auto ci = prev(last);
        auto bi = prev(tmpVec.end());
        while (bi >= tmpVec.begin() && ai >= first)
        {
            if (*ai <= *bi)
            {
                *ci = *bi;
                bi--;
            }
            else
                *ci = *ai;
                ai--;
            ci--;
        }
```

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```
while (bi >= tmpVec.begin())
{
    *ci = *bi;
    bi--;
    ci--;
}
```

7.7 Quick sort Array

描述

Quick Sort and STD iterator

分析

無

```
// 時間複雜度 O(nlogn), 空間複雜度 O(1)
class Solution {
public:
    vector<int> sortArray(vector<int>& nums) {
        quickSort(nums.begin(), nums.end());
        return nums;
    }
private:
    template <class RandIT>
        void quickSort(RandIT first, RandIT last)
    {
        if (first < last)</pre>
            // template overload 的例子
            typename std::iterator_traits<RandIT>::iterator_category t;
            auto pivot = partition(first, last, t);
            quickSort(first, pivot);
            quickSort(next(pivot), last);
        }
    template <class RandIT>
        RandIT partition(RandIT first, RandIT last, std::bidirectional_iterator_tag)
        RandIT pivot = prev(last);
        RandIT cur = first;
        while (first < last)
            if (*first < *pivot)</pre>
                mySwap(first, cur);
                cur++;
```

7.7 Quick sort Array 219

```
first++;
         mySwap(pivot, cur);
         return cur;
     }
     template <class RandIT>
         void mySwap(RandIT first, RandIT second)
         auto tmp = *first;
         *first = *second;
         *second = tmp;
     }
 }
代碼 2
 // 時間複雜度 O(nlogn), 空間複雜度 O(1)
 class Solution {
 public:
     vector<int> sortArray(vector<int>& nums) {
         if (nums.size() > 0)
              quickSort(nums, 0, nums.size() - 1);
         return nums;
     }
 private:
     void quickSort(vector<int>& nums, int first, int last)
         if (first < last)
              int pivot = partition(nums, first, last);
              quickSort(nums, first, pivot - 1);
              quickSort(nums, pivot + 1, last);
     int partition(vector<int>& nums, int first, int last)
         int cur = first;
         while (first < last)
             if (nums[first] < nums[last])</pre>
                  mySwap(&nums[cur], &nums[first]);
                  cur++;
              }
              first++;
         mySwap(&nums[cur], &nums[last]);
         return cur;
     void mySwap(int *a, int *b)
```

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```
{
    int tmp = *a;
    *a = *b;
    *b = tmp;
}

相關題目
    No
```

相關題目

No

7.8 Quick sort List

描述

Quick Sort with singal linked list

分析

無

```
// Not from LeetCode
// 時間複雜度 O(nlogn), 空間複雜度 O(1)
class Solution {
public:
    void QuickSortList(ListNode *&head, ListNode *last = nullptr)
        // return when not enough nodes
        if (head == nullptr || head->next == nullptr) return;
        if (head == last || head->next == last) return;
        ListNode *pivot = Q_PartitionList(head, last);
        QuickSortList(head, pivot);
        if (pivot != nullptr)
            QuickSortList(pivot->next, last);
private:
    ListNode *Q_PartitionList(ListNode *&head, ListNode* last)
        ListNode *pivot = head;
        ListNode left(-1), right(-1);
        right.next = last;
        ListNode *cur = head;
```

```
while (cur != last)
        ListNode *next = cur->next;
        if (pivot->val >= cur->val)
            cur->next = left.next;
            left.next = cur;
        }
        else
        {
            cur->next = right.next;
            right.next = cur;
        cur = next;
    }
    pivot->next = right.next;
    head = left.next;
    return pivot;
}
```

相關題目

No

7.9 First Missing Positive

描述

Given an unsorted integer array, find the first missing positive integer.

For example, Given [1,2,0] return 3, and [3,4,-1,1] return 2.

Your algorithm should run in O(n) time and uses constant space.

分析

本質上是桶排序 (bucket sort), 每當 A[i]!=i+1 的時候, 將 A[i] 與 A[A[i]-1] 交換, 直到無法交換為止, 終止條件是 A[i]==A[A[i]-1]。

```
// LeetCode, First Missing Positive
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    int firstMissingPositive(vector<int>& nums) {
        bucket_sort(nums);
        for (int i = 0; i < nums.size(); ++i)</pre>
```

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```
if (nums[i] != (i + 1))
                 return i + 1;
        return nums.size() + 1;
    }
private:
    static void bucket_sort(vector<int>& A) {
        const int n = A.size();
        for (int i = 0; i < n; i++) {
            while (A[i] != i + 1) {
                 if (A[i] \le 0 \mid | A[i] > n \mid | A[i] == A[A[i] - 1])
                     break;
                 swap(A[i], A[A[i] - 1]);
            }
        }
    }
};
```

相關題目

• Sort Colors, 見 §7.10

7.10 Sort Colors

描述

Given an array with n objects colored red, white or blue, sort them so that objects of the same color are adjacent, with the colors in the order red, white and blue.

Here, we will use the integers 0, 1, and 2 to represent the color red, white, and blue respectively.

Note: You are not suppose to use the library's sort function for this problem.

Follow up:

A rather straight forward solution is a two-pass algorithm using counting sort.

First, iterate the array counting number of 0's, 1's, and 2's, then overwrite array with total number of 0's, then 1's and followed by 2's.

Could you come up with an one-pass algorithm using only constant space?

分析

由於 0,1,2 非常緊凑,首先想到計數排序 (counting sort),但需要掃描兩遍,不符合題目要求。 由於只有三種顏色,可以設置兩個 index,一個是 red 的 index,一個是 blue 的 index,兩邊往中間走。時間複雜度 O(n),空間複雜度 O(1)。

第3種思路,利用快速排序裏 partition 的思想,第一次將數組按0分割,第二次按1分割,排序 完畢,可以推廣到n種顏色,每種顏色有重複元素的情況。

7.10 Sort Colors 223

```
// LeetCode, Sort Colors
 // Counting Sort
 // 時間複雜度 O(n), 空間複雜度 O(1)
 class Solution {
 public:
     void sortColors(vector<int>& A) {
         int counts[3] = { 0 }; // 記錄每個顏色出現的次數
         for (int i = 0; i < A.size(); i++)
             counts[A[i]]++;
         for (int i = 0, index = 0; i < 3; i++)
             for (int j = 0; j < counts[i]; j++)
                 A[index++] = i;
     }
 };
代碼 2
 // LeetCode, Sort Colors
 // 雙指針, 時間複雜度 O(n), 空間複雜度 O(1)
 class Solution {
 public:
     void sortColors(vector<int>& A) {
         // 一個是 red 的 index, 一個是 blue 的 index, 兩邊往中間走
         int red = 0, blue = A.size() - 1;
         for (int i = 0; i < blue + 1;) {
             if (A[i] == 0)
                 swap(A[i++], A[red++]);
             else if (A[i] == 2)
                 swap(A[i], A[blue--]);
             else
                 i++;
         }
     }
 };
代碼3
 // LeetCode, Sort Colors
 // use partition()
 // 時間複雜度 O(n), 空間複雜度 O(1)
 class Solution {
 public:
     void sortColors(vector<int>& nums) {
         partition(partition(nums.begin(), nums.end(), bind1st(equal_to<int>(), 0)),
                 nums.end(), bind1st(equal_to<int>(), 1));
```

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```
}
 };
代碼 4
 // LeetCode, Sort Colors
 // 重新實現 partition()
 // 時間複雜度 O(n), 空間複雜度 O(1)
 class Solution {
 public:
     void sortColors(vector<int>& nums) {
         partition(partition(nums.begin(), nums.end(), bind1st(equal_to<int>(), 0)),
                  nums.end(), bind1st(equal_to<int>(), 1));
 private:
     template<typename ForwardIterator, typename UnaryPredicate>
     ForwardIterator partition(ForwardIterator first, ForwardIterator last,
             UnaryPredicate pred) {
         auto pos = first;
         for (; first != last; ++first)
             if (pred(*first))
                 swap(*first, *pos++);
         return pos;
     }
 };
```

相關題目

• First Missing Positive, 見 §7.9

7.11 Heap Sort

描述

Remake std heap sort heap make heap pop heap push, also using iterator type

分析

Learn from STL 源碼剖析 侯捷

```
// LeetCode, Heap Sort
// Heap Sort
// 時間複雜度 O(nlogn), 空間複雜度 O(1)
class Solution {
public:
    template<class T>
```

7.11 Heap Sort 225

```
void PushHeap(T first, T last)
    {
        // Assume the value is pushed to the vector
        typename std::iterator_traits<T>::iterator_category t;
        __PushHeapAux(first, last, t);
    }
    template<class T>
        void PopHeap(T first, T last)
    {
        // will move the value to the last element
        typename std::iterator_traits<T>::iterator_category t;
        __PopHeapAux(first, last, t);
    template <class RandomAccessIterator>
        void SortHeap (RandomAccessIterator first, RandomAccessIterator last)
    {
        while (last - first > 1)
            PopHeap(first, last--);
    template <class T>
        inline void MakeHeap (T first, T last)
    {
        typename std::iterator_traits<T>::iterator_category t;
        __MakeHeap(first, last, t);
    }
private:
    template <class RandomAccessIterator, class Distance, class T>
    void __PushHeap (RandomAccessIterator first
                    , Distance holeIndex, Distance topIndex, T value)
    {
        // percolate up
        Distance parent = (holeIndex - 1) / 2; // find father node
        while (holeIndex > topIndex && *next(first, parent) < value)</pre>
            *(first + holeIndex) = *(first + parent);
            holeIndex = parent;
            parent = (holeIndex - 1) / 2;
        *(first + holeIndex) = value;
    template<class T>
        void __PushHeapAux(T first, T last, std::random_access_iterator_tag)
    {
        __PushHeap(first, distance(first, prev(last)), distance(first, first), *prev(last));
    }
    template <class RandomAccessIterator, class Distance, class T>
    void __AdjustHeap (RandomAccessIterator first
                      , Distance holeIndex, Distance len, T value)
    {
        // percolate down
        Distance topIndex = holeIndex;
        Distance secondChild = 2 * (holeIndex + 1);
        while (secondChild < len)
```

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```
{
            if (*(first + secondChild) < *(first + (secondChild - 1)))</pre>
                secondChild--;
            *(first + holeIndex) = *(first + secondChild);
            holeIndex = secondChild;
            secondChild = 2 * (secondChild + 1);
        }
        if (secondChild == len) // only left child case
            *(first + holeIndex) = *(first + (secondChild - 1));
            holeIndex = secondChild - 1;
        PushHeap (first, holeIndex, topIndex, value);
    }
    template <class RandomAccessIterator, class T>
    void __PopHeap (RandomAccessIterator first
                    , RandomAccessIterator last, RandomAccessIterator result, T value)
    {
        *result = *first;
        __AdjustHeap(first, distance(first, first), distance(first, last), value);
    }
    template<class T>
        void __PopHeapAux(T first, T last, std::random_access_iterator_tag)
    {
        __PopHeap(first, prev(last), prev(last), *prev(last));
    }
    template <class T>
        void __MakeHeap (T first, T last, std::random_access_iterator_tag)
    {
        if (last - first < 2) return;
        auto len = distance(first, last);
        auto holeIndex = len / 2 - 1;
        while (true)
        {
             _AdjustHeap(first, holeIndex, len, *next(first, holeIndex));
            if (holeIndex == 0) return;
            holeIndex--;
        }
    }
};
void TryHeap()
    using namespace std;
    vector<int> ivec = \{0,1,2,3,4,8,9,3,5\};
    RM::MakeHeap(ivec.begin(), ivec.end());
    for (size_t i = 0; i < ivec.size(); ++i)
        cout << ivec[i] << " ";</pre>
    cout << endl;</pre>
    ivec.push_back(7);
```

7.12 Partial Sort 227

```
cout << distance(ivec.begin(), ivec.end())</pre>
          << " " << distance(ivec.begin(), prev(ivec.end())) << endl;</pre>
    RM::PushHeap(ivec.begin(), ivec.end());
    for (size_t i = 0; i < ivec.size(); ++i)</pre>
         cout << ivec[i] << " ";
    cout << endl;</pre>
    RM::PopHeap(ivec.begin(), ivec.end());
    cout << ivec.back() << endl;</pre>
    ivec.pop_back();
    for (size_t i = 0; i < ivec.size(); ++i)</pre>
         cout << ivec[i] << " ";
    cout << endl;</pre>
    RM::SortHeap(ivec.begin(), ivec.end());
    for (size_t i = 0; i < ivec.size(); ++i)</pre>
         cout << ivec[i] << " ";
    cout << endl;</pre>
}
```

相關題目

7.12 Partial Sort

描述

Partial Sort

分析

Learn from STL 源碼剖析 侯捷

```
// LeetCode, Partial Sort
// Partial Sort
// 時間複雜度 O(mlogk), 空間複雜度 O(1)
class Solution {
public:
    template<class T>
    inline void PartialSort(T first, T middle, T last)
    {
        typename std::iterator_traits<T>::iterator_category t;
        __PartialSort(first, middle, last, t);
    }
private:
    template <class T>
```

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相關題目

7.13 Topological Sort

描述

Topological Sort



Result: BEACDFG

https://www.youtube.com/watch?v=ddTC4Zovtbc

分析

This is useful for software compile, project sequence when having dependency

```
// LeetCode, Topological Sort
// Topological Sort
// 時間複雜度 O(), 空間複雜度 O()
class Solution {
public:
    vector<int> TopologicalSort(const vector<vector<int>>& adjList) {
    unordered_map<int, bool> visited;
    vector<int> result; result.reserve(adjList.size());
```

```
// random pick a point to start
        // DFS to leaf
        // Put to when all child is visited
        for (int i = 0; i < (int)adjList.size(); i++) {</pre>
            if (!DFS(adjList, i, visited, result)) return "";
        return result;
    }
private:
    void DFS(const vector<vector<int>>& adjList, int step, unordered_map<int, bool>& visited,
        if (visited.find(step) != visited.end())
            return visited[step]; // If the node was grey (false), a cycle was detected.
        visited[step] = false;
        for (const auto& nei : adjList[step]) {
             if (!DFS(adjList, nei, visited, result)) return false;
        visited[step] = true;
        result.insert(result.begin(), step);
    }
};
int main(int argc, char *argv[]) {
    Solution solution;
    vector<vector<int>> adjList(7, vector<int>()); // DAG
    adjList[0] = \{2\}; // A \rightarrow C
    adjList[1] = \{2, 4\}; // B \rightarrow C, B \rightarrow E
    adjList[2] = {3}; // C -> D
    adjList[3] = \{5\}; // D -> F
    adjList[4] = {5}; // E -> F
    adjList[5] = {6}; // F -> G
    adjList[6] = {}; // G ->
    for (const auto& val : solution.TopologicalSort(adjList))
        cout << (char)(val + 'A') << " ";</pre>
    cout << endl;</pre>
    return 0;
}
```

相關題目

7.14 Sort Characters By Frequency

描述

```
Given a string, sort it in decreasing order based on the frequency of characters.
```

```
Example 1: Input: "tree"
```

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```
Output:
 "eert"
 Explanation:
 'e' appears twice while 'r' and 't' both appear once.
 So 'e' must appear before both 'r' and 't'. Therefore "eetr" is also a valid answer.
   Example 2:
 Input:
 "cccaaa"
 Output:
 "cccaaa"
 Explanation:
 Both 'c' and 'a' appear three times, so "aaaccc" is also a valid answer.
 Note that "cacaca" is incorrect, as the same characters must be together.
分析
   method 1: 初始化 vec 來儲存出現次數,計算出現次數,由大至細依出現次數排序
   method 2: Bucket sort, 計算每個字母出現的次數, 以 bucket 來儲存每個出現次數的字每, 製造答案
代碼
 // LeetCode,
 // 時間複雜度 O(nlogn), 空間複雜度 O(n)
 class Solution {
 public:
     string frequencySort(string s) {
         // 初始化 vec 來儲存出現次數
         vector<pair<char, int>> countVec(256);
         for (size_t i = 0; i < countVec.size(); i++)</pre>
             countVec[i].first = i;
             countVec[i].second = 0;
         }
         // 計算出現次數
         for (const char& c : s)
             countVec[c].second++;
         // , 由大至細依出現次數排序
         sort(countVec.begin(), countVec.end()
              , [&](const auto& first, const auto& second)
                      return first.second > second.second;
                  });
```

string result;

```
for (const auto& count : countVec)
             if (count.second > 0)
                 result.append(count.second, count.first);
         return result;
     }
 };
代碼
 // LeetCode,
 // 時間複雜度 O(n), 空間複雜度 O(n)
 class Solution {
 public:
     string frequencySort(string s) {
         if (s.size() == 0) return "";
         // Bucket sort
         vector<int> counter(256, 0);
         // 計算每個字母出現的次數
         int maxCount = INT_MIN;
         for (const char& c : s)
         {
             counter[c]++;
             if (counter[c] > maxCount)
                 maxCount = counter[c];
         }
         // 以 bucket 來儲存每個出現次數的字每
         vector<list<char>> buckets(maxCount);
         for (size_t i = 0; i < counter.size(); i++)</pre>
         {
             if (counter[i] > 0)
                 buckets[counter[i]-1].push_back((char)i);
         }
         // 製造答案
         string result;
         for (int i = (int)buckets.size()-1; i >= 0; i--)
         {
             for (const char& c : buckets[i])
                 result.append(i+1, c);
         return result;
     }
 };
```

相關題目

No

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7.15 Top K Frequent Words

描述

Given a non-empty list of words, return the k most frequent elements.

Your answer should be sorted by frequency from highest to lowest. If two words have the same frequency, then the word with the lower alphabetical order comes first.

Example 1:

```
Input: ["i", "love", "leetcode", "i", "love", "coding"], k = 2
Output: ["i", "love"]
Explanation: "i" and "love" are the two most frequent words.
    Note that "i" comes before "love" due to a lower alphabetical order.

Example 2:
Input: ["the", "day", "is", "sunny", "the", "the", "the", "sunny", "is", "is"], k = 4
Output: ["the", "is", "sunny", "day"]
Explanation: "the", "is", "sunny" and "day" are the four most frequent words,
    with the number of occurrence being 4, 3, 2 and 1 respectively.
```

Note:

- You may assume k is always valid, $1 \le k \le$ number of unique elements.
- Input words contain only lowercase letters.

Follow up:

• Try to solve it in O(n log k) time and O(n) extra space.

分析

用 hash map 來統計每個字的出現次數, 以 vector 來保存 pair, 以 partial heap sort 得到答案

```
{
                          if (first.second > second.second)
                              return true;
                          else if (first.second < second.second)</pre>
                              return false;
                          else
                          {
                              return (first.first < second.first);</pre>
                      });
        // 取得答案
        vector<string> result; result.reserve(k);
        for_each(vecCache.begin(), next(vecCache.begin(), k)
                 , [&](const auto& e)
                      result.push_back(e.first);
                 });
        return result;
    }
};
```

相關題目

No

第 8 章 查找

8.1 Search for a Range

描述

Given a sorted array of integers, find the starting and ending position of a given target value.

Your algorithm's runtime complexity must be in the order of $O(\log n)$.

If the target is not found in the array, return

-1, -1

For example, Given

5, 7, 7, 8, 8, 10

and target value 8, return

3, 4

分析

已經排好了序,用二分查找。

使用 STL

else

```
return vector<int> { 1, u };
     }
 };
重新實現 lower bound 和 upper bound
 // LeetCode, Search for a Range
 // 重新實現 lower_bound 和 upper_bound
 // 時間複雜度 O(logn), 空間複雜度 O(1)
 class Solution {
 public:
     vector<int> searchRange (vector<int>& nums, int target) {
         auto lower = lower_bound(nums.begin(), nums.end(), target);
         auto uppper = upper_bound(lower, nums.end(), target);
         if (lower == nums.end() || *lower != target)
             return vector<int> { -1, -1 };
         else
             return vector<int> {distance(nums.begin(), lower),
                                 distance(nums.begin(), prev(uppper)));
     }
     template<typename ForwardIterator, typename T>
     ForwardIterator lower_bound (ForwardIterator first,
             ForwardIterator last, T value) {
         while (first != last) {
             auto mid = next(first, distance(first, last) / 2);
             if (value > *mid)
                                 first = ++mid;
             else
                                 last = mid;
         }
         return first;
     }
     template<typename ForwardIterator, typename T>
     ForwardIterator upper_bound (ForwardIterator first,
             ForwardIterator last, T value) {
         while (first != last) {
             auto mid = next(first, distance (first, last) / 2);
                                  first = ++mid; // 與 lower_bound 僅此不同
             if (value >= *mid)
             else
                                  last = mid;
         }
         return first;
     }
 };
```

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相關題目

• Search Insert Position, 見 §8.2

8.2 Search Insert Position

描述

Given a sorted array and a target value, return the index if the target is found. If not, return the index where it would be if it were inserted in order.

You may assume no duplicates in the array.

```
Here are few examples. [1,3,5,6], 5 \rightarrow 2
```

```
[1,3,5,6], 5 \rightarrow 2

[1,3,5,6], 2 \rightarrow 1

[1,3,5,6], 7 \rightarrow 4

[1,3,5,6], 0 \rightarrow 0
```

分析

```
即 std::lower_bound()。
```

代碼

```
// LeetCode, Search Insert Position
// 重新實現 lower_bound
// 時間複雜度 O(logn), 空間複雜度 O(1)
class Solution {
public:
    int searchInsert(vector<int>& nums, int target) {
       return distance(nums.begin(), lower_bound(nums.begin(), nums.end(), target));
    }
    template<typename ForwardIterator, typename T>
    ForwardIterator lower_bound (ForwardIterator first,
            ForwardIterator last, T value) {
        while (first != last) {
            auto mid = next(first, distance(first, last) / 2);
            if (value > *mid)
                                first = ++mid;
            else
                                last = mid;
       return first;
    }
};
```

相關題目

• Search for a Range, 見 §8.1

8.3 Search a 2D Matrix 237

8.3 Search a 2D Matrix

描述

Write an efficient algorithm that searches for a value in an $m \times n$ matrix. This matrix has the following properties:

- Integers in each row are sorted from left to right.
- The first integer of each row is greater than the last integer of the previous row.

```
For example, Consider the following matrix:
```

```
[1, 3, 5, 7],
[10, 11, 16, 20],
[23, 30, 34, 50]
```

Given target = 3, return true.

分析

二分查找。

```
// LeetCode, Search a 2D Matrix
// 時間複雜度 O(logn), 空間複雜度 O(1)
class Solution {
public:
    bool searchMatrix(const vector<vector<int>>& matrix, int target) {
        if (matrix.empty()) return false;
        const size_t m = matrix.size();
        const size_t n = matrix.front().size();
        int first = 0;
        int last = m * n;
        while (first < last) {</pre>
            int mid = first + (last - first) / 2;
            int value = matrix[mid / n] [mid % n];
            if (value == target)
                return true;
            else if (value < target)
                first = mid + 1;
            else
                last = mid;
        }
        return false;
    }
};
```

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相關題目

• 無

8.4 Search a 2D Matrix II

描述

Write an efficient algorithm that searches for a value in an $m \times n$ matrix. This matrix has the following properties:

- Integers in each row are sorted in ascending from left to right.
- Integers in each column are sorted in ascending from top to bottom.

For example, Consider the following matrix:

```
[
[1, 4, 7, 11, 15],
[2, 5, 8, 12, 19],
[3, 6, 9, 16, 22],
[10, 13, 14, 17, 24],
[18, 21, 23, 26, 30]
]
```

Given target = 3, return true.

分析

二分查找。

```
// 時間複雜度 O(m+n), 空間複雜度 O(1)
class Solution {
public:
    bool searchMatrix(vector<vector<int>>& matrix, int target) {
        int row = matrix.size() - 1;
        if (row < 0) return false;
        int col = 0;
        while (row >= 0 && col < matrix[0].size())
            if (matrix[row][col] > target)
                row--;
            else if (matrix[row][col] < target)</pre>
                col++;
            else
                return true;
        }
        return false;
    }
};
```

8.5 Find Peak Element 239

分治

```
// 時間複雜度 O(nlogn), 空間複雜度 O(logn)
class Solution {
public:
    bool searchMatrix(vector<vector<int>>& matrix, int target) {
        int M = matrix.size();
        if (M == 0) return false;
        int N = matrix[0].size();
        if (N == 0) return false;
        return searchRec(matrix, target, 0, 0, N-1, M-1);
    }
private:
    bool searchRec(vector<vector<int>>& matrix, const int& target
                   , int left, int up, int right, int down)
    {
        // 若果 matrix 已經不成形
        if (left > right || up > down)
            return false;
        else if (target < matrix[up][left] || target > matrix[down][right])
            return false; // target 不在 matrix 之中
        int mid = left + (right - left) / 2; // 使用 index 中
        int row = up;
        while (row <= down && matrix[row][mid] <= target)</pre>
            if (matrix[row][mid] == target)
                return true;
            row++;
        return searchRec(matrix, target, left, row, mid-1, down)
            || searchRec(matrix, target, mid+1, up, right, row-1);
    }
}:
```

相關題目

無

8.5 Find Peak Element

描述

A peak element is an element that is greater than its neighbors.

Given an input array nums, where nums[i] \neq nums[i+1], find a peak element and return its index.

The array may contain multiple peaks, in that case return the index to any one of the peaks is fine.

You may imagine that $nums[-1] = nums[n] = -\infty$.

Example 1:

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```
Input: nums = [1,2,3,1]
Output: 2
Explanation: 3 is a peak element and your function should return the index number 2.

Example 2:
Input: nums = [1,2,1,3,5,6,4]
Output: 1 or 5
Explanation: Your function can return either index number 1 where the peak element is 2, or index number 5 where the peak element is 6.
```

分析

二分查找。

8.5.1 迭代

```
// 時間複雜度 O(logn), 空間複雜度 O(logn)
class Solution {
public:
    int findPeakElement(vector<int>& nums) {
        return findPeak(nums, 0, nums.size()-1);
    }
private:
    int findPeak(const vector<int>& nums, int left, int right)
        while (left <= right)
            int mid = left + (right - left) / 2;
            if (left == right)
                return left;
            if (nums[mid] > nums[mid + 1])
                right = mid;
            else
                left = ++mid;
        return left;
    }
};
```

8.5.2 遞歸

```
// 時間複雜度 O(logn), 空間複雜度 O(logn)
class Solution {
public:
    int findPeakElement(vector<int>& nums) {
        return findPeak(nums, 0, nums.size()-1);
    }
private:
    int findPeak(const vector<int>& nums, int left, int right)
    {
```

相關題目

• 無

8.6 Find Minimum in Rotated Sorted Array

描述

```
Suppose an array sorted in ascending order is rotated at some pivot unknown to you beforehand.

(i.e., [0,1,2,4,5,6,7] might become [4,5,6,7,0,1,2]).

Find the minimum element.

You may assume no duplicate exists in the array.

Example 1:

Input: [3,4,5,1,2]

Output: 1

Example 2:

Input: [4,5,6,7,0,1,2]
```

分析

二分查找。

Output: 0

8.6.1 迭代

```
// 時間複雜度 O(logn), 空間複雜度 O(logn)
class Solution {
public:
    int findMin(vector<int>& nums) {
        int left = 0;
        int right = nums.size();

        int minVal = INT_MAX;
        while (left < right) {
            int mid = left + (right - left) / 2;
        int index = 0;</pre>
```

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```
if (mid == left) {
                 minVal = min(minVal, nums[mid]);
                 break;
            if (nums[left] < nums[mid]) {</pre>
                 index = left;
                 left = ++mid;
            else if (nums[left] > nums[mid]) {
                 index = mid;
                 right = mid;
            }
            else
                 left++;
            minVal = min(minVal, nums[index]);
        }
        return minVal;
    }
};
```

8.7 Find K Closest Elements

描述

Given a sorted array arr, two integers k and x, find the k closest elements to x in the array. The result should also be sorted in ascending order. If there is a tie, the smaller elements are always preferred.

```
Example 1:
Input: arr = [1,2,3,4,5], k = 4, x = 3
Output: [1,2,3,4]

Example 2:
Input: arr = [1,2,3,4,5], k = 4, x = -1
Output: [1,2,3,4]
```

二分杳找。

8.7.1 迭代

```
// 時間複雜度 O(logn), 空間複雜度 O(logn)
class Solution {
public:
    vector<int> findClosestElements(vector<int>& arr, int k, int x) {
    if ((int)arr.size() <= k) return arr;
    auto pos = ClosestSearch(arr.begin(), arr.end(), x);</pre>
```

```
// 使用兩個指針, 往左右走開, 若差相同, 先取左(細), 後取右(大)
        if (pos == arr.end()) {
            return vector<int>(prev(arr.end(), k), arr.end());
        else {
            auto left = pos;
            auto right = next(pos);
            cout << *pos << endl;</pre>
            --k;
            while (k && left != arr.begin() && right != arr.end()) {
                // 若差相同, 先取左(細), 後取右(大)
                if (abs(*prev(left) - x) \le abs(*right - x))
                    left = prev(left);
                else
                    right = next(right);
                --k;
            }
            if (k) {
                if (left == arr.begin()) {
                    while (k--) right = next(right);
                }
                else {
                    while (k--) left = prev(left);
                }
            }
            return vector<int>(left, right);
        }
    }
private:
    template <class RandIT, class T>
        RandIT ClosestSearch(RandIT left, RandIT right, const T& target) {
        RandIT first = left;
        RandIT last = right;
        while (left != right) {
            auto mid = next(left, distance(left, right) / 2);
            if (*mid == target) return mid;
            if (*mid < target)
                left = next(mid);
            else
                right = mid;
        }
        if (left == first) return left;
        if (left != last) {
            if (abs(*prev(left) - target) <= abs(*left - target))</pre>
                return prev(left);
            else
                return left;
        }
```

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```
return left;
};
```

8.8 Closest Binary Search Tree Value

描述

Given a non-empty binary search tree and a target value, find the value in the BST that is closest to the target.

Note:

- Given target value is a floating point.
- You are guaranteed to have only one unique value in the BST that is closest to the target.

Example 1:

```
Input: root = [4,2,5,1,3], target = 3.714286

4
/\
2 5
/\
1 3
Output: 4
```

分析

二分查找。

8.8.1 迭代

```
// 時間複雜度 O(logn), 空間複雜度 O(1)
class Solution {
public:
    int closestValue(TreeNode* root, double target) {
        if (root == nullptr) return target;

        int curMin = root->val;

        queue<TreeNode*> q;
        q.push(root);
        while (!q.empty()) {
            TreeNode *cur = q.front();
            q.pop();

        if (abs(cur->val - target) < abs(curMin - target)) {
            curMin = cur->val;
            if (abs(curMin - target) == 0) return curMin;
        }
}
```

```
if (cur->val > target && cur->left)
                  q.push(cur->left);
              else if (cur->val < target && cur->right)
                  q.push(cur->right);
          }
         return curMin;
     }
 };
       禠歸
8.8.2
 // 時間複雜度 O(logn), 空間複雜度 O(1)
 class Solution {
 public:
     int closestValue(TreeNode* root, double target) {
          double closest = root->val;
          PreOrder(root, target, closest);
          return closest;
     }
 private:
     void PreOrder(TreeNode *root, const double& target, double& closest) {
          if (closest == target) return;
          if (root == nullptr) return;
          if (abs(root->val - target) < abs(closest - target)) {
              closest = root->val;
              if (closest == target) return;
          }
          if (root->val > target)
              PreOrder(root->left, target, closest);
          else
             PreOrder(root->right, target, closest);
     }
 };
```

8.9 Search in a Sorted Array of Unknown Size

描述

Given an integer array sorted in ascending order, write a function to search target in nums. If target exists, then return its index, otherwise return -1. However, the array size is unknown to you. You may only access the array using an ArrayReader interface, where ArrayReader.get(k) returns the element of the array at index k (0-indexed).

You may assume all integers in the array are less than 10000, and if you access the array out of bounds, ArrayReader.get will return 2147483647.

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```
Example 1:
Input: array = [-1,0,3,5,9,12], target = 9
Output: 4
Explanation: 9 exists in nums and its index is 4

Example 2:
Input: array = [-1,0,3,5,9,12], target = 2
Output: -1
Explanation: 2 does not exist in nums so return -1
Note:
```

- You may assume that all elements in the array are unique.
- The value of each element in the array will be in the range [-9999, 9999].

分析

二分查找。

8.9.1 迭代

```
// 時間複雜度 O(logn), 空間複雜度 O(1)
class Solution {
public:
    int search(const ArrayReader& reader, int target) {
        // 由 0 開始的 binary search
        int left = 0;
        int right = 1;
        int OutBound = 2147483647;
        while (left < right) {
            int mid = left + (right - left) / 2;
            if (reader.get(mid) == target) return mid;
            if (reader.get(mid) == OutBound)
                right = mid;
            else if (reader.get(mid) < target) {</pre>
                left = ++mid;
                right <<= 1; // times 2
            }
            else
                right = mid;
        }
        return -1;
    }
};
```

8.10 Find Smallest Letter Greater Than Target

描述

Given a list of sorted characters letters containing only lowercase letters, and given a target letter target, find the smallest element in the list that is larger than the given target.

Letters also wrap around. For example, if the target is target = 'z' and letters = ['a', 'b'], the answer is 'a'.

```
Example:
```

```
Input:
letters = ["c", "f", "j"]
target = "a"
Output: "c"
Input:
letters = ["c", "f", "j"]
target = "c"
Output: "f"
Input:
letters = ["c", "f", "j"]
target = "d"
Output: "f"
Input:
letters = ["c", "f", "j"]
target = "g"
Output: "j"
Input:
letters = ["c", "f", "j"]
target = "j"
Output: "c"
letters = ["c", "f", "j"]
target = "k"
Output: "c"
```

Note:

- letters has a length in range [2, 10000].
- letters consists of lowercase letters, and contains at least 2 unique letters.
- target is a lowercase letter.

分析

Use upper bound.

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8.10.1 迭代

```
// 時間複雜度 O(logn), 空間複雜度 O(1)
class Solution {
public:
    char nextGreatestLetter(vector<char>& letters, char target) {
        if (letters.size() == 0) return 'a';
        if (letters.size() == 1) return letters[0];
        int left = 0;
        int right = letters.size();
        while (left < right) {</pre>
            int mid = left + (right - left) / 2;
            if (letters[mid] <= target)</pre>
                left = ++mid;
            else
                right = mid;
        }
        if (left >= (int)letters.size() || letters[left] < target)</pre>
            return letters[0];
            return letters[left];
    }
};
```

8.11 Split Array Largest Sum

描述

Given an array which consists of non-negative integers and an integer m, you can split the array into m non-empty continuous subarrays. Write an algorithm to minimize the largest sum among these m subarrays.

Example:

```
Input:
nums = [7,2,5,10,8]
m = 2

Output:
18

Explanation:
There are four ways to split nums into two subarrays.
The best way is to split it into [7,2,5] and [10,8],
where the largest sum among the two subarrays is only 18.
```

Note: If n is the length of array, assume the following constraints are satisfied:

- $1 \le n \le 1000$
- $1 \le m \le \min(50, n)$

8.11.1 暴力 - Brute Force

```
// 時間複雜度 O(n^m), 空間複雜度 O(n)
class Solution {
public:
    int ans;
    int n, m;
    void dfs(vector<int>& nums, int i, int cntSubarrays, int curSum, int curMax) {
        if (i == n && cntSubarrays == m) {
            ans = min(ans, curMax);
            return;
        if (i == n) {
            return:
        if (i > 0) {
            dfs(nums, i + 1, cntSubarrays, curSum + nums[i], max(curMax, curSum + nums[i]));
        }
        if (cntSubarrays < m) {</pre>
            dfs(nums, i + 1, cntSubarrays + 1, nums[i], max(curMax, nums[i]));
        }
    }
    int splitArray(vector<int>& nums, int M) {
        ans = INT MAX;
        n = nums.size();
        m = M:
        dfs(nums, 0, 0, 0, 0);
        return ans;
    }
};
```

分析

Let's define f[i][j] to be the minimum largest subarray sum for splitting nums[0..i] into j parts.

Consider the jth subarray. We can split the array from a smaller index k to i to form it. Thus f[i][j] can be derived from max(f[k][j-1], nums[k+1] + ... + nums[i]). For all valid index k, f[i][j] should choose the minimum value of the above formula.

The final answer should be f[n][m], where n is the size of the array.

For corner situations, all the invalid f[i][j] should be assigned with INFINITY, and f[0][0] should be initialized with 0.

8.11.2 動規

```
// 時間複雜度 O(n^2 * m), 空間複雜度 O(n*m)
class Solution {
public:
    int splitArray(vector<int>& nums, int m) {
        int n = nums.size();
        vector<vector<int>> f(n + 1, vector<int>(m + 1, INT_MAX));
```

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```
vector<int> sub(n + 1, 0);
         for (int i = 0; i < n; i++) {
             sub[i + 1] = sub[i] + nums[i];
         f[0][0] = 0;
         for (int i = 1; i <= n; i++) {
             for (int j = 1; j \le m; j++) {
                 for (int k = 0; k < i; k++) {
                     f[i][j] = min(f[i][j], max(f[k][j-1], sub[i] - sub[k]));
                 }
             }
         return f[n][m];
     }
 };
8.11.3 二分尋找
 // 時間複雜度 O(n), 空間複雜度 O(n)
  #define LL long long
 class Solution {
 public:
      int splitArray(vector<int>& nums, int m) {
         LL 1 = 0, r = 0;
         int n = nums.size();
         for (int i = 0; i < n; i++) {
             r += nums[i];
             if (1 < nums[i]) {
                 1 = nums[i];
             }
         }
         LL ans = r;
         while (1 <= r) {
             LL mid = (1 + r) >> 1; // mid 是 sub-vector 的平均總加
             LL sum = 0; // 當下的 sub-vector 的總加
             int cnt = 1; // sub-vector 的總數
             for (int i = 0; i < n; i++) {
                 if (sum + nums[i] > mid) {
                     cnt ++;
                     sum = nums[i];
                 } else {
                     sum += nums[i];
             if (cnt <= m) {
                 ans = min(ans, mid);
                 r = mid - 1;
             } else {
                 l = mid + 1;
             }
```

return ans;

};

8.12 Minimum Size Subarray Sum

8.12.1 描述

Given an array of n positive integers and a positive integer s, find the minimal length of a contiguous subarray of which the sum \geq s. If there isn't one, return 0 instead.

Example:

```
Input: s = 7, nums = [2,3,1,2,4,3]
Output: 2
Explanation: the subarray [4,3] has the minimal length under the problem constraint.
```

Follow up:

If you have figured out the O(n) solution, try coding another solution of which the time complexity is $O(n \log n)$.

8.12.2 分析

使用兩個指針,當累積總和大過目標數時,左指針往右推進,否則右指針往右推進。

8.12.3 雙指針

```
// LeetCode
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    int minSubArrayLen(int s, vector<int>& nums)
    {
        int n = nums.size();
        int ans = INT_MAX;
        int left = 0;
        int sum = 0;
        for (int i = 0; i < n; i++) {
            sum += nums[i];
            while (sum >= s) {
                ans = min(ans, i + 1 - left);
                sum -= nums[left++];
            }
        }
        return (ans != INT_MAX) ? ans : 0;
    }
};
```

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8.12.4 分析

在順序的 array 當中計算得出移動總和。然後順序找尋合條件的 subarray。並計算其長短。可以利用當前數值為 shifting value,加上目標數值和 lower bound 找到合條件的 subarray。

8.12.5 移動總加

```
// LeetCode
// 時間複雜度 O(nlogn), 空間複雜度 O(n)
class Solution {
public:
    int minSubArrayLen(int s, vector<int>& nums)
        int n = nums.size();
        if (n == 0)
            return 0:
        int ans = INT MAX;
        vector<int> sums(n + 1, 0); //size = n+1 for easier calculations
        //sums[0]=0 : Meaning that it is the sum of first 0 elements
        //sums[1]=A[0] : Sum of first 1 elements
        //ans so on...
        for (int i = 1; i <= n; i++)
            sums[i] = sums[i - 1] + nums[i - 1];
        for (int i = 1; i <= n; i++) {
            int to find = s + sums[i - 1];
            auto bound = lower_bound(sums.begin(), sums.end(), to_find);
            if (bound != sums.end()) {
                ans = min(ans, static_cast<int>(bound - (sums.begin() + i - 1)));
            }
        return (ans != INT_MAX) ? ans : 0;
    }
}:
```

8.13 Find Median from Data Stream

8.13.1 描述

Median is the middle value in an ordered integer list. If the size of the list is even, there is no middle value. So the median is the mean of the two middle value.

For example,

```
[2,3,4], the median is 3 [2,3], the median is (2+3) / 2 = 2.5
```

Design a data structure that supports the following two operations:

- void addNum(int num) Add a integer number from the data stream to the data structure.
- double findMedian() Return the median of all elements so far.

```
Example:
  addNum(1)
  addNum(2)
 findMedian() -> 1.5
  addNum(3)
 findMedian() -> 2
        保持順序
8.13.2
  // LeetCode
  // 時間複雜度 O(n), 空間複雜度 O(1)
  class MedianFinder {
 public:
     /** initialize your data structure here. */
     MedianFinder() {
     }
     void addNum(int num) {
         if (m_cache.empty())
             m_cache.push_back(num);
         else
             m_cache.insert(lower_bound(m_cache.begin(), m_cache.end(), num), num);
     }
     double findMedian() {
         int N = m_cache.size();
         if (N & 1)
             return m_cache[N/2];
         else
             return (m_{cache}[N/2 - 1] + m_{cache}[N/2]) / 2.0;
     }
 private:
     vector<int> m_cache;
  };
  /**
  * Your MedianFinder object will be instantiated and called as such:
  * MedianFinder* obj = new MedianFinder();
  * obj->addNum(num);
  * double param_2 = obj->findMedian();
  */
        兩個 heap
8.13.3
 // LeetCode
 // 時間複雜度 O(n), 空間複雜度 O(1)
  class MedianFinder {
     // lo 會維持住數值細過一半的數字
     priority_queue<int> lo; // max heap
     // hi 會維持住數值大過一半的數字
```

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```
priority queue<int, vector<int>, greater<int>> hi; // min heap
public:
    // Adds a number into the data structure.
    void addNum(int num)
        lo.push(num); // Add to max heap
        hi.push(lo.top()); // balancing step
        lo.pop();
        if (lo.size() < hi.size()) { // maintain size property</pre>
            lo.push(hi.top());
            hi.pop();
        }
    }
    // Returns the median of current data stream
    double findMedian()
        return lo.size() > hi.size() ? lo.top() : ((double) lo.top() + hi.top()) * 0.5;
    }
};
```

8.13.4 STD method - AVL tree

```
// LeetCode
// 時間複雜度 O(n), 空間複雜度 O(1)
class MedianFinder {
public:
    /** initialize your data structure here. */
    MedianFinder()
        : m_mid(m_data.end()) {
    }
    void addNum(int num) {
        const int n = m_data.size();
        m_data.insert(num);
        if (!n)
                                                // first element inserted
            m_mid = m_data.begin();
        else if (num < *m_mid)
                                                  // median is decreased
            m_mid = (n & 1 ? m_mid : prev(m_mid));
        else
                                                // median is increased
            m_mid = (n & 1 ? next(m_mid) : m_mid);
    }
    double findMedian() {
        const int n = m_data.size();
        return ((double) *m_mid + *next(m_mid, n % 2 - 1)) * 0.5;
    }
```

```
private:
    multiset<int> m_data;
    multiset<int>::iterator m_mid;
};
```

第9章 暴力枚舉法

9.1 Subsets

描述

Given a set of distinct integers, S, return all possible subsets.

Note

- Elements in a subset must be in non-descending order.
- The solution set must not contain duplicate subsets.

```
For example, If S = [1,2,3], a solution is:

[
[3],
[1],
[2],
[1,2,3],
[1,3],
[2,3],
[1,2],
[]
```

9.1.1 遞歸

增量構造法1

```
每個元素,都有兩種選擇,選或者不選。
// LeetCode, Subsets
```

```
// 增量構造法,深搜,時間複雜度 O(2^n),空間複雜度 O(n) class Solution {
public:
    vector<vector<int> > subsets(vector<int> &S) {
        sort(S.begin(), S.end()); // 輸出要求有序
        vector<vector<int> > result;
        vector<int> path;
        subsets(S, path, 0, result);
        return result;
```

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```
}
 private:
     static void subsets(const vector<int> &S, vector<int> &path, int step,
             vector<vector<int> > &result) {
         if (step == S.size()) {
             result.push_back(path);
             return;
         }
         // 不選 S[step]
         subsets(S, path, step + 1, result);
         // 選 S[step]
         path.push_back(S[step]);
         subsets(S, path, step + 1, result);
         path.pop_back();
     }
 };
增量構造法 2
   每個元素,都有兩種選擇,選或者不選。
 // LeetCode, Subsets
 // 增量構造法,深搜,時間複雜度 O(2<sup>n</sup>),空間複雜度 O(n)
 class Solution {
 public:
     vector<vector<int> > subsets(vector<int> &S) {
         sort(S.begin(), S.end()); // 輸出要求有序
         vector<vector<int> > result;
         vector<int> path;
         subsets(S, path, 0, result);
         return result;
     }
 private:
     static void subsets(const vector<int> &S, vector<int> &path, int step,
                         vector<vector<int> > &result) {
         result.push_back(path);
         for (int i = step; i < S.size(); i++) {</pre>
             // 選 S[step]
             path.push_back(S[i]);
             subsets(S, path, i + 1, result);
             // 不選 S[step]
             path.pop_back();
         }
     }
 };
```

位向量法

開一個位向量 bool selected [n],每個元素可以選或者不選。

第9章 暴力枚舉法

```
// LeetCode, Subsets
// 位向量法,深搜,時間複雜度 D(2<sup>n</sup>),空間複雜度 D(n)
class Solution {
public:
    vector<vector<int> > subsets(vector<int> &S) {
        sort(S.begin(), S.end()); // 輸出要求有序
        vector<vector<int> > result;
        vector<bool> selected(S.size(), false);
        subsets(S, selected, 0, result);
        return result;
    }
private:
    static void subsets(const vector<int> &S, vector<bool> &selected, int step,
            vector<vector<int> > &result) {
        if (step == S.size()) {
            vector<int> subset;
            for (int i = 0; i < S.size(); i++) {
                if (selected[i]) subset.push_back(S[i]);
            }
            result.push_back(subset);
            return;
        }
        // 不選 S[step]
        selected[step] = false;
        subsets(S, selected, step + 1, result);
        // 選 S[step]
        selected[step] = true;
        subsets(S, selected, step + 1, result);
    }
};
```

9.1.2 迭代

增量構造法

9.2 Subsets II 259

```
return result;
};
```

二進制法

本方法的前提是:集合的元素不超過 int 位數。用一個 int 整數表示位向量,第 i 位為 1,則表示選擇 S[i],為 0 則不選擇。例如 $S=\{A,B,C,D\}$,則 0110=6 表示子集 $\{B,C\}$ 。

這種方法最巧妙。因為它不僅能生成子集,還能方便的表示集合的並、交、差等集合運算。設兩個集合的位向量分別為 B_1 和 B_2 ,則 $B_1 \cup B_2$, $B_1 \cap B_2$, $B_1 \cap B_2$, $B_1 \cap B_2$, $B_1 \cap B_2$

二進制法, 也可以看做是位向量法, 只不過更加優化。

```
// LeetCode, Subsets
// 二進制法, 時間複雜度 O(2<sup>n</sup>), 空間複雜度 O(1)
class Solution {
public:
    vector<vector<int> > subsets(vector<int> &S) {
        sort(S.begin(), S.end()); // 輸出要求有序
        vector<vector<int> > result;
        const size_t n = S.size();
        vector<int> v;
        for (size_t i = 0; i < 1 << n; i++) {
            for (size_t j = 0; j < n; j++) {
                if (i & 1 << j) v.push_back(S[j]);</pre>
            result.push_back(v);
            v.clear();
        return result;
    }
};
```

相關題目

• Subsets II, 見 §9.2

9.2 Subsets II

描述

Given a collection of integers that might contain duplicates, S, return all possible subsets.

Note:

Elements in a subset must be in non-descending order. The solution set must not contain duplicate subsets. For example, If S = [1,2,2], a solution is:

```
[
[2],
[1],
```

```
[1,2,2],
[2,2],
[1,2],
[]
```

分析

這題有重複元素,但本質上,跟上一題很類似,上一題中元素沒有重複,相當於每個元素只能選0或1次,這裏擴充到了每個元素可以選0到若干次而已。

9.2.1 遞歸

增量構造法

```
// LeetCode, Subsets II
// 增量構造法, 版本 1, 時間複雜度 0(2<sup>n</sup>), 空間複雜度 0(n)
class Solution {
public:
    vector<vector<int> > subsetsWithDup(vector<int> &S) {
        sort(S.begin(), S.end()); // 必須排序
        vector<vector<int> > result;
        vector<int> path;
        dfs(S, S.begin(), path, result);
        return result;
    }
private:
    static void dfs(const vector<int> &S, vector<int>::iterator start,
            vector<int> &path, vector<vector<int> > &result) {
        result.push_back(path);
        for (auto i = start; i < S.end(); i++) {</pre>
            if (i != start && *i == *(i-1)) continue;
            path.push_back(*i);
            dfs(S, i + 1, path, result);
            path.pop_back();
        }
    }
}:
// LeetCode, Subsets II
// 增量構造法, 版本 2, 時間複雜度 O(2<sup>n</sup>), 空間複雜度 O(n)
class Solution {
public:
    vector<vector<int> > subsetsWithDup(vector<int> &S) {
        vector<vector<int> > result;
        sort(S.begin(), S.end()); // 必須排序
```

9.2 Subsets II 261

```
unordered_map<int, int> count_map; // 記錄每個元素的出現次數
         for_each(S.begin(), S.end(), [&count_map](int e) {
             if (count map.find(e) != count map.end())
                 count_map[e]++;
             else
                 count_map[e] = 1;
         });
         // 將 map 裏的 pair 拷貝到一個 vector 裏
         vector<pair<int, int> > elems;
         for_each(count_map.begin(), count_map.end(),
                 [&elems](const pair<int, int> &e) {
                     elems.push_back(e);
                 });
         sort(elems.begin(), elems.end());
         vector<int> path; // 中間結果
         subsets(elems, 0, path, result);
         return result;
     }
 private:
     static void subsets(const vector<pair<int, int> > &elems,
             size_t step, vector<int> &path, vector<vector<int> > &result) {
         if (step == elems.size()) {
             result.push_back(path);
             return;
         }
         for (int i = 0; i <= elems[step].second; i++) {</pre>
             for (int j = 0; j < i; ++j) {
                 path.push_back(elems[step].first);
             subsets(elems, step + 1, path, result);
             for (int j = 0; j < i; ++j) {
                 path.pop_back();
         }
     }
 };
位向量法
 // LeetCode, Subsets II
 // 位向量法, 時間複雜度 O(2<sup>n</sup>), 空間複雜度 O(n)
 class Solution {
 public:
     vector<vector<int> > subsetsWithDup(vector<int> &S) {
         vector<vector<int> > result; // 必須排序
         sort(S.begin(), S.end());
         vector<int> count(S.back() - S.front() + 1, 0);
         // 計算所有元素的個數
```

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```
for (auto i : S) {
            count[i - S[0]]++;
        // 每個元素選擇了多少個
        vector<int> selected(S.back() - S.front() + 1, -1);
        subsets(S, count, selected, 0, result);
        return result;
    }
private:
    static void subsets(const vector<int> &S, vector<int> &count,
            vector<int> &selected, size_t step, vector<vector<int> > &result) {
        if (step == count.size()) {
            vector<int> subset;
            for(size_t i = 0; i < selected.size(); i++) {</pre>
                for (int j = 0; j < selected[i]; j++) {</pre>
                     subset.push_back(i+S[0]);
            }
            result.push_back(subset);
            return;
        }
        for (int i = 0; i <= count[step]; i++) {</pre>
            selected[step] = i;
            subsets(S, count, selected, step + 1, result);
    }
};
```

9.2.2 迭代

增量構造法

```
// LeetCode, Subsets II
// 增量構造法
// 時間複雜度 O(2^n), 空間複雜度 O(1)
class Solution {
public:
    vector<vector<int> > subsetsWithDup(vector<int> &S) {
        sort(S.begin(), S.end()); // 必須排序
        vector<vector<int> > result(1);

        size_t previous_size = 0;
        for (size_t i = 0; i < S.size(); ++i) {
            const size_t size = result.size();
            for (size_t j = 0; j < size; ++j) {
                if (i == 0 || S[i] != S[i-1] || j >= previous_size) {
                     result.push_back(result[j]);
                     result.back().push_back(S[i]);
                     result.back().push_back(S[i]);
```

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```
}
             }
             previous_size = size;
         return result;
     }
 };
二進制法
 // LeetCode, Subsets II
 // 二進制法, 時間複雜度 O(2<sup>n</sup>), 空間複雜度 O(1)
 class Solution {
 public:
     vector<vector<int> > subsetsWithDup(vector<int> &S) {
         sort(S.begin(), S.end()); // 必須排序
         // 用 set 去重, 不能用 unordered_set, 因為輸出要求有序
         set<vector<int> > result;
         const size_t n = S.size();
         vector<int> v;
         for (size_t i = 0; i < 1U << n; ++i) {
             for (size_t j = 0; j < n; ++j) {
                 if (i & 1 << j)
                     v.push_back(S[j]);
             result.insert(v);
             v.clear();
         vector<vector<int> > real_result;
         copy(result.begin(), result.end(), back_inserter(real_result));
         return real_result;
     }
 }:
```

相關題目

• Subsets, 見 §9.1

9.3 Permutations

描述

Given a collection of numbers, return all possible permutations.

```
For example, [1,2,3] have the following permutations: [1,2,3], [1,3,2], [2,1,3], [2,3,1], [3,1,2], and [3,2,1].
```

9.3.1 next permutation()

偷懶的做法,可以直接使用 std::next_permutation()。如果是在 OJ 網站上,可以用這個 API 偷個懶;如果是在面試中,面試官肯定會讓你重新實現。

代碼

```
// LeetCode, Permutations
// 時間複雜度 O(n!), 空間複雜度 O(1)
class Solution {
public:
    vector<vector<int> > permute(vector<int> &num) {
        vector<vector(int> > result;
        sort(num.begin(), num.end());

        do {
            result.push_back(num);
        } while(next_permutation(num.begin(), num.end()));
        return result;
    }
};
```

9.3.2 重新實現 next_permutation()

見第 §2.1.14 節。

代碼

```
// LeetCode, Permutations
// 重新實現 next_permutation()
// 時間複雜度 O(n!), 空間複雜度 O(1)
class Solution {
public:
    vector<vector<int> > permute(vector<int> &num) {
       vector<vector<int> > result;
       sort(num.begin(), num.end());
       do {
           result.push_back(num);
       // 調用的是 2.1.12 節的 next_permutation()
       // 而不是 std::next_permutation()
       } while(next_permutation(num.begin(), num.end()));
       return result;
   }
};
```

9.3 Permutations 265

9.3.3 遞歸

本題是求路徑本身,求所有解,函數參數需要標記當前走到了哪步,還需要中間結果的引用,最終結果的引用。

擴展節點,每次從左到右,選一個沒有出現過的元素。

本題不需要判重、因為狀態裝換圖是一顆有層次的樹。收斂條件是當前走到了最後一個元素。

代碼

```
// LeetCode, Permutations
// 深搜, 增量構造法
// 時間複雜度 O(n!), 空間複雜度 O(n)
class Solution {
public:
    vector<vector<int> > permute(vector<int>& num) {
       sort(num.begin(), num.end());
       vector<vector<int>> result;
       vector<int> path; // 中間結果
       dfs(num, path, result);
       return result;
    }
private:
    void dfs(const vector<int>& num, vector<int> &path,
           vector<vector<int> > &result) {
        if (path.size() == num.size()) { // 收斂條件
           result.push_back(path);
           return;
       }
       // 擴展狀態
       for (auto i : num) {
           // 查找 i 是否在 path 中出現過
           auto pos = find(path.begin(), path.end(), i);
           if (pos == path.end()) {
               path.push_back(i);
               dfs(num, path, result);
               path.pop_back();
           }
       }
   }
};
```

相關題目

- Next Permutation, 見 §2.1.14
- Permutation Sequence, 見 §2.1.16

- Permutations II, 見 §9.4
- Combinations, 見 §9.5

9.4 Permutations II

描述

Given a collection of numbers that might contain duplicates, return all possible unique permutations. For example, [1,1,2] have the following unique permutations: [1,1,2], [1,2,1], and [2,1,1].

9.4.1 next permutation()

直接使用 std::next_permutation(),代碼與上一題相同。

9.4.2 重新實現 next permutation()

重新實現 std::next_permutation(), 代碼與上一題相同。

9.4.3 遞歸

遞歸函數 permute() 的參數 p, 是中間結果, 它的長度又能標記當前走到了哪一步, 用於判斷收斂條件。

擴展節點,每次從小到大,選一個沒有被用光的元素,直到所有元素被用光。 本題不需要判重,因為狀態裝換圖是一顆有層次的樹。

代碼

```
// LeetCode, Permutations II
// 深搜, 時間複雜度 O(n!), 空間複雜度 O(n)
class Solution {
public:
    vector<vector<int> > permuteUnique(vector<int>& num) {
        sort(num.begin(), num.end());
       unordered_map<int, int> count_map; // 記錄每個元素的出現次數
       for_each(num.begin(), num.end(), [&count_map](int e) {
           if (count_map.find(e) != count_map.end())
               count_map[e]++;
           else
               count_map[e] = 1;
       });
       // 將 map 裏的 pair 拷貝到一個 vector 裏
       vector<pair<int, int> > elems;
       for_each(count_map.begin(), count_map.end(),
               [&elems](const pair<int, int> &e) {
```

9.5 Combinations 267

```
elems.push back(e);
               });
       vector<vector<int>> result; // 最終結果
       vector<int> p; // 中間結果
       n = num.size();
       permute(elems.begin(), elems.end(), p, result);
       return result;
    }
private:
   size t n;
    typedef vector<pair<int, int> >::const_iterator Iter;
    void permute(Iter first, Iter last, vector<int> &p,
           vector<vector<int> > &result) {
       if (n == p.size()) { // 收斂條件
           result.push_back(p);
       // 擴展狀態
       for (auto i = first; i != last; i++) {
           int count = 0; // 統計 *i 在 p 中出現過多少次
           for (auto j = p.begin(); j != p.end(); j++) {
               if (i->first == *j) {
                   count ++;
               }
           }
           if (count < i->second) {
               p.push_back(i->first);
               permute(first, last, p, result);
               p.pop_back(); // 撤銷動作, 返回上一層
       }
   }
};
```

相關題目

- Next Permutation, 見 §2.1.14
- Permutation Sequence, 見 §2.1.16
- Permutations, 見 §9.3
- Combinations, 見 §9.5

9.5 Combinations

描述

Given two integers n and k, return all possible combinations of k numbers out of 1...n. For example, If n=4 and k=2, a solution is:

```
Γ
    [2,4],
    [3,4],
    [2,3],
    [1,2],
    [1,3],
   [1,4],
 ٦
       禠歸
9.5.1
 // LeetCode, Combinations
  // 深搜, 遞歸
  // 時間複雜度 O(n!), 空間複雜度 O(n)
  class Solution {
 public:
     vector<vector<int> > combine(int n, int k) {
         vector<vector<int> > result;
         vector<int> path;
         dfs(n, k, 1, 0, path, result);
         return result;
     }
 private:
     // start, 開始的數, cur, 已經選擇的數目
     static void dfs(int n, int k, int start, int cur,
             vector<int> &path, vector<vector<int> > &result) {
         if (cur == k) {
             result.push_back(path);
         for (int i = start; i <= n; ++i) {
             path.push_back(i);
             dfs(n, k, i + 1, cur + 1, path, result);
             path.pop_back();
         }
     }
 };
9.5.2 迭代
 // LeetCode, Combinations
 // use prev_permutation()
 // 時間複雜度 O((n-k)!), 空間複雜度 O(n)
 class Solution {
 public:
     vector<vector<int> > combine(int n, int k) {
         vector<int> values(n);
         iota(values.begin(), values.end(), 1);
```

vector<bool> select(n, false);
fill_n(select.begin(), k, true);

```
vector<vector<int> > result;
do{
    vector<int> one(k);
    for (int i = 0, index = 0; i < n; ++i)
        if (select[i])
        one[index++] = values[i];
    result.push_back(one);
} while(prev_permutation(select.begin(), select.end()));
    return result;
};</pre>
```

相關題目

- Next Permutation, 見 §2.1.14
- Permutation Sequence, 見 §2.1.16
- Permutations, 見 §9.3
- Permutations II, 見 §9.4

9.6 Letter Combinations of a Phone Number

描述

Given a digit string, return all possible letter combinations that the number could represent. A mapping of digit to letters (just like on the telephone buttons) is given below.



图 9-1 Phone Keyboard

```
Input:Digit string "23"
Output:
```

Note: Although the above answer is in lexicographical order, your answer could be in any order you want.

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分析

270

無

9.6.1 遞歸

```
// LeetCode, Letter Combinations of a Phone Number
 // 時間複雜度 O(3<sup>n</sup>), 空間複雜度 O(n)
 class Solution {
 public:
      const vector
<string> keyboard { " ", "", "abc", "def", // '0',
'1',
'2',...
              "ghi", "jkl", "mno", "pqrs", "tuv", "wxyz" };
      vector<string> letterCombinations (const string &digits) {
          vector<string> result;
          if (digits.empty()) return result;
          dfs(digits, 0, "", result);
          return result;
      }
      void dfs(const string &digits, size_t cur, string path,
              vector<string> &result) {
          if (cur == digits.size()) {
              result.push_back(path);
              return;
          for (auto c : keyboard[digits[cur] - '0']) {
              dfs(digits, cur + 1, path + c, result);
      }
 };
9.6.2 迭代
 // LeetCode, Letter Combinations of a Phone Number
 // 時間複雜度 O(3<sup>n</sup>), 空間複雜度 O(1)
  class Solution {
 public:
      const vector<string> keyboard { " ", "", "abc", "def", // '0','1','2',...
              "ghi", "jkl", "mno", "pqrs", "tuv", "wxyz" };
      vector<string> letterCombinations (const string &digits) {
          if (digits.empty()) return vector<string>();
          vector<string> result(1, "");
          for (auto d : digits) {
              const size_t n = result.size();
              const size_t m = keyboard[d - '0'].size();
              result.resize(n * m);
              for (size_t i = 0; i < m; ++i)
```

copy(result.begin(), result.begin() + n, result.begin() + n * i);

```
for (size_t i = 0; i < m; ++i) {
            auto begin = result.begin();
            for_each(begin + n * i, begin + n * (i+1), [&](string &s) {
                s += keyboard[d - '0'][i];
            });
        }
        return result;
    }
};</pre>
```

相關題目

• 無

第 10 章 廣度優先搜索

當題目看不出任何規律,既不能用分治,貪心,也不能用動規時,這時候萬能方法——搜索,就派上用場了。搜索分為廣搜和深搜,廣搜裏面又有普通廣搜,雙向廣搜,A*搜索等。深搜裏面又有普通深搜,回溯法等。

廣搜和深搜非常類似 (除了在擴展節點這部分不一樣),二者有相同的框架,如何表示狀態?如何擴展狀態?如何判重?尤其是判重,解決了這個問題,基本上整個問題就解決了。

10.1 Word Ladder

描述

Given two words (start and end), and a dictionary, find the length of shortest transformation sequence from start to end, such that:

- Only one letter can be changed at a time
- Each intermediate word must exist in the dictionary

For example, Given:

```
start = "hit"
end = "cog"
dict = ["hot","dot","dog","lot","log","cog"]
```

As one shortest transformation is "hit" -> "hot" -> "dot" -> "dog" -> "cog", return its length 5.

- Return 0 if there is no such transformation sequence.
- All words have the same length.
- All words contain only lowercase alphabetic characters.

分析

求最短路徑, 用廣搜。

10.1 Word Ladder 273

單隊列

```
//LeetCode, Word Ladder
// 時間複雜度 O(n), 空間複雜度 O(n)
struct state_t {
    string word;
    int level;
    state_t() { word = ""; level = 0; }
    state t(const string& word, int level) {
        this->word = word;
        this->level = level;
    }
    bool operator==(const state t &other) const {
        return this->word == other.word;
};
namespace std {
    template<> struct hash<state_t> {
    public:
        size_t operator()(const state_t& s) const {
            return str_hash(s.word);
    private:
        std::hash<std::string> str_hash;
    };
}
class Solution {
public:
    int ladderLength(const string& start, const string &end,
            const unordered_set<string> &dict) {
        queue<state_t> q;
        unordered_set<state_t> visited; // 判重
        auto state_is_valid = [&](const state_t& s) {
            return dict.find(s.word) != dict.end();
        auto state_is_target = [&](const state_t &s) {return s.word == end; };
        auto state_extend = [&](const state_t &s) {
            unordered_set<state_t> result;
            for (size t i = 0; i < s.word.size(); ++i) {
                state_t new_state(s.word, s.level + 1);
                for (char c = 'a'; c \le 'z'; c++) {
                    // 防止同字母替换
                    if (c == new_state.word[i]) continue;
                    swap(c, new_state.word[i]);
```

```
if (state is valid(new state) &&
                         visited.find(new state) == visited.end()) {
                         result.insert(new state);
                     swap(c, new_state.word[i]); // 恢復該單詞
                 }
             }
             return result;
         };
         state_t start_state(start, 0);
         q.push(start_state);
         visited.insert(start state);
         while (!q.empty()) {
             // 千萬不能用 const auto&, pop() 會刪除元素,
             // 引用就變成了懸空引用
             const auto state = q.front();
             q.pop();
             if (state is target(state)) {
                 return state.level + 1;
             }
             const auto& new_states = state_extend(state);
             for (const auto& new_state : new_states) {
                 q.push(new_state);
                 visited.insert(new_state);
             }
         }
         return 0;
 };
雙隊列
 //LeetCode, Word Ladder
 // 時間複雜度 O(n), 空間複雜度 O(n)
 class Solution {
 public:
     int ladderLength(const string& start, const string &end,
             const unordered_set<string> &dict) {
                                        // 當前層, 下一層
         queue<string> current, next;
         unordered_set<string> visited; // 判重
         int level = -1; // 層次
         auto state_is_valid = [&](const string& s) {
             return dict.find(s) != dict.end();
         };
         auto state_is_target = [&](const string &s) {return s == end;};
         auto state_extend = [&](const string &s) {
```

10.1 Word Ladder 275

```
unordered set<string> result;
            for (size t i = 0; i < s.size(); ++i) {
                string new_word(s);
                for (char c = 'a'; c \leftarrow 'z'; c++) {
                    // 防止同字母替换
                    if (c == new_word[i]) continue;
                    swap(c, new_word[i]);
                    if (state_is_valid(new_word) &&
                        visited.find(new_word) == visited.end()) {
                        result.insert(new_word);
                    }
                    swap(c, new_word[i]); // 恢復該單詞
                }
            }
            return result;
        };
        current.push(start);
        visited.insert(start);
        while (!current.empty()) {
            ++level;
            while (!current.empty()) {
                // 千萬不能用 const auto&, pop() 會刪除元素,
                // 引用就變成了懸空引用
                const auto state = current.front();
                current.pop();
                if (state_is_target(state)) {
                    return level + 1;
                }
                const auto& new_states = state_extend(state);
                for (const auto& new_state : new_states) {
                    next.push(new_state);
                    visited.insert(new_state);
                }
            }
            swap(next, current);
        }
        return 0;
    }
};
```

相關題目

• Word Ladder II, 見 §10.2

10.2 Word Ladder II

描述

Given two words (start and end), and a dictionary, find all shortest transformation sequence(s) from start to end, such that:

- · Only one letter can be changed at a time
- · Each intermediate word must exist in the dictionary

Note:

- · All words have the same length.
- All words contain only lowercase alphabetic characters.

分析

跟 Word Ladder 比, 這題是求路徑本身, 不是路徑長度, 也是 BFS, 略微麻煩點。

求一條路徑和求所有路徑有很大的不同,求一條路徑,每個狀態節點只需要記錄一個前驅即可; 求所有路徑時,有的狀態節點可能有多個父節點,即要記錄多個前驅。

如果當前路徑長度已經超過當前最短路徑長度,可以中止對該路徑的處理,因為我們要找的是最短路徑。

單隊列

```
//LeetCode, Word Ladder II
// 時間複雜度 O(n), 空間複雜度 O(n)
struct state_t {
    string word;
    int level;

    state_t() { word = ""; level = 0; }
    state_t(const string& word, int level) {
        this->word = word;
        this->level = level;
    }
```

10.2 Word Ladder II 277

```
bool operator==(const state t &other) const {
        return this->word == other.word;
    }
};
namespace std {
    template<> struct hash<state_t> {
    public:
        size_t operator()(const state_t& s) const {
            return str_hash(s.word);
        }
    private:
        std::hash<std::string> str_hash;
    };
}
class Solution {
public:
    vector<vector<string> > findLadders(const string& start,
        const string& end, const unordered_set<string> &dict) {
        queue<state_t> q;
        unordered_set<state_t> visited; // 判重
        unordered_map<state_t, vector<state_t> > father; // DAG (樹) key: child value: father
        auto state_is_valid = [&](const state_t& s) {
            return dict.find(s.word) != dict.end();
        }:
        auto state_is_target = [&](const state_t &s) {return s.word == end; };
        auto state_extend = [&](const state_t &s) {
            unordered_set<state_t> result;
            for (size_t i = 0; i < s.word.size(); ++i) {
                state_t new_state(s.word, s.level + 1);
                for (char c = 'a'; c \le 'z'; c++) {
                    // 防止同字母替换
                    if (c == new_state.word[i]) continue;
                    swap(c, new_state.word[i]);
                    if (state_is_valid(new_state)) {
                        auto visited_iter = visited.find(new_state);
                        if (visited_iter != visited.end()) {
                            if (visited_iter->level < new_state.level) {</pre>
                                // do nothing
                            } else if (visited_iter->level == new_state.level) {
                                result.insert(new_state);
                            } else { // not possible
                                throw std::logic_error("not possible to get here");
                        } else {
                            result.insert(new_state);
```

```
}
                   swap(c, new_state.word[i]); // 恢復該單詞
           }
           return result;
       };
       vector<vector<string>> result;
       state_t start_state(start, 0);
       q.push(start_state);
       visited.insert(start state);
       while (!q.empty()) {
           // 千萬不能用 const auto&, pop() 會刪除元素,
           // 引用就變成了懸空引用
           const auto state = q.front();
           q.pop();
           // 如果當前路徑長度已經超過當前最短路徑長度,
           // 可以中止對該路徑的處理, 因為我們要找的是最短路徑
           if (!result.empty() && state.level + 1 > result[0].size()) break;
           if (state_is_target(state)) {
               vector<string> path;
               gen_path(father, start_state, state, path, result);
               continue;
           }
           // 必須挪到下面, 比如同一層 A 和 B 兩個節點均指向了目標節點,
           // 那麼目標節點就會在 q 中出現兩次, 輸出路徑就會翻倍
           // visited.insert(state);
           // 擴展節點
           const auto& new_states = state_extend(state);
           for (const auto& new_state : new_states) {
               if (visited.find(new_state) == visited.end()) {
                   q.push(new_state);
               visited.insert(new_state);
               father[new_state].push_back(state);
           }
       }
       return result;
   }
private:
   void gen_path(unordered_map<state_t, vector<state_t> > &father,
       const state_t &start, const state_t &state, vector<string> &path,
       vector<vector<string> > &result) {
       path.push_back(state.word);
       if (state == start) {
           if (!result.empty()) {
               if (path.size() < result[0].size()) {</pre>
```

10.2 Word Ladder II 279

```
result.clear();
                    result.push back(path);
                    reverse(result.back().begin(), result.back().end());
                 } else if (path.size() == result[0].size()) {
                    result.push_back(path);
                    reverse(result.back().begin(), result.back().end());
                 } else { // not possible
                    throw std::logic error("not possible to get here ");
                }
             } else {
                result.push_back(path);
                 reverse(result.back().begin(), result.back().end());
             }
         } else {
             for (const auto& f : father[state]) {
                 gen_path(father, start, f, path, result);
         path.pop_back();
     }
 };
雙隊列
 //LeetCode, Word Ladder II
 // 時間複雜度 O(n), 空間複雜度 O(n)
 class Solution {
 public:
     vector<vector<string> > findLadders(const string& start,
             const string& end, const unordered_set<string> &dict) {
         // 當前層, 下一層, 用 unordered_set 是為了去重, 例如兩個父節點指向
         // 同一個子節點,如果用 vector,子節點就會在 next 裏出現兩次,其實此
         // 時 father 已經記錄了兩個父節點, next 裏重複出現兩次是沒必要的
         unordered_set<string> current, next;
         unordered_set<string> visited; // 判重
         unordered_map<string, vector<string> > father; // DAG
         int level = -1; // 層次
         auto state_is_valid = [&](const string& s) {
             return dict.find(s) != dict.end();
         };
         auto state_is_target = [&](const string &s) {return s == end;};
         auto state_extend = [&](const string &s) {
             unordered_set<string> result;
             for (size_t i = 0; i < s.size(); ++i) {
                 string new_word(s);
                for (char c = 'a'; c <= 'z'; c++) {
                    // 防止同字母替换
                    if (c == new_word[i]) continue;
```

```
swap(c, new_word[i]);
                  if (state_is_valid(new_word) &&
                          visited.find(new_word) == visited.end()) {
                      result.insert(new_word);
                  swap(c, new_word[i]); // 恢復該單詞
               }
           }
           return result;
       };
       vector<vector<string> > result;
       current.insert(start);
       while (!current.empty()) {
           ++ level:
           // 如果當前路徑長度已經超過當前最短路徑長度, 可以中止對該路徑的
           // 處理, 因為我們要找的是最短路徑
           if (!result.empty() && level+1 > result[0].size()) break;
           // 1. 延遲加入 visited, 這樣才能允許兩個父節點指向同一個子節點
           // 2. 一股腦 current 全部加入 visited, 是防止本層前一個節點擴展
           // 節點時, 指向了本層後面尚未處理的節點, 這條路徑必然不是最短的
           for (const auto& state : current)
               visited.insert(state);
           for (const auto& state : current) {
               if (state_is_target(state)) {
                  vector<string> path;
                  gen_path(father, path, start, state, result);
                  continue;
               }
               const auto new_states = state_extend(state);
               for (const auto& new_state : new_states) {
                  next.insert(new_state);
                  father[new_state].push_back(state);
               }
           }
           current.clear();
           swap(current, next);
       }
       return result;
   }
private:
   void gen_path(unordered_map<string, vector<string> > &father,
           vector<string> &path, const string &start, const string &word,
           vector<vector<string> > &result) {
       path.push_back(word);
       if (word == start) {
```

10.2 Word Ladder II 281

```
if (!result.empty()) {
                if (path.size() < result[0].size()) {</pre>
                    result.clear();
                     result.push_back(path);
                } else if(path.size() == result[0].size()) {
                    result.push_back(path);
                } else {
                     // not possible
                    throw std::logic_error("not possible to get here");
                }
            } else {
                result.push_back(path);
            reverse(result.back().begin(), result.back().end());
        } else {
            for (const auto& f : father[word]) {
                gen_path(father, path, start, f, result);
        path.pop_back();
    }
};
```

圖的廣搜

本題還可以看做是圖上的廣搜。給定了字典 dict,可以基於它畫出一個無向圖,表示單詞之間可以互相轉換。本題的本質就是已知起點和終點,在圖上找出所有最短路徑。

```
//LeetCode, Word Ladder II
// 時間複雜度 O(n), 空間複雜度 O(n)
class Solution {
public:
   vector<vector<string> > findLadders(const string& start,
           const string &end, const unordered_set<string> &dict) {
       const auto& g = build_graph(dict);
       vector<state_t*> pool;
       queue<state_t*> q; // 未處理的節點
       // value 是所在層次
       unordered_map<string, int> visited;
       auto state_is_target = [&](const state_t *s) {return s->word == end; };
       vector<vector<string>> result;
       q.push(create_state(nullptr, start, 0, pool));
       while (!q.empty()) {
           state_t* state = q.front();
           q.pop();
           // 如果當前路徑長度已經超過當前最短路徑長度,
           // 可以中止對該路徑的處理, 因為我們要找的是最短路徑
           if (!result.empty() && state->level+1 > result[0].size()) break;
```

```
if (state_is_target(state)) {
                const auto& path = gen_path(state);
                if (result.empty()) {
                    result.push_back(path);
                } else {
                    if (path.size() < result[0].size()) {</pre>
                        result.clear();
                        result.push back(path);
                    } else if (path.size() == result[0].size()) {
                        result.push_back(path);
                    } else {
                        // not possible
                        throw std::logic_error("not possible to get here");
                }
                continue;
            }
            // 擴展節點
            auto iter = g.find(state->word);
            if (iter == g.end()) continue;
            for (const auto& neighbor : iter->second) {
                auto visited_iter = visited.find(neighbor);
                if (visited_iter != visited.end() &&
                    visited_iter->second < state->level + 1) {
                    continue;
                }
                visited[neighbor] = state->level;
                q.push(create_state(state, neighbor, state->level + 1, pool));
            }
        }
        // release all states
        for (auto state : pool) {
            delete state;
        return result;
    }
private:
    struct state_t {
        state_t* father;
        string word;
        int level; // 所在層次, 從 0 開始編號
        state_t(state_t* father_, const string& word_, int level_) :
            father(father_), word(word_), level(level_) {}
    };
    state_t* create_state(state_t* parent, const string& value,
```

10.2 Word Ladder II 283

```
int length, vector<state_t*>& pool) {
        state_t* node = new state_t(parent, value, length);
        pool.push back(node);
        return node;
    }
    vector<string> gen_path(const state_t* node) {
        vector<string> path;
        while(node != nullptr) {
            path.push_back(node->word);
            node = node->father;
        reverse(path.begin(), path.end());
        return path;
    }
    unordered_map<string, unordered_set<string> > build_graph(
            const unordered_set<string>& dict) {
        unordered_map<string, unordered_set<string> > adjacency_list;
        for (const auto& word : dict) {
            for (size_t i = 0; i < word.size(); ++i) {</pre>
                string new_word(word);
                for (char c = 'a'; c <= 'z'; c++) {
                    // 防止同字母替换
                    if (c == new_word[i]) continue;
                    swap(c, new_word[i]);
                    if ((dict.find(new_word) != dict.end())) {
                        auto iter = adjacency_list.find(word);
                        if (iter != adjacency_list.end()) {
                            iter->second.insert(new_word);
                        } else {
                            adjacency_list.insert(pair<string,
                                unordered_set<string>>(word, unordered_set<string>()));
                            adjacency_list[word].insert(new_word);
                        }
                    swap(c, new_word[i]); // 恢復該單詞
                }
            }
        }
        return adjacency_list;
    }
};
```

相關題目

• Word Ladder, 見 §10.1

10.3 Surrounded Regions

描述

Given a 2D board containing 'X' and 'O', capture all regions surrounded by 'X'.

A region is captured by flipping all 'O's into 'X's in that surrounded region .

For example,

After running your function, the board should be:

分析

廣搜。從上下左右四個邊界往裏走,凡是能碰到的'0',都是跟邊界接壤的,應該保留。

```
// LeetCode, Surrounded Regions
// BFS, 時間複雜度 O(n), 空間複雜度 O(n)
class Solution {
public:
    void solve(vector<vector<char>> &board) {
        if (board.empty()) return;
        const int m = board.size();
        const int n = board[0].size();
        for (int i = 0; i < n; i++) {
            bfs(board, 0, i);
            bfs(board, m - 1, i);
        }
        for (int j = 1; j < m - 1; j++) {
            bfs(board, j, 0);
            bfs(board, j, n - 1);
        for (int i = 0; i < m; i++)
            for (int j = 0; j < n; j++)
                if (board[i][j] == '0')
                    board[i][j] = 'X';
                else if (board[i][j] == '+')
                    board[i][j] = '0';
    }
private:
    void bfs(vector<vector<char>> &board, int i, int j) {
```

```
typedef pair<int, int> state_t;
        queue<state_t> q;
        const int m = board.size();
        const int n = board[0].size();
        auto state_is_valid = [&](const state_t &s) {
            const int x = s.first;
            const int v = s.second;
            if (x < 0 | | x >= m | | y < 0 | | y >= n | | board[x][y] != '0')
                return false;
            return true;
        };
        auto state extend = [&](const state t &s) {
            vector<state_t> result;
            const int x = s.first;
            const int y = s.second;
            // 上下左右
            const state_t new_states[4] = \{\{x-1,y\}, \{x+1,y\},
                    \{x,y-1\}, \{x,y+1\}\};
            for (int k = 0; k < 4; ++k) {
                if (state_is_valid(new_states[k])) {
                    // 既有標記功能又有去重功能
                    board[new_states[k].first][new_states[k].second] = '+';
                    result.push_back(new_states[k]);
                }
            }
            return result;
        };
        state_t start = { i, j };
        if (state_is_valid(start)) {
            board[i][j] = '+';
            q.push(start);
        while (!q.empty()) {
            auto cur = q.front();
            q.pop();
            auto new_states = state_extend(cur);
            for (auto s : new_states) q.push(s);
    }
};
```

相關題目

• 無

10.4 Walls and Gates

描述

You are given a m x n 2D grid initialized with these three possible values.

- -1 A wall or an obstacle.
- 0 A gate.
- INF Infinity means an empty room. We use the value 231 1 = 2147483647 to represent INF as you may assume that the distance to a gate is less than 2147483647.

Fill each empty room with the distance to its nearest gate. If it is impossible to reach a gate, it should be filled with INF.

Example: Given the 2D grid:

```
INF -1 0 INF
INF INF INF -1
INF -1 INF -1
0 -1 INF INF
```

After running your function, the 2D grid should be:

```
3 -1 0 1
2 2 1 -1
1 -1 2 -1
0 -1 3 4
```

BFS

```
// LeetCode
// 時間複雜度 O(n*m), 空間複雜度 O(1)
int rows[] = \{0, 0, 1, -1\};
int cols[] = \{1,-1, 0, 0\};
#define INF 2147483647
class Solution {
public:
    bool isSafe(vector<vector<int>>& rooms,int i, int j)
        if( i <0 or i>=rooms.size() or j <0 or j >= rooms[0].size() or rooms[i][j] != INF )
            return false;
        return true;
    }
    void wallsAndGates(vector<vector<int>>& rooms) {
        int r = rooms.size();
        if (r < 1) return;
        int c = rooms[0].size();
        queue<pair<int,int>> q;
        for (int i=0; i < r; i++)
            for(int j=0; j <c; j++)
                if (rooms[i][j]==0)
```

10.5 Open the Lock 287

```
q.push({i, j}); // 由每一個閘口開始

while(!q.empty())
{
    auto p = q.front(); q.pop();

    for(int d=0; d<4; d++)
    {
        int x = p.first + rows[d];
        int y = p.second + cols[d];
        if (isSafe(rooms,x,y))
        {
            rooms[x][y] = rooms[p.first][p.second] + 1;
            q.push({x,y});
        }
    }
}
```

10.5 Open the Lock

10.5.1 描述

You have a lock in front of you with 4 circular wheels. Each wheel has 10 slots: '0', '1', '2', '3', '4', '5', '6', '7', '8', '9'. The wheels can rotate freely and wrap around: for example we can turn '9' to be '0', or '0' to be '9'. Each move consists of turning one wheel one slot.

The lock initially starts at '0000', a string representing the state of the 4 wheels.

You are given a list of deadends dead ends, meaning if the lock displays any of these codes, the wheels of the lock will stop turning and you will be unable to open it.

Given a target representing the value of the wheels that will unlock the lock, return the minimum total number of turns required to open the lock, or -1 if it is impossible.

```
Example 1:

Input: deadends = ["0201","0101","0102","1212","2002"], target = "0202"

Output: 6

Explanation:
A sequence of valid moves would be "0000" -> "1000" -> "1100" -> "1200" -> "1201" -> "1202" -> Note that a sequence like "0000" -> "0001" -> "0002" -> "0102" -> "0202" would be invalid, because the wheels of the lock become stuck after the display becomes the dead end "0102".

Example 2:

Input: deadends = ["8888"], target = "0009"

Output: 1

Explanation:
We can turn the last wheel in reverse to move from "0000" -> "0009".

Example 3:

Input: deadends = ["8887","8889","8878","8898","8788","8988","7888","9888"], target = "8888"

Output: -1
```

```
Explanation:
We can't reach the target without getting stuck.
   Example 4:
Input: deadends = ["0000"], target = "8888"
Output: -1
```

- The length of deadends will be in the range [1, 500].
- target will not be in the list deadends.
- Every string in deadends and the string target will be a string of 4 digits from the 10,000 possibilities '0000' to '9999'.

10.5.2 分析

Nil

10.5.3 BFS

```
// LeetCode
// 時間複雜度 O(N^2 * A^N + D), 空間複雜度 O(A^N + D)
// D is the size of deadends, A is the number of digits in our alphabet
// N is the number of digits
class Solution {
public:
    int openLock(vector<string>& deadends, string target) {
        unordered_set<string> deadendsMap(deadends.begin(), deadends.end());
        unordered_set<string> visited;
        queue<pair<string, int>> q;
        q.push({"0000", 0});
        int level = 0;
        while (!q.empty())
            auto cur = q.front();
           q.pop();
            // 到了 dead end 處理下一個
            if (deadendsMap.find(cur.first) != deadendsMap.end()) continue;
            // 找到了答案
            if (cur.first == target) return cur.second;
            for (const auto& nextPW : GetNextPW(cur.first, visited))
                visited.insert(nextPW);
                q.push({nextPW, cur.second + 1});
            }
        }
```

10.5 Open the Lock 289

```
return -1;
     }
 private:
     const vector<int> steps{-1, 1};
     vector<string> GetNextPW(string curPW, const unordered_set<string>& visited)
     {
         vector<string> result; result.reserve(curPW.size() * 2);
         for (char& c : curPW)
             char prev = c;
             for (const auto& n : steps)
                 c = ((10 + c - '0' + n) \% 10) + '0';
                  if (visited.find(curPW) == visited.end())
                     result.push_back(curPW);
                  c = prev;
             }
         }
         return result;
     }
 };
10.5.4 Counting
 // LeetCode
 // 時間複雜度 D(), 空間複雜度 D()
 class Solution {
 public:
     int openLock(vector<string>& deadends, string target) {
         vector<int> bucket(10000, 0);
         vector<int> rotate = { 0, 1, 2, 3, 4, 5, 4, 3, 2, 1 };
         for (auto& s : deadends) {
             bucket[stoi(s)] = 1;
         if (1 == bucket[0]) return -1;
         vector<string> diffOne;
         for (int i = 0; i < 4; ++i) {
             diffOne.push_back(add(target, i, -1));
             diffOne.push_back(add(target, i, 1));
         }
         int ans = numeric_limits<int>::max();
         for (auto& s : diffOne) {
             if (0 == bucket[stoi(s)]) {
                 ans = min(ans, moves(s, rotate) + 1);
             }
```

```
}
        if (ans == numeric limits<int>::max()) ans = -1;
        return ans;
    }
private:
    string add(const string& num, int idx, int delta)
        string ans = num;
        char ch = num[idx];
        if ('0' == ch && delta == -1) {
            ans[idx] = '9';
        else if ('9' == ch && delta == 1) {
            ans[idx] = '0';
        }
        else {
            ans[idx] += delta;
        return ans;
    }
    int moves(const string& num, const vector<int>& rotate)
    {
        int ans = 0;
        for (auto c : num) {
            ans += rotate[c - '0'];
        return ans;
    }
};
```

10.6 Perfect Squares

10.6.1 描述

Given a positive integer n, find the least number of perfect square numbers (for example, 1, 4, 9, 16, ...) which sum to n.

```
Example 1:
Input: n = 12
Output: 3
Explanation: 12 = 4 + 4 + 4.

Example 2:
Input: n = 13
Output: 2
Explanation: 13 = 4 + 9.
```

10.6 Perfect Squares 291

10.6.2 暴力 - DFS - 會超時

```
// LeetCode
// 時間複雜度 0(), 空間複雜度 0()
class Solution {
public:
    int numSquares(int n) {
        m_minStep = INT_MAX;
        DFS(n, 0, 1);
        return m_minStep;
    }
private:
    int m_minStep;
    void DFS(int n, int step, int start)
        if (n == 0)
            m_minStep = min(m_minStep, step);
            return;
        else if (n < 0)
            return;
        else if (step > m_minStep)
            return;
        for (int i = start; i*i <= n; i++)
            DFS(n - (i*i), step + 1, i);
        }
    }
};
```

10.6.3 貪心法 - DFS - I

```
// LeetCode
// 時間複雜度 O(), 空間複雜度 O()
class Solution {
public:
    int numSquares(int n) {
       m_minStep = INT_MAX;
       m_N = n;
       DFS(n, 0, 1);
       return m_minStep;
   }
private:
   int m_minStep;
   int m_N;
   void DFS(int n, int step)
        if (n == 0)
           m_minStep = min(m_minStep, step);
           return;
```

```
else if (n < 0)
             return;
         else if (step > m_minStep || step > m_N)
             return;
         for (int i = (int) sqrt(n); i \ge 1; i--)
             DFS(n - (i*i), step + 1);
             if (step + 1 >= m_minStep) return; // 求得最短, 節枝
     }
 };
10.6.4 拿心法 - DFS - II
 // LeetCode
 // 時間複雜度 O(n ^h/2), 空間複雜度 O(sqrt(n))
 class Solution {
 public:
     int numSquares(int n) {
         for (int i = 1; i * i <= n; ++i)
             m_squareNums.insert(i * i);
         int count = 1;
         for (; count <= n; ++count) {</pre>
             if (isDividedBy(n, count))
                 return count;
         return count;
     }
 private:
     unordered_set<int> m_squareNums;
     bool isDividedBy(int n, int count)
     {
         if (count == 1)
             return m_squareNums.find(n) != m_squareNums.end();
         for (const int& square : m_squareNums) {
             if (isDividedBy(n - square, count - 1))
                 return true;
         return false;
     }
 };
10.6.5 貪心法 - BFS
 // LeetCode
```

// 時間複雜度 O(n ^h/2), 空間複雜度 O(sqrt(n))

```
class Solution {
public:
    int numSquares(int n) {
        unordered_set<int> squareNums;
        for (int i = 1; i * i <= n; i++)
            squareNums.insert(i*i);
        int level = 1;
        queue<int> cur, next;
        cur.push(n);
        while (!cur.empty())
            while (!cur.empty())
                auto curN = cur.front();
                cur.pop();
                for (int i = sqrt(curN); i >= 1; i--)
                    int tmpSq = i*i;
                    if (curN == tmpSq) return level; // 找到答案
                    else if (curN < tmpSq) continue; // 變成負數, 節枝
                    else
                        next.push(curN - tmpSq);
                }
            }
            swap(cur, next);
            level++;
        }
        return n;
    }
};
```

10.6.6 動規

public:

dp[0] = 0;

```
numSquares(n) = min (numSquares(n-k) + 1)
                                                      \forall k \in \{\text{square numbers}\}\
                               图 10-1 Perfect Squares
// LeetCode
// 時間複雜度 O(n*sqtr(n)), 空間複雜度 O(n)
class Solution {
    int numSquares(int n) {
        vector<int> dp(n+1, INT_MAX);
        // bottom case
```

```
// pre-calculate the square numbers.
int max_square_index = (int) sqrt(n) + 1;
vector<int> square_nums(max_square_index);

for (int i = 1; i < max_square_index; ++i) {
    square_nums[i] = i * i;
}

for (int i = 1; i <= n; ++i) {
    for (int s = 1; s < max_square_index; ++s) {
        if (i < square_nums[s])
            break;
        dp[i] = min(dp[i], dp[i - square_nums[s]] + 1);
    }
}

return dp[n];
}
</pre>
```

10.7 01 Matrix

10.7.1 描述

Given a matrix consists of 0 and 1, find the distance of the nearest 0 for each cell.

The distance between two adjacent cells is 1.

```
Example 1:
Input:
[[0,0,0],
 [0,1,0],
 [0,0,0]]
Output:
[[0,0,0],
 [0,1,0],
 [0,0,0]
  Example 2:
Input:
[[0,0,0]]
 [0,1,0],
 [1,1,1]]
Output:
[[0,0,0],
 [0,1,0]
 [1,2,1]
```

- The number of elements of the given matrix will not exceed 10,000.
- There are at least one 0 in the given matrix.
- The cells are adjacent in only four directions: up, down, left and right.

10.7 01 Matrix 295

10.7.2 分析

Nil

10.7.3 代碼

```
// LeetCode
// 時間複雜度 O(), 空間複雜度 O()
class Solution {
public:
   const vector<int> xLoc{-1, 0, 1, 0};
   const vector<int> yLoc{0, -1, 0, 1};
   vector<vector<int>> updateMatrix(vector<vector<int>>& matrix) {
        if (matrix.empty()) return vector<vector<int>>();
        // 準備 result structure
        // 記低所有 o 的位置
       // 其餘位置為 MAX
        int M = matrix.size();
        int N = matrix[0].size();
        vector<vector<int>> result(M, vector<int>(N, INT_MAX));
       for (int i = 0; i < M; i++)
           for (int j = 0; j < N; j++)
            {
                if (matrix[i][j] == 0)
                   result[i][j] = 0;
        }
        // 開始 BFS
        queue<pair<int, int>> q;
       for (int i = 0; i < M; i++)
        {
            for (int j = 0; j < N; j++)
                if (result[i][j] == 0)
                   q.push(make_pair(i,j));
        }
        while (!q.empty())
            auto loc = q.front();
           q.pop();
            // 展開
           for (int i = 0; i < 4; i++)
                int x = loc.first + xLoc[i];
                int y = loc.second + yLoc[i];
```

10.8 Keys and Rooms

10.8.1 描述

There are N rooms and you start in room 0. Each room has a distinct number in 0, 1, 2, ..., N-1, and each room may have some keys to access the next room.

Formally, each room i has a list of keys rooms[i], and each key rooms[i][j] is an integer in [0, 1, ..., N-1] where N = rooms.length. A key rooms[i][j] = v opens the room with number v.

Initially, all the rooms start locked (except for room 0).

You can walk back and forth between rooms freely.

Return true if and only if you can enter every room.

```
Example 1:
```

```
Input: [[1],[2],[3],[]]
Output: true
Explanation:
We start in room 0, and pick up key 1.
We then go to room 1, and pick up key 2.
We then go to room 2, and pick up key 3.
We then go to room 3. Since we were able to go to every room, we return true.

Example 2:
Input: [[1,3],[3,0,1],[2],[0]]
Output: false
Explanation: We can't enter the room with number 2.

• 1 <= rooms.length <= 1000</pre>
```

- 0 <= rooms[i].length <= 1000
- The number of keys in all rooms combined is at most 3000.

10.8.2 分析

Nil

10.8.3 BFS

```
// LeetCode
 // 時間複雜度 O(N+E), 空間複雜度 O(N)
 class Solution {
 public:
     bool canVisitAllRooms(vector<vector<int>>& rooms) {
         if (rooms.empty()) return true;
         int M = rooms.size();
         vector<bool> visited(M, false);
         // BFS
         queue<int> q;
         for (const auto& room : rooms.front())
             q.push(room);
         visited.front() = true;
         int totalVisited = 1;
         while (!q.empty())
             auto room = q.front();
             q.pop();
             if (visited[room] == false)
             {
                 totalVisited++;
                 if (totalVisited == M) return true;
                 visited[room] = true;
                 // 擴展
                 for (const auto& nei : rooms[room])
                     q.push(nei);
             }
         }
         return find if(visited.begin(), visited.end(), [&](const auto& e){ return !e; })
                        == visited.end();
     }
 };
10.8.4 DFS
 // LeetCode
 // 時間複雜度 O(N+E), 空間複雜度 O(N)
 class Solution {
 public:
     bool canVisitAllRooms(vector<vector<int>>& rooms) {
         if (rooms.empty()) return true;
         int M = rooms.size();
         vector<bool> visited(M, false);
```

```
// DFS
        stack<int> q; // 使用 stack, 不同於 BFS
        for (auto it = rooms.front().rbegin(); it != rooms.front().rend(); it++)
            q.push(*it);
        visited.front() = true;
        int totalVisited = 1;
        while (!q.empty())
            auto room = q.top();
            q.pop();
            if (visited[room] == false)
                totalVisited++;
                if (totalVisited == M) return true;
                visited[room] = true;
                // 擴展
                for (auto it = rooms[room].rbegin(); it != rooms[room].rend(); it++)
                    q.push(*it);
            }
        }
        return find if(visited.begin(), visited.end(), [&](const auto& e){ return !e; })
                       == visited.end();
   }
};
```

10.9 小結

10.9.1 適用場景

輸入數據:沒什麼特徵,不像深搜,需要有"遞歸"的性質。如果是樹或者圖,概率更大。

狀態轉換圖:樹或者 DAG 圖。

求解目標: 求最短。

10.9.2 思考的步驟

- 1. 是求路徑長度、還是路徑本身(或動作序列)?
 - (a) 如果是求路徑長度,則狀態裏面要存路徑長度(或雙隊列+一個全局變量)
 - (b) 如果是求路徑本身或動作序列
 - i. 要用一棵樹存儲寬搜過程中的路徑
 - ii. 是否可以預估狀態個數的上限? 能夠預估狀態總數,則開一個大數組,用樹的雙親表示法;如果不能預估狀態總數,則要使用一棵通用的樹。這一步也是第 4 步的必要不充分條件。

- 2. 如何表示狀態?即一個狀態需要存儲哪些些必要的數據,才能夠完整提供如何擴展到下一步狀態的所有信息。一般記錄當前位置或整體局面。
- 3. 如何擴展狀態? 這一步跟第2步相關。狀態裏記錄的數據不同,擴展方法就不同。對於固定不變的數據結構(一般題目直接給出,作為輸入數據),如二叉樹,圖等,擴展方法很簡單,直接往下一層走,對於隱式圖,要先在第1步裏想清楚狀態所帶的數據,想清楚了這點,那如何擴展就很簡單了。
- 4. 如何判斷重複? 如果狀態轉換圖是一顆樹, 則永遠不會出現迴路, 不需要判重; 如果狀態轉換圖是一個圖(這時候是一個圖上的 BFS), 則需要判重。
 - (a) 如果是求最短路徑長度或一條路徑,則只需要讓"點"(即狀態)不重複出現,即可保證 不出現迴路
 - (b) 如果是求所有路徑,注意此時,狀態轉換圖是 DAG,即允許兩個父節點指向同一個子節點。具體實現時,每個節點要 "延遲" 加入到已訪問集合 visited,要等一層全部訪問完後,再加入到 visited 集合。

(c) 具體實現

- i. 狀態是否存在完美哈希方案? 即將狀態——映射到整數, 互相之間不會衝突。
- ii. 如果不存在,則需要使用通用的哈希表(自己實現或用標準庫,例如 unordered_set)來判重;自己實現哈希表的話,如果能夠預估狀態個數的上限,則可以開兩個數組,head 和 next,表示哈希表,參考第 §??節方案 2。
- iii. 如果存在,則可以開一個大布爾數組,來判重,且此時可以精確計算出狀態總數,而不僅僅是預估上限。
- 5. 目標狀態是否已知?如果題目已經給出了目標狀態,可以帶來很大便利,這時候可以從起始狀態出發,正向廣搜;也可以從目標狀態出發,逆向廣搜;也可以同時出發,雙向廣搜。

10.9.3 代碼模板

廣搜需要一個隊列,用於一層一層擴展,一個 hashset,用於判重,一棵樹 (只求長度時不需要), 用於存儲整棵樹。

對於隊列,可以用 queue, 也可以把 vector 當做隊列使用。當求長度時, 有兩種做法:

- 1. 只用一個隊列,但在狀態結構體 state_t 裏增加一個整數字段 level,表示當前所在的層次,當碰到目標狀態,直接輸出 level 即可。這個方案,可以很容易的變成 A*算法,把 queue 替換為 priority queue 即可。
- 2. 用兩個隊列, current, next, 分別表示當前層次和下一層, 另設一個全局整數 level, 表示層數 (也即路徑長度), 當碰到目標狀態, 輸出 level 即可。這個方案, 狀態裏可以不存路徑長度, 只需全局設置一個整數 level, 比較節省內存;

對於 hashset,如果有完美哈希方案,用布爾數組 (bool visited[STATE_MAX]或 vector
bool>visited(STATE_MAX, false))來表示:如果沒有,可以用 STL 裏的 set 或 unordered set。

對於樹,如果用STL,可以用unordered_map<state_t, state_t > father表示一顆樹,代碼非常簡潔。如果能夠預估狀態總數的上限(設為STATE_MAX),可以用數組(state_t nodes[STATE_MAX]),即樹的雙親表示法來表示樹,效率更高,當然,需要寫更多代碼。

如何表示狀態

```
    bfs common.h

/** 狀態 */
struct state t {
   int data1; /** 狀態的數據, 可以有多個字段. */
   int data2; /** 狀態的數據, 可以有多個字段. */
   // dataN; /** 其他字段 */
   int action; /** 由父狀態移動到本狀態的動作, 求動作序列時需要. */
   int level; /** 所在的層次(從0開始), 也即路徑長度-1, 求路徑長度時需要;
                不過, 採用雙隊列時不需要本字段, 只需全局設一個整數 */
   bool operator==(const state_t &other) const {
      return true; // 根據具體問題實現
   }
};
// 定義 hash 函數
// 方法 1 : 模板特化,當 hash 函數只需要狀態本身,不需要其他數據時,用這個方法比較簡潔
namespace std {
template<> struct hash<state_t> {
   size_t operator()(const state_t & x) const {
      return 0; // 根據具體問題實現
   }
};
// 方法 2:函數對象, 如果 hash 函數需要運行時數據, 則用這種方法
class Hasher {
public:
   Hasher(int _m) : m(_m) {};
   size_t operator()(const state_t &s) const {
      return 0; // 根據具體問題實現
   }
private:
   int m; // 存放外面傳入的數據
};
/**
* Obrief 反向生成路徑, 求一條路徑.
* @param[in] father 樹
* Oparam[in] target 目標節點
* Oreturn 從起點到 target 的路徑
*/
```

10.9 小結

```
vector<state t> gen path(const unordered map<state t, state t> &father,
        const state t &target) {
    vector<state t> path;
   path.push_back(target);
    for (state_t cur = target; father.find(cur) != father.end();
            cur = father.at(cur))
        path.push back(cur);
    reverse(path.begin(), path.end());
   return path;
}
 * 反向生成路徑, 求所有路徑.
 * Oparam[in] father 存放了所有路徑的樹
 * @param[in] start 起點
 * Oparam[in] state 終點
 * @return 從起點到終點的所有路徑
void gen_path(unordered_map<state_t, vector<state_t> > &father,
        const string &start, const state_t& state, vector<state_t> &path,
        vector<vector<state_t> > &result) {
    path.push_back(state);
    if (state == start) {
        if (!result.empty()) {
            if (path.size() < result[0].size()) {</pre>
                result.clear();
                result.push_back(path);
            } else if(path.size() == result[0].size()) {
                result.push_back(path);
            } else {
                // not possible
                throw std::logic_error("not possible to get here");
            }
        } else {
           result.push_back(path);
        reverse(result.back().begin(), result.back().end());
    } else {
        for (const auto& f : father[state]) {
            gen_path(father, start, f, path, result);
   path.pop_back();
}
                                                                      bfs common.h
```

求最短路徑長度或一條路徑

單隊列的寫法

bfs_template.cpp

```
#include "bfs common.h"
/**
 * @brief 廣搜, 只用一個隊列.
 * Oparam[in] start 起點
 * @param[in] data 輸入數據
 * @return 從起點到目標狀態的一條最短路徑
 */
vector<state_t> bfs(state_t &start, const vector<vector<int>> &grid) {
   queue<state_t> q; // 隊列
   unordered set<state t> visited; // 判重
   unordered_map<state_t, state_t> father; // 樹, 求路徑本身時才需要
   // 判斷狀態是否合法
   auto state_is_valid = [&](const state_t &s) { /*...*/ };
   // 判斷當前狀態是否為所求目標
   auto state_is_target = [&](const state_t &s) { /*...*/ };
   // 擴展當前狀態
   auto state_extend = [&](const state_t &s) {
       unordered set<state t> result;
       for (/*...*/) {
           const state_t new_state = /*...*/;
           if (state_is_valid(new_state) &&
                   visited.find(new_state) != visited.end()) {
               result.insert(new_state);
           }
       }
       return result;
   };
   assert (start.level == 0);
   q.push(start);
   while (!q.empty()) {
       // 千萬不能用 const auto&, pop() 會刪除元素,
       // 引用就變成了懸空引用
       const state_t state = q.front();
       q.pop();
       visited.insert(state);
       // 訪問節點
       if (state_is_target(state)) {
           return return gen_path(father, target); // 求一條路徑
           // return state.level + 1; // 求路徑長度
       // 擴展節點
       vector<state_t> new_states = state_extend(state);
       for (const auto& new_state : new_states) {
           q.push(new_state);
```

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```
father[new state] = state; // 求一條路徑
           // visited.insert(state); // 優化:可以提前加入 visited 集合,
           // 從而縮小狀態擴展。這時 q 的含義略有變化, 裏面存放的是處理了一半
           // 的節點:已經加入了 visited, 但還沒有擴展。別忘記 while 循環開始
           // 前,要加一行代碼, visited.insert(start)
   }
   return vector<state_t>();
   //return 0:
}
                                                               bfs template.cpp
  雙隊列的寫法
                                                             bfs template1.cpp
#include "bfs_common.h"
/**
 * Obrief 廣搜, 使用兩個隊列,
 * Oparam[in] start 起點
 * Oparam[in] data 輸入數據
 * Creturn 從起點到目標狀態的一條最短路徑
 */
vector<state_t> bfs(const state_t &start, const type& data) {
   queue<state_t> next, current; // 當前層, 下一層
   unordered_set<state_t> visited; // 判重
   unordered_map<state_t, state_t> father; // 樹, 求路徑本身時才需要
   int level = -1; // 層次
   // 判斷狀態是否合法
   auto state_is_valid = [&](const state_t &s) { /*...*/ };
   // 判斷當前狀態是否為所求目標
   auto state_is_target = [&](const state_t &s) { /*...*/ };
   // 擴展當前狀態
   auto state_extend = [&](const state_t &s) {
       unordered_set<state_t> result;
       for (/*...*/) {
           const state_t new_state = /*...*/;
           if (state_is_valid(new_state) &&
                  visited.find(new_state) != visited.end()) {
              result.insert(new_state);
           }
       return result;
   };
   current.push(start);
   while (!current.empty()) {
       ++level;
       while (!current.empty()) {
```

```
// 千萬不能用 const auto&, pop() 會刪除元素,
          // 引用就變成了懸空引用
          const auto state = current.front();
           current.pop();
          visited.insert(state);
           if (state_is_target(state)) {
              return return gen path(father, state); // 求一條路徑
              // return state.level + 1; // 求路徑長度
          }
          const auto& new_states = state_extend(state);
          for (const auto& new state : new states) {
              next.push(new_state);
              father[new_state] = state;
              // visited.insert(state); // 優化:可以提前加入 visited 集合.
              // 從而縮小狀態擴展。這時 current 的含義略有變化, 裏面存放的是處
              // 理了一半的節點:已經加入了 visited, 但還沒有擴展。別忘記 while
              // 循環開始前, 要加一行代碼, visited.insert(start)
          }
       }
       swap(next, current); //!!! 交換兩個隊列
   }
   return vector<state_t>();
   // return 0;
}
                                                            bfs template1.cpp
```

求所有路徑

單隊列

```
bfs_template.cpp
/**
* @brief 廣搜, 使用一個隊列.
* @param[in] start 起點
* Oparam[in] data 輸入數據
* Creturn 從起點到目標狀態的所有最短路徑
*/
vector<vector<state_t> > bfs(const state_t &start, const type& data) {
   queue<state_t> q;
   unordered_set<state_t> visited; // 判重
   unordered_map<state_t, vector<state_t> > father; // DAG
   auto state_is_valid = [&](const state_t& s) { /*...*/ };
   auto state_is_target = [&](const state_t &s) { /*...*/ };
   auto state_extend = [&](const state_t &s) {
       unordered set<state t> result;
       for (/*...*/) {
           const state t new state = /*...*/;
           if (state_is_valid(new_state)) {
```

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```
auto visited iter = visited.find(new state);
           if (visited iter != visited.end()) {
               if (visited_iter->level < new_state.level) {</pre>
                   // do nothing
               } else if (visited_iter->level == new_state.level) {
                  result.insert(new state);
               } else { // not possible
                  throw std::logic_error("not possible to get here");
               }
           } else {
               result.insert(new_state);
       }
   }
   return result;
}:
vector<vector<string>> result;
state_t start_state(start, 0);
q.push(start_state);
visited.insert(start_state);
while (!q.empty()) {
   // 千萬不能用 const auto&, pop() 會刪除元素,
   // 引用就變成了懸空引用
   const auto state = q.front();
   q.pop();
   // 如果當前路徑長度已經超過當前最短路徑長度,
   // 可以中止對該路徑的處理. 因為我們要找的是最短路徑
   if (!result.empty() && state.level + 1 > result[0].size()) break;
    if (state_is_target(state)) {
       vector<string> path;
       gen_path(father, start_state, state, path, result);
       continue;
   }
   // 必須挪到下面, 比如同一層 A和 B兩個節點均指向了目標節點,
   // 那麼目標節點就會在 q 中出現兩次, 輸出路徑就會翻倍
   // visited.insert(state);
   // 擴展節點
   const auto& new_states = state_extend(state);
   for (const auto& new_state : new_states) {
       if (visited.find(new_state) == visited.end()) {
           q.push(new_state);
       visited.insert(new_state);
       father[new_state].push_back(state);
   }
}
```

```
return result;
}

    bfs template.cpp

  雙隊列的寫法
                                                              bfs_template.cpp
#include "bfs_common.h"
/**
 * @brief 廣搜, 使用兩個隊列,
 * Oparam[in] start 起點
 * @param[in] data 輸入數據
 * @return 從起點到目標狀態的所有最短路徑
vector<vector<state t> > bfs(const state t &start, const type& data) {
   // 當前層, 下一層, 用 unordered_set 是為了去重, 例如兩個父節點指向
   // 同一個子節點,如果用 vector,子節點就會在 next 裏出現兩次,其實此
   // 時 father 已經記錄了兩個父節點, next 裏重複出現兩次是沒必要的
   unordered_set<string> current, next;
   unordered_set<state_t> visited; // 判重
   unordered_map<state_t, vector<state_t> > father; // DAG
   int level = -1; // 層次
   // 判斷狀態是否合法
   auto state_is_valid = [&](const state_t &s) { /*...*/ };
   // 判斷當前狀態是否為所求目標
   auto state_is_target = [&](const state_t &s) { /*...*/ };
   // 擴展當前狀態
   auto state_extend = [&](const state_t &s) {
       unordered_set<state_t> result;
       for (/*...*/) {
          const state_t new_state = /*...*/;
          if (state_is_valid(new_state) &&
                  visited.find(new_state) != visited.end()) {
              result.insert(new_state);
          }
       }
       return result;
   };
   vector<vector<state_t> > result;
   current.insert(start):
   while (!current.empty()) {
       ++ level;
       // 如果當前路徑長度已經超過當前最短路徑長度, 可以中止對該路徑的
       // 處理, 因為我們要找的是最短路徑
       if (!result.empty() && level+1 > result[0].size()) break;
```

// 1. 延遲加入 visited, 這樣才能允許兩個父節點指向同一個子節點 // 2. 一股腦 current 全部加入 visited, 是防止本層前一個節點擴展 10.9 小結 307

```
// 節點時, 指向了本層後面尚未處理的節點, 這條路徑必然不是最短的
       for (const auto& state : current)
           visited.insert(state);
       for (const auto& state : current) {
           if (state_is_target(state)) {
               vector<string> path;
               gen_path(father, path, start, state, result);
               continue;
           }
           const auto new_states = state_extend(state);
           for (const auto& new_state : new_states) {
               next.insert(new_state);
               father[new_state].push_back(state);
           }
       }
       current.clear();
       swap(current, next);
   }
   return result;
}
```

bfs_template.cpp

第 11 章 深度優先搜索

11.1 Palindrome Partitioning

描述

Given a string s, partition s such that every substring of the partition is a palindrome.

Return all possible palindrome partitioning of s.

```
For example, given s = "aab", Return
[
    ["aa","b"],
    ["a","a","b"]
]
```

分析

在每一步都可以判斷中間結果是否為合法結果、用回溯法。

一個長度為n的字符串,有n-1個地方可以砍斷,每個地方可斷可不斷,因此複雜度為 $O(2^{n-1})$

深搜1

```
//LeetCode, Palindrome Partitioning
// 時間複雜度 O(2<sup>n</sup>), 空間複雜度 O(n)
class Solution {
public:
    vector<vector<string>> partition(string s) {
       vector<vector<string>> result;
       vector<string> path; // 一個 partition 方案
       dfs(s, path, result, 0, 1);
       return result;
    }
    // prev 表示前一個隔板, start 表示當前隔板
    void dfs(string &s, vector<string>& path,
           vector<vector<string>> &result, size_t prev, size_t start) {
       if (start == s.size()) { // 最後一個隔板
           if (isPalindrome(s, prev, start - 1)) { // 必須使用
               path.push_back(s.substr(prev, start - prev));
```

```
result.push back(path);
                 path.pop_back();
             }
             return;
         // 不斷開
         dfs(s, path, result, prev, start + 1);
         // 如果 [prev, start-1] 是迴文, 則可以斷開, 也可以不斷開(上一行已經做了)
         if (isPalindrome(s, prev, start - 1)) {
             // 斷開
             path.push_back(s.substr(prev, start - prev));
             dfs(s, path, result, start, start + 1);
             path.pop_back();
         }
     }
     bool isPalindrome(const string &s, int start, int end) {
         while (start < end && s[start] == s[end]) {
             ++start;
             --end:
         }
         return start >= end;
     }
 };
深搜 2
   另一種寫法,更加簡潔。這種寫法也在 Combination Sum, Combination Sum II 中出現過。
 //LeetCode, Palindrome Partitioning
 // 時間複雜度 O(2<sup>n</sup>), 空間複雜度 O(n)
 class Solution {
 public:
     vector<vector<string>> partition(string s) {
         vector<vector<string>> result;
         vector<string> path; // 一個 partition 方案
         DFS(s, path, result, 0);
         return result;
     }
     // 搜索必須以 s[start] 開頭的 partition 方案
     void DFS(string &s, vector<string>& path,
             vector<vector<string>> &result, int start) {
         if (start == s.size()) {
             result.push_back(path);
             return;
         for (int i = start; i < s.size(); i++) {</pre>
             if (isPalindrome(s, start, i)) { // 從i位置砍一刀
                 path.push_back(s.substr(start, i - start + 1));
                 DFS(s, path, result, i + 1); // 繼續往下砍
                 path.pop_back(); // 撤銷上上行
             }
```

```
}
}
bool isPalindrome(const string &s, int start, int end) {
    while (start < end && s[start] == s[end]) {
        ++start;
        --end;
    }
    return start >= end;
}
```

Example	abcbm										
								sub_palins			
			0	1	2	3	4		n		
		(т	F	F	F	F		0	abcbm	a .bcb .m
		١,		т	F	т	F		1	bcbm	bcb .m
		2	2	Ė	T	_	F		_	cbm	
		3	3			Т	F		3	bm	
		4	1				Т		4	m	

图 11-1 example

動規

```
// LeetCode, Palindrome Partitioning
// 動規, 時間複雜度 O(n^2), 空間複雜度 O(1)
class Solution {
public:
    vector<vector<string> > partition(string s) {
        const int n = s.size();
        bool p[n][n]; // whether s[i,j] is palindrome
        fill_n(&p[0][0], n * n, false);
        for (int i = n - 1; i \ge 0; --i)
            for (int j = i; j < n; ++j)
                p[i][j] = s[i] == s[j] \&\& ((j - i < 2) || p[i + 1][j - 1]);
        vector<vector<string> > sub_palins[n]; // sub palindromes of s[i,n]
        for (int i = n - 1; i \ge 0; --i) {
            for (int j = i; j < n; ++j)
                if (p[i][j]) {
                    const string palindrome = s.substr(i, j - i + 1);
                    if (j + 1 < n) {
                        for (auto v : sub_palins[j + 1]) {
                            v.insert(v.begin(), palindrome);
                            sub_palins[i].push_back(v);
                        }
                    } else {
                        sub_palins[i].push_back(vector<string> { palindrome });
                }
        }
```

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```
return sub_palins[0];
};
```

相關題目

• Palindrome Partitioning II, 見 §14.5

11.2 Unique Paths

描述

A robot is located at the top-left corner of a $m \times n$ grid (marked 'Start' in the diagram below).

The robot can only move either down or right at any point in time. The robot is trying to reach the bottom-right corner of the grid (marked 'Finish' in the diagram below).

How many possible unique paths are there?



 \boxtimes 11-2 Above is a 3×7 grid. How many possible unique paths are there?

Note: m and n will be at most 100.

11.2.1 深搜

深搜, 小集合可以過, 大集合會超時

```
// LeetCode, Unique Paths
// 深搜, 小集合可以過, 大集合會超時
// 時間複雜度 O(n^4), 空間複雜度 O(n)
class Solution {
public:
    int uniquePaths(int m, int n) {
        if (m < 1 || n < 1) return 0; // 終止條件
        if (m == 1 && n == 1) return 1; // 收斂條件
        return uniquePaths(m - 1, n) + uniquePaths(m, n - 1);
    }
};</pre>
```

11.2.2 備忘錄法

給前面的深搜,加個緩存,就可以過大集合了。即備忘錄法。

代碼

```
// LeetCode, Unique Paths
// 深搜 + 緩存, 即備忘錄法
// 時間複雜度 O(n^2), 空間複雜度 O(n^2)
class Solution {
public:
   int uniquePaths(int m, int n) {
       // f[x][y] 表示 從(0,0)到(x,y)的路徑條數
       f = vector<vector<int> >(m, vector<int>(n, 0));
       f[0][0] = 1;
       return dfs(m-1, n-1);
   }
private:
   vector<vector<int> > f; // 緩存
   int dfs(int x, int y) {
       if (x < 0 || y < 0) return 0; // 數據非法, 終止條件
       if (x == 0 && y == 0) return f[0][0]; // 回到起點, 收斂條件
       if (f[x][y] > 0) {
           return f[x][y];
           return f[x][y] = dfs(x - 1, y) + dfs(x, y - 1);
       }
   }
};
```

11.2.3 動規

既然可以用備忘錄法自頂向下解決,也一定可以用動規自底向上解決。 設狀態為 $\mathbf{f[i]}[j]$,表示從起點 (1,1) 到達 (i,j) 的路線條數,則狀態轉移方程為:

```
f[i][j]=f[i-1][j]+f[i][j-1]
```

```
// LeetCode, Unique Paths
// 動規, 滾動數組
// 時間複雜度 O(n^2), 空間複雜度 O(n)
class Solution {
public:
    int uniquePaths(int m, int n) {
        vector<int> f(n, 0);
        f[0] = 1;
```

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```
for (int i = 0; i < m; i++) {
    for (int j = 1; j < n; j++) {
        // 左邊的 f[j], 表示更新後的 f[j], 與公式中的 f[i][j] 對應
        // 右邊的 f[j], 表示老的 f[j], 與公式中的 f[i-1][j] 對應
        f[j] = f[j] + f[j - 1];
    }
}
return f[n - 1];
}
```

11.2.4 數學公式

一個 m 行,n 列的矩陣,機器人從左上走到右下總共需要的步數是 m+n-2,其中向下走的步數是 m-1,因此問題變成了在 m+n-2 個操作中,選擇 m-1 個時間點向下走,選擇方式有多少種。即 C_{m+n-2}^{m-1} 。

```
// LeetCode, Unique Paths
// 數學公式
class Solution {
public:
    typedef long long int64_t;
    // 求階乘, n!/(start-1)!, 即 n*(n-1)...start, 要求 n >= 1
    static int64_t factor(int n, int start = 1) {
       int64 t ret = 1;
       for(int i = start; i \le n; ++i)
           ret *= i;
       return ret;
   // 求組合數 C_n^k
    static int64_t combination(int n, int k) {
       // 常數優化
       if (k == 0) return 1;
       if (k == 1) return n;
       int64_t ret = factor(n, k+1);
       ret /= factor(n - k);
       return ret;
   }
    int uniquePaths(int m, int n) {
       // max 可以防止n和k差距過大,從而防止 combination()溢出
       return combination(m+n-2, max(m-1, n-1));
    }
};
```

相關題目

- Unique Paths II, 見 §11.3
- Minimum Path Sum, 見 §14.10

11.3 Unique Paths II

描述

Follow up for "Unique Paths":

Now consider if some obstacles are added to the grids. How many unique paths would there be?

An obstacle and empty space is marked as 1 and 0 respectively in the grid.

For example,

There is one obstacle in the middle of a 3×3 grid as illustrated below.

```
[0,0,0],
[0,1,0],
[0,0,0]
```

The total number of unique paths is 2.

Note: m and n will be at most 100.

11.3.1 備忘錄法

在上一題的基礎上改一下即可。相比動規,簡單得多。

代碼

٦

```
// LeetCode, Unique Paths II
// 深搜 + 緩存, 即備忘錄法
class Solution {
public:
    int uniquePathsWithObstacles(const vector<vector<int> >& obstacleGrid) {
        const int m = obstacleGrid.size();
        const int n = obstacleGrid[0].size();
        if (obstacleGrid[0][0] || obstacleGrid[m - 1][n - 1]) return 0;
        f = vector<vector<int> >(m, vector<int>(n, 0));
        f[0][0] = obstacleGrid[0][0] ? 0 : 1;
        return dfs(obstacleGrid, m - 1, n - 1);
    }
private:
   vector<vector<int> > f; // 緩存
    // Creturn 從 (0, 0) 到 (x, y) 的路徑總數
    int dfs(const vector<vector<int> >& obstacleGrid,
           int x, int y) {
```

11.3.2 動規

與上一題類似,但要特別注意第一列的障礙。在上一題中,第一列全部是1,但是在這一題中不同,第一列如果某一行有障礙物,那麼後面的行全為0。

代碼

```
// LeetCode, Unique Paths II
// 動規, 滾動數組
// 時間複雜度 O(n^2), 空間複雜度 O(n)
class Solution {
public:
    int uniquePathsWithObstacles(vector<vector<int> > &obstacleGrid) {
        const int m = obstacleGrid.size();
        const int n = obstacleGrid[0].size();
        if (obstacleGrid[0][0] || obstacleGrid[m-1][n-1]) return 0;
        vector<int> f(n, 0);
        f[0] = obstacleGrid[0][0] ? 0 : 1;
        for (int i = 0; i < m; i++) {
            f[0] = f[0] == 0 ? 0 : (obstacleGrid[i][0] ? 0 : 1);
            for (int j = 1; j < n; j++)
                f[j] = obstacleGrid[i][j] ? 0 : (f[j] + f[j - 1]);
        }
       return f[n - 1];
   }
};
```

相關題目

- Unique Paths, 見 §11.2
- Minimum Path Sum, 見 §14.10

11.4 N-Queens

描述

The <u>n</u>-queens <u>puzzle</u> is the problem of placing n queens on an $n \times n$ chessboard such that no two queens attack each other.

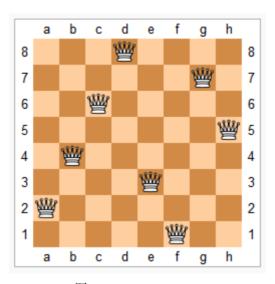


图 11-3 Eight Queens

Given an integer n, return all distinct solutions to the n-queens puzzle.

Each solution contains a distinct board configuration of the n-queens' placement, where 'Q' and '.' both indicate a queen and an empty space respectively.

For example, There exist two distinct solutions to the 4-queens puzzle:

```
[
[".Q..", // Solution 1
"...Q",
"Q...",
"..Q."],

["..Q.", // Solution 2
"Q...",
"...Q",
"...Q",
".Q.."]
]
```

分析

經典的深搜題。

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設置一個數組 vector<int> C(n, 0), C[i] 表示第 i 行皇后所在的列編號,即在位置 (i, C[i]) 上放了一個皇后,這樣用一個一維數組,就能記錄整個棋盤。

```
// LeetCode, N-Queens
// 深搜+剪枝
// 時間複雜度 O(n!*n), 空間複雜度 O(n)
class Solution {
public:
   vector<vector<string> > solveNQueens(int n) {
       vector<vector<string> > result;
       vector<int> C(n, -1); // C[i] 表示第 i 行皇后所在的列編號
       dfs(C, result, 0);
       return result;
   }
private:
   void dfs(vector<int> &C. vector<vector<string> > &result. int row) {
       const int N = C.size();
       if (row == N) { // 終止條件, 也是收斂條件, 意味着找到了一個可行解
           vector<string> solution;
           for (int i = 0; i < N; ++i) {
              string s(N, '.');
              for (int j = 0; j < N; ++j) {
                  if (i == C[i]) s[i] = 'Q';
              solution.push_back(s);
           }
           result.push back(solution);
          return;
       for (int j = 0; j < N; ++j) { // 擴展狀態, 一列一列的試
           const bool ok = isValid(C, row, j);
           if (!ok) continue; // 剪枝, 如果非法, 繼續嘗試下一列
           // 執行擴展動作
           C[row] = j;
           dfs(C, result, row + 1);
           // 撤銷動作
           // C[row] = -1;
       }
   }
    * 能否在 (row, col) 位置放一個皇后.
    * Oparam C 棋局
    * Oparam row 當前正在處理的行,前面的行都已經放了皇后了
    * Oparam col 當前列
    * @return 能否放一個皇后
    */
   bool isValid(const vector<int> &C, int row, int col) {
```

```
for (int i = 0; i < row; ++i) {
            // 在同一列
            if (C[i] == col) return false;
            // 在同一對角線上
            if (abs(i - row) == abs(C[i] - col)) return false;
        return true;
     }
 };
代碼 2
 // LeetCode, N-Queens
 // 深搜+剪枝
 // 時間複雜度 O(n!), 空間複雜度 O(n)
 class Solution {
 public:
     vector<vector<string> > solveNQueens(int n) {
         this->columns = vector<bool>(n, false);
         this->main_diag = vector<bool>(2 * n - 1, false);
         this->anti_diag = vector<bool>(2 * n - 1, false);
         vector<vector<string> > result;
         vector<int> C(n, -1); // C[i] 表示第 i 行皇后所在的列編號
         dfs(C, result, 0);
         return result;
     }
 private:
     // 這三個變量用於剪枝
     vector<bool> columns; // 表示已經放置的皇后佔據了哪些列
     vector<bool> main_diag; // 佔據了哪些主對角線
     vector<bool> anti_diag; // 佔據了哪些副對角線
     void dfs(vector<int> &C, vector<vector<string> > &result, int row) {
         const int N = C.size();
         if (row == N) { // 終止條件, 也是收斂條件, 意味着找到了一個可行解
            vector<string> solution;
            for (int i = 0; i < N; ++i) {
                string s(N, '.');
                for (int j = 0; j < N; ++j) {
                    if (j == C[i]) s[j] = 'Q';
                solution.push_back(s);
            }
            result.push_back(solution);
            return;
         for (int j = 0; j < N; ++j) { // 擴展狀態, 一列一列的試
            const bool ok = !columns[j] && !main_diag[row - j + N - 1] &&
                    !anti_diag[row + j];
            if (!ok) continue; // 剪枝, 如果非法, 繼續嘗試下一列
```

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相關題目

• N-Queens II, 見 §11.5

11.5 N-Queens II

描述

Follow up for N-Queens problem.

Now, instead outputting board configurations, return the total number of distinct solutions.

分析

只需要輸出解的個數,不需要輸出所有解,代碼要比上一題簡化很多。設一個全局計數器,每 找到一個解就增1。

```
// LeetCode, N-Queens II
// 深搜+剪枝
// 時間複雜度 O(n!*n), 空間複雜度 O(n)
class Solution {
public:
   int totalNQueens(int n) {
       this->count = 0;
       vector<int> C(n, 0); // C[i] 表示第 i 行皇后所在的列編號
       dfs(C, 0);
       return this->count;
   }
private:
   int count; // 解的個數
   void dfs(vector<int> &C, int row) {
       const int N = C.size();
       if (row == N) { // 終止條件, 也是收斂條件, 意味着找到了一個可行解
          ++this->count;
          return;
       }
```

```
for (int j = 0; j < N; ++j) { // 擴展狀態, 一列一列的試
            const bool ok = isValid(C, row, j);
            if (!ok) continue; // 剪枝:如果合法, 繼續遞歸
            // 執行擴展動作
            C[row] = j;
            dfs(C, row + 1);
            // 撤銷動作
            // C[row] = -1;
        }
     }
     /**
      * 能否在 (row, col) 位置放一個皇后.
      * @param C 棋局
      * Oparam row 當前正在處理的行, 前面的行都已經放了皇后了
      * Oparam col 當前列
      * @return 能否放一個皇后
      */
     bool isValid(const vector<int> &C, int row, int col) {
        for (int i = 0; i < row; ++i) {
            // 在同一列
            if (C[i] == col) return false;
            // 在同一對角線上
            if (abs(i - row) == abs(C[i] - col)) return false;
        }
        return true;
     }
 };
代碼 2
 // LeetCode, N-Queens II
 // 深搜+剪枝
 // 時間複雜度 O(n!), 空間複雜度 O(n)
 class Solution {
 public:
     int totalNQueens(int n) {
        this->count = 0;
        this->columns = vector<bool>(n, false);
        this->main_diag = vector<bool>(2 * n - 1, false);
        this->anti_diag = vector<bool>(2 * n - 1, false);
        vector<int> C(n, 0); // C[i] 表示第 i 行皇后所在的列編號
        dfs(C, 0);
        return this->count;
     }
 private:
     int count; // 解的個數
     // 這三個變量用於剪枝
     vector<bool> columns; // 表示已經放置的皇后佔據了哪些列
     vector<bool> main_diag; // 佔據了哪些主對角線
```

11.6 Restore IP Addresses 321

```
vector<bool> anti diag; // 佔據了哪些副對角線
   void dfs(vector<int> &C, int row) {
       const int N = C.size();
       if (row == N) { // 終止條件, 也是收斂條件, 意味着找到了一個可行解
           ++this->count;
           return;
       }
       for (int j = 0; j < N; ++j) { // 擴展狀態, 一列一列的試
           const bool ok = !columns[j] &&
                  !main_diag[row - j + N] &&
                  !anti_diag[row + j];
           if (!ok) continue; // 剪枝:如果合法, 繼續遞歸
           // 執行擴展動作
           C[row] = j;
           columns[j] = main_diag[row - j + N] =
                  anti_diag[row + j] = true;
           dfs(C, row + 1);
           // 撤銷動作
           // C[row] = -1;
           columns[j] = main_diag[row - j + N] =
                  anti_diag[row + j] = false;
       }
   }
};
```

相關題目

• N-Queens, 見 §11.4

11.6 Restore IP Addresses

描述

Given a string containing only digits, restore it by returning all possible valid IP address combinations. For example: Given "25525511135", return

"255.255.11.135", "255.255.111.35"

. (Order does not matter)

分析

必須要走到底部才能判斷解是否合法、深搜。

```
// LeetCode, Restore IP Addresses
// 時間複雜度 O(n^4), 空間複雜度 O(n)
```

```
class Solution {
public:
    vector<string> restoreIpAddresses(const string& s) {
       vector<string> result;
       vector<string> ip; // 存放中間結果
       dfs(s, ip, result, 0);
       return result;
    }
    /**
    * @brief 解析字符串
    * Oparam[in] s 字符串, 輸入數據
    * @param[out] ip 存放中間結果
    * @param[out] result 存放所有可能的 IP 地址
     * @param[in] start 當前正在處理的 index
     * @return 無
    */
    void dfs(string s, vector<string>& ip, vector<string> &result,
           size_t start) {
       if (ip.size() == 4 && start == s.size()) { // 找到一個合法解
           result.push_back(ip[0] + '.' + ip[1] + '.' + ip[2] + '.' + ip[3]);
           return;
       if (s.size() - start > (4 - ip.size()) * 3)
           return; // 剪枝
       if (s.size() - start < (4 - ip.size()))</pre>
           return; // 剪枝
        int num = 0;
       for (size_t i = start; i < start + 3; i++) {</pre>
           num = num * 10 + (s[i] - '0');
           if (num < 0 || num > 255) continue; // 剪枝
           ip.push_back(s.substr(start, i - start + 1));
           dfs(s, ip, result, i + 1);
           ip.pop_back();
           if (num == 0) break; // 不允許前綴 0, 但允許單個 0
       }
   }
};
```

無

11.7 Combination Sum 323

11.7 Combination Sum

描述

Given a set of candidate numbers (C) and a target number (T), find all unique combinations in C where the candidate numbers sums to T.

The same repeated number may be chosen from C unlimited number of times.

Note:

- All numbers (including target) will be positive integers.
- Elements in a combination $(a_1, a_2, ..., a_k)$ must be in non-descending order. (ie, $a_1 \le a_2 \le ... \le a_k$).
- The solution set must not contain duplicate combinations.

For example, given candidate set 2,3,6,7 and target 7, A solution set is:

```
[7] [2, 2, 3]
```

分析

無

```
// LeetCode, Combination Sum
// 時間複雜度 O(n!), 空間複雜度 O(n)
class Solution {
public:
    vector<vector<int> > combinationSum(vector<int> &nums, int target) {
       sort(nums.begin(), nums.end());
       vector<vector<int> > result; // 最終結果
       vector<int> path; // 中間結果
       dfs(nums, path, result, target, 0);
       return result;
    }
private:
    void dfs(vector<int>& nums, vector<int>& path, vector<vector<int> > &result,
           int gap, int start) {
        if (gap == 0) { // 找到一個合法解
           result.push_back(path);
           return;
       for (size_t i = start; i < nums.size(); i++) { // 擴展狀態
           if (gap < nums[i]) return; // 剪枝
           path.push_back(nums[i]); // 執行擴展動作
           dfs(nums, path, result, gap - nums[i], i);
           path.pop_back(); // 撤銷動作
```

```
}
};
```

• Combination Sum II , 見 §11.8

11.8 Combination Sum II

描述

Given a collection of candidate numbers (C) and a target number (T), find all unique combinations in C where the candidate numbers sums to T.

Each number in C may only be used once in the combination.

Note:

- All numbers (including target) will be positive integers.
- Elements in a combination $(a_1, a_2, ..., a_k)$ must be in non-descending order. (ie, $a_1 > a_2 > ... > a_k$).
- The solution set must not contain duplicate combinations.

For example, given candidate set 10,1,2,7,6,1,5 and target 8, A solution set is:

```
[1, 7]
[1, 2, 5]
[2, 6]
[1, 1, 6]
```

分析

無

```
vector<vector<int> > &result, int gap, int start) {
       if (gap == 0) { // 找到一個合法解
           result.push_back(path);
           return:
       }
       int previous = -1;
       for (size_t i = start; i < nums.size(); i++) {</pre>
           // 如果上一輪循環已經使用了 nums[i], 則本次循環就不能再選 nums[i],
           // 確保 nums[i] 最多隻用一次
           if (previous == nums[i]) continue;
           if (gap < nums[i]) return; // 剪枝
           previous = nums[i];
           path.push_back(nums[i]);
           dfs(nums, path, result, gap - nums[i], i + 1);
           path.pop_back(); // 恢復環境
       }
   }
};
```

• Combination Sum , 見 §11.7

11.9 Generate Parentheses

描述

Given n pairs of parentheses, write a function to generate all combinations of well-formed parentheses. For example, given n=3, a solution set is:

```
"((()))", "(()())", "(())()", "()(())", "()()()"
```

分析

小括號串是一個遞歸結構,跟單鏈表、二叉樹等遞歸結構一樣,首先想到用遞歸。

一步步構造字符串。當左括號出現次數 < n 時,就可以放置新的左括號。當右括號出現次數小於左括號出現次數時,就可以放置新的右括號。

```
// LeetCode, Generate Parentheses
// 時間複雜度 O(TODO), 空間複雜度 O(n)
class Solution {
public:
    vector<string> generateParenthesis(int n) {
    vector<string> result;
```

```
string path;
         if (n > 0) generate(n, path, result, 0, 0);
         return result;
     // 1 表示 ( 出現的次數, r 表示 ) 出現的次數
     void generate(int n, string& path, vector<string> &result, int l, int r) {
         if (1 == n) {
             string s(path);
             result.push_back(s.append(n - r, ')'));
             return;
         }
         path.push_back('(');
         generate(n, path, result, l + 1, r);
         path.pop_back();
         if (1 > r) {
             path.push_back(')');
             generate(n, path, result, 1, r + 1);
             path.pop_back();
         }
     }
 };
代碼 2
   另一種遞歸寫法, 更加簡潔。
 // LeetCode, Generate Parentheses
 // Cauthor 連城 (http://weibo.com/lianchengzju)
 class Solution {
 public:
     vector<string> generateParenthesis (int n) {
         if (n == 0) return vector<string>(1, "");
         if (n == 1) return vector<string> (1, "()");
         vector<string> result;
         for (int i = 0; i < n; ++i)
             for (auto inner : generateParenthesis (i))
                 for (auto outer : generateParenthesis (n - 1 - i))
                     result.push_back ("(" + inner + ")" + outer);
         return result;
     }
 };
```

- Valid Parentheses, 見 §5.1.1
- Longest Valid Parentheses, 見 §5.1.2

11.10 Sudoku Solver 327

11.10 Sudoku Solver

描述

Write a program to solve a Sudoku puzzle by filling the empty cells.

Empty cells are indicated by the character '.'.

You may assume that there will be only one unique solution.

5	3			7				
6			1	9	5			
	9	8					6	
8				6				3
4			8		3			1
7				2				6
	6					2	8	
			4	1	9			5
				8			7	9

图 11-4 A sudoku puzzle...



图 11-5 ...and its solution numbers marked in red

分析

代碼

```
// LeetCode, Sudoku Solver
// 時間複雜度 O(9<sup>4</sup>), 空間複雜度 O(1)
class Solution {
public:
    bool solveSudoku(vector<vector<char> > &board) {
        for (int i = 0; i < 9; ++i)
            for (int j = 0; j < 9; ++j) {
                if (board[i][j] == '.') {
                    for (int k = 0; k < 9; ++k) {
                        board[i][j] = '1' + k;
                        if (isValid(board, i, j) && solveSudoku(board))
                            return true;
                        board[i][j] = '.';
                    return false;
                }
            }
        return true;
    }
private:
    // 檢查 (x, y) 是否合法
    bool isValid(const vector<vector<char> > &board, int x, int y) {
        int i, j;
        for (i = 0; i < 9; i++) // 檢查 y 列
            if (i != x && board[i][y] == board[x][y])
                return false;
        for (j = 0; j < 9; j++) // 檢查 x 行
            if (j != y && board[x][j] == board[x][y])
                return false;
        for (i = 3 * (x / 3); i < 3 * (x / 3 + 1); i++)
            for (j = 3 * (y / 3); j < 3 * (y / 3 + 1); j++)
                if ((i != x || j != y) && board[i][j] == board[x][y])
                    return false;
        return true;
    }
};
```

相關題目

• Valid Sudoku, 見 §2.1.17

11.11 Word Search

描述

Given a 2D board and a word, find if the word exists in the grid.

The word can be constructed from letters of sequentially adjacent cell, where "adjacent" cells are those horizontally or vertically neighbouring. The same letter cell may not be used more than once.

For example, Given board =

11.11 Word Search 329

```
Γ
    ["ABCE"],
    ["SFCS"],
    ["ADEE"]
 ٦
word = "ABCCED", -> returns true,
word = "SEE", -> returns true,
word = "ABCB", -> returns false.
分析
    無。
代碼
 // LeetCode, Word Search
 // 深搜, 遞歸
 // 時間複雜度 O(n^2*m^2), 空間複雜度 O(n^2)
 class Solution {
 public:
     bool exist(const vector<vector<char> > &board, const string& word) {
         const int m = board.size();
         const int n = board[0].size();
         vector<vector<bool> > visited(m, vector<bool>(n, false));
         for (int i = 0; i < m; ++i)
             for (int j = 0; j < n; ++j)
                  if (dfs(board, word, 0, i, j, visited))
                     return true:
         return false;
     }
 private:
     static bool dfs(const vector<vector<char> > &board, const string &word,
             int index, int x, int y, vector<vector<bool> > &visited) {
         if (index == word.size())
             return true; // 收斂條件
         if (x < 0 || y < 0 || x >= board.size() || y >= board[0].size())
             return false: // 越界, 終止條件
         if (visited[x][y]) return false; // 已經訪問過, 剪枝
         if (board[x][y] != word[index]) return false; // 不相等, 剪枝
         visited[x][y] = true;
         bool ret = dfs(board, word, index + 1, x - 1, y, visited) | | // 上
                 dfs(board, word, index + 1, x + 1, y, visited)
                                                                    11 // 下
                 dfs(board, word, index + 1, x, y - 1, visited)
                                                                    11 // 左
                 dfs(board, word, index + 1, x, y + 1, visited);
                                                                      // 右
         visited[x][y] = false;
         return ret;
```

};

相關題目

• 無

11.12 Optimal Account Balancing

描述

A group of friends went on holiday and sometimes lent each other money. For example, Alice paid for Bill's lunch for \$10. Then later Chris gave Alice \$5 for a taxi ride. We can model each transaction as a tuple (x, y, z) which means person x gave person y \$z. Assuming Alice, Bill, and Chris are person 0, 1, and 2 respectively (0, 1, 2 are the person's ID), the transactions can be represented as [[0, 1, 10], [2, 0, 5]].

A transaction will be given as a tuple (x, y, z). Note that x? y and z > 0. Person's IDs may not be linear, e.g. we could have the persons 0, 1, 2 or we could also have the persons 0, 2, 6.

Example 1:

Input: [[0,1,10], [2,0,5]] Output: 2 Explanation: Person #0 gave person #1 \$10. Person #2 gave person #0 \$5. Two transactions are needed. One way to settle the debt is person #1 pays person #0 and #2 \$5 each.

Example 2:

Input: [[0,1,10], [1,0,1], [1,2,5], [2,0,5]] Output: 1 Explanation:

- 1. Person #0 gave person #1 \$10.
- 2. Person #1 gave person #0 \$1.
- 3. Person #1 gave person #2 \$5.
- 4. Person #2 gave person #0 \$5.
- 5. Therefore, person #1 only need to give person #0 \$4, and all debt is settled.

分析

先計算每個人的 balance。然後嘗試所有的可能性,記低最細的交易次數。Reference https://www.youtube.com/watch?v=l8lLGTgb9LU

代碼 - DFS

```
// LeetCode, Optimal Account Balancing
// dfs, 時間複雜度 O(), 空間複雜度 O()
class Solution {
public:
    int minTransfers(const vector<vector<int>>% transactions)
```

```
{
        unordered_map<int, int> map; // key: person value: balance
        for (const auto& tran : transactions)
            int personGive = tran[0];
            int personGet = tran[1];
            int balance = tran[2];
            auto giveIT = map.find(personGive);
            if (giveIT == map.end()) giveIT = map.insert(giveIT, make_pair(personGive, 0));
            auto getIT = map.find(personGet);
            if (getIT == map.end()) getIT = map.insert(getIT, make_pair(personGet, 0));
            giveIT->second += balance;
            getIT->second -= balance;
        }
        vector<int> vec; vec.reserve(map.size());
        for (const auto& m : map)
        {
            vec.push_back(m.second);
        return dfs(0, vec);
    }
private:
    int dfs(size_t k, vector<int>& vec)
        if (k == vec.size()) return 0;
        int cur = vec[k];
        if (cur == 0)
            return dfs(k + 1, vec);
        int minTrans = INT_MAX;
        for (size_t i = k + 1; i < vec.size(); i++)
        {
            int next = vec[i];
            if (cur * next < 0)
                vec[i] = cur + next;
                minTrans = min(minTrans, 1 + dfs(k + 1, vec));
                vec[i] = next;
            }
            if (cur + next == 0) break;
        return minTrans;
    }
};
```

• 無

11.13 Candy Crush II

描述

This question is about implementing a basic elimination algorithm for Candy Crush. This example for demo only. Greedy crushing the longest possible solution.

分析

DFS to find the longest possible crush

代碼 - DFS

```
// LeetCode, Candy Crush II
// dfs, 時間複雜度 O(), 空間複雜度 O()
class Solution {
public:
    struct Point
    {
        int m_x;
        int m_y;
        Point(int x, int y) : m_x(x), m_y(y) {}
    void printCandy(vector<vector<int>>& board) {
        for (const auto& r : board)
        {
            for (const auto& c : r)
                cout << c << "\t";
            cout << endl;</pre>
    }
    vector<vector<int>> candyCrush(vector<vector<int>>& board) {
        m_M = board.size();
        m_N = board[0].size();
        bool isNeedScan = true;
        while (isNeedScan)
            vector<Point> points = DoCrush(board);
            if (points.size() >= 3)
            {
                DoDrop(board, points);
                isNeedScan = true;
            else
                isNeedScan = false;
```

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```
}
        return board;
    }
private:
    void FindLongestPath(vector<vector<bool>>& visited
      , vector<vector<int>>& board, int i, int j, int target, vector<Point>& points)
        if (i < 0 || j < 0 || i >= m_M || j >= m_N || board[i][j] != target) return;
        if (visited[i][j]) return;
        if (board[i][j] == target)
            points.emplace_back(i, j);
        visited[i][j] = true;
        FindLongestPath(visited, board, i + 1, j, target, points);
        FindLongestPath(visited, board, i, j + 1, target, points);
        FindLongestPath(visited, board, i - 1, j, target, points);
        FindLongestPath(visited, board, i, j - 1, target, points);
        visited[i][j] = false;
        return;
    }
    vector<Point> DoCrush(vector<vector<int>>& board)
        for (int i = 0; i < m_M; i++)
            for (int j = 0; j < m_N; j++)
                if (board[i][j] == 0) continue;
                vector<Point> points;
                vector<vector<bool>> visited(m_M, vector<bool>(m_N, false));
                FindLongestPath(visited, board, i, j, board[i][j], points);
                if (points.size() >= 3)
                {
                    // Clear the candy
                    for (const auto& p : points)
                        board[p.m_x][p.m_y] = 0;
                    return points;
                }
            }
        }
        return vector<Point>();
    }
    void DoDrop(vector<vector<int>>& board, vector<Point>& points)
        for (const auto& p : points)
        {
            DoDropCol(board, p.m_y);
    }
```

```
void DoDropCol(vector<vector<int>>& board, int col)
        // find the lowest zero
        int lowestZ = m_M - 1;
        for (; lowestZ >= 0; lowestZ--)
            if (board[lowestZ][col] == 0) break;
        // find the highest zero
        int highestZ = lowestZ;
        for (; highestZ >= 0; highestZ--)
            if (board[highestZ][col] != 0) break;
        // move numbers one by one
        for (int i = highestZ; i >= 0; i--)
            board[lowestZ--][col] = board[i][col];
        // padding zero if needed
        for (; lowestZ >= 0; lowestZ--)
            board[lowestZ][col] = 0;
    }
private:
    int m_M;
    int m_N;
};
```

• 無

11.14 K-th Symbol in Grammar

描述

On the first row, we write a 0. Now in every subsequent row, we look at the previous row and replace each occurrence of 0 with 01, and each occurrence of 1 with 10.

Given row N and index K, return the K-th indexed symbol in row N. (The values of K are 1-indexed.) (1 indexed).

```
Examples:
Input: N = 1, K = 1
Output: O

Input: N = 2, K = 1
Output: O

Input: N = 2, K = 2
Output: 1

Input: N = 4, K = 5
Output: 1

Explanation:
row 1: O
row 2: O1
```

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```
row 3: 0110
row 4: 01101001

分析
Nil

代碼-DFS

// LeetCode
// 時間複雜度 O(logn), 空間複雜度 O(1)
class Solution {
public:
    int kthGrammar(int N, int K) {
        if (N == 1) return 0;
```

相關題目

• 無

};

11.15 Robot Room Cleaner

if (K <= 1 << N-2)

return kthGrammar(N-1, K);

return kthGrammar(N-1, K - (1 << N-2)) ^ 1;

描述

Given a robot cleaner in a room modeled as a grid.

Each cell in the grid can be empty or blocked.

The robot cleaner with 4 given APIs can move forward, turn left or turn right. Each turn it made is 90 degrees.

When it tries to move into a blocked cell, its bumper sensor detects the obstacle and it stays on the current cell.

Design an algorithm to clean the entire room using only the 4 given APIs shown below.

```
interface Robot {
    // returns true if next cell is open and robot moves into the cell.
    // returns false if next cell is obstacle and robot stays on the current cell.
    boolean move();

    // Robot will stay on the same cell after calling turnLeft/turnRight.
    // Each turn will be 90 degrees.
    void turnLeft();
    void turnRight();

    // Clean the current cell.
```

```
void clean();
}
  Example:
Input:
room = [
  [1,1,1,1,1,0,1,1],
  [1,1,1,1,1,0,1,1]
  [1,0,1,1,1,1,1,1]
  [0,0,0,1,0,0,0,0]
  [1,1,1,1,1,1,1,1]
٦.
row = 1,
col = 3
Explanation:
All grids in the room are marked by either 0 or 1.
O means the cell is blocked, while 1 means the cell is accessible.
The robot initially starts at the position of row=1, col=3.
From the top left corner, its position is one row below and three columns right.
```

Notes:

- 1. The input is only given to initialize the room and the robot's position internally. You must solve this problem "blindfolded". In other words, you must control the robot using only the mentioned 4 APIs, without knowing the room layout and the initial robot's position.
- 2. The robot's initial position will always be in an accessible cell.
- 3. The initial direction of the robot will be facing up.
- All accessible cells are connected, which means the all cells marked as 1 will be accessible by the robot.
- 5. Assume all four edges of the grid are all surrounded by wall.

分析

Nil

代碼 - DFS

```
// LeetCode
// 時間複雜度 O(todo), 空間複雜度 O(todo)
/**

* // This is the robot's control interface.

* // You should not implement it, or speculate about its implementation

* class Robot {

* public:

* // Returns true if the cell in front is open and robot moves into the cell.

* // Returns false if the cell in front is blocked and robot stays in the current cell.
```

```
bool move();
 *
       // Robot will stay in the same cell after calling turnLeft/turnRight.
       // Each turn will be 90 degrees.
       void turnLeft();
       void turnRight();
 *
       // Clean the current cell.
       void clean();
* };
 */
namespace std
{
    template <>
        struct hash<pair<int, int>>
            size_t operator()(pair<int, int> const& p) const
                return ((size_t)&(p.first) ^ (size_t)&(p.second));
        };
class Solution {
public:
    void cleanRoom(Robot& robot) {
        backtrack(robot, 0, 0, 0);
    }
private:
    const vector<pair<int, int>> m directions\{\{-1,0\},\{0,1\},\{1,0\},\{0,-1\}\};
    unordered_set<pair<int, int>> m_visited;
private:
    void backtrack(Robot& robot, int row, int col, int d)
        m_visited.emplace(row, col);
        robot.clean();
        // 以順時針方向出法, 0:上, 1:右, 2:下, 3:左
        for (int i = 0; i < 4; i++)
        {
            int newD = (d + i) \% 4;
            int newRow = row + m_directions[newD].first;
            int newCol = col + m_directions[newD].second;
            if (m_visited.find(make_pair(newRow, newCol)) == m_visited.end() && robot.move())
                backtrack(robot, newRow, newCol, newD);
                GoBack(robot);
            robot.turnRight();
        }
    }
    void GoBack(Robot& robot)
```

```
{
         robot.turnRight();
          robot.turnRight();
          robot.move();
          robot.turnRight();
          robot.turnRight();
     }
 };
代碼 - DFS
 // LeetCode
 // 時間複雜度 D(todo), 空間複雜度 D(todo)
 class Solution {
 public:
     #define ii pair<int,int>
     int getr(int x, int y) {
         return max(abs(x), abs(y));
     int xy2n(int x, int y) {
          int r = max(abs(x), abs(y));
          if(r==0) return 0;
          int start = (2*r-1)*(2*r-1);
          if(x==r) return start + (x+y);
          if(y==r) return start + 2*r + (y-x);
          if (x==-r) return start + 4*r - (x+y);
          if (y==-r) return start + 6*r + (x-y);
          return -1;
     }
     vector<int> grid;
     int x, y, dir, r;
     #define VISITING 1
     #define VISITED 2
     #define BLOCK 3
     #define N 0
     #define W 1
     #define S 2
     #define E 3
     bool move(Robot &robot) {
          int nx=x,ny=y;
          switch(dir) {
              case N: ny++; break;
              case S: ny--; break;
              case E: nx++; break;
              case W: nx--; break;
          if(r < getr(nx,ny)) {</pre>
              grid.resize(grid.size() + 8*(r+1), 0);
             r = getr(nx,ny);
          }
          int n = xy2n(nx,ny);
          if(grid[n] != 0) return false;
          if(robot.move()) {
```

```
grid[xy2n(nx,ny)] = 1;
             x=nx, y=ny;
             return true;
         } else {
             grid[xy2n(nx,ny)] = BLOCK;
             return false;
         return false;
     void turnLeft(Robot &r) { dir = (dir+1)%4; r.turnLeft(); }
     void turnRight(Robot &r) { dir =(dir+3)%4; r.turnRight(); }
     bool dfs(Robot &r) {
         //printf("(%c,%d) ", dir, xy2n(x,y));
         grid[xy2n(x,y)] = VISITING;
         r.clean();
         int curx=x, cury=y;
         for(int i=0; i<4; i++) {
             if(move(r)) {
                 dfs(r);
                 // pull back the robot back to current cell
                 grid[xy2n(curx,cury)] = 0;
                 move(r); turnRight(r); turnRight(r);
                 grid[xy2n(curx,cury)] = VISITING;
             turnLeft(r);
         turnRight(r); turnRight(r); // point back to the path how we came in
         grid[xy2n(x,y)] = VISITED;
         return false;
     }
     void cleanRoom(Robot& robot) {
         x = y = r = 0;
         dir = N;
         grid.resize(1,0);
         grid[0]=1;
         dfs(robot);
     }
 };
代碼 - DFS
 // LeetCode
 // 時間複雜度 O(todo), 空間複雜度 O(todo)
 class Solution {
 public:
     void dfs(Robot& robot, unordered_map<int, set<int>>& visited, int x, int y)
         //cout << x << " " << y << endl;
         visited[x].insert(y);
         robot.clean();
         if ((visited.count(x-1) == 0 || visited[x-1].count(y) == 0) &&
             robot.move())
```

```
{
    dfs(robot, visited, x-1, y);
    robot.turnRight();
    robot.turnRight();
    robot.move();
}
else
{
    robot.turnRight();
    robot.turnRight();
if ((visited.count(x+1) == 0 || visited[x+1].count(y) == 0) &&
    robot.move())
{
    robot.turnLeft();
    robot.turnLeft();
    dfs(robot, visited, x+1, y);
    robot.move();
    robot.turnRight();
}
else
{
    robot.turnLeft();
if (visited[x].count(y+1) == 0 &&
    robot.move())
    robot.turnLeft();
    dfs(robot, visited, x, y+1);
    robot.turnLeft();
    robot.move();
}
else
{
    robot.turnLeft();
    robot.turnLeft();
if (visited[x].count(y-1) == 0 &&
    robot.move())
    robot.turnRight();
    dfs(robot, visited, x, y-1);
    robot.turnRight();
    robot.move();
    robot.turnLeft();
else
{
    robot.turnRight();
```

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```
}

void cleanRoom(Robot& robot) {
    ios_base::sync_with_stdio(false);
    cin.tie(NULL);
    cout.tie(NULL);
    unordered_map<int, set<int>> visited;

    dfs(robot, visited, 0, 0);
}
};
```

相關題目

• 無

11.16 小結

11.16.1 適用場景

輸入數據:如果是遞歸數據結構,如單鏈表,二叉樹,集合,則百分之百可以用深搜;如果是非 遞歸數據結構,如一維數組,二維數組,字符串、圖,則概率小一些。

狀態轉換圖:樹或者圖。

求解目標:必須要走到最深(例如對於樹,必須要走到葉子節點)才能得到一個解,這種情況適合用深搜。

11.16.2 思考的步驟

- 1. 是求路徑條數,還是路徑本身(或動作序列)? 深搜最常見的三個問題,求可行解的總數,求 一個可行解,求所有可行解。
 - (a) 如果是路徑條數,則不需要存儲路徑。
 - (b) 如果是求路徑本身,則要用一個數組 path[] 存儲路徑。跟寬搜不同,寬搜雖然最終求的也是一條路徑,但是需要存儲擴展過程中的所有路徑,在沒找到答案之前所有路徑都不能放棄;而深搜,在搜索過程中始終只有一條路徑,因此用一個數組就足夠了。
- 2. 只要求一個解,還是要求所有解?如果只要求一個解,那找到一個就可以返回;如果要求所有解,找到了一個後,還要繼續擴展,直到遍歷完。廣搜一般只要求一個解,因而不需要考慮這個問題(廣搜當然也可以求所有解,這時需要擴展到所有葉子節點,相當於在內存中存儲整個狀態轉換圖,非常佔內存,因此廣搜不適合解這類問題)。
- 3. 如何表示狀態?即一個狀態需要存儲哪些些必要的數據,才能夠完整提供如何擴展到下一步狀態的所有信息。跟廣搜不同,深搜的慣用寫法,不是把數據記錄在狀態 struct 裏,而是添加函數參數 (有時為了節省遞歸堆棧,用全局變量), struct 裏的字段與函數參數一一對應。

- 4. 如何擴展狀態?這一步跟上一步相關。狀態裏記錄的數據不同,擴展方法就不同。對於固定不變的數據結構(一般題目直接給出,作為輸入數據),如二叉樹,圖等,擴展方法很簡單,直接往下一層走,對於隱式圖,要先在第1步裏想清楚狀態所帶的數據,想清楚了這點,那如何擴展就很簡單了。
- 5. 終止條件是什麼?終止條件是指到了不能擴展的末端節點。對於樹,是葉子節點,對於圖或隱式圖,是出度為0的節點。
- 6. 收斂條件是什麼?收斂條件是指找到了一個合法解的時刻。如果是正向深搜(父狀態處理完了才進行遞歸,即父狀態不依賴子狀態,遞歸語句一定是在最後,尾遞歸),則是指是否達到目標狀態;如果是逆向深搜(處理父狀態時需要先知道子狀態的結果,此時遞歸語句不在最後),則是指是否到達初始狀態。

由於很多時候終止條件和收斂條件是是合二為一的,因此很多人不區分這兩種條件。仔細區分這兩種條件,還是很有必要的。

為了判斷是否到了收斂條件,要在函數接口裏用一個參數記錄當前的位置(或距離目標還有多遠)。如果是求一個解,直接返回這個解;如果是求所有解,要在這裏收集解,即把第一步中表示路徑的數組 path[]複製到解集合裏。

7. 關於判重

- (a) 是否需要判重?如果狀態轉換圖是一棵樹,則不需要判重,因為在遍歷過程中不可能重複;如果狀態轉換圖是一個 DAG,則需要判重。這一點跟 BFS 不一樣, BFS 的狀態轉換圖總是 DAG,必須要判重。
- (b) 怎樣判重? 跟廣搜相同, 見第 §10.9 節。同時, DAG 説明存在重疊子問題, 此時可以用 緩存加速, 見第 8 步。

8 如何加速?

- (a) 剪枝。深搜一定要好好考慮怎麼剪枝,成本小收益大,加幾行代碼,就能大大加速。這 裏沒有通用方法,只能具體問題具體分析,要充分觀察,充分利用各種信息來剪枝,在 中間節點提前返回。
- (b) 緩存。
 - i. 前提條件: 狀態轉換圖是一個 DAG。DAG=>存在重疊子問題=>子問題的解會被重複利用, 用緩存自然會有加速效果。如果依賴關係是樹狀的 (例如樹, 單鏈表等), 沒必要加緩存, 因為子問題只會一層層往下, 用一次就再也不會用到, 加了緩存也沒什麼加速效果。
 - ii. 具體實現:可以用數組或 HashMap。維度簡單的,用數組;維度複雜的,用 HashMap, C++有 map, C++ 11 以後有 unordered map, 比 map 快。

拿到一個題目,當感覺它適合用深搜解決時,在心裏面把上面 8 個問題默默回答一遍,代碼基本上就能寫出來了。對於樹,不需要回答第 5 和第 8 個問題。如果讀者對上面的經驗總結看不懂或

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感覺 "不實用",很正常,因為這些經驗總結是我做了很多題目後總結出來的,從思維的發展過程看, "經驗總結"要晚於感性認識,所以這時候建議讀者先做做前面的題目,積累一定的感性認識後,再 回過頭來看這一節的總結.一定會有共鳴。

11.16.3 代碼模板

```
dfs template.cpp
/**
 * dfs 模板.
 * @param[in] input 輸入數據指針
 * @param[out] path 當前路徑, 也是中間結果
 * Oparam[out] result 存放最終結果
 * Oparam[inout] cur or gap 標記當前位置或距離目標的距離
 * Oreturn 路徑長度,如果是求路徑本身,則不需要返回長度
void dfs(type &input, type &path, type &result, int cur or gap) {
   if (數據非法) return 0; // 終止條件
   if (cur == input.size()) { // 收斂條件
   // \text{ if } (gap == 0) \{
       將 path 放入 result
   }
   if (可以剪枝) return:
   for(...) { // 執行所有可能的擴展動作
       執行動作,修改 path
       dfs(input, step + 1 or gap--, result);
       恢復 path
   }
}
                                                             dfs template.cpp
```

11.16.4 深搜與回溯法的區別

深搜 (Depth-first search, DFS) 的定義見 http://en.wikipedia.org/wiki/Depth_first_search, 回溯法 (backtracking) 的定義見 http://en.wikipedia.org/wiki/Backtracking

回溯法 = 深搜 + 剪枝。一般大家用深搜時,或多或少會剪枝,因此深搜與回溯法沒有什麼不同,可以在它們之間畫上一個等號。本書同時使用深搜和回溯法兩個術語,但讀者可以認為二者等價。

深搜一般用遞歸 (recursion) 來實現,這樣比較簡潔。

深搜能夠在候選答案生成到一半時,就進行判斷,拋棄不滿足要求的答案,所以深搜比暴力搜索法要快。

11.16.5 深搜與遞歸的區別

深搜經常用遞歸 (recursion) 來實現, 二者常常同時出現, 導致很多人誤以為他倆是一個東西。

深搜,是邏輯意義上的算法,遞歸,是一種物理意義上的實現,它和迭代 (iteration) 是對應的。深搜,可以用遞歸來實現,也可以用棧來實現;而遞歸,一般總是用來實現深搜。可以說,**遞歸一定是深搜,深搜不一定用遞歸**。

遞歸有兩種加速策略,一種是**剪枝 (prunning)**,對中間結果進行判斷,提前返回;一種是**緩存**,緩存中間結果、防止重複計算、用空間換時間。

其實,遞歸+緩存,就是 memoization。所謂 memoization(翻譯為備忘錄法,見第 §??節),就是"top-down with cache" (自頂向下+緩存),它是 Donald Michie 在 1968 年創造的術語,表示一種優化技術,在 top-down 形式的程序中,使用緩存來避免重複計算,從而達到加速的目的。

memoization 不一定用遞歸,就像深搜不一定用遞歸一樣,可以在迭代 (iterative) 中使用 memoization 。**遞歸也不一定用 memoization**,可以用 memoization 來加速,但不是必須的。只有當遞歸使用了緩存,它才是 memoization 。

既然遞歸一定是深搜,為什麼很多書籍都同時使用這兩個術語呢?在遞歸味道更濃的地方,一般用遞歸這個術語,在深搜更濃的場景下,用深搜這個術語,讀者心裏要弄清楚他倆大部分時候是一回事。在單鏈表、二叉樹等遞歸數據結構上,遞歸的味道更濃,這時用遞歸這個術語;在圖、隱式圖等數據結構上,深搜的味道更濃,這時用深搜這個術語。

第 12 章 分治法

12.1 Pow(x,n)

描述

Implement pow(x, n).

分析

```
二分法、x^n = x^{n/2} \times x^{n/2} \times x^{n\%2}
```

代碼

```
//LeetCode, Pow(x, n)
// 二分法, x^n = x^{n/2} * x^{n/2} * x^{n\%2}
// 時間複雜度 O(logn), 空間複雜度 O(1)
class Solution {
public:
    double myPow(double x, int n) {
       long long nn = n // 使用 64 bit 來處理 INT_MIN 由負變正 case
       if (nn < 0) return 1.0 / power(x, -nn);
       else return power(x, nn);
   }
private:
   double power(double x, long long nn) {
       if (nn == 0) return 1;
       double v = power(x, nn / 2);
       if (nn \% 2 == 0) return v * v;
       else return v * v * x;
   }
};
```

相關題目

• Sqrt(x), 見 §12.2

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$12.2 \quad Sqrt(x)$

描述

```
Implement int sqrt(int x).

Compute and return the square root of x.
```

分析

二分查找

代碼

```
// LeetCode, Sqrt(x)
// 二分查找
// 時間複雜度 O(logn), 空間複雜度 O(1)
class Solution {
public:
    int mySqrt(int x) {
        int left = 1, right = x / 2;
        int last_mid; // 記錄最近一次 mid
        if (x < 2) return x;
        while(left <= right) {</pre>
            const int mid = left + (right - left) / 2;
            if(x / mid > mid) { // 不要用 x > mid * mid, 會溢出
                left = mid + 1;
                last_mid = mid;
            } else if(x / mid < mid) {</pre>
                right = mid - 1;
            } else {
                return mid;
        return last_mid;
    }
};
```

相關題目

• Pow(x), 見 §12.1

12.3 The Skyline Problem

描述

A city's skyline is the outer contour of the silhouette formed by all the buildings in that city when viewed from a distance. Now suppose you are given the locations and height of all the buildings as shown on a

cityscape photo (Figure A), write a program to output the skyline formed by these buildings collectively (Figure B).



The geometric information of each building is represented by a triplet of integers [Li, Ri, Hi], where Li and Ri are the x coordinates of the left and right edge of the ith building, respectively, and Hi is its height. It is guaranteed that $0 \le \text{Li}$, $\text{Ri} \le \text{INT_MAX}$, $0 < \text{Hi} \le \text{INT_MAX}$, and Ri - Li > 0. You may assume all buildings are perfect rectangles grounded on an absolutely flat surface at height 0.

For instance, the dimensions of all buildings in Figure A are recorded as: [[2 9 10], [3 7 15], [5 12 12], [15 20 10], [19 24 8]].

The output is a list of "key points" (red dots in Figure B) in the format of [[x1,y1], [x2,y2], [x3,y3], ...] that uniquely defines a skyline. A key point is the left endpoint of a horizontal line segment. Note that the last key point, where the rightmost building ends, is merely used to mark the termination of the skyline, and always has zero height. Also, the ground in between any two adjacent buildings should be considered part of the skyline contour.

For instance, the skyline in Figure B should be represented as: [2 10], [3 15], [7 12], [12 0], [15 10], [20 8], [24, 0]].

Notes:

- 1. The number of buildings in any input list is guaranteed to be in the range [0, 10000].
- 2. The input list is already sorted in ascending order by the left x position Li.
- 3. The output list must be sorted by the x position.
- 4. There must be no consecutive horizontal lines of equal height in the output skyline. For instance, [...[2 3], [4 5], [7 5], [11 5], [12 7]...] is not acceptable; the three lines of height 5 should be merged into one in the final output as such: [...[2 3], [4 5], [12 7], ...]

分析

Nil

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分治法

```
// 時間複雜度 O(nlogn), 空間複雜度 O(n)
class Solution {
public:
    vector<vector<int>> getSkyline(vector<vector<int>>& buildings) {
        return DFS(buildings, 0, buildings.size());
private:
    vector<vector<int>> DFS(vector<vector<int>>& buildings, int start, int end)
        if (start == end)
        {
            return vector<vector<int>>();
        else if (end - start == 1)
            vector<vector<int>> result;
            int& startX = buildings[start][0];
            int& startY = buildings[start][2];
            int& endX = buildings[start][1];
            result.push_back({startX, startY});
            result.push_back({endX, 0});
            return result;
        }
        int mid = start + (end - start) / 2;
        auto left = DFS(buildings, start, mid);
        auto right = DFS(buildings, mid, end);
        return mergeSkylines(left, right);
    }
    vector<vector<int>> mergeSkylines(const vector<vector<int>>& left
                                       , const vector<vector<int>>& right)
    {
        int lN = left.size();
        int rN = right.size();
        int lp, rp, curP;
        int ly, ry, curY;
        int x, maxY;
        vector<vector<int>> output; output.reserve(lN + rN);
        lp = rp = curP = 0;
        ly = ry = curY = 0;
        x = maxY = 0;
        while (lp < lN && rp < rN)
            if (left[lp][0] < right[rp][0])
                x = left[lp][0];
                ly = left[lp][1];
                lp++;
```

```
}
            else
            {
                x = right[rp][0];
                ry = right[rp][1];
                rp++;
            }
            maxY = max(ly, ry);
            if (curY != maxY)
                UpdateOutput(output, x, maxY);
                curY = maxY;
            }
        }
        if (lp < lN)
            AppendSkylines(output, left, lp, lN, curY);
        else
            AppendSkylines(output, right, rp, rN, curY);
        return output;
    }
    void UpdateOutput(vector<vector<int>>& output, int x, int y)
        if (output.empty() || output.back()[0] != x)
            output.push_back({x, y});
        else
            output.back()[1] = y;
    }
    void AppendSkylines(vector<vector<int>>& output
                         , const vector<vector<int>>& skyline, int p, int N, int curY)
    {
        while (p < N)
            const int& x = skyline[p][0];
            const int& y = skyline[p][1];
            p++;
            if (curY != y)
            {
                UpdateOutput(output, x, y);
                curY = y;
            }
        }
   }
};
```

第 13 章 貪心法

13.1 Jump Game

描述

Given an array of non-negative integers, you are initially positioned at the first index of the array.

Each element in the array represents your maximum jump length at that position.

Determine if you are able to reach the last index.

For example:

A = [2,3,1,1,4], return true.

A = [3,2,1,0,4], return false.

分析

由於每層最多可以跳 A[i] 步,也可以跳 0 或 1 步,因此如果能到達最高層,則説明每一層都可以到達。有了這個條件,説明可以用貪心法。

思路一:正向,從0出發,一層一層網上跳,看最後能不能超過最高層,能超過,説明能到達, 否則不能到達。

思路二:逆向,從最高層下樓梯,一層一層下降,看最後能不能下降到第0層。

思路三:如果不敢用貪心,可以用動規,設狀態為f[i],表示從第0層出發,走到A[i]時剩餘的最大步數,則狀態轉移方程為:

$$f[i] = \max(f[i-1], A[i-1]) - 1, i > 0$$

```
// LeetCode, Jump Game
// 思路 1, 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
   bool canJump(const vector<int>& nums) {
      int reach = 1; // 最右能跳到哪裏
      for (int i = 0; i < reach && reach < nums.size(); ++i)
            reach = max(reach, i + 1 + nums[i]);</pre>
```

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```
return reach >= nums.size();
     }
 };
代碼 2
 // LeetCode, Jump Game
 // 思路 2, 時間複雜度 O(n), 空間複雜度 O(1)
 class Solution {
 public:
     bool canJump (const vector<int>& nums) {
         if (nums.empty()) return true;
         // 逆向下樓梯, 最左能下降到第幾層
         int left_most = nums.size() - 1;
         for (int i = nums.size() - 2; i >= 0; --i)
             if (i + nums[i] >= left_most)
                 left_most = i;
         return left_most == 0;
 };
代碼3
 // LeetCode, Jump Game
 // 思路三, 動規, 時間複雜度 O(n), 空間複雜度 O(n)
 class Solution {
 public:
     bool canJump(const vector<int>& nums) {
         vector<int> f(nums.size(), 0);
         f[0] = 0;
         for (int i = 1; i < nums.size(); i++) {
             f[i] = max(f[i - 1], nums[i - 1]) - 1;
             if (f[i] < 0) return false;;</pre>
         return f[nums.size() - 1] >= 0;
 };
```

相關題目

• Jump Game II , 見 §13.2

13.2 Jump Game II

描述

Given an array of non-negative integers, you are initially positioned at the first index of the array. Each element in the array represents your maximum jump length at that position.

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Your goal is to reach the last index in the minimum number of jumps.

```
For example: Given array A = [2,3,1,1,4]
```

The minimum number of jumps to reach the last index is 2. (Jump 1 step from index 0 to 1, then 3 steps to the last index.)

分析

貪心法。

代碼1

```
// LeetCode, Jump Game II
 // 時間複雜度 O(n), 空間複雜度 O(1)
 class Solution {
 public:
     int jump(const vector<int>& nums) {
         int step = 0; // 最小步數
         int left = 0;
         int right = 0; // [left, right] 是當前能覆蓋的區間
         if (nums.size() == 1) return 0;
         while (left <= right) { // 嘗試從每一層跳最遠
             ++step;
             const int old_right = right;
             for (int i = left; i <= old_right; ++i) {</pre>
                 int new_right = i + nums[i];
                 if (new_right >= nums.size() - 1) return step;
                 if (new_right > right) right = new_right;
             }
             left = old_right + 1;
         return 0;
     }
 };
代碼2
 // LeetCode, Jump Game II
 // 時間複雜度 O(n), 空間複雜度 O(1)
 class Solution {
 public:
     int jump(vector<int>& nums) {
         // the maximum distance that has been reached
         int last = 1;
         // the maximum distance that can be reached by using "ret+1" steps
         int cur = 1;
         int step = 0;
         for (int i = 0; i < last && last < (int)nums.size(); i++) {</pre>
```

cur = max(cur, i + 1 + nums[i]);

相關題目

• Jump Game , 見 §13.1

13.3 Best Time to Buy and Sell Stock

描述

Say you have an array for which the i-th element is the price of a given stock on day i.

If you were only permitted to complete at most one transaction (ie, buy one and sell one share of the stock), design an algorithm to find the maximum profit.

分析

貪心法,分別找到價格最低和最高的一天,低進高出,注意最低的一天要在最高的一天之前。 把原始價格序列變成差分序列,本題也可以做是最大m子段和,m=1。

代碼

```
// LeetCode, Best Time to Buy and Sell Stock
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    int maxProfit(vector<int> &prices) {
        if (prices.size() < 2) return 0;
        int profit = 0; // 差價, 也就是利潤
        int cur_min = prices[0]; // 當前最小

        for (int i = 1; i < prices.size(); i++) {
            profit = max(profit, prices[i] - cur_min);
            cur_min = min(cur_min, prices[i]);
        }
        return profit;
    }
};</pre>
```

相關題目

• Best Time to Buy and Sell Stock II, 見 §13.4

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• Best Time to Buy and Sell Stock III, 見 §14.7

13.4 Best Time to Buy and Sell Stock II

描述

Say you have an array for which the i-th element is the price of a given stock on day i.

Design an algorithm to find the maximum profit. You may complete as many transactions as you like (ie, buy one and sell one share of the stock multiple times). However, you may not engage in multiple transactions at the same time (ie, you must sell the stock before you buy again).

分析

貪心法, 低進高出, 把所有正的價格差價相加起來。 把原始價格序列變成差分序列, 本題也可以做是最大 m 子段和, m =數組長度。

代碼

```
// LeetCode, Best Time to Buy and Sell Stock II
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    int maxProfit(vector<int> &prices) {
        int sum = 0;
        for (int i = 1; i < prices.size(); i++) {
            int diff = prices[i] - prices[i - 1];
            if (diff > 0) sum += diff;
        }
        return sum;
    }
};
```

相關題目

- Best Time to Buy and Sell Stock, 見 §13.3
- Best Time to Buy and Sell Stock III, 見 §14.7

13.5 Longest Substring Without Repeating Characters

描述

Given a string, find the length of the longest substring without repeating characters. For example, the longest substring without repeating letters for "abcabcbb" is "abc", which the length is 3. For "bbbbb" the longest substring is "b", with the length of 1.

分析

假設子串裏含有重複字符,則父串一定含有重複字符,單個子問題就可以決定父問題,因此可以用貪心法。跟動規不同,動規裏,單個子問題只能影響父問題,不足以決定父問題。

從左往右掃描,當遇到重複字母時,以上一個重複字母的 index+1,作為新的搜索起始位置,直到最後一個字母、複雜度是 O(n)。如圖 13-1 所示。

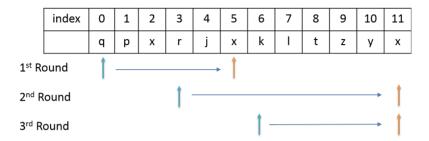


图 13-1 不含重複字符的最長子串

代碼

```
// LeetCode, Longest Substring Without Repeating Characters
// 時間複雜度 O(n), 空間複雜度 O(1)
// 考慮非字母的情況
class Solution {
public:
   int lengthOfLongestSubstring(string s) {
       const int ASCII MAX = 255;
       int last[ASCII_MAX]; // 記錄字符上次出現過的位置
       int start = 0; // 記錄當前子串的起始位置
       fill(last, last + ASCII_MAX, -1); // 0 也是有效位置, 因此初始化為-1
       int max_len = 0;
       for (int i = 0; i < s.size(); i++) {
           if (last[s[i]] >= start) {
              max_len = max(i - start, max_len);
              start = last[s[i]] + 1;
           last[s[i]] = i;
       return max((int)s.size() - start, max_len); // 別忘了最後一次, 例如"abcd"
   }
};
```

相關題目

• 無

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13.6 Container With Most Water

描述

Given n non-negative integers $a_1, a_2, ..., a_n$, where each represents a point at coordinate (i, a_i) . In vertical lines are drawn such that the two endpoints of line i is at (i, a_i) and (i, 0). Find two lines, which together with x-axis forms a container, such that the container contains the most water.

Note: You may not slant the container.

分析

每個容器的面積, 取決於最短的木板。

代碼

```
// LeetCode, Container With Most Water
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    int maxArea(vector<int> &height) {
        int start = 0;
        int end = height.size() - 1;
        int result = INT_MIN;
        while (start < end) {
            int area = min(height[end], height[start]) * (end - start);
            result = max(result, area);
            if (height[start] <= height[end]) {</pre>
                start++;
            } else {
                end--;
        return result;
    }
};
```

相關題目

- Trapping Rain Water, 見 §2.1.18
- Largest Rectangle in Histogram, 見 §5.1.3

14.1 Triangle

描述

Given a triangle, find the minimum path sum from top to bottom. Each step you may move to adjacent numbers on the row below.

For example, given the following triangle

The minimum path sum from top to bottom is 11 (i.e., 2 + 3 + 5 + 1 = 11).

Note: Bonus point if you are able to do this using only O(n) extra space, where n is the total number of rows in the triangle.

分析

設狀態為 f(i,j), 表示從從位置 (i,j) 出發, 路徑的最小和, 則狀態轉移方程為

```
f(i, j) = \min \{ f(i+1, j), f(i+1, j+1) \} + (i, j)
```

代碼

```
return triangle [0][0];
};
```

prevMax = temp;

}

相關題目

無

14.2 House Robber

描述

You are a professional robber planning to rob houses along a street. Each house has a certain amount of money stashed, the only constraint stopping you from robbing each of them is that adjacent houses have security system connected and it will automatically contact the police if two adjacent houses were broken into on the same night.

Given a list of non-negative integers representing the amount of money of each house, determine the maximum amount of money you can rob tonight without alerting the police.

```
Example 1:
 Input: nums = [1,2,3,1]
 Output: 4
 Explanation: Rob house 1 (money = 1) and then rob house 3 (money = 3).
              Total amount you can rob = 1 + 3 = 4.
   Example 2:
 Input: nums = [2,7,9,3,1]
 Output: 12
 Explanation: Rob house 1 (money = 2), rob house 3 (money = 9) and rob house 5 (money = 1).
              Total amount you can rob = 2 + 9 + 1 = 12.
   • 0 <= nums.length <= 100
   • 0 \le nums[i] \le 400
動規
 // 時間複雜度 O(n), 空間複雜度 O(1)
 class Solution {
 public:
     int rob(vector<int>& nums) {
          int prevMax = 0;
         int curMax = 0;
         for (const int& n : nums)
             int temp = curMax;
             curMax = max(prevMax + n, curMax);
```

```
return curMax;
};
```

14.3 Maximum Product Subarray

if(curProd==0) curProd=1;

return ans;

};

描述

Given an integer array nums, find the contiguous subarray within an array (containing at least one number) which has the largest product.

```
Example 1:
 Input: [2,3,-2,4]
 Output: 6
 Explanation: [2,3] has the largest product 6.
   Example 2:
 Input: [-2,0,-1]
 Output: 0
 Explanation: The result cannot be 2, because [-2,-1] is not a subarray.
動規
 // 時間複雜度 O(n), 空間複雜度 O(1)
 //
 // 先由左至右累計一次, 再由右至左累計一次, 取最大值
 // 若果負數出現的次數為雙數, 必定可以用盡全個數組。所以必定可以得到最大數
 // 若果負數出現的次數為單數, 由左至右或由右至左必定可以得到答案, 答案會包括其中的子數組, 其中負數出
 class Solution {
 public:
     int maxProduct(vector<int>& nums) {
        int ans = INT_MIN, curProd = 1;
        // 由左至右
        for (int i = 0; i < nums.size(); i++)</pre>
            curProd *= nums[i];
            if (curProd > ans) ans = curProd;
            if (curProd == 0) curProd = 1;
        }
        curProd = 1;
        // 由右至左
        for (int i = nums.size()-1; i > 0; i--)
            curProd *= nums[i];
            if(curProd>ans) ans = curProd;
```

14.4 Maximum Subarray

描述

Find the contiguous subarray within an array (containing at least one number) which has the largest sum. For example, given the array

$$-2, 1, -3, 4, -1, 2, 1, -5, 4$$

, the contiguous subarray

$$4, -1, 2, 1$$

has the largest sum = 6.

分析

最大連續子序列和, 非常經典的題。

當我們從頭到尾遍歷這個數組的時候,對於數組裏的一個整數,它有幾種選擇呢?它只有兩種選擇: 1、加入之前的 SubArray; 2. 自己另起一個 SubArray。那什麼時候會出現這兩種情況呢?

如果之前 SubArray 的總體和大於 0 的話,我們認為其對後續結果是有貢獻的。這種情況下我們選擇加入之前的 SubArray

如果之前 SubArray 的總體和為0或者小於0的話,我們認為其對後續結果是沒有貢獻,甚至是有害的(小於 0時)。這種情況下我們選擇以這個數字開始,另起一個 SubArray。

設狀態為 f[j],表示以 S[j] 結尾的最大連續子序列和,則狀態轉移方程如下:

$$f[j] = \max \{f[j-1] + S[j], S[j]\}, 其中 1 \le j \le n$$

$$target = \max \{f[j]\}, 其中 1 \le j \le n$$

解釋如下:

- 情況一, S[j] 不獨立, 與前面的某些數組成一個連續子序列, 則最大連續子序列和為 f[j-1]+S[j]。
- 情況二, S[j]獨立劃分成為一段, 即連續子序列僅包含一個數 S[j], 則最大連續子序列和為 S[j]。 其他思路:
- 思路 2:直接在 i 到 j 之間暴力枚舉,複雜度是 $O(n^3)$
- 思路 3: 處理後枚舉,連續子序列的和等於兩個前綴和之差,複雜度 $O(n^2)$ 。
- 思路 4:分治法,把序列分為兩段,分別求最大連續子序列和,然後歸併,複雜度 $O(n \log n)$
- 思路 5: 把思路 $2O(n^2)$ 的代碼稍作處理,得到 O(n) 的算法
- 思路 6: 當成 M=1 的最大 M 子段和

動規

```
// LeetCode, Maximum Subarray
 // 時間複雜度 O(n), 空間複雜度 O(1)
 class Solution {
 public:
     int maxSubArray(vector<int>& nums) {
         int result = INT_MIN, f = 0;
         for (int i = 0; i < nums.size(); ++i) {</pre>
             f = max(f + nums[i], nums[i]);
             result = max(result, f);
         return result;
     }
 };
思路5
 // LeetCode, Maximum Subarray
 // 時間複雜度 O(n), 空間複雜度 O(n)
 class Solution {
 public:
     int maxSubArray(vector<int>& A) {
         return mcss(A.begin(), A.end());
 private:
     // 思路 5, 求最大連續子序列和
     template <typename Iter>
     static int mcss(Iter begin, Iter end) {
         int result, cur_min;
         const int n = distance(begin, end);
         int *sum = new int[n + 1]; // 前n項和
         sum[0] = 0;
         result = INT_MIN;
         cur_min = sum[0];
         for (int i = 1; i <= n; i++) {
             sum[i] = sum[i - 1] + *(begin + i - 1);
         for (int i = 1; i <= n; i++) {
             result = max(result, sum[i] - cur_min);
             cur_min = min(cur_min, sum[i]);
         delete[] sum;
         return result;
     }
 };
```

相關題目

• Binary Tree Maximum Path Sum, 見 §6.4.5

14.5 Palindrome Partitioning II

描述

Given a string s, partition s such that every substring of the partition is a palindrome.

Return the minimum cuts needed for a palindrome partitioning of s.

For example, given s = "aab",

Return 1 since the palindrome partitioning

could be produced using 1 cut.

Reference https://www.youtube.com/watch?v=IDYIvtBVmgo

分析

定義狀態 f(i,j) 表示區間 [i,j] 之間最小的 cut 數,則狀態轉移方程為

$$f(i,j) = \min \{ f(i,k) + f(k+1,j) \}, i \le k \le j, 0 \le i \le j < n$$

這是一個二維函數,實際寫代碼比較麻煩。

所以要轉換成一維 DP。如果每次,從 i 往右掃描,每找到一個迴文就算一次 DP 的話,就可以轉換為 f(i)=區間 [i, n-1] 之間最小的 cut 數, n 為字符串長度,則狀態轉移方程為

$$f(i) = \min \{f(j+1) + 1\}, i \le j < n$$

一個問題出現了,就是如何判斷 [i,j] 是否是迴文?每次都從i到j比較一遍?太浪費了,這裏也是一個 DP 問題。

```
定義狀態 P[i][j] = true if [i,j] 為迴文, 那麼 P[i][j] = str[i] == str[j] && P[i+1][j-1]
```

代碼

```
// LeetCode, Palindrome Partitioning II
// 時間複雜度 O(n^2), 空間複雜度 O(n^2)
class Solution {
public:
    int minCut(const string& s) {
        const int n = s.size();
        int f[n+1];
        bool p[n][n];
        fill_n(&p[0][0], n * n, false);
        //the worst case is cutting by each char for (int i = 0; i <= n; i++)
        f[i] = n - 1 - i; // 最後一個 f[n]=-1 for (int i = n - 1; i >= 0; i--) {
```

```
for (int j = i; j < n; j++) {
        if (s[i] == s[j] && (j - i < 2 || p[i + 1][j - 1])) {
            p[i][j] = true;
            f[i] = min(f[i], f[j + 1] + 1);
        }
    }
    return f[0];
}</pre>
```

相關題目

• Palindrome Partitioning, 見 §11.1

14.6 Maximal Rectangle

描述

Given a 2D binary matrix filled with 0's and 1's, find the largest rectangle containing all ones and return its area.

分析

Example		0	1	2	3	4
	0		1	1		
	1		1	1		
	2					
	3		1	1	1	
	4					
		_		_	_	
Н	-	0	1	2	3	4
	0	-	1	1	-	
	1	_	2	2	_	
	2		0	0		
	3		1	1	1	
	4					
L		0	1	2	3	4
	0		1	1		
	1		1	1		
	2					
	3		1	1	1	
	4					
R		0	1	2	3	4
	0		3	3		
	1		3	3		
	2					
	3		4	4	4	
	4					

图 14-1 Maximal Rectangle

代碼

```
// LeetCode, Maximal Rectangle
// 時間複雜度 O(n^2), 空間複雜度 O(n)
class Solution {
public:
    int maximalRectangle(vector<vector<char> > &matrix) {
        if (matrix.empty()) return 0;

        const int m = matrix.size();
        const int n = matrix[0].size();
        vector<int> H(n, 0);
        vector<int> L(n, 0);
```

```
vector<int> R(n, n);
        int ret = 0;
        for (int i = 0; i < m; ++i) {
            int left = 0, right = n;
            // calculate L(i, j) from left to right
            for (int j = 0; j < n; ++j) {
                if (matrix[i][j] == '1') {
                    ++H[j];
                    L[i] = max(L[i], left);
                } else {
                    left = j+1;
                    H[j] = 0; L[j] = 0; R[j] = n;
                }
            }
            // calculate R(i, j) from right to left
            for (int j = n-1; j \ge 0; --j) {
                if (matrix[i][j] == '1') {
                    R[j] = min(R[j], right);
                    ret = max(ret, H[j]*(R[j]-L[j]));
                } else {
                    right = j;
            }
        }
        return ret;
    }
};
```

相關題目

• 無

14.7 Best Time to Buy and Sell Stock III

描述

Say you have an array for which the i-th element is the price of a given stock on day i.

Design an algorithm to find the maximum profit. You may complete at most two transactions.

Note: You may not engage in multiple transactions at the same time (ie, you must sell the stock before you buy again).

分析

設狀態 f(i),表示區間 $[0,i](0 \le i \le n-1)$ 的最大利潤,狀態 g(i),表示區間 $[i,n-1](0 \le i \le n-1)$ 的最大利潤,則最終答案為 $\max\{f(i)+g(i)\},0 \le i \le n-1$ 。 允許在一天內買進又賣出、相當於不交易、因為題目的規定是最多兩次,而不是一定要兩次。

將原數組變成差分數組,本題也可以看做是最大m子段和,m=2,參考代碼: https://qist.github.com/soulmachine/5906637

代碼

```
// LeetCode, Best Time to Buy and Sell Stock III
// 時間複雜度 O(n). 空間複雜度 O(n)
class Solution {
public:
    int maxProfit(vector<int>& prices) {
        if (prices.size() < 2) return 0;</pre>
        const int n = prices.size();
        vector<int> f(n, 0);
        vector<int> g(n, 0);
        for (int i = 1, valley = prices[0]; i < n; ++i) {</pre>
            valley = min(valley, prices[i]);
            f[i] = max(f[i - 1], prices[i] - valley);
        }
        for (int i = n - 2, peak = prices[n - 1]; i \ge 0; --i) {
            peak = max(peak, prices[i]);
            g[i] = max(g[i], peak - prices[i]);
        }
        int max profit = 0;
        for (int i = 0; i < n; ++i)
            max_profit = max(max_profit, f[i] + g[i]);
        return max_profit;
    }
};
```

相關題目

- Best Time to Buy and Sell Stock, 見 §13.3
- Best Time to Buy and Sell Stock II, 見 §13.4

14.8 Interleaving String

描述

```
Given s1, s2, s3, find whether s3 is formed by the interleaving of s1 and s2. For example, Given: s1 = "aabcc", s2 = "dbbca", When s3 = "aadbbcbcac", return true. When s3 = "aadbbbaccc", return false.
```

分析

設狀態 f[i][j], 表示 s1[0,i] 和 s2[0,j], 匹配 s3[0,i+j]。如果 s1 的最後一個字符等於 s3 的最後一個字符,則 f[i][j]=f[i-1][j];如果 s2 的最後一個字符等於 s3 的最後一個字符,則 f[i][j]=f[i][j-1]。因此狀態轉移方程如下:

```
f[i][j] = (s1[i-1] == s3 [i+j-1] \&\& f[i-1][j])
|| (s2[j-1] == s3 [i+j-1] \&\& f[i][j-1]);
```

Reference https://www.youtube.com/watch?v=ih2OZ9-M3OM

S1	axy					
S1 S2 S3	aab					
S3	aaxaby					
			NULL	a	a	b
		NULL	T ->	T	ŁΤΥ	F
		a	T V	T,	F	F
		X	F	T	T.	Ta
		у	F	F	F	T

图 14-2 Interleaving String Example

遞歸

```
// LeetCode, Interleaving String
// 遞歸, 會超時, 僅用來幫助理解
class Solution {
public:
   bool isInterleave(const string& s1, const string& s2, const string& s3) {
        if (s3.length() != s1.length() + s2.length())
            return false;
       return isInterleave(begin(s1), end(s1), begin(s2), end(s2),
                begin(s3), end(s3));
   }
    template<typename InIt>
    bool isInterleave(InIt first1, InIt last1, InIt first2, InIt last2,
            InIt first3, InIt last3) {
        if (first3 == last3)
            return first1 == last1 && first2 == last2;
        return (*first1 == *first3
                && isInterleave(next(first1), last1, first2, last2,
                        next(first3), last3))
                || (*first2 == *first3
                        && isInterleave(first1, last1, next(first2), last2,
                                next(first3), last3));
};
```

動規

```
// LeetCode, Interleaving String
 // 二維動規, 時間複雜度 O(n^2), 空間複雜度 O(n^2)
 class Solution {
 public:
     bool isInterleave(const string& s1, const string& s2, const string& s3) {
         if (s3.length() != s1.length() + s2.length())
             return false:
         vector<vector<bool>> f(s1.length() + 1,
                 vector<bool>(s2.length() + 1, true));
         for (size_t i = 1; i <= s1.length(); ++i)
             f[i][0] = f[i - 1][0] && s1[i - 1] == s3[i - 1];
         for (size_t i = 1; i <= s2.length(); ++i)
             f[0][i] = f[0][i - 1] && s2[i - 1] == s3[i - 1];
         for (size_t i = 1; i <= s1.length(); ++i)
             for (size_t j = 1; j <= s2.length(); ++j)
                 f[i][j] = (s1[i-1] == s3[i+j-1] && f[i-1][j])
                         || (s2[j-1] == s3[i+j-1] \&\& f[i][j-1]);
         return f[s1.length()][s2.length()];
     }
 };
動規+滾動數組
 // LeetCode, Interleaving String
 // 二維動規+滾動數組, 時間複雜度 D(n^2), 空間複雜度 D(n)
 class Solution {
 public:
     bool isInterleave(const string& s1, const string& s2, const string& s3) {
         if (s1.length() + s2.length() != s3.length())
             return false;
         if (s1.length() < s2.length())
             return isInterleave(s2, s1, s3);
         vector<bool> f(s2.length() + 1, true);
         for (size_t i = 1; i <= s2.length(); ++i)
             f[i] = s2[i - 1] == s3[i - 1] && f[i - 1];
         for (size_t i = 1; i <= s1.length(); ++i) {
             f[0] = s1[i - 1] == s3[i - 1] && f[0];
             for (size_t j = 1; j <= s2.length(); ++j)
                 f[j] = (s1[i - 1] == s3[i + j - 1] \&\& f[j])
                         || (s2[j-1] == s3[i+j-1] \&\& f[j-1]);
         }
```

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```
return f[s2.length()];
};
```

相關題目

• 無

14.9 Scramble String

描述

Given a string s1, we may represent it as a binary tree by partitioning it to two non-empty substrings recursively.

Below is one possible representation of s1 = "great":



To scramble the string, we may choose any non-leaf node and swap its two children.

For example, if we choose the node "gr" and swap its two children, it produces a scrambled string "rgeat".



We say that "rgeat" is a scrambled string of "great".

Similarly, if we continue to swap the children of nodes "eat" and "at", it produces a scrambled string "rgtae".



We say that "rgtae" is a scrambled string of "great".

Given two strings s1 and s2 of the same length, determine if s2 is a scrambled string of s1.

分析

首先想到的是遞歸(即深搜),對兩個 string 進行分割,然後比較四對字符串。代碼雖然簡單,但是複雜度比較高。有兩種加速策略,一種是剪枝,提前返回;一種是加緩存,緩存中間結果,即memoization(翻譯為記憶化搜索)。

剪枝可以五花八門,要充分觀察,充分利用信息,找到能讓節點提前返回的條件。例如,判斷兩個字符串是否互為 scamble,至少要求每個字符在兩個字符串中出現的次數要相等,如果不相等則返回 false。

加緩存,可以用數組或 HashMap。本題維數較高,用 HashMap,map 和 unordered_map 均可。 既然可以用記憶化搜索,這題也一定可以用動規。設狀態為 f[n][i][j],表示長度為 n,起點 為 s1[i] 和起點為 s2[i] 兩個字符串是否互為 scramble,則狀態轉移方程為

```
 \begin{array}{lll} f[n][i][j] \} = & (f[k][i][j] \&\& f[n-k][i+k][j+k]) \\ & & | | & (f[k][i][j+n-k] \&\& f[n-k][i+k][j]) \end{array}
```

禠歸

class Solution {

```
// LeetCode, Scramble String
 // 遞歸, 會超時, 僅用來幫助理解
 // 時間複雜度 O(n^6), 空間複雜度 O(1)
 class Solution {
 public:
     bool isScramble(const string& s1, const string& s2) {
         return isScramble(s1.begin(), s1.end(), s2.begin());
     }
 private:
     typedef string::iterator Iterator;
     bool isScramble(Iterator first1, Iterator last1, Iterator first2) {
         auto length = distance(first1, last1);
         auto last2 = next(first2, length);
         if (length == 1) return *first1 == *first2;
         for (int i = 1; i < length; ++i)
             if ((isScramble(first1, first1 + i, first2)
                  && isScramble(first1 + i, last1, first2 + i))
                     || (isScramble(first1, first1 + i, last2 - i)
                             && isScramble(first1 + i, last1, first2)))
                 return true;
         return false;
     }
 };
動規
 // LeetCode, Scramble String
 // 動規, 時間複雜度 O(n^3), 空間複雜度 O(n^3)
```

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```
public:
     bool isScramble(const string& s1, const string& s2) {
         const int N = s1.size();
         if (N != s2.size()) return false;
         // f[n][i][j], 表示長度為 n, 起點為 s1[i] 和
         // 起點為 s2[j] 兩個字符串是否互為 scramble
         bool f[N + 1][N][N];
         fill_n(&f[0][0][0], (N + 1) * N * N, false);
         for (int i = 0; i < N; i++)
             for (int j = 0; j < N; j++)
                 f[1][i][j] = s1[i] == s2[j];
         for (int n = 1; n \le N; ++n) {
             for (int i = 0; i + n \le N; ++i) {
                 for (int j = 0; j + n \le N; ++j) {
                     for (int k = 1; k < n; ++k) {
                         if ((f[k][i][j] && f[n - k][i + k][j + k]) ||
                                 (f[k][i][j + n - k] && f[n - k][i + k][j])) {
                             f[n][i][j] = true;
                             break;
                         }
                     }
                 }
             }
         return f[N][0][0];
     }
 };
遞歸+剪枝
 // LeetCode, Scramble String
 // 遞歸+剪枝
 // 時間複雜度 O(n^6), 空間複雜度 O(1)
 class Solution {
 public:
     bool isScramble(const string& s1, const string& s2) {
         return isScramble(s1.begin(), s1.end(), s2.begin());
     }
 private:
     typedef string::const_iterator Iterator;
     bool isScramble(Iterator first1, Iterator last1, Iterator first2) {
         auto length = distance(first1, last1);
         auto last2 = next(first2, length);
         if (length == 1) return *first1 == *first2;
         // 剪枝, 提前返回
         int A[26]; // 每個字符的計數器
         fill(A, A + 26, 0);
         for(int i = 0; i < length; i++) A[*(first1+i)-'a']++;
```

```
for(int i = 0; i < length; i++) A[*(first2+i)-'a']--;
         for(int i = 0; i < 26; i++) if (A[i] != 0) return false;
         for (int i = 1; i < length; ++i)
              if ((isScramble(first1, first1 + i, first2)
                  && isScramble(first1 + i, last1, first2 + i))
                      || (isScramble(first1, first1 + i, last2 - i)
                              && isScramble(first1 + i, last1, first2)))
                 return true;
         return false;
 };
備忘錄法
 // LeetCode, Scramble String
 // 遞歸+map 做 cache
 // 時間複雜度 O(n^3), 空間複雜度 O(n^3), TLE
 class Solution {
 public:
     bool isScramble(const string& s1, const string& s2) {
         cache.clear();
         return isScramble(s1.begin(), s1.end(), s2.begin());
 private:
     typedef string::const_iterator Iterator;
     map<tuple<Iterator, Iterator, Iterator>, bool> cache;
     bool isScramble(Iterator first1, Iterator last1, Iterator first2) {
         auto length = distance(first1, last1);
         auto last2 = next(first2, length);
         if (length == 1) return *first1 == *first2;
         for (int i = 1; i < length; ++i)
              if ((getOrUpdate(first1, first1 + i, first2)
                     && getOrUpdate(first1 + i, last1, first2 + i))
                      || (getOrUpdate(first1, first1 + i, last2 - i)
                             && getOrUpdate(first1 + i, last1, first2)))
                 return true:
         return false;
     }
     bool getOrUpdate(Iterator first1, Iterator last1, Iterator first2) {
         auto key = make_tuple(first1, last1, first2);
         auto pos = cache.find(key);
         return (pos != cache.end()) ?
                 pos->second : (cache[key] = isScramble(first1, last1, first2));
     }
```

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```
};
```

備忘錄法

```
typedef string::const_iterator Iterator;
typedef tuple<Iterator, Iterator, Iterator> Key;
// 定製一個哈希函數
namespace std {
template<> struct hash<Key> {
    size_t operator()(const Key & x) const {
        Iterator first1, last1, first2;
        tie(first1, last1, first2) = x;
        int result = *first1;
        result = result * 31 + *last1;
        result = result * 31 + *first2;
        result = result * 31 + *(next(first2, distance(first1, last1)-1));
        return result;
    }
};
// LeetCode, Scramble String
// 遞歸+unordered_map 做 cache, 比 map 快
// 時間複雜度 O(n^3), 空間複雜度 O(n^3)
class Solution {
public:
    unordered_map<Key, bool> cache;
    bool isScramble(const string& s1, const string& s2) {
        cache.clear();
        return isScramble(s1.begin(), s1.end(), s2.begin());
    }
    bool isScramble(Iterator first1, Iterator last1, Iterator first2) {
        auto length = distance(first1, last1);
        auto last2 = next(first2, length);
        if (length == 1)
            return *first1 == *first2;
        for (int i = 1; i < length; ++i)
            if ((getOrUpdate(first1, first1 + i, first2)
                    && getOrUpdate(first1 + i, last1, first2 + i))
                    || (getOrUpdate(first1, first1 + i, last2 - i)
                            && getOrUpdate(first1 + i, last1, first2)))
                return true;
        return false;
    }
    bool getOrUpdate(Iterator first1, Iterator last1, Iterator first2) {
```

相關題目

• 無

14.10 Minimum Path Sum

描述

Given a $m \times n$ grid filled with non-negative numbers, find a path from top left to bottom right which minimizes the sum of all numbers along its path.

Note: You can only move either down or right at any point in time

分析

```
跟 Unique Paths (見 §11.2) 很類似。
```

```
設狀態為 f[i][j], 表示從起點 (0,0) 到達 (i,j) 的最小路徑和,則狀態轉移方程為: f[i][j]=\min(f[i-1][j], f[i][j-1])+grid[i][j]
```

Grid	0	1	2
0	1	4	5
1	3	5	7
2	8	2	1
f	0	1	2
0	1	5	9
1	4	6	12
2	12	6	7

图 14-3 Minimum Path Sum

備忘錄法

```
// LeetCode, Minimum Path Sum
// 備忘錄法
class Solution {
public:
```

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```
int minPathSum(vector<vector<int> > &grid) {
         const int m = grid.size();
         const int n = grid[0].size();
         this->f = vector<vector<int> >(m, vector<int>(n, -1));
         return dfs(grid, m-1, n-1);
 private:
     vector<vector<int> > f; // 緩存
     int dfs(const vector<vector<int> > &grid, int x, int y) {
         if (x < 0 | | y < 0) return INT_MAX; // 越界, 終止條件, 注意, 不是 0
         if (x == 0 && y == 0) return grid[0][0]; // 回到起點, 收斂條件
         return min(getOrUpdate(grid, x - 1, y),
                 getOrUpdate(grid, x, y - 1)) + grid[x][y];
     }
     int getOrUpdate(const vector<vector<int> > &grid, int x, int y) {
         if (x < 0 | | y < 0) return INT_MAX; // 越界, 注意, 不是 0
         if (f[x][y] >= 0) return f[x][y];
         else return f[x][y] = dfs(grid, x, y);
     }
 }:
動規
 // LeetCode, Minimum Path Sum
 // 二維動規
 class Solution {
 public:
     int minPathSum(vector<vector<int> > &grid) {
         if (grid.size() == 0) return 0;
         const int m = grid.size();
         const int n = grid[0].size();
         int f[m][n];
         f[0][0] = grid[0][0];
         for (int i = 1; i < m; i++) {
             f[i][0] = f[i - 1][0] + grid[i][0];
         }
         for (int i = 1; i < n; i++) {
             f[0][i] = f[0][i - 1] + grid[0][i];
         for (int i = 1; i < m; i++) {
             for (int j = 1; j < n; j++) {
                 f[i][j] = min(f[i - 1][j], f[i][j - 1]) + grid[i][j];
         return f[m - 1][n - 1];
     }
```

};

動規+滾動數組

```
// LeetCode, Minimum Path Sum
// 二維動規+滾動數組
class Solution {
public:
   int minPathSum(vector<vector<int> > &grid) {
       const int m = grid.size();
       const int n = grid[0].size();
       int f[n];
       fill(f, f+n, INT_MAX); // 初始值是 INT_MAX, 因為後面用了 min 函數。
       f[0] = 0;
       for (int i = 0; i < m; i++) {
           f[0] += grid[i][0];
           for (int j = 1; j < n; j++) {
               // 左邊的 f [j],表示更新後的 f [j],與公式中的 f [i [[j] 對應
               // 右邊的 f [j], 表示老的 f [j], 與公式中的 f [i-1] [j] 對應
               f[j] = min(f[j - 1], f[j]) + grid[i][j];
           }
       }
       return f[n - 1];
   }
};
```

相關題目

- Unique Paths, 見 §11.2
- Unique Paths II, 見 §11.3

14.11 Edit Distance

描述

Given two words word1 and word2, find the minimum number of steps required to convert word1 to word2. (each operation is counted as 1 step.)

You have the following 3 operations permitted on a word:

- · Insert a character
- · Delete a character
- Replace a character

14.11 Edit Distance 377

分析

設狀態為 f[i][j], 表示 A[0,i] 和 B[0,j] 之間的最小編輯距離。設 A[0,i] 的形式是 str1c, B[0,j] 的形式是 str2d,

- 1. 如果 c==d, 則 f[i][j]=f[i-1][j-1];
- 2. 如果 c!=d,
 - (a) 如果將 c 替換成 d, 則 f[i][j]=f[i-1][j-1]+1;
 - (b) 如果在 c 後面添加一個 d, 則 f [i] [j] =f [i] [j-1] +1;
 - (c) 如果將 c 刪除, 則 f [i] [j] = f [i-1] [j] + 1;

		a	р	р
	0	1	2	3
a	1	0	1	2
a	2	1	1	2
p	3	2	1	1
р	4	3	2	1

图 14-4 Edit Distance

動規

```
// LeetCode, Edit Distance
// 二維動規, 時間複雜度 O(n*m), 空間複雜度 O(n*m)
class Solution {
public:
    int minDistance(const string &word1, const string &word2) {
        const size_t n = word1.size();
        const size_t m = word2.size();
        // 長度為 n 的字符串, 有 n+1 個隔板
        int f[n + 1][m + 1];
        for (size_t i = 0; i <= n; i++)
            f[i][0] = i;
        for (size_t j = 0; j \le m; j++)
            f[0][j] = j;
        for (size_t i = 1; i <= n; i++) {
            for (size_t j = 1; j <= m; j++) {
                if (word1[i - 1] == word2[j - 1])
                   f[i][j] = f[i - 1][j - 1];
               else {
                   int mn = min(f[i - 1][j], f[i][j - 1]);
                   f[i][j] = 1 + min(f[i - 1][j - 1], mn);
               }
            }
        return f[n][m];
```

```
};
```

動規+滾動數組

```
// LeetCode, Edit Distance
// 二維動規+滾動數組
// 時間複雜度 O(n*m), 空間複雜度 O(n)
class Solution {
public:
    int minDistance(const string &word1, const string &word2) {
        if (word1.length() < word2.length())</pre>
            return minDistance(word2, word1);
        int f[word2.length() + 1];
        int upper_left = 0; // 額外用一個變量記錄 f[i-1][j-1]
        for (size_t i = 0; i <= word2.size(); ++i)</pre>
            f[i] = i;
        for (size_t i = 1; i <= word1.size(); ++i) {</pre>
            upper_left = f[0];
            f[0] = i;
            for (size_t j = 1; j <= word2.size(); ++j) {</pre>
                int upper = f[j];
                if (word1[i - 1] == word2[j - 1])
                    f[j] = upper_left;
                else
                    f[j] = 1 + min(upper_left, min(f[j], f[j-1]));
                upper_left = upper;
            }
        }
        return f[word2.length()];
    }
};
```

相關題目

• 無

14.12 Decode Ways

描述

A message containing letters from A-Z is being encoded to numbers using the following mapping:

```
'A' -> 1
'B' -> 2
```

```
'Z' -> 26
```

Given an encoded message containing digits, determine the total number of ways to decode it. For example, Given encoded message "12", it could be decoded as "AB" (1 2) or "L" (12). The number of ways decoding "12" is 2.

分析

跟 Climbing Stairs (見 §2.1.21) 很類似,不過多加一些判斷邏輯。

代碼

```
// LeetCode, Decode Ways
// 動規, 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    int numDecodings(const string &s) {
        if (s.empty() || s[0] == '0') return 0;
        int prev = 0;
        int cur = 1;
        // 長度為 n 的字符串, 有 n+1 個階梯
        for (size_t i = 1; i <= s.size(); ++i) {
            if (s[i-1] == '0') cur = 0;
            if (i < 2 \mid | !(s[i - 2] == '1' \mid |
                     (s[i-2] == '2' \&\& s[i-1] <= '6')))
               prev = 0;
            int tmp = cur;
            cur = prev + cur;
           prev = tmp;
       return cur;
   }
};
```

相關題目

• Climbing Stairs, 見 §2.1.21

14.13 Distinct Subsequences

描述

Given a string S and a string T, count the number of distinct subsequences of T in S.

A subsequence of a string is a new string which is formed from the original string by deleting some (can be none) of the characters without disturbing the relative positions of the remaining characters. (ie, "ACE" is a subsequence of "ABCDE" while "AEC" is not).

```
Here is an example: S = "rabbbit", T = "rabbit"
Return 3.
```

分析

設狀態為 f(i,j), 表示 T[0,j] 在 S[0,i] 裏出現的次數。首先,無論 S[i] 和 T[j] 是否相等,若不使用 S[i],則 f(i,j) = f(i-1,j);若 S[i] == T[j],則可以使用 S[i],此時 f(i,j) = f(i-1,j) + f(i-1,j-1)。

		r	a	b	b	i	t			
	1	0	0	0	0	0	0			
r	1	1		0	0	0	0			
a	1	1	1	0	0	0	0			
-		1	_	1	_	0	0			
b	1	_	_	_	_					
b	1	_	_	2		0	0			
b	1		_	3	3	0	0			
İ	1	1	1	3	3	3	0			
t	1	1	1	3	3	3	3			
		r	a	b	b	İ	t			
f										
	1	1	0	0	0	0	0	, i =	0	
	1	1	1	0	0	0	0	, i =	1	
	1	1	1	1	0	0	0	, i =	2	

图 14-5 Distinct Subsequences

代碼

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```
}
    return f[T.size()];
};
```

相關題目

• 無

14.14 Word Break

描述

Given a string s and a dictionary of words dict, determine if s can be segmented into a space-separated sequence of one or more dictionary words.

```
For example, given s = "leetcode", \\ dict = ["leet", "code"]. \\ Return true because "leetcode" can be segmented as "leet code".
```

分析

設狀態為 f(i), 表示 s[0,i] 是否可以分詞, 則狀態轉移方程為

```
f(i) = any\_of(f(j)\&\&s[j+1,i] \in dict), 0 \le j < i
```

深搜

```
// LeetCode, Word Break
// 深搜, 超時
// 時間複雜度 O(2<sup>n</sup>), 空間複雜度 O(n)
class Solution {
public:
    bool wordBreak(string s, unordered_set<string> &dict) {
        return dfs(s, dict, 0, 0);
    }
private:
    static bool dfs(const string &s, unordered_set<string> &dict,
            size_t start, size_t cur) {
        if (cur == s.size()) {
            return dict.find(s.substr(start, cur-start+1)) != dict.end();
        if (dfs(s, dict, start, cur+1)) return true;
        if (dict.find(s.substr(start, cur-start+1)) != dict.end())
            if (dfs(s, dict, cur+1, cur+1)) return true;
        return false;
```

```
}
 };
動規
 // LeetCode, Word Break
 // 動規, 時間複雜度 O(n^2), 空間複雜度 O(n)
 class Solution {
 public:
     bool wordBreak(string s, unordered_set<string> &dict) {
         // 長度為 n 的字符串有 n+1 個隔板
         vector<bool> f(s.size() + 1, false);
         f[0] = true; // 空字符串
         for (int i = 1; i <= s.size(); ++i) {</pre>
             for (int j = i - 1; j >= 0; --j) {
                 if (f[j] && dict.find(s.substr(j, i - j)) != dict.end()) {
                     f[i] = true;
                     break;
                 }
             }
         }
         return f[s.size()];
     }
 };
```

相關題目

• Word Break II, 見 §14.15

14.15 Word Break II

描述

Given a string s and a dictionary of words dict, add spaces in s to construct a sentence where each word is a valid dictionary word.

Return all such possible sentences.

```
For example, given s = "catsanddog", \\ dict = ["cat", "cats", "and", "sand", "dog"]. \\ A solution is ["cats and dog", "cat sand dog"].
```

分析

在上一題的基礎上, 要返回解本身。

14.15 Word Break II 383

prev		İ	a	m	a	С	е			
		j							Input	iamace
	İ	0	1	2	3	4	5	6	Dict	İ
	0									am
	1	Т								ace
	2	F	Т							
	3	F	Т	F						
	4	F	F	F	Т					
	5	F	F	F	F	F				
	6	F	F	F	Т	F	F			

图 14-6 Word Break Example iamace

代碼

```
// LeetCode, Word Break II
// 動規, 時間複雜度 O(n^2), 空間複雜度 O(n^2)
class Solution {
public:
   vector<string> wordBreak(string s, unordered_set<string> &dict) {
       // 長度為 n 的字符串有 n+1 個隔板
       vector<bool> f(s.length() + 1, false);
       // prev[i][j] 為 true,表示 s[j, i)是一個合法單詞,可以從 j 處切開
       // 第一行未用
       vector<vector<bool> > prev(s.length() + 1, vector<bool>(s.length()));
       f[0] = true;
       for (size_t i = 1; i <= s.length(); ++i) {
           for (int j = i - 1; j \ge 0; --j) {
               if (f[j] && dict.find(s.substr(j, i - j)) != dict.end()) {
                   f[i] = true;
                   prev[i][j] = true;
               }
           }
       }
       vector<string> result;
       vector<string> path;
       gen_path(s, prev, s.length(), path, result);
       return result;
    }
private:
    // DFS 遍歷樹, 生成路徑
    void gen_path(const string &s, const vector<vector<bool> > &prev,
           int cur, vector<string> &path, vector<string> &result) {
       if (cur == 0) {
           string tmp;
           for (auto iter = path.crbegin(); iter != path.crend(); ++iter)
               tmp += *iter + " ";
            tmp.erase(tmp.end() - 1);
           result.push_back(tmp);
```

```
}
    for (size_t i = 0; i < s.size(); ++i) {
        if (prev[cur][i]) {
            path.push_back(s.substr(i, cur - i));
            gen_path(s, prev, i, path, result);
            path.pop_back();
        }
    }
}</pre>
```

相關題目

• Word Break, 見 §14.14

14.16 Target Sum

14.16.1 描述

You are given a list of non-negative integers, a1, a2, ..., an, and a target, S. Now you have 2 symbols + and -. For each integer, you should choose one from + and - as its new symbol.

Find out how many ways to assign symbols to make sum of integers equal to target S.

Example 1:

```
Input: nums is [1, 1, 1, 1, 1], S is 3.
Output: 5
Explanation:
-1+1+1+1+1 = 3
+1-1+1+1+1 = 3
+1+1-1+1+1 = 3
+1+1+1-1+1 = 3
+1+1+1-1+1 = 3
```

There are 5 ways to assign symbols to make the sum of nums be target 3.

- The length of the given array is positive and will not exceed 20.
- The sum of elements in the given array will not exceed 1000.
- Your output answer is guaranteed to be fitted in a 32-bit integer.

14.16.2 深搜

```
// LeetCode
// 時間複雜度 O(2^n), 空間複雜度 O(n)
class Solution {
public:
    int findTargetSumWays(vector<int>& nums, int S) {
        m_ways = 0;
```

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```
DFS(nums, 0, 0, S);
         return m ways;
     }
 private:
     int m_ways;
     void DFS(vector<int>& nums, int step, int curS, int S)
         if (step == nums.size() && S == curS)
         {
             m_ways++;
             return;
         else if (step >= nums.size())
             return;
         DFS(nums, step + 1, curS + nums[step], S);
         DFS(nums, step + 1, curS - nums[step], S);
     }
 };
         備忘錄法
14.16.3
 // LeetCode
 // 時間複雜度 O(1*n), 空間複雜度 O(1*n)
 class Solution {
 public:
     int findTargetSumWays(vector<int>& nums, int S) {
         vector<vector<int>> cache(nums.size(), vector<int>(2001, INT_MIN));
         return DFS(nums, 0, 0, S, cache);
     }
 private:
     int DFS(vector<int>& nums, int step, int curS, int S, vector<vector<int>>& cache)
         if (step == nums.size())
             if (S == curS)
                 return 1;
             else
                 return 0;
         }
         else
         {
             if (cache[step][curS + 1000] != INT_MIN)
                 return cache[step][curS + 1000];
              int add = DFS(nums, step + 1, curS + nums[step], S, cache);
              int subtract = DFS(nums, step + 1, curS - nums[step], S, cache);
             cache[step][curS + 1000] = add + subtract;
             return cache[step][curS + 1000];
```

}

```
};
```

14.16.4 動規

```
// LeetCode
// 時間複雜度 O(1*n), 空間複雜度 O(1*n)
class Solution {
public:
    int findTargetSumWays(vector<int>& nums, int S) {
        vector<vector<int>> dp(nums.size(), vector<int>(2001, 0));
        dp[0][nums[0] + 1000] = 1;
        dp[0][-nums[0] + 1000] += 1;
        for (int step = 1; step < nums.size(); step++)</pre>
            for (int sum = -1000; sum <= 1000; sum++)
                if (dp[step - 1][sum + 1000] > 0)
                    dp[step][sum + nums[step] + 1000] += dp[step - 1][sum + 1000];
                    dp[step][sum - nums[step] + 1000] += dp[step - 1][sum + 1000];
            }
        }
        return S > 1000 ? 0 : dp[nums.size() - 1][S + 1000];
    }
};
```

14.16.5 動規+滾動數組

```
// LeetCode
// 時間複雜度 O(1*n), 空間複雜度 O(n)
class Solution {
public:
    int findTargetSumWays(vector<int>& nums, int S) {
        vector<int> dp(2001, 0);
        dp[nums[0] + 1000] = 1;
        dp[-nums[0] + 1000] += 1;
        for (int step = 1; step < nums.size(); step++)</pre>
            vector<int> next(2001, 0);
            for (int sum = -1000; sum <= 1000; sum++)
                if (dp[sum + 1000] > 0)
                {
                    next[sum + nums[step] + 1000] += dp[sum + 1000];
                    next[sum - nums[step] + 1000] += dp[sum + 1000];
                }
            }
            dp = next;
        return S > 1000 ? 0 : dp[S + 1000];
```

14.16 Target Sum 387

};

第 15 章



```
無向圖的節點定義如下:
// 無向圖的節點
struct UndirectedGraphNode {
   int label;
   vector<UndirectedGraphNode *> neighbors;
   UndirectedGraphNode(int x) : label(x) {};
};
```

15.1 Clone Graph

描述

Clone an undirected graph. Each node in the graph contains a label and a list of its neighbours.

OJ's undirected graph serialization: Nodes are labeled uniquely.

We use # as a separator for each node, and , as a separator for node label and each neighbour of the node. As an example, consider the serialized graph {0,1,2#1,2#2,2}.

The graph has a total of three nodes, and therefore contains three parts as separated by #.

- 1. First node is labeled as 0. Connect node 0 to both nodes 1 and 2.
- 2. Second node is labeled as 1. Connect node 1 to node 2.
- 3. Third node is labeled as 2. Connect node 2 to node 2 (itself), thus forming a self-cycle.

Visually, the graph looks like the following:



分析

廣度優先遍歷或深度優先遍歷都可以。

15.1 Clone Graph 389

DFS

```
// LeetCode, Clone Graph
 // DFS, 時間複雜度 O(n), 空間複雜度 O(n)
 class Solution {
 public:
     UndirectedGraphNode *cloneGraph(const UndirectedGraphNode *node) {
          if(node == nullptr) return nullptr;
          // key is original node, value is copied node
         unordered_map<const UndirectedGraphNode *,
                              UndirectedGraphNode *> copied;
         clone(node, copied);
          return copied[node];
 private:
     // DFS
     static UndirectedGraphNode* clone(const UndirectedGraphNode *node,
             unordered_map<const UndirectedGraphNode *,
             UndirectedGraphNode *> &copied) {
          // a copy already exists
          if (copied.find(node) != copied.end()) return copied[node];
         UndirectedGraphNode *new_node = new UndirectedGraphNode(node->label);
          copied[node] = new_node;
         for (auto nbr : node->neighbors)
             new_node->neighbors.push_back(clone(nbr, copied));
         return new_node;
     }
 };
BFS
 // LeetCode, Clone Graph
 // BFS, 時間複雜度 O(n), 空間複雜度 O(n)
 class Solution {
 public:
     UndirectedGraphNode *cloneGraph(const UndirectedGraphNode *node) {
          if (node == nullptr) return nullptr;
          // key is original node, value is copied node
         unordered_map<const UndirectedGraphNode *,
                              UndirectedGraphNode *> copied;
          // each node in queue is already copied itself
          // but neighbors are not copied yet
         queue < const Undirected Graph Node *> q;
         q.push(node);
          copied[node] = new UndirectedGraphNode(node->label);
          while (!q.empty()) {
              const UndirectedGraphNode *cur = q.front();
             q.pop();
              for (auto nbr : cur->neighbors) {
                  // a copy already exists
                  if (copied.find(nbr) != copied.end()) {
                      copied[cur] ->neighbors.push_back(copied[nbr]);
```

390 第 15 章 圖

相關題目

• 無

15.2 Network Delay Time

描述

There are N network nodes, labelled 1 to N.

Given times, a list of travel times as directed edges times[i] = (u, v, w), where u is the source node, v is the target node, and w is the time it takes for a signal to travel from source to target.

Now, we send a signal from a certain node K. How long will it take for all nodes to receive the signal? If it is impossible, return -1.



图 15-1 Rotate Image

```
Input: times = [[2,1,1],[2,3,1],[3,4,1]], N = 4, K = 2 Output: 2
```

- 1. N will be in the range [1, 100]
- 2. K will be in the range [1, N]
- 3. The length of times will be in the range [1, 6000].
- 4. All edges times[i] = (u, v, w) will have $1 \le u, v \le N$ and $0 \le w \le 100$.

分析

廣度優先遍歷 Use Djikstra Algorithm. Find a minium path from one source to one end.

Djikstra

```
// LeetCode, Clone Graph
// DFS with graph, 時間複雜度 O(ELogV), 空間複雜度 O(V^2)
class Solution {
public:
    struct Node {
        int m_node;
        int m_dist;
        Node (int node, int dist)
            : m_node(node), m_dist(dist) {}
    };
    int networkDelayTime(vector<vector<int>>& times, int N, int K) {
        // create graph
        unordered_map<int, list<Node>> graph; // key: nodeNumber value: nodes
        for (const auto& t : times) // startNode: t[0], endNode: t[1], dist: t[2]
            graph[t[0]].push_back(Node(t[1], t[2]));
        unordered_map<int, int> dist; // key: nodeNumber value: dist
        multimap<int, int> dq; // djikstra queue, key: dist value: nodeNumber
        // do until no more node in queue
        dq.insert(make_pair(0, K));
        while (!dq.empty()) {
            pair<int, int> cur = *dq.begin();
            dq.erase(dq.begin());
            // filter out if shortest path is found
            if (dist.find(cur.second) != dist.end()) continue;
            // record the shortest parth
            dist.insert(make_pair(cur.second, cur.first));
            // push the neighbour to dq
            auto it = graph.find(cur.second);
            if (it == graph.end()) continue;
            for (const auto& nei : it->second) {
                if (dist.find(nei.m_node) != dist.end()) continue;
                dq.insert(make_pair(nei.m_dist + cur.first, nei.m_node));
            }
        }
        // pick the max dist, return -1 if not all node is visited
        if ((int)dist.size() == N)
            return max_element(dist.begin(), dist.end()
              , [&] (const pair<int, int>& first, const pair<int, int>& second)
                                    return first.second < second.second;
                                })->second;
```

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```
return -1;
 };
Djikstra
 // LeetCode, Clone Graph
 // DFS with adjacency list, 時間複雜度 O(ELogV), 空間複雜度 O(V^2)
 class Solution {
 public:
     int networkDelayTime(vector<vector<int>>& times, int N, int K)
         // Build adjacency list
         // index 0 is dummy for easy implementation
         vector<vector<pair<int, int>>> adjList(N + 1);
         for (const auto& v : times)
             adjList[v[0]].emplace_back(v[1], v[2]);
         vector<int> dist(N + 1, INT_MAX);
         // initialize pq and source vertex distance
         dist[K] = 0;
         set<pair<int, int>> pq {{dist[K], K}};
         while (!pq.empty()) {
             const auto u = pq.begin()->second;
             pq.erase(pq.begin()); // pop the top, i.e., first element in set
             for (const auto& [v, w]: adjList[u]) {
                  if (dist[u] + w < dist[v]) { // if edge can be relaxed
                     pq.erase({dist[v], v}); // remove old info
                      dist[v] = dist[u] + w; // update distance
                     pq.emplace(dist[v], v); // insert new info
                 }
             }
         }
         const int longestTime = *max_element(dist.begin() + 1, dist.end());
         return longestTime == INT_MAX ? -1 : longestTime;
     }
 };
```

相關題目

無

15.3 Alien Dictionary

else

描述

There is a new alien language which uses the latin alphabet. However, the order among letters are unknown to you. You receive a list of non-empty words from the dictionary, where words are sorted lexico-

graphically by the rules of this new language. Derive the order of letters in this language.

```
Example 1:
Input:
Γ
  "wrt",
  "wrf".
  "er",
  "ett".
  "rftt"
٦
Output: "wertf"
  Example 2:
Input:
  "z"
  "x"
]
Output: "zx"
  Example 3:
Input:
  "z",
  "x",
  "z"
Output: ""
```

分析

Make DAG from sorted strings, do topological sort by BFS or DFS

BFS with List

```
// LeetCode, Alien Dictionary
// BFS Topological sort, 時間複雜度 O(N), 空間複雜度 O(N)
class Solution {
public:
    string alienOrder(vector<string>& words) {
        unordered_map<char, list<char>> adjList; // 用來記低依賴關係
        unordered_map<char, int> depenCount; // 用來儲存每個字母的依賴數目
        for (const auto& w : words)
            for (const auto& c : w)
            {
                  depenCount[c] = 0;
            }
}
```

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```
adjList.insert(make_pair(c, list<char>()));
        // 製造 adjList DAG
        for (size_t i = 0; i < words.size() - 1; i++)</pre>
        {
            const string& w1 = words[i];
            const string& w2 = words[i+1];
            // 剪枝, 若 prefix 一樣
            if (w1.size() > w2.size() && w1.find(w2) == 0) return "";
            // 找尋第一個不同的字母
            for (size_t j = 0; j < w1.size() && j < w2.size(); j++)
            {
                const char& c1 = w1[j];
                const char& c2 = w2[j];
                if (c1 != c2)
                    adjList[c1].push_back(c2);
                    depenCount[c2]++;
                    break;
                }
            }
        }
        // 利用 Topological Sort 來解決相關的依賴關係
        queue < char > cur;
        // 先處理沒有依賴的字母
        for (const auto& [k, v] : depenCount)
            if (v == 0)
                cur.push(k);
        string result;
        // BFS
        while (!cur.empty())
            char c = cur.front();
            cur.pop();
            result.push_back(c);
            auto it = adjList.find(c);
            if (it == adjList.end()) continue;
            for (const auto& nei : it->second)
                if (--(depenCount[nei]) == 0)
                    cur.push(nei);
            }
        }
        if (result.size() < depenCount.size())</pre>
            return "";
        else
            return result;
    }
};
```

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BFS with Set

```
// LeetCode, Alien Dictionary
// BFS Topological sort, 時間複雜度 O(N), 空間複雜度 O(N)
class Solution {
public:
   string alienOrder(vector<string>& words) {
       unordered_map<char, set<char>> adjList; // 用來記低依賴關係
       unordered_map<char, int> depenCount; // 用來儲存每個字母的依賴數目
       for (const auto& w : words)
           for (const auto& c : w)
               depenCount[c] = 0;
               adjList.insert(make_pair(c, set<char>()));
       // 製造 adjList DAG
       for (size_t i = 0; i < words.size() - 1; i++)
       {
           const string& w1 = words[i];
           const string& w2 = words[i+1];
           // 剪枝, 若 prefix 一樣
           if (w1.size() > w2.size() && w1.find(w2) == 0) return "";
           // 找尋第一個不同的字母
           for (size_t j = 0; j < w1.size() && j < w2.size(); j++)
           {
               const char& c1 = w1[j];
               const char& c2 = w2[j];
               if (c1 != c2)
                   if (adjList[c1].find(c2) == adjList[c1].end()) // 這裏不同
                       adjList[c1].insert(c2);
                      depenCount[c2]++;
                   }
                   break;
               }
           }
       // 之後的動作和上一個例子一樣, 略去。。。 //
   }
};
```

DFS with List

```
// LeetCode, Alien Dictionary
// DFS Topological sort, 時間複雜度 O(N), 空間複雜度 O(N)
class Solution {
public:
    string alienOrder(vector<string>& words) {
        unordered_map<char, list<char>> adjList; // 用來記低依賴關係
```

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```
// 製造 DAG, 令到所有字母也有被歷篇的機會
        for (const auto& w : words)
            for (const auto& c : w)
                adjList.insert(make_pair(c, list<char>()));
        // 製造剩下的 DAG
        for (size_t i = 0; i < words.size() - 1; i++)</pre>
            const string& w1 = words[i];
            const string& w2 = words[i+1];
            // 找到 prefix case
            if (w1.size() > w2.size() && w1.find(w2) == 0) return "";
            for (size_t j = 0; j < w1.size() && j < w2.size(); j++)
            {
                const char& c1 = w1[i];
                const char& c2 = w2[j];
                if (c1 != c2)
                {
                    adjList[c1].push_back(c2);
                    break;
                }
            }
        }
        string result;
        unordered map<char, bool> visited;
        for (const auto& [k, v] : adjList)
            if (!DFS(adjList, visited, k, result))
                return "";
        if (result.size() < adjList.size())</pre>
            return "";
        else
            return result;
    }
private:
    bool DFS(unordered_map<char, list<char>>& adjList, unordered_map<char, bool>& visited, char
    {
        if (visited.find(k) != visited.end())
            return visited[k]; // If this node was grey (false), a cycle was detected.
        visited[k] = false;
        auto it = adjList.find(k);
        for (const auto& nei : adjList[k])
        {
            if (!DFS(adjList, visited, *nei, result)) return false;
        }
        visited[k] = true;
        result.insert(result.begin(), k);
```

```
return true;
};
```

• Topological sort, 見 §7.13

15.4 Redundant Connection

描述

In this problem, a tree is an undirected graph that is connected and has no cycles.

The given input is a graph that started as a tree with N nodes (with distinct values 1, 2, ..., N), with one additional edge added. The added edge has two different vertices chosen from 1 to N, and was not an edge that already existed.

The resulting graph is given as a 2D-array of edges. Each element of edges is a pair [u, v] with u < v, that represents an undirected edge connecting nodes u and v.

Return an edge that can be removed so that the resulting graph is a tree of N nodes. If there are multiple answers, return the answer that occurs last in the given 2D-array. The answer edge [u, v] should be in the same format, with u < v.

- Note:
- The size of the input 2D-array will be between 3 and 1000.
- Every integer represented in the 2D-array will be between 1 and N, where N is the size of the input array.

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DFS

```
// 時間複雜度 O(N^2), 空間複雜度 O(N)
 // 重點:當發現有多過一個路徑可由 u 走到 v. 便發現答案
 class Solution {
 public:
     vector<int> findRedundantConnection(vector<vector<int>>& edges) {
         // 記低見過的 edges, 由 u -> v
         unordered_map<int, unordered_set<int>> cache;
         for (const auto& edge : edges)
         {
             const int& u = edge[0];
             const int& v = edge[1];
             // 利用 DFS 來驗證有沒有另一個方法可以由 u 跑到 v
             unordered set<int> visited;
             if (cache.count(u) && cache.count(v) && DFS(cache, visited, u, v))
                return vector<int>{u, v};
             cache[u].insert(v);
             cache[v].insert(u);
         }
         return vector<int>();
     }
 private:
     template <class eMap, class Vis>
         bool DFS(eMap& cache, Vis& visited, const int& start, const int& target)
         if (start == target) return true;
         if (cache.find(start) == cache.end()) return false;
         visited.insert(start);
         for (const int& nei : cache[start])
             if (!visited.count(nei) && DFS(cache, visited, nei, target))
                return true;
         return false;
     }
 };
DSU - Without Rank
 // 時間複雜度 O(N), 空間複雜度 O(N)
 // 一開始每個點都以自己為一個集合 (set)
 // 歷遍所有 edge, 把點放於同一個集合。
 // 若果兩點早已是同一集合, 那個 edge 便是多餘。
 // https://www.youtube.com/watch?time_continue=1124&v=wU6udHRIkcc&feature=emb_title
 class DSU // Disjoint Set Union (DSU)
 public:
     DSU(int N)
```

```
{
         m parent.reserve(N);
         for (int i = 0; i < N; i++) m parent.push back(i);
     ~DSU() {}
     int FindParent(const int& x)
         if (m_parent[x] == x) // 當 x 為集合的父親時
            return x;
         return m parent[x] = FindParent(m parent[x]); // x 的集合等如 x 的父親的集合
     bool Union(const int& x, const int& y)
         const int xpar = FindParent(x);
         const int ypar = FindParent(y);
         if (xpar == ypar) return false;
         m_parent[xpar] = ypar; // perform union
         return true;
     }
 private:
     vector<int> m_parent; // 利用數列來記低點的所在集合
 }:
 class Solution
 public:
     vector<int> findRedundantConnection(vector<vector<int>>& edges) {
         DSU dsu(1001);
         for (const auto& edge : edges)
            const int& u = edge[0];
            const int& v = edge[1];
            if (!dsu.Union(u, v))
                return vector<int>{u, v};
         }
         return vector<int>();
     }
 };
DSU - Rank
 // 時間複雜度 O(N), 空間複雜度 O(N)
 // 一開始每個點都以自己為一個集合 (set)
 // 歷遍所有 edge, 把點放於同一個集合。
 // 若果兩點早已是同一集合, 那個 edge 便是多餘。
 class DSU // Disjoint Set Union (DSU)
 {
```

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```
public:
   DSU(int N)
    {
        // 負數意指該合集的父親
        // 所以一開始,每個點都是某個合集的父親
        // 負數的值代表 rank, 也是該合集的點的總數
        // 正數的值代表父的 index
       m_parent.resize(N, -1);
    ~DSU() {}
    int FindParent(const int& x)
    {
        if (m_parent[x] < 0)</pre>
           return x;
       return m_parent[x] = FindParent(m_parent[x]);
    }
   bool Union(const int& x, const int& y)
        const int xpar = FindParent(x);
        const int ypar = FindParent(y);
        if (xpar == ypar) return false;
        if (abs(m_parent[xpar]) < abs(m_parent[ypar]))</pre>
           m_parent[ypar] += m_parent[xpar];
           m_parent[xpar] = ypar;
        }
        else
        {
           m_parent[xpar] += m_parent[ypar];
           m_parent[ypar] = xpar;
        }
       return true;
   }
private:
   vector<int> m_parent;
};
class Solution {
public:
    vector<int> findRedundantConnection(vector<vector<int>>& edges) {
        DSU dsu(1001);
       for (const auto& edge : edges)
           const int& u = edge[0];
           const int& v = edge[1];
           if (!dsu.Union(u, v))
               return vector<int>{u, v};
        }
```

```
return vector<int>();
};
```

第16章 細節實現題

這類題目不考特定的算法,純粹考察寫代碼的熟練度。

16.1 Reverse Integer

描述

Reverse digits of an integer. Example1: x = 123, return 321 Example2: x = -123, return -321

Have you thought about this?

Here are some good questions to ask before coding. Bonus points for you if you have already thought through this!

If the integer's last digit is 0, what should the output be? ie, cases such as 10, 100.

Did you notice that the reversed integer might overflow? Assume the input is a 32-bit integer, then the reverse of 1000000003 overflows. How should you handle such cases?

Throw an exception? Good, but what if throwing an exception is not an option? You would then have to re-design the function (ie, add an extra parameter).

分析

短小精悍的題, 代碼也可以寫的很短小。

```
//LeetCode, Reverse Integer
// 時間複雜度 O(logn), 空間複雜度 O(1)
// 考慮 1. 負數的情況 2. 溢出的情況 (正溢出&&負溢出, 比如 x = -2147483648(即-2^31))
class Solution {
public:
    int reverse (int x) {
        long long r = 0;
        long long t = x;
        t = t > 0 ? t : -t;
        for (; t; t /= 10)
```

16.2 Palindrome Number 403

```
r = r * 10 + t % 10;

bool sign = x > 0 ? false: true;
if (r > 2147483647 || (sign && r > 2147483648)) {
    return 0;
} else {
    if (sign) {
        return -r;
} else {
        return r;
} }
}
```

相關題目

• Palindrome Number, 見 §16.2

16.2 Palindrome Number

描述

Determine whether an integer is a palindrome. Do this without extra space.

Some hints:

Could negative integers be palindromes? (ie, -1)

If you are thinking of converting the integer to string, note the restriction of using extra space.

You could also try reversing an integer. However, if you have solved the problem "Reverse Integer", you know that the reversed integer might overflow. How would you handle such case?

There is a more generic way of solving this problem.

分析

首先想到,可以利用上一題,將整數反轉,然後與原來的整數比較,是否相等,相等則為Palindrome的。可是 reverse() 會溢出。

正確的解法是,不斷地取第一位和最後一位 (10 進制下) 進行比較,相等則取第二位和倒數第二位,直到完成比較或者中途找到了不一致的位。

```
//LeetCode, Palindrome Number
// 時間複雜度 O(1), 空間複雜度 O(1)
class Solution {
public:
    bool isPalindrome(int x) {
        if (x < 0) return false;
        int d = 1; // divisor</pre>
```

```
while (x / d >= 10) d *= 10;

while (x > 0) {
    int q = x / d; // quotient
    int r = x % 10; // remainder
    if (q != r) return false;
    x = x % d / 10;
    d /= 100;
}
    return true;
}
```

- Reverse Integer, 見 §16.1
- Valid Palindrome, 見 §4.1

16.3 Insert Interval

描述

Given a set of non-overlapping intervals, insert a new interval into the intervals (merge if necessary).

You may assume that the intervals were initially sorted according to their start times.

Example 1: Given intervals $\{[1,3],[6,9]\}$, insert and merge $\{[2,5]\}$ in as $\{[1,5],[6,9]\}$.

Example 2: Given $\{[1,2],[3,5],[6,7],[8,10],[12,16]\}$, insert and merge $\{[4,9]\}$ in as $\{[1,2],[3,10],[12,16]\}$.

This is because the new interval $\{[4,9]\}$ overlaps with $\{[3,5],[6,7],[8,10]\}$.

分析

無

```
struct Interval {
    int start;
    int end;
    Interval(): start(0), end(0) { }
    Interval(int s, int e): start(s), end(e) { }
};

//LeetCode, Insert Interval
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    vector<Interval> insert(vector<Interval> &intervals, Interval newInterval) {
        vector<Interval>::iterator it = intervals.begin();
    }
}
```

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```
while (it != intervals.end()) {
              if (newInterval.end < it->start) {
                  intervals.insert(it, newInterval);
                  return intervals;
              } else if (newInterval.start > it->end) {
                  it++;
                  continue;
              } else {
                  newInterval.start = min(newInterval.start, it->start);
                  newInterval.end = max(newInterval.end, it->end);
                  it = intervals.erase(it);
              }
         intervals.insert(intervals.end(), newInterval);
         return intervals;
     }
 };
代碼
 //LeetCode. Insert Interval
 // 時間複雜度 O(n), 空間複雜度 O(1)
 class Solution {
 public:
     vector<vector<int>> insert(vector<vector<int>>& intervals, vector<int>& newInterval) {
          vector<vector<int>> result:
         bool isDone = false;
         for (const auto& interval : intervals)
              if (!isDone && newInterval[0] <= interval[0])</pre>
                  MyMerge(result, newInterval);
                  isDone = true;
             MyMerge(result, interval);
         if (!isDone)
              MyMerge(result, newInterval);
         return result;
     }
 private:
     void MyMerge(vector<vector<int>>& result, const vector<int>& interval)
         if (result.empty())
              result.push_back(interval);
         else
         {
              int& end = result.back()[1];
              if (end < interval[0])
                  result.push_back(interval);
              else
                  end = max(end, interval[1]);
```

```
}
};
```

• Merge Intervals, 見 §16.4

16.4 Merge Intervals

描述

Given a collection of intervals, merge all overlapping intervals. For example, Given $\{[1,3],[2,6],[8,10],[15,18]\}$, return $\{[1,6],[8,10],[15,18]\}$

分析

複用一下 Insert Intervals 的解法即可,創建一個新的 interval 集合,然後每次從舊的裏面取一個 interval 出來、然後插入到新的集合中。

```
struct Interval {
    int start;
    int end;
    Interval() : start(0), end(0) { }
    Interval(int s, int e) : start(s), end(e) { }
};
//LeetCode, Merge Interval
//複用一下 Insert Intervals 的解法即可
// 時間複雜度 O(n1+n2+...), 空間複雜度 O(1)
class Solution {
public:
    vector<Interval> merge(vector<Interval> &intervals) {
        vector<Interval> result;
        for (int i = 0; i < intervals.size(); i++) {</pre>
            insert(result, intervals[i]);
        return result;
    }
private:
    vector<Interval> insert(vector<Interval> &intervals, Interval newInterval) {
        vector<Interval>::iterator it = intervals.begin();
        while (it != intervals.end()) {
            if (newInterval.end < it->start) {
                intervals.insert(it, newInterval);
                return intervals:
            } else if (newInterval.start > it->end) {
                it++;
```

```
continue;
              } else {
                  newInterval.start = min(newInterval.start, it->start);
                  newInterval.end = max(newInterval.end, it->end);
                  it = intervals.erase(it):
              }
         }
         intervals.insert(intervals.end(), newInterval);
         return intervals;
     }
 }:
代碼
 //LeetCode, Merge Interval
 // Sort it and always push back into a reserved vector
 // 時間複雜度 O(nlogn), 空間複雜度 O(n)
 class Solution {
 public:
     vector<vector<int>> merge(vector<vector<int>>& intervals) {
         // sort it first
         sort(intervals.begin(), intervals.end(), [&](const auto& first, const auto& second)
                  return first[0] < second[0];</pre>
              });
         vector<vector<int>> result;
         result.reserve(intervals.size());
         for (const auto& interval : intervals)
              mergeBack(result, interval);
         return result;
     }
 private:
     void mergeBack(vector<vector<int>>& result, const vector<int>& interval) {
          if (result.size() == 0) result.push_back(interval);
          int& start = result.back()[0];
         int& end = result.back()[1];
         if (interval[0] >= start && interval[0] <= end)</pre>
              end = max(end, interval[1]);
         else
              result.push_back(interval);
     }
 };
```

• Insert Interval, 見 §16.3

16.5 Minimum Window Substring

描述

Given a string S and a string T, find the minimum window in S which will contain all the characters in T in complexity O(n).

```
For example, S = "ADOBECODEBANC", T = "ABC" Minimum window is "BANC".

Note:
```

- If there is no such window in S that covers all characters in T, return the emtpy string "".
- If there are multiple such windows, you are guaranteed that there will always be only one unique minimum window in S.

分析

雙指針,動態維護一個區間。尾指針不斷往後掃,當掃到有一個窗口包含了所有 T 的字符後, 然後再收縮頭指針,直到不能再收縮為止。最後記錄所有可能的情況中窗口最小的

```
// LeetCode, Minimum Window Substring
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    string minWindow(string S, string T) {
        if (S.empty()) return "";
        if (S.size() < T.size()) return "";</pre>
        const int ASCII_MAX = 256;
        int appeared_count[ASCII_MAX];
        int expected_count[ASCII_MAX];
        fill(appeared_count, appeared_count + ASCII_MAX, 0);
        fill(expected_count, expected_count + ASCII_MAX, 0);
        for (size_t i = 0; i < T.size(); i++) expected_count[T[i]]++;</pre>
        int minWidth = INT_MAX, min_start = 0; // 窗口大小, 起點
        int wnd_start = 0;
        int appeared = 0; // 完整包含了一個 T
        //尾指針不斷往後掃
        for (size_t wnd_end = 0; wnd_end < S.size(); wnd_end++) {</pre>
            if (expected_count[S[wnd_end]] > 0) { // this char is a part of T
                appeared_count[S[wnd_end]]++;
                if (appeared_count[S[wnd_end]] <= expected_count[S[wnd_end]])</pre>
                    appeared++;
            }
            if (appeared == T.size()) { // 完整包含了一個 T
```

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```
// 收縮頭指針
                while (appeared_count[S[wnd_start]] > expected_count[S[wnd_start]]
                        || expected count[S[wnd start]] == 0) {
                    appeared_count[S[wnd_start]]--;
                    wnd_start++;
                }
                if (minWidth > (wnd_end - wnd_start + 1)) {
                    minWidth = wnd_end - wnd_start + 1;
                    min_start = wnd_start;
                }
            }
        }
        if (minWidth == INT MAX) return "";
        else return S.substr(min_start, minWidth);
    }
};
```

相關題目

• 無

16.6 Multiply Strings

描述

Given two numbers represented as strings, return multiplication of the numbers as a string.

Note: The numbers can be arbitrarily large and are non-negative.

分析

高精度乘法。

常見的做法是將字符轉化為一個 int, 一一對應, 形成一個 int 數組。但是這樣很浪費空間, 一個 int32 的最大值是 $2^{31}-1=2147483647$, 可以與 9 個字符對應, 由於有乘法, 減半, 則至少可以與 4 個字符一一對應。一個 int64 可以與 9 個字符對應。

```
}
 string to string(bigint const& n) {
     string str;
     transform(find_if(n.rbegin(), prev(n.rend()),
             [](char c) { return c > '\0'; }), n.rend(), back_inserter(str),
             [](char c) { return c + '0'; });
     return str;
 }
 bigint operator*(bigint const& x, bigint const& y) {
     bigint z(x.size() + y.size());
     for (size t i = 0; i < x.size(); ++i)
         for (size_t j = 0; j < y.size(); ++j) {</pre>
             z[i + j] += x[i] * y[j];
             z[i + j + 1] += z[i + j] / 10;
             z[i + j] \% = 10;
     return z;
 }
 class Solution {
 public:
     string multiply(string num1, string num2) {
         return to_string(make_bigint(num1) * make_bigint(num2));
 };
代碼 2
 // LeetCode, Multiply Strings
 // 9 個字符對應一個 int64_t
 // 時間複雜度 O(n*m/81), 空間複雜度 O((n+m)/9)
 /** 大整數類. */
 class BigInt {
 public:
     /**
      * @brief 構造函數, 將字符串轉化為大整數.
      * @param[in] s 輸入的字符串
      * @return 無
      */
     BigInt(string s) {
         vector<int64 t> result;
         result.reserve(s.size() / RADIX_LEN + 1);
         for (int i = s.size(); i > 0; i -= RADIX_LEN) { // [i-RADIX_LEN, i)
             int temp = 0;
             const int low = max(i - RADIX_LEN, 0);
             for (int j = low; j < i; j++) {
                 temp = temp * 10 + s[j] - '0';
```

```
result.push_back(temp);
       elems = result;
   }
   /**
     * @brief 將整數轉化為字符串.
    * @return 字符串
   string toString() {
       stringstream result;
       bool started = false; // 用於跳過前導 0
       for (auto i = elems.rbegin(); i != elems.rend(); i++) {
           if (started) { // 如果多餘的 O 已經都跳過, 則輸出
               result << setw(RADIX LEN) << setfill('0') << *i;
           } else {
               result << *i;
               started = true; // 碰到第一個非 0 的值, 就説明多餘的 0 已經都跳過
           }
       }
       if (!started) return "0"; // 當 x 全為 0 時
       else return result.str();
   }
   /**
    * @brief 大整數乘法.
    * @param[in] x x
    * @param[in] y y
    * @return 大整數
    */
   static BigInt multiply(const BigInt &x, const BigInt &y) {
       vector<int64_t> z(x.elems.size() + y.elems.size(), 0);
       for (size_t i = 0; i < y.elems.size(); i++) {
           for (size_t j = 0; j < x.elems.size(); j++) { // 用 y[i] 去乘以 x 的各位
               // 兩數第 i, j 位相乘, 累加到結果的第 i+j 位
               z[i + j] += y.elems[i] * x.elems[j];
               if (z[i + j] >= BIGINT_RADIX) { // 看是否要進位
                  z[i + j + 1] += z[i + j] / BIGINT_RADIX; // 進位
                  z[i + j] %= BIGINT_RADIX;
               }
           }
       while (z.back() == 0) z.pop_back(); // 沒有進位, 去掉最高位的 0
       return BigInt(z);
   }
private:
   typedef long long int64_t;
   /** 一個數組元素對應 9 個十進制位, 即數組是億進制的
```

```
* 因為 1000000000 * 1000000000 沒有超過 2~63-1
     */
    const static int BIGINT_RADIX = 1000000000;
    const static int RADIX_LEN = 9;
    /** 萬進制整數. */
    vector<int64_t> elems;
   BigInt(const vector<int64_t> num) : elems(num) {}
};
class Solution {
public:
    string multiply(string num1, string num2) {
        BigInt x(num1);
       BigInt y(num2);
        return BigInt::multiply(x, y).toString();
    }
}:
```

無

16.7 Substring with Concatenation of All Words

描述

You are given a string, S, and a list of words, L, that are all of the same length. Find all starting indices of substring(s) in S that is a concatenation of each word in L exactly once and without any intervening characters.

For example, given:

```
S: "barfoothefoobarman"
L: ["foo", "bar"]
```

You should return the indices: $\{[0,9]\}$. (order does not matter).

分析

無

```
// LeetCode, Substring with Concatenation of All Words
// 時間複雜度 O(n*m), 空間複雜度 O(m)
class Solution {
public:
    vector<int> findSubstring(string s, vector<string>& dict) {
        size_t wordLength = dict.front().length();
        size_t catLength = wordLength * dict.size();
        vector<int> result;
```

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相關題目

• 無

16.8 Pascal's Triangle

描述

```
Given numRows, generate the first numRows of Pascal's triangle. For example, given numRows=5, Return [ [1], [1,1], [1,2,1], [1,3,3,1], [1,4,6,4,1]
```

分析

本題可以用隊列,計算下一行時,給上一行左右各加一個 0,然後下一行的每個元素,就等於左上角和右上角之和。

另一種思路,下一行第一個元素和最後一個元素賦值為1,中間的每個元素,等於上一行的左上 角和右上角元素之和。

從左到右

```
// LeetCode, Pascal's Triangle
 // 時間複雜度 O(n^2), 空間複雜度 O(n)
 class Solution {
 public:
     vector<vector<int> > generate(int numRows) {
         vector<vector<int> > result;
         if(numRows == 0) return result;
         result.push_back(vector<int>(1,1)); //first row
         for(int i = 2; i <= numRows; ++i) {</pre>
             vector<int> current(i,1); // 本行
             const vector<int> &prev = result[i-2]; // 上一行
             for(int j = 1; j < i - 1; ++j) {
                 current[j] = prev[j-1] + prev[j]; // 左上角和右上角之和
             result.push_back(current);
         return result;
     }
 };
從右到左
 // LeetCode, Pascal's Triangle
 // 時間複雜度 O(n^2), 空間複雜度 O(n)
 class Solution {
 public:
     vector<vector<int> > generate(int numRows) {
         vector<vector<int> > result;
         vector<int> array;
         for (int i = 1; i <= numRows; i++) {
             for (int j = i - 2; j > 0; j--) {
                 array[j] = array[j - 1] + array[j];
             array.push_back(1);
             result.push_back(array);
         return result;
     }
 };
```

相關題目

• Pascal's Triangle II, 見 §??

16.9 Pascal's Triangle II

描述

```
Given an index k, return the k^{th} row of the Pascal's triangle.
   For example, given k = 3,
   Return \{[1,3,3,1]\}.
   Note: Could you optimize your algorithm to use only O(k) extra space?
分析
   滾動數組。
代碼
 // LeetCode, Pascal's Triangle II
 // 滾動數組, 時間複雜度 O(n<sup>2</sup>), 空間複雜度 O(n)
 class Solution {
 public:
   vector<int> getRow(int rowIndex) {
     vector<int> array;
     for (int i = 0; i <= rowIndex; i++) {
        for (int j = i - 1; j > 0; j--){
          array[j] = array[j - 1] + array[j];
        array.push_back(1);
     }
     return array;
   }
 };
搋歸
 // LeetCode, Pascal's Triangle II
 // 滾動數組, 時間複雜度 O(n<sup>2</sup>), 空間複雜度 O(n)
 class Solution {
 public:
      vector<int> getRow(int rowIndex) {
          vector<int> result;
          getRow(result, rowIndex, 0);
          return result;
      }
 private:
      void getRow(vector<int>& result, int rowIndex, int step) {
          if (step > rowIndex) return;
          for (int i = step - 1; i > 0; i--)
```

result[i] = result[i-1] + result[i];

result.push_back(1);

```
getRow(result, rowIndex, step+1);
};
```

• Pascal's Triangle, 見 §16.8

16.10 Spiral Matrix

描述

Given a matrix of $m \times n$ elements (m rows, n columns), return all elements of the matrix in spiral order. For example, Given the following matrix:

```
[ 1, 2, 3 ],
[ 4, 5, 6 ],
[ 7, 8, 9 ]
```

You should return [1,2,3,6,9,8,7,4,5].

分析

模擬。

```
// LeetCode, Spiral Matrix
// @author 龔陸安 (http://weibo.com/luangong)
// 時間複雜度 O(n^2), 空間複雜度 O(1)
class Solution {
public:
    vector<int> spiralOrder(vector<vector<int> >& matrix) {
        vector<int> result;
        if (matrix.empty()) return result;
        int beginX = 0, endX = matrix[0].size() - 1;
        int beginY = 0, endY = matrix.size() - 1;
        while (true) {
            // From left to right
            for (int j = beginX; j <= endX; ++j) result.push_back(matrix[beginY][j]);</pre>
            if (++beginY > endY) break;
            // From top to bottom
            for (int i = beginY; i <= endY; ++i) result.push_back(matrix[i][endX]);</pre>
            if (beginX > --endX) break;
            // From right to left
            for (int j = endX; j >= beginX; --j) result.push_back(matrix[endY][j]);
            if (beginY > --endY) break;
            // From bottom to top
```

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```
for (int i = endY; i >= beginY; --i) result.push_back(matrix[i][beginX]);
    if (++beginX > endX) break;
}
    return result;
};
```

相關題目

• Spiral Matrix II , 見 §16.11

16.11 Spiral Matrix II

描述

```
Given an integer n, generate a square matrix filled with elements from 1 to n^2 in spiral order.
```

For example, Given n = 3,

You should return the following matrix:

```
[ 1, 2, 3 ], [ 8, 9, 4 ], [ 7, 6, 5 ]
```

分析

這題比上一題要簡單。

```
// LeetCode, Spiral Matrix II
// 時間複雜度 O(n^2), 空間複雜度 O(n^2)
class Solution {
public:
    vector<vector<int> > generateMatrix(int n) {
        vector<vector<int> > matrix(n, vector<int>(n));
        int begin = 0, end = n - 1;
        int num = 1;
        while (begin < end) {
            for (int j = begin; j < end; ++j) matrix[begin][j] = num++;</pre>
            for (int i = begin; i < end; ++i) matrix[i][end] = num++;</pre>
            for (int j = end; j > begin; --j) matrix[end][j] = num++;
            for (int i = end; i > begin; --i) matrix[i][begin] = num++;
            ++begin;
            --end;
        }
        if (begin == end) matrix[begin][begin] = num;
```

```
return matrix;
     }
 };
代碼 2
 // LeetCode, Spiral Matrix II
 // @author 龔陸安 (http://weibo.com/luangong)
 // 時間複雜度 O(n^2), 空間複雜度 O(n^2)
 class Solution {
 public:
     vector<vector<int> > generateMatrix(int n) {
         vector< vector<int> > matrix(n, vector<int>(n));
         if (n == 0) return matrix;
         int beginX = 0, endX = n - 1;
         int beginY = 0, endY = n - 1;
         int num = 1:
         while (true) {
              for (int j = beginX; j <= endX; ++j) matrix[beginY][j] = num++;</pre>
              if (++beginY > endY) break;
              for (int i = beginY; i <= endY; ++i) matrix[i][endX] = num++;</pre>
              if (beginX > --endX) break;
              for (int j = endX; j >= beginX; --j) matrix[endY][j] = num++;
              if (beginY > --endY) break;
              for (int i = endY; i >= beginY; --i) matrix[i][beginX] = num++;
              if (++beginX > endX) break;
         }
         return matrix;
     }
 };
```

• Spiral Matrix, 見 §16.10

16.12 ZigZag Conversion

描述

The string "PAYPALISHIRING" is written in a zigzag pattern on a given number of rows like this: (you may want to display this pattern in a fixed font for better legibility)

```
P A H N
A P L S I I G
Y I R
```

And then read line by line: "PAHNAPLSIIGYIR"

Write the code that will take a string and make this conversion given a number of rows:

```
string convert(string text, int nRows);
convert("PAYPALISHIRING", 3) should return "PAHNAPLSIIGYIR".
```

分析

要找到數學規律。真正面試中,不大可能出這種問題。

```
n=4:
Р
     Ι
           N
  L S
         ΙG
Y A H R
     Ι
 n=5:
Р
       Η
     SI
Y
   Ι
       R
ΡL
       I G
       N
```

所以,對於每一層垂直元素的座標 (i,j) = (j+1)*n+i; 對於每兩層垂直元素之間的插入元素 (斜對角元素), (i,j) = (j+1)*n-i

代碼

```
// LeetCode, ZigZag Conversion
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    string convert(string s, int nRows) {
        if (nRows <= 1 || s.size() <= 1) return s;
        string result;
        for (int i = 0; i < nRows; i++) {
            for (int j = 0, index = i; index < s.size();</pre>
                    j++, index = (2 * nRows - 2) * j + i) {
                result.append(1, s[index]); // 垂直元素
                                                          // 斜對角元素
                if (i == 0 \mid | i == nRows - 1) continue;
                if (index + (nRows - i - 1) * 2 < s.size())
                    result.append(1, s[index + (nRows - i - 1) * 2]);
            }
        }
        return result;
    }
};
```

相關題目

• 無

16.13 Divide Two Integers

描述

Divide two integers without using multiplication, division and mod operator.

分析

不能用乘、除和取模,那剩下的,還有加、減和位運算。

最簡單的方法,是不斷減去被除數。在這個基礎上,可以做一點優化,每次把被除數翻倍,從 而加速。

```
// LeetCode, Divide Two Integers
 // 時間複雜度 O(logn), 空間複雜度 O(1)
 class Solution {
 public:
     int divide(int dividend, int divisor) {
         // 當 dividend = INT_MIN 時, -dividend 會溢出, 所以用 long long
         long long a = dividend >= 0 ? dividend : -(long long)dividend;
         long long b = divisor >= 0 ? divisor : -(long long)divisor;
         // 當 dividend = INT_MIN 時, divisor = -1 時, 結果會溢出, 所以用 long long
         long long result = 0;
         while (a >= b) {
             long long c = b;
             for (int i = 0; a >= c; ++i, c <<= 1) {
                 a -= c;
                 result += 1 << i;
         }
         return ((dividend^divisor) >> 31) ? (-result) : (result);
     }
 };
代碼 2
 // LeetCode, Divide Two Integers
 // 時間複雜度 O(logn), 空間複雜度 O(1)
 class Solution {
 public:
     int divide(int dividend, int divisor) {
         int result = 0; // 當 dividend = INT_MIN 時, divisor = -1 時, 結果會溢出
         const bool sign = (dividend > 0 && divisor < 0) ||</pre>
                 (dividend < 0 && divisor > 0); // 異號
         // 當 dividend = INT_MIN 時, -dividend 會溢出, 所以用 unsigned int
```

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```
unsigned int a = dividend >= 0 ? dividend : -dividend;
        unsigned int b = divisor >= 0 ? divisor : -divisor;
        while (a >= b) {
            int multi = 1;
            unsigned int bb = b;
            while (a >= bb) {
                a -= bb;
                result += multi;
                if (bb < INT_MAX >> 1) { // 防止溢出
                    bb += bb;
                    multi += multi;
                }
            }
        }
        if (sign) return -result;
        else return result;
    }
};
```

相關題目

• 無

16.14 Text Justification

描述

Given an array of words and a length L, format the text such that each line has exactly L characters and is fully (left and right) justified.

You should pack your words in a greedy approach; that is, pack as many words as you can in each line. Pad extra spaces ' ' when necessary so that each line has exactly L characters.

Extra spaces between words should be distributed as evenly as possible. If the number of spaces on a line do not divide evenly between words, the empty slots on the left will be assigned more spaces than the slots on the right.

For the last line of text, it should be left justified and no extra space is inserted between words.

For example,

words:

```
"This", "is", "an", "example", "of", "text", "justification."
```

```
L: 16.

Return the formatted lines as:

[

"This is an",

"example of text",
```

```
"justification. "
```

Note: Each word is guaranteed not to exceed L in length.

Corner Cases:

- A line other than the last line might contain only one word. What should you do in this case?
- In this case, that line should be left

分析

無

```
// LeetCode, Text Justification
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
   vector<string> fullJustify(vector<string> &words, int L) {
       vector<string> result;
       const int n = words.size();
       int begin = 0, len = 0; // 當前行的起點, 當前長度
       for (int i = 0; i < n; ++i) {
           if (len + words[i].size() + (i - begin) > L) {
               result.push_back(connect(words, begin, i - 1, len, L, false));
               begin = i;
               len = 0;
           }
           len += words[i].size();
       // 最後一行不足 L
       result.push_back(connect(words, begin, n - 1, len, L, true));
       return result;
   }
   /**
     * @brief 將 words[begin, end] 連成一行
     * Oparam[in] words 單詞列表
     * @param[in] begin 開始
     * @param[in] end 結束
     * Oparam[in] len words[begin, end] 所有單詞加起來的長度
     * @param[in] L 題目規定的一行長度
     * @param[in] is_last 是否是最後一行
     * @return 對齊後的當前行
    string connect(vector<string> &words, int begin, int end,
           int len, int L, bool is_last) {
       string s;
       int n = end - begin + 1;
       for (int i = 0; i < n; ++i) {
```

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```
s += words[begin + i];
           addSpaces(s, i, n - 1, L - len, is last);
        }
        if (s.size() < L) s.append(L - s.size(), ' ');</pre>
        return s;
    }
    /**
     * @brief 添加空格.
     * @param[inout]s 一行
     * Oparam[in] i 當前空隙的序號
     * Oparam[in] n 空隙總數
     * @param[in] L 總共需要添加的空額數
     * Oparam[in] is_last 是否是最後一行
     * @return 無
     */
    void addSpaces(string &s, int i, int n, int L, bool is_last) {
        if (n < 1 || i > n - 1) return;
        int spaces = is_last ? 1 : (L / n + (i < (L % n) ? 1 : 0));</pre>
        s.append(spaces, ' ');
   }
};
```

相關題目

• 無

16.15 Max Points on a Line

描述

Given n points on a 2D plane, find the maximum number of points that lie on the same straight line.

分析

暴力枚舉法。兩點決定一條直線,n 個點兩兩組合,可以得到 $\frac{1}{2}n(n+1)$ 條直線,對每一條直線,判斷 n 個點是否在該直線上,從而可以得到這條直線上的點的個數,選擇最大的那條直線返回。複雜度 $O(n^3)$ 。

上面的暴力枚舉法以"邊"為中心,再看另一種暴力枚舉法,以每個"點"為中心,然後遍歷剩餘點,找到所有的斜率,如果斜率相同,那麼一定共線對每個點,用一個哈希表,key 為斜率,value 為該直線上的點數,計算出哈希表後,取最大值,並更新全局最大值,最後就是結果。時間複雜度 $O(n^2)$,空間複雜度 O(n)。

以邊為中心

```
// LeetCode, Max Points on a Line
// 暴力枚舉法,以邊為中心,時間複雜度 O(n^3),空間複雜度 O(1)
```

```
class Solution {
 public:
     int maxPoints(vector<Point> &points) {
         if (points.size() < 3) return points.size();</pre>
         int result = 0;
         for (int i = 0; i < points.size() - 1; i++) {</pre>
             for (int j = i + 1; j < points.size(); j++) {</pre>
                 int sign = 0;
                  int a, b, c;
                  if (points[i].x == points[j].x) sign = 1;
                  else {
                      a = points[j].x - points[i].x;
                      b = points[j].y - points[i].y;
                      c = a * points[i].y - b * points[i].x;
                 }
                 int count = 0;
                 for (int k = 0; k < points.size(); k++) {
                      if ((0 == sign \&\& a * points[k].y == c + b * points[k].x) ||
                          (1 == sign\&&points[k].x == points[j].x))
                          count++;
                  if (count > result) result = count;
             }
         }
         return result;
 };
以點為中心
 // LeetCode, Max Points on a Line
 // 暴力枚舉, 以點為中心, 時間複雜度 O(n^2), 空間複雜度 O(n)
 class Solution {
 public:
     int maxPoints(vector<Point> &points) {
         if (points.size() < 3) return points.size();</pre>
         int result = 0;
         unordered_map<double, int> slope_count;
         for (int i = 0; i < points.size()-1; i++) {</pre>
             slope_count.clear();
              int samePointNum = 0; // 與i 重合的點
                                   // 和i共線的最大點數
              int point_max = 1;
             for (int j = i + 1; j < points.size(); j++) {
                  double slope; // 斜率
                  if (points[i].x == points[j].x) {
                      slope = std::numeric_limits<double>::infinity();
                      if (points[i].y == points[j].y) {
                          ++ samePointNum;
                          continue;
```

```
}
                } else {
                     slope = 1.0 * (points[i].y - points[j].y) /
                         (points[i].x - points[j].x);
                }
                int count = 0;
                 if (slope count.find(slope) != slope count.end())
                     count = ++slope_count[slope];
                 else {
                     count = 2;
                     slope_count[slope] = 2;
                }
                if (point_max < count) point_max = count;</pre>
            }
            result = max(result, point_max + samePointNum);
        return result;
    }
};
```

相關題目

• 無

16.16 Calculate Number of Weeks

描述

Gvien a year, start month, end month and the first week day of that year. Calculate the maximum number of weeks that is included. A week must start from Monday to Sunday. There has 29 day in February when the year can be multiple by 4.

分析

Nil

代碼

```
class Solution
{
public:
    Solution() { PrepareDB(); }
    ~Solution() {}

    int numOfWeeks(int Y, const string& A, const string& B, const string& W)
    {
        int startMon = m_strMon2Int[A];
        int endMon = m_strMon2Int[B];
    }
}
```

```
int yearStartWeekDay = m strWeek2Int[W];
        // Get the date of first Monday
        int startDay = GetFirstMonday(Y, startMon, yearStartWeekDay);
        // Get the date of last Sunday
        int endDay = GetLastSunday(Y, endMon, yearStartWeekDay);
        // Get the total of days
        int dayDiff = GetDayDiff(Y, startMon, startDay, endMon, endDay);
        // return answer
        return (dayDiff + 1) / 7;
    }
private:
    int GetFirstMonday(int Y, int Mon, int yearStartWeekDay)
        int dayDiff = GetDayDiff(Y, 1, 1, Mon, 1);
        dayDiff %= 7;
        int wday = (yearStartWeekDay + dayDiff) % 7;
        int curDay = 1;
        while (wday != 1)
            curDay++;
            wday++;
            wday %= 7;
        return curDay;
    int GetLastSunday(int Y, int Mon, int yearStartWeekDay)
        int dayDiff = GetDayDiff(Y, 1, 1, Mon, GetMonLength(Y, Mon));
        dayDiff %= 7;
        int wday = (yearStartWeekDay + dayDiff) % 7;
        int curDay = GetMonLength(Y, Mon);
        while (wday != 0)
        {
            curDay--;
            wday--;
            if (wday == -1) wday = 6;
        return curDay;
    int GetDayDiff(int Y, int firstMon, int firstDate, int secondMon, int secondDate)
        int result = 0;
        for (int i = firstMon; i < secondMon; i++)</pre>
        {
            if (i == firstMon)
                result += GetMonLength(Y, i) - firstDate + 1;
            else
                result += GetMonLength(Y, i);
        result += secondDate;
```

```
return result - 1;
    }
    int GetMonLength(int Y, int Mon)
        if (Mon == 2)
        {
            if (Y \% 4 == 0)
                 return 29;
            else
                 return 28;
        }
        else
            return m_Mon2Length[Mon];
    }
    void PrepareDB()
    {
        m_strMon2Int["January"] = 1;
        m_strMon2Int["February"] = 2;
        m_strMon2Int["March"] = 3;
        m_strMon2Int["April"] = 4;
        m_strMon2Int["May"] = 5;
        m_strMon2Int["June"] = 6;
        m_strMon2Int["July"] = 7;
        m_strMon2Int["August"] = 8;
        m_strMon2Int["September"] = 9;
        m_strMon2Int["October"] = 10;
        m_strMon2Int["November"] = 11;
        m_strMon2Int["December"] = 12;
        m_Mon2Length[1] = 31;
        m_{Mon2Length[3]} = 31;
        m_{Mon2Length[4]} = 30;
        m_{Mon2Length[5]} = 31;
        m_Mon2Length[6] = 30;
        m_{\text{Mon2Length}}[7] = 31;
        m_Mon2Length[8] = 31;
        m_{Mon2Length}[9] = 30;
        m_{Mon2Length[10]} = 31;
        m_{Mon2Length[11]} = 30;
        m_{Mon2Length[12]} = 31;
        m_strWeek2Int["Monday"] = 1;
        m_strWeek2Int["Tuesday"] = 2;
        m_strWeek2Int["Wednesday"] = 3;
        m_strWeek2Int["Thursday"] = 4;
        m_strWeek2Int["Friday"] = 5;
        m_strWeek2Int["Saturday"] = 6;
        m_strWeek2Int["Sunday"] = 0;
private:
    unordered_map<string, int> m_strMon2Int;
    unordered_map<int, int> m_Mon2Length;
```

```
unordered_map<string, int> m_strWeek2Int;
};
相關題目
```

16.17 Integer to English Words

描述

Bloomberg questions

Input: 123

Output: One Hundred Twenty Three

分析

Nil

代碼

```
class Solution
public:
    string numberToWords(int num) {
        if (num == 0) return "Zero";
        const vector<string> bigUnit{"","Thousand","Million","Billion"};
        const vector<string> strNum{"","One","Two","Three","Four","Five"
          ,"Six", "Seven", "Eight", "Nine"
          ,"Ten","Eleven","Twelve","Thirteen"
          , "Fourteen", "Fifteen", "Sixteen", "Seventeen", "Eighteen", "Nineteen");
        const vector<string> str10Num{"","","Twenty","Thirty","Forty"
          ,"Fifty","Sixty","Seventy","Eighty","Ninety"};
        string result;
        while (num > 0) {
            int t = num;
            int step = 0;
            int d = 1; // one unit
            while (t \ge 1000) {
                t /= 1000;
                d *= 1000;
                step++;
            }
            int u3 = t / 100; t %= 100;
            if (t > 19) {
```

```
int u2 = t / 10; t \% = 10;
                int u1 = t;
                if (u3 > 0)
                    result += " " + strNum[u3] + " " + "Hundred";
                result += " " + str10Num[u2];
                // prevent edge case, example 20, u1 == 0
                if (u1 > 0) result += " " + strNum[u1];
            }
            else {
                if (u3 > 0)
                    result += " " + strNum[u3] + " " + "Hundred";
                if (t != 0)
                    result += " " + strNum[t];
            // handle big unit
            if (step > 0) result += " " + bigUnit[step];
            if (num < 1000) break;
            num %= d;
        }
        return result.substr(1, result.size() - 1);
    }
};
```

相關題目

16.18 String Compression

描述

```
Bloomberg questions

Example 1:
Input:
    ["a","a","b","b","c","c","c"]

Output:
    Return 6, and the first 6 characters of the
        input array should be: ["a","2","b","2","c","3"]

Explanation:
    "aa" is replaced by "a2". "bb" is replaced by "b2". "ccc" is replaced by "c3".

Example 2:
Input:
    ["a"]

Output:
    Return 1, and the first 1 characters of the input array should be: ["a"]
```

```
Explanation:
     Nothing is replaced.
分析
   Nil
代碼
 class Solution
 public:
     int compress(vector<char>& chars) {
          auto PushNum = [&](int& count, int& index)
              int d = 1;
              while (count / d >= 10) // find the largest decimal
                  d *= 10;
              while (d > 0)
                  chars[index++] = (char)(count / d + '0');
                  count %= d;
                  d /= 10;
              }
         };
         // use 2 pointers
          int count = 1;
          int index = 0;
          for (int i = 1; i < (int)chars.size(); i++)</pre>
          {
              if (chars[i] == chars[i-1])
              {
                  count++;
              }
              else
                  chars[index++] = chars[i-1];
                  if (count != 1)
                      // get num to char
                      PushNum(count, index);
                      count = 1;
                  }
              }
          }
          chars[index++] = chars.back();
          if (count > 1)
              PushNum(count, index);
          return index;
```

};

相關題目

16.19 Diagonal Traverse

16.19.1 描述

Given a matrix of M x N elements (M rows, N columns), return all elements of the matrix in diagonal order as shown in the below image.

Input: [[1, 2, 3], [4, 5, 6], [7, 8, 9]] Output: [1,2,4,7,5,3,6,8,9] Explanation:

图 16-1 Diagonal Traverse

Note: The total number of elements of the given matrix will not exceed 10,000.

16.19.2 分析

Nil

16.19.3 代碼

```
// LeetCode
 // 時間複雜度 D(), 空間複雜度 D()
 class Solution {
 public:
     vector<int> findDiagonalOrder(vector<vector<int>>& matrix) {
         int M = matrix.size();
         if (M == 0) return vector<int>();
         int N = matrix[0].size();
         if (N == 0) return vector<int>();
         vector<int> result; result.reserve(M + N);
         for (int d = 0; d < M + N - 1; d++) {
             int r = (d < N) ? 0 : d - N + 1;
             int c = (d < N) ? d : N - 1;
             vector<int> row;
             while (r < M \&\& c > -1)
             {
                 row.push_back(matrix[r][c]);
                 r++;
                 c--;
             }
             if (d % 2 == 0) reverse(row.begin(), row.end());
             result.insert(result.end(), row.begin(), row.end());
         return result;
     }
 };
16.19.4
          代碼
 // LeetCode
 // 時間複雜度 D(), 空間複雜度 D()
 class Solution {
 public:
     vector<int> findDiagonalOrder(vector<vector<int>>& matrix) {
          if(matrix.empty()) return {};
         int m = matrix.size(), n = matrix[0].size();
         vector<int> res(m * n);
         for(int i = 0, r = 0, c = 0; i < m * n; i++) {
             res[i] = matrix[r][c];
             if((r + c) \% 2 == 0) {
                  if(c == n - 1) r++;
                 else if(r == 0) c++;
                 else r--, c++;
             } else {
                 if(r == m - 1) c++;
                 else if(c == 0) r++;
```

```
else r++, c--;
}

return res;
}
```

第 17 章 字首樹 Trie

Things related to Trie data structure.

17.1 Implement Trie (Prefix Tree)

描述

Implement a trie with insert, search, and startsWith methods.

Example:

```
Trie trie = new Trie();

trie.insert("apple");
trie.search("apple");  // returns true
trie.search("app");  // returns false
trie.startsWith("app");  // returns true
trie.insert("app");
trie.search("app");  // returns true
```

Note:

- You may assume that all inputs are consist of lowercase letters a-z.
- All inputs are guaranteed to be non-empty strings.

代碼

```
// 時間複雜度 O(), 空間複雜度 O()
struct TrieNode {
    bool flag;
    map<char, TrieNode*> next;
};
class Trie {
private:
    TrieNode* root;

public:
    /** Initialize your data structure here. */
    Trie() {
        root = new TrieNode();
}
```

17.2 Map Sum Pairs 435

```
/** Inserts a word into the trie. */
    void insert(string word) {
        TrieNode* p = root;
        for (int i = 0; i < word.length(); ++i) {
            if ((p->next).count(word[i]) <= 0) {</pre>
                // insert a new node if the path does not exist
                 (p->next).insert(make_pair(word[i], new TrieNode()));
            p = (p->next)[word[i]];
        p->flag = true;
    }
    /** Returns if the word is in the trie. */
    bool search(string word) {
        TrieNode* p = root;
        for (int i = 0; i < word.length(); ++i) {
            if ((p->next).count(word[i]) <= 0) {</pre>
                return false;
            p = (p->next)[word[i]];
        return p->flag;
    }
    /** Returns if there is any word in the trie that starts with the given prefix. */
    bool startsWith(string prefix) {
        TrieNode* p = root;
        for (int i = 0; i < prefix.length(); ++i) {</pre>
            if ((p->next).count(prefix[i]) <= 0) {</pre>
                return false;
            p = (p->next)[prefix[i]];
        return true;
    }
};
/**
 * Your Trie object will be instantiated and called as such:
 * Trie obj = new Trie();
 * obj.insert(word);
 * bool param_2 = obj.search(word);
 * bool param_3 = obj.startsWith(prefix);
 */
```

17.2 Map Sum Pairs

描述

Implement a MapSum class with insert, and sum methods.

For the method insert, you'll be given a pair of (string, integer). The string represents the key and the

integer represents the value. If the key already existed, then the original key-value pair will be overridden to the new one.

For the method sum, you'll be given a string representing the prefix, and you need to return the sum of all the pairs' value whose key starts with the prefix.

Example 1:

```
Input: insert("apple", 3), Output: Null
Input: sum("ap"), Output: 3
Input: insert("app", 2), Output: Null
Input: sum("ap"), Output: 5
```

分析

- 1. 暴力, 先記低每一個加入的文字和其數值, 當要求總加時, 歷遍所有
- 2. 利用字首樹

字首樹

```
// 時間複雜度 O(k), 空間複雜度 O(n)
class MapSum {
public:
    /** Initialize your data structure here. */
    MapSum() {
    }
    void insert(string key, int val) {
        TrieNode *p = &m_root;
        // delta 是關鍵,用來解決 value replacement 的問題。
        int delta = val - m_cache[key];
        m_cache[key] = val;
        for (const auto& c : key)
        {
            if ((p\rightarrow m_next).count(c) \le 0)
                (p->m_next).emplace(c, new TrieNode());
            p = (p->m_next)[c];
            p->m_val += delta;
        }
    }
    int sum(string prefix) {
        TrieNode *p = &m_root;
        for (const char& c : prefix)
            if ((p->m_next).count(c) <= 0)
                return 0;
            p = (p->m_next)[c];
```

17.3 Replace Words 437

```
return p->m_val;
}
private:
    TrieNode m_root;
    unordered_map<string, int> m_cache;
};

/**
    * Your MapSum object will be instantiated and called as such:
    * MapSum* obj = new MapSum();
    * obj->insert(key,val);
    * int param_2 = obj->sum(prefix);
    */
```

17.3 Replace Words

描述

In English, we have a concept called root, which can be followed by some other words to form another longer word - let's call this word successor. For example, the root an, followed by other, which can form another word another.

Now, given a dictionary consisting of many roots and a sentence. You need to replace all the successor in the sentence with the root forming it. If a successor has many roots can form it, replace it with the root with the shortest length.

You need to output the sentence after the replacement.

```
Example 1:
```

```
Input: dict = ["cat","bat","rat"], sentence = "the cattle was rattled by the battery"
Output: "the cat was rat by the bat"
```

Constraints:

- The input will only have lower-case letters.
- 1 <= dict.length <= 1000
- 1 <= dict[i].length <= 100
- 1 <= sentence words number <= 1000
- 1 <= sentence words length <= 1000

暴力計算

```
// 時間複雜度 O(sum of all w^2), 空間複雜度 O(n)
// 先記低全部 prefix, 然後每個文子, 每個 substring 都檢查一次並且取代原本的文字。
class Solution {
public:
    string replaceWords(vector<string>& dict, string sentence) {
    unordered_set<string> prefixDict(dict.begin(), dict.end());
```

```
string result;
          bool isFirst = true;
          for (const string& word : GetVec(sentence))
          {
              string tmp;
              for (const char& w : word)
                  tmp += w;
                  if (prefixDict.count(tmp) > 0)
                      break;
              if (isFirst)
                  result += tmp;
              else
                  result += " " + tmp;
              isFirst = false;
          return result;
      }
 private:
      vector<string> GetVec(const string& sentence)
          vector<string> result;
          for (auto i = sentence.begin(); i != sentence.end(); )
              i = find_if(i, sentence.end(), [&](const char& c){ return (c >= 'a' && c <= 'z');</pre>
              if (i == sentence.end()) return result;
              auto j = find_if(i, sentence.end(), [&](const char& c){ return c == ' '; });
              result.push_back(string(i, j));
              i = j;
          return result;
      }
 };
Tier
  // 時間複雜度 O(k), 空間複雜度 O(n)
 struct TrieNode
      bool m_isWord;
      unordered_map<char, TrieNode*> m_next;
      TrieNode () { m_isWord = false; };
 };
 class Solution {
 public:
      string replaceWords(vector<string>& dict, string sentence) {
          // 造字首樹
```

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```
TrieNode root;
        for (const string& s : dict)
            TrieNode *p = &root;
            // 每一個字母
            for (const char& c : s)
                if (p->m_next.count(c) <= 0) p->m_next.insert(make_pair(c, new TrieNode));
                p = p-m_next[c];
                if (p->m_isWord) break; // 剪枝, 當已經有 prefix 存在
            p->m_isWord = true;
        }
        string result;
        bool isFirst = true;
        for (const string& word : GetVec(sentence, ' '))
            string tmp = GetByPrefix(root, word);
            if (isFirst)
                result += tmp;
            else
                result += " " + tmp;
            isFirst = false;
        return result;
    }
private:
    vector<string> GetVec(const string& sentence, char delimiter)
    {
        string result;
        vector<string> res;
        istringstream iss(sentence);
        while (getline(iss, result, delimiter)) {
            res.push_back(result);
        return res;
    }
    string GetByPrefix(const TrieNode& root, const string& word)
    {
        string result;
        TrieNode const * p = &root;
        for (const char& c : word)
        {
            result += c;
            auto it = p->m_next.find(c);
            if (it != p->m_next.end())
            {
                p = it->second;
                if (p->m_isWord) return result;
            }
            else
```

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```
return word;
}
return word;
};
```

17.4 Design Search Autocomplete System

描述

Design a search autocomplete system for a search engine. Users may input a sentence (at least one word and end with a special character '#'). For each character they type except '#', you need to return the top 3 historical hot sentences that have prefix the same as the part of sentence already typed. Here are the specific rules:

- The hot degree for a sentence is defined as the number of times a user typed the exactly same sentence before
- The returned top 3 hot sentences should be sorted by hot degree (The first is the hottest one). If several sentences have the same degree of hot, you need to use ASCII-code order (smaller one appears first).
- If less than 3 hot sentences exist, then just return as many as you can.
- When the input is a special character, it means the sentence ends, and in this case, you need to return
 an empty list.

Your job is to implement the following functions:

The constructor function:

AutocompleteSystem(String[] sentences, int[] times): This is the constructor. The input is historical data. Sentences is a string array consists of previously typed sentences. Times is the corresponding times a sentence has been typed. Your system should record these historical data.

Now, the user wants to input a new sentence. The following function will provide the next character the user types:

List<String> input(char c): The input c is the next character typed by the user. The character will only be lower-case letters ('a' to 'z'), blank space ('') or a special character ('#'). Also, the previously typed sentence should be recorded in your system. The output will be the top 3 historical hot sentences that have prefix the same as the part of sentence already typed.

Example: Operation: AutocompleteSystem(["i love you", "island", "ironman", "i love leetcode"], [5,3,2,2]) The system have already tracked down the following sentences and their corresponding times: "i love you": 5 times "island": 3 times "ironman": 2 times "i love leetcode": 2 times Now, the user begins another search:

Operation: input('i') Output: ["i love you", "island","i love leetcode"] Explanation: There are four sentences that have prefix "i". Among them, "ironman" and "i love leetcode" have same hot degree. Since '

' has ASCII code 32 and 'r' has ASCII code 114, "i love leetcode" should be in front of "ironman". Also we only need to output top 3 hot sentences, so "ironman" will be ignored.

Operation: input(' ') Output: ["i love you","i love leetcode"] Explanation: There are only two sentences that have prefix "i".

Operation: input('a') Output: [] Explanation: There are no sentences that have prefix "i a".

Operation: input('#') Output: [] Explanation: The user finished the input, the sentence "i a" should be saved as a historical sentence in system. And the following input will be counted as a new search.

暴力計算

```
// 時間複雜度 O(k * 1), 空間複雜度 O(n + mlogm)
class AutocompleteSystem {
public:
    AutocompleteSystem(vector<string>& sentences, vector<int>& times) {
        if (sentences.size() == times.size())
        {
           // 記低每個字句的出現次數
           for (size_t i = 0; i < sentences.size(); i++)</pre>
               m_cache.emplace(sentences[i], times[i]);
        }
    }
    vector<string> input(char c) {
        if (c == '#')
        {
           m_cache[m_curSentence] += 1;
           m_curSentence = "";
           return vector<string>();
        else
        {
           m_curSentence += c;
           vector<pair<string, int>> resultCount;
           // 歷遍每一個 sentence 找出 prefix
           for (const auto& [k, v] : m_cache)
           {
               // 找尋 prefix
                if (k.find(m_curSentence) == 0)
                   resultCount.emplace_back(k, v);
           }
           sort(resultCount.begin(), resultCount.end()
                  [&](const auto& left, const auto& right)
                    // 先比較出現次數的多少
                    if (left.second == right.second)
                    {
```

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```
// 後比較文字的先後
                         return left.first < right.first;</pre>
                     }
                     else
                         return left.second > right.second;
                 });
            vector<string> result; result.reserve(3);
            int loop = 0;
            for (const auto& [str, count] : resultCount)
                result.push_back(str);
                if (++loop >= 3) break;
            }
            return result;
        }
    }
private:
    unordered_map<string, int> m_cache;
    string m_curSentence;
};
```

Google interview questions

18.1 Odd Even Jump

描述

You are given an integer array A. From some starting index, you can make a series of jumps. The (1st, 3rd, 5th, ...) jumps in the series are called odd numbered jumps, and the (2nd, 4th, 6th, ...) jumps in the series are called even numbered jumps.

You may from index i jump forward to index j (with i < j) in the following way:

During odd numbered jumps (ie. jumps 1, 3, 5, ...), you jump to the index j such that $A[i] \le A[j]$ and A[j] is the smallest possible value. If there are multiple such indexes j, you can only jump to the smallest such index j. During even numbered jumps (ie. jumps 2, 4, 6, ...), you jump to the index j such that $A[i] \ge A[j]$ and A[j] is the largest possible value. If there are multiple such indexes j, you can only jump to the smallest such index j. (It may be the case that for some index i, there are no legal jumps.) A starting index is good if, starting from that index, you can reach the end of the array (index A.length - 1) by jumping some number of times (possibly 0 or more than once.)

Return the number of good starting indexes.

```
Example 1:

Input: [10,13,12,14,15]
Output: 2

Explanation:

From starting index i = 0, we can jump to i = 2 (since A[2] is the smallest among A[1], A[2], From starting index i = 1 and i = 2, we can jump to i = 3, then we can't jump any more.

From starting index i = 3, we can jump to i = 4, so we've reached the end.

From starting index i = 4, we've reached the end already.

In total, there are 2 different starting indexes (i = 3, i = 4) where we can reach the end with Example 2:

Input: [2,3,1,1,4]
```

Output: 3
Explanation:
From starting index i = 0, we make jumps to i = 1, i = 2, i = 3:

```
During our 1st jump (odd numbered), we first jump to i = 1 because A[1] is the smallest value
 During our 2nd jump (even numbered), we jump from i = 1 to i = 2 because A[2] is the largest v
 During our 3rd jump (odd numbered), we jump from i = 2 to i = 3 because A[3] is the smallest v
 We can't jump from i = 3 to i = 4, so the starting index i = 0 is not good.
 In a similar manner, we can deduce that:
 From starting index i = 1, we jump to i = 4, so we reach the end.
 From starting index i = 2, we jump to i = 3, and then we can't jump anymore.
 From starting index i = 3, we jump to i = 4, so we reach the end.
 From starting index i = 4, we are already at the end.
 In total, there are 3 different starting indexes (i = 1, i = 3, i = 4) where we can reach the
   Example 3:
 Input: [5,1,3,4,2]
 Output: 3
 Explanation:
 We can reach the end from starting indexes 1, 2, and 4.
動規 - Monotonic Stack
 // 思路: 先求得單和雙數往後跳的目的地, 再用動規, 得知由某點能否跳往目的地
 // 時間複雜度 O(nlogn), 空間複雜度 O(n)
 class Solution {
 public:
     int oddEvenJumps(vector<int>& A) {
         vector<pair<int, int>> cache; cache.reserve(A.size());
         for (int i = 0; i < A.size(); i++)
             cache.emplace_back(A[i], i);
         // 找尋增大順序的下標
         sort(cache.begin(), cache.end()
                [&] (const auto& left, const auto& right)
                  if (left.first == right.first)
                      return left.second < right.second;</pre>
                  else
                      return left.first < right.first;</pre>
              });
         vector<int> sortedIndex;
         sortedIndex.reserve(cache.size());
         for_each(cache.begin(), cache.end()
                 , [&](const auto& ele) { sortedIndex.push_back(ele.second); } );
         // 求得單數跳躍的下標
         vector<int> oddNext = GetNext(sortedIndex);
         // 找尋減少順序的下標
         sort(cache.begin(), cache.end()
              , [&](const auto& left, const auto& right)
                  if (left.first == right.first)
```

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```
return left.second < right.second;
                 else
                    return left.first > right.first;
            });
        sortedIndex.clear();
        sortedIndex.reserve(cache.size());
        for_each(cache.begin(), cache.end()
                , [&](const auto& ele) { sortedIndex.push_back(ele.second); } );
        // 求得雙數跳躍的下標
        vector<int> evenNext = GetNext(sortedIndex);
        // 設 odd[i]: 單數跳躍時可以由 i 到 N
        vector<bool> odd(A.size(), false);
        // 設 even[i]: 雙數跳躍時可以由 i 到 N
        vector<bool> even(A.size(), false);
        odd.back() = even.back() = true;
        // odd 的總數便是答案
        for (int i = A.size() - 1; i >= 0; i--)
        {
           if (oddNext[i] != -1)
                odd[i] = even[oddNext[i]];
           if (evenNext[i] != -1)
               even[i] = odd[evenNext[i]];
        }
        int result = 0;
        for (const auto& o : odd)
           if (o) result++;
        return result;
    }
private:
    vector<int> GetNext(const vector<int>& inputIndex)
    {
        // 使用了 Monotonic Stack
        stack<int> cache;
        vector<int> result(inputIndex.size(), -1); // -1 代表沒法再往後跳躍
        for (const auto& index : inputIndex)
           while (!cache.empty() && cache.top() < index)</pre>
               result[cache.top()] = index;
               cache.pop();
           cache.push(index);
       return result;
   }
};
```

動規 - Map

```
// 思路: 利用 BST 由尾至頭歷遍, 找出每一個對應的跳躍目的地
// 時間複雜度 O(nlogn), 空間複雜度 O(n)
class Solution {
public:
    int oddEvenJumps(vector<int>& A) {
        int N = A.size();
       // 設 odd[i]: 單數跳躍時可以由 i 到 N
       vector<bool> odd(A.size(), false);
       // 設 even[i]: 雙數跳躍時可以由 i 到 N
       vector<bool> even(A.size(), false);
       odd.back() = even.back() = true;
       map<int, int> cache; // key: A[i] value: i
       cache.emplace(A[N-1], N-1);
       for (int i = N - 2; i >= 0; i--)
           auto it = cache.find(A[i]);
           if (it != cache.end())
               odd[i] = even[it->second];
               even[i] = odd[it->second];
           }
           else
           {
               auto bigger = GetBigger(cache, A[i]);
               auto smaller = GetSmaller(cache, A[i]);
               if (bigger != cache.end())
                   odd[i] = even[bigger->second];
               if (smaller != cache.end())
                   even[i] = odd[smaller->second];
           }
           cache[A[i]] = i;
       }
       // odd 的總數便是答案
       int result = 0;
       for (const auto& o : odd)
           if (o) result++;
       return result;
    }
private:
    template <class MyMap, class T>
       typename MyMap::iterator GetBigger(MyMap& cache, T val)
    {
       auto bigger = cache.lower_bound(val);
       if (bigger == cache.end())
           return bigger;
       else
```

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```
return bigger;
     }
     template <class MyMap, class T>
         typename MyMap::iterator GetSmaller(MyMap& cache, T val)
         auto smaller = cache.lower_bound(val);
         if (smaller == cache.begin())
             return cache.end();
         else
             return prev(smaller);
     }
 };
動規 - Multimap
 // 思路: 利用 BST 由尾至頭歷遍, 找出每一個對應的跳躍目的地
 // 時間複雜度 O(nlogn), 空間複雜度 O(n)
 class Solution {
 public:
     int oddEvenJumps(vector<int>& A) {
         int N = A.size();
         // 設 odd[i]: 單數跳躍時可以由 i 到 N
         vector<bool> odd(A.size(), false);
         // 設 even[i]: 雙數跳躍時可以由 i 到 N
         vector<bool> even(A.size(), false);
         odd.back() = even.back() = true;
         multimap<int, int> cache; // key: A[i] value: i
         cache.emplace(A[N-1], N-1);
         for (int i = N - 2; i >= 0; i--)
             auto it = cache.find(A[i]);
             if (it != cache.end())
                 // 找尋同值最細下標
                 it = GetSmallestIndex(cache, it);
                 odd[i] = even[it->second];
                 even[i] = odd[it->second];
             }
             else
             {
                 auto bigger = GetBigger(cache, A[i]);
                 auto smaller = GetSmaller(cache, A[i]);
                 if (smaller != cache.end())
                     even[i] = odd[smaller->second];
                 if (bigger != cache.end())
                     odd[i] = even[bigger->second];
             }
             cache.emplace(A[i], i);
```

```
// odd 的總數便是答案
        int result = 0;
        for (const auto& o : odd)
            if (o) result++;
       return result;
   }
private:
    template <class MyMap, class T>
        typename MyMap::iterator GetBigger(MyMap& cache, T val)
    {
        auto bigger = cache.lower_bound(val);
        if (bigger == cache.end())
           return bigger;
        else
           return GetSmallestIndex(cache, bigger); // 找尋同值最細下標
    }
    template <class MyMap, class T>
        typename MyMap::iterator GetSmaller(MyMap& cache, T val)
    {
        auto smaller = cache.lower_bound(val);
        if (smaller == cache.begin())
            return cache.end();
        else
           return GetSmallestIndex(cache, prev(smaller)); // 找尋同值最細下標
    template <class MyMap, class MapIT>
        MapIT GetSmallestIndex(MyMap& cache, MapIT target)
    {
        auto range = cache.equal_range(target->first);
            // 找尋同值最細下標
            int minIndex = INT_MAX;
            for (auto j = range.first; j != range.second; j++)
                if (minIndex > j->second)
                {
                    target = j;
                    minIndex = j->second;
            }
        return target;
   }
};
```

18.2 Course Schedule II

描述

There are a total of n courses you have to take, labeled from 0 to n-1.

Some courses may have prerequisites, for example to take course 0 you have to first take course 1, which

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```
is expressed as a pair: [0,1]
```

Given the total number of courses and a list of prerequisite pairs, return the ordering of courses you should take to finish all courses.

There may be multiple correct orders, you just need to return one of them. If it is impossible to finish all courses, return an empty array.

```
Example 1:
```

Note:

- The input prerequisites is a graph represented by a list of edges, not adjacency matrices. Read more about how a graph is represented.
- You may assume that there are no duplicate edges in the input prerequisites.

DFS - Topological Sort

```
// 時間複雜度 O(n), 空間複雜度 O(n)
class Solution {
public:
    vector<int> findOrder(int numCourses, vector<vector<int>>& prerequisites) {
       vector<int> result; result.reserve(numCourses);
       // Topological Sort
       // 先造出 dependency graph
       // 也記低有什麼 course 出現過
       unordered_map<int, list<int>> dGraph;
       unordered_set<int> seenCourse;
       for (const auto& p : prerequisites)
           dGraph[p[0]].push_back(p[1]);
           seenCourse.insert(p[0]);
           seenCourse.insert(p[1]);
       }
       // 先補上在 graph 中沒有出現的 course
       for (int i = 0; i < numCourses; i++)</pre>
```

```
if (seenCourse.count(i) == 0) result.push back(i);
        // 利用 DFS 造出答案
        unordered_map<int, bool> visited;
        for (const auto& [k, v] : dGraph)
            if (!DFS(dGraph, k, result, visited)) return vector<int>();
        return result;
private:
    bool DFS(const unordered map<int, list<int>>& dGraph, int k
             , vector<int>& result, unordered_map<int, bool>& visited)
    {
        if (visited.find(k) != visited.end()) return visited[k];
        visited[k] = false;
        auto it = dGraph.find(k);
        if (it != dGraph.end())
            for (const auto& nei : it->second)
                if (!DFS(dGraph, nei, result, visited)) return false;
        }
        visited[k] = true;
        result.push_back(k);
        return true;
    }
};
```

18.3 Longest Increasing Path in a Matrix

描述

Given an integer matrix, find the length of the longest increasing path.

From each cell, you can either move to four directions: left, right, up or down. You may NOT move diagonally or move outside of the boundary (i.e. wrap-around is not allowed).

```
Example 1:
Input: nums =
[
    [9,9,4],
    [6,6,8],
    [2,1,1]
]
Output: 4
Explanation: The longest increasing path is [1, 2, 6, 9].
```

```
Example 2:
 Input: nums =
    [3,4,5],
    [3,2,6],
   [2,2,1]
 ٦
 Output: 4
 Explanation: The longest increasing path is [3, 4, 5, 6]. Moving diagonally is not allowed.
備忘錄法
 // 時間複雜度 O(m*n), 空間複雜度 O(m*n)
 class Solution {
 public:
     int longestIncreasingPath(vector<vector<int>>& matrix) {
         m_M = matrix.size();
         if (m_M == 0) return 0;
         m_N = matrix[0].size();
         if (m_N == 0) return 0;
         vector<vector<bool>> visited(m_M, vector<bool>(m_N, false));
         // 設 cache[i][j] 為 i,j 的最長答案
         // 這個答案是由 O 開始總加的, 所以 DFS 也要由 O 開始總加
         vector<vector<int>> cache(m_M, vector<int>(m_N, -1));
          int maxLen = INT_MIN;
         for (int i = 0; i < m_M; i++)
         {
             for (int j = 0; j < m_N; j++)
             {
                 maxLen = max(maxLen, DFS(i, j, matrix, cache, visited));
             }
         }
         return maxLen;
     }
 private:
     const vector<pair<int, int>> directions{{1,0}, {0,1}, {-1,0}, {0,-1}};
      int DFS(int i, int j, const vector<vector<int>>& matrix
              , vector<vector<int>>& cache, vector<vector<bool>>& visited)
     {
          if (cache[i][j] != -1) return cache[i][j];
         visited[i][j] = true;
          int maxLen = 0;
         for (int d = 0; d < 4; d++)
             int newI = i + directions[d].first;
             int newJ = j + directions[d].second;
             if (newI >= 0 \&\& newI < m_M \&\& newJ >= 0 \&\& newJ < m_N
                 && !visited[newI][newJ]
```

```
&& matrix[i][j] > matrix[newI][newJ])// 由大至細地找尋答案 (由細至大也可以)
maxLen = max(maxLen, DFS(newI, newJ, matrix, cache, visited));
}
visited[i][j] = false;
return cache[i][j] = maxLen + 1; // 注意: 由細至大保存中途答案
}
private:
int m_M;
int m_N;
};
```

18.4 Count Complete Tree Nodes

描述

Given a complete binary tree, count the number of nodes.

Note:

Definition of a complete binary tree from Wikipedia: In a complete binary tree every level, except possibly the last, is completely filled, and all nodes in the last level are as far left as possible. It can have between 1 and 2h nodes inclusive at the last level h.

```
Example:
```

```
1
/\
2 3
/\ /
4 5 6

Output: 6
```

Input:

暴力

```
// 時間複雜度 O(n), 空間複雜度 O(n)
class Solution {
public:
    int countNodes(TreeNode* root) {
        if (root == nullptr) return 0;
        return 1 + countNodes(root->left) + countNodes(root->right);
    }
};
```

Binary Search

```
// 時間複雜度 O(d^2), 空間複雜度 O(n) class Solution { public: int countNodes(TreeNode* root) {
```

```
// 若果樹沒有元素
        if (root == nullptr) return 0;
        int d = ComputeDepth(root);
        // 若果樹只有一個元素
        if (d == 0) return 1;
        // left: 為最低層的最左的 node index
        // right: 為最低層的最右的 node index
        int left = 1; int right = pow(2, d) - 1;
        while (left <= right)</pre>
        {
            int pivot = (left + right) / 2;
            if (IsExist(pivot, d, root))
                left = pivot + 1;
            else
                right = pivot - 1;
        }
        return pow(2, d) - 1 + left;
    }
private:
    int ComputeDepth(TreeNode *root)
        int d = 0;
        while (root->left)
            root = root->left;
            d++;
        return d;
    bool IsExist(int idx, int d, TreeNode* node)
        int left = 0; int right = pow(2, d) - 1;
        for (int i = 0; i < d; i++)
            int pivot = (left + right) / 2;
            if (idx <= pivot)</pre>
            {
                node = node->left;
                right = pivot;
            }
            else
            {
                node = node->right;
                left = ++pivot;
            }
        return node != nullptr;
    }
};
```

18.5 Flip Equivalent Binary Trees

描述

For a binary tree T, we can define a flip operation as follows: choose any node, and swap the left and right child subtrees.

A binary tree X is flip equivalent to a binary tree Y if and only if we can make X equal to Y after some number of flip operations.

Write a function that determines whether two binary trees are flip equivalent. The trees are given by root nodes root1 and root2.

Example 1:

```
Input: root1 = [1,2,3,4,5,6,null,null,null,7,8], root2 = [1,3,2,null,6,4,5,null,null,null,null,null)
Output: true
Explanation: We flipped at nodes with values 1, 3, and 5.
```

•

Note:

- Each tree will have at most 100 nodes.
- Each value in each tree will be a unique integer in the range [0, 99]

遞歸

Canonical Traversal

```
// 時間複雜度 O(min(N1, N2)), 空間複雜度 O(min(H1, H2)) class Solution { public:
```

```
bool flipEquiv(TreeNode* root1, TreeNode* root2) {
        list<TreeNode*> vals1;
        list<TreeNode*> vals2;
        // 由細至大把二叉樹放到鏈表中
        DFS(root1, vals1);
        DFS(root2, vals2);
        // 當兩個表是一樣, 回 true
        return vals1.size() == vals2.size()
            && equal(vals1.begin(), vals1.end(), vals2.begin()
                     , [](const auto& left, const auto& right)
                         if (left == nullptr && right == nullptr) return true;
                         else if (left == nullptr || right == nullptr) return false;
                         else return left->val == right->val;
                     });
    }
private:
    void DFS(TreeNode *root, list<TreeNode*>& vals)
    {
        if (root == nullptr) return;
        vals.push_back(root);
        int L = root->left == nullptr ? -1 : root->left->val;
        int R = root->right == nullptr ? -1 : root->right->val;
        if (L < R)
            DFS(root->left, vals);
            DFS(root->right, vals);
        }
        else
        {
            DFS(root->right, vals);
            DFS(root->left, vals);
        }
        vals.push_back(nullptr);
    }
};
```

18.6 Diameter of Binary Tree

描述

Given a binary tree, you need to compute the length of the diameter of the tree. The diameter of a binary tree is the length of the longest path between any two nodes in a tree. This path may or may not pass through the root.

Example: Given a binary tree

1

```
/\
23
/\
45
```

Return 3, which is the length of the path [4,2,1,3] or [5,2,1,3].

Note: The length of path between two nodes is represented by the number of edges between them.

遞歸

```
// 時間複雜度 O(n), 空間複雜度 O(1)
class Solution {
public:
    int diameterOfBinaryTree(TreeNode* root) {
       m result = 1;
       DFS(root);
       return m_result - 1;
   }
private:
    int DFS(TreeNode *root)
    {
       if (root == nullptr) return 0;
       int L = DFS(root->left);
       int R = DFS(root->right);
       m_result = max(m_result, L+R+1); // 由左至右總加起來
       return max(L, R) + 1; // 注意: 只取最長的子樹
    }
private:
    int m_result;
```

18.7 Evaluate Division

描述

Equations are given in the format A / B = k, where A and B are variables represented as strings, and k is a real number (floating point number). Given some queries, return the answers. If the answer does not exist, return -1.0.

```
Example: Given a/b = 2.0, b/c = 3.0. queries are: a/c = ?, b/a = ?, a/e = ?, a/a = ?, x/x = ?. return [6.0, 0.5, -1.0, 1.0, -1.0].
```

```
The input is: vector<pair<string, string>> equations, vector<double>& values , vector<pair<string, string>> queries , where equations.size() == values.size() , and the values are positive. This represents the equations. Return vector<double>.
```

According to the example above:

```
equations = [ ["a", "b"], ["b", "c"] ], values = [2.0, 3.0], queries = [ ["a", "c"], ["b", "a"], ["a", "e"], ["a", "a"], ["x", "x"] ].
```

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The input is always valid. You may assume that evaluating the queries will result in no division by zero and there is no contradiction.

遞歸 - DFS

```
// 時間複雜度 O(n), 空間複雜度 O(n)
class Solution {
public:
    vector<double> calcEquation(vector<vector<string>>& equations
                                , vector<double>& values
                                , vector<vector<string>>& queries){
        // 造圖
        unordered_map<string,vector<pair<double,string>>> g;
        for (int i = 0; i < equations.size(); i++)</pre>
            string& strA = equations[i][0];
            string& strB = equations[i][1];
            // 記錄 A / B
            g[strA].emplace_back(values[i], strB);
            // 記錄 B / A
            g[strB].emplace_back(1 / values[i], strA);
        vector<double> result:
        for (int i = 0; i < queries.size(); i++)</pre>
            const string& qStart = queries[i][0];
            const string& qEnd = queries[i][1];
            // 若整個除數關係沒有記錄
            if (g.find(qStart) == g.end() || g.find(qEnd) == g.end())
                result.push_back(-1.0);
            else
            {
                // 若有記錄
                set<string> visited;
                int ansLen = result.size();
                DFS(qStart, qEnd, 1, visited, result, g);
                if (result.size() == ansLen)
                    result.push_back(-1); // 若找不到答案
            }
        }
        return result;
    }
private:
    void DFS(string start, string end, double cost
             , set<string>& visited
             , vector<double>& result
             , unordered_map<string,vector<pair<double,string>>>& g)
    {
        visited.insert(start);
        if (start == end)
```

```
{
    result.push_back(cost);
    return;
}

for (const auto& [num, neigbor] : g[start])
{
    if (visited.find(neigbor) != visited.end()) continue;
    int ansLen = result.size();
    DFS(neigbor, end, cost * num, visited, result, g);
    if (ansLen != result.size()) return; // 已找到答案, 剪枝
}
};
```

18.8 Cracking the Safe

描述

There is a box protected by a password. The password is a sequence of n digits where each digit can be one of the first k digits 0, 1, ..., k-1.

While entering a password, the last n digits entered will automatically be matched against the correct password.

For example, assuming the correct password is "345", if you type "012345", the box will open because the correct password matches the suffix of the entered password.

Return any password of minimum length that is guaranteed to open the box at some point of entering it.

```
Example 1:
```

```
Input: n = 1, k = 2
Output: "01"
Note: "10" will be accepted too.

Example 2:
Input: n = 2, k = 2
Output: "00110"
Note: "01100", "10011", "11001" will be accepted too.

Note:
• n will be in the range (1, 4).
• k will be in the range (1, 10).
```

遞歸 - DFS - Hierholzer's Algorithm

• pow(k, n) will be at most 4096.

```
// 時間複雜度 O(n * k^n), 空間複雜度 O(n * k^n)
// 利用 Hierholzer's Algorithm 歷遍所有 edges 並記錄所有的 nodes
// Hierholzer's Algorithm 用來找尋 Eulerian Path
```

```
class Solution {
public:
    string crackSafe(int n, int k) {
        if (n == 1 && k == 1) return "0";
       // seen 用來存放見過的 node
       unordered_set<string> seen;
       string result;
       // 準備開始點
       string start; start.append(n-1, '0');
       DFS(start, k, seen, result);
       result += start;
       return result;
   }
private:
    void DFS(const string& node, int k, unordered set<string>& seen, string& result)
       // 這是 post order travel 的做法
       for (int x = 0; x < k; x++)
           // nei 是下一個歷遍的 node + edge
           // x 為 edge, 0, 1, 2 ... k-1
           string nei = node + to_string(x);
           if (seen.find(nei) == seen.end())
           {
               seen.insert(nei):
               // nei.substr(1) 可以提取下一個 node
               // 例子: 01(上一個 node) -> 010(edge) -> 10(下一個 node)
               DFS(nei.substr(1), k, seen, result);
               result += to_string(x); // 完成後, 記低 edge
           }
       }
   }
}:
```

18.9 Most Stones Removed with Same Row or Column

描述

On a 2D plane, we place stones at some integer coordinate points. Each coordinate point may have at most one stone.

Now, a move consists of removing a stone that shares a column or row with another stone on the grid.

What is the largest possible number of moves we can make?

```
Example 1:
```

```
Input: stones = [[0,0],[0,1],[1,0],[1,2],[2,1],[2,2]]
Output: 5
   Example 2:
```

```
Input: stones = [[0,0],[0,2],[1,1],[2,0],[2,2]]
 Output: 3
   Example 3:
 Input: stones = [[0,0]]
 Output: 0
   Note:
   • 1 <= stones.length <= 1000
   • 0 \le \text{stones}[i][j] \le 10000
迭代 - DFS - stack
 // 時間複雜度 O(n^2), 空間複雜度 O(n^2)
 class Solution {
 public:
     int removeStones(vector<vector<int>>& stones) {
         int N = stones.size();
         // graph[i][0]: 代表總共有多少個石頭和第 i 個石頭位於同列或欄
         // graph[i][x]: 1 <= x <= N-1, x 存了 stones 的 index
         // 例子 graph[0][2] == 5: stones[0] 的第二個同列或欄石頭 是 stones[5]
         vector<vector<int>> graph(N, vector<int>(N, 0));
         for (int i = 0; i < N; i++)
         {
             for (int j = i+1; j < N; j++)
                 // 若找到同列或同欄
                 if (stones[i][0] == stones[j][0]
                     || stones[i][1] == stones[j][1])
                 {
                     // 交叉記錄
                     graph[i][++graph[i][0]] = j;
                     graph[j][++graph[j][0]] = i;
                 }
             }
         }
         int ans = 0;
         vector<bool> seen(N, false);
         stack<int> cache;
         for (int i = 0; i < N; i++)
         {
             if (!seen[i])
             {
                 cache.push(i);
                 seen[i] = true;
                 ans--;
                 while (!cache.empty())
                     int node = cache.top();
```

```
cache.pop();
                      ans++;
                      for (int k = 1; k \le graph[node][0]; k++)
                          int nei = graph[node][k];
                          if (!seen[nei])
                          {
                              cache.push(nei);
                              seen[nei] = true;
                          }
                     }
                 }
             }
         }
         return ans;
     }
 };
Union
 // 時間複雜度 O(nlogn), 空間複雜度 O(n)
 class DSU // Disjoint Set Union
 {
 public:
     DSU(int N)
         m_parent.resize(N);
         for (int i = 0; i < N; i++) m_parent[i] = i;
     ~DSU() {}
     int Find(const int& x)
         if (m_parent[x] == x) return x;
         return m_parent[x] = Find(m_parent[x]);
     void Union(const int& x, const int& y)
         const int& xpar = Find(x);
         const int& ypar = Find(y);
         if (xpar == ypar) return;
         m_parent[xpar] = ypar;
     }
 private:
     vector<int> m_parent;
 };
 class Solution {
 public:
     int removeStones(vector<vector<int>>& stones) {
```

18.10 Strobogrammatic Number II

描述

A strobogrammatic number is a number that looks the same when rotated 180 degrees (looked at upside down).

Find all strobogrammatic numbers that are of length = n.

Example:

```
Input: n = 2
Output: ["11","69","88","96"]
```

遞歸 - DFS

```
// 時間複雜度 O(), 空間複雜度 O()
class Solution {
public:
    vector<string> findStrobogrammatic(int n)
    {
        return helper(n, n);
    }

    vector<string>helper(int n, int m)
    {
        if (n == 0) return vector<string> {""};
        if (n == 1) return vector<string> {"0","1","8"};

        vector<string> list = helper(n-2, m);
        vector<string> result;

        for (int i = 0;i < list.size(); i++)
        {
            string s = list[i];
            if (n != m) result.push_back("0" + s + "0");
            result.push_back("1" + s + "1");</pre>
```

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```
result.push_back("6" + s + "9");
    result.push_back("8" + s + "8");
    result.push_back("9" + s + "6");
}
    return result;
}
};
```

18.11 Word Search II

描述

Given a 2D board and a list of words from the dictionary, find all words in the board.

Each word must be constructed from letters of sequentially adjacent cell, where "adjacent" cells are those horizontally or vertically neighboring. The same letter cell may not be used more than once in a word.

Example:

```
Input:
board = [
    ['o','a','a','n'],
    ['e','t','a','e'],
    ['i','h','k','r'],
    ['i','f','l','v']
]
words = ["oath","pea","eat","rain"]
Output: ["eat","oath"]
```

- All inputs are consist of lowercase letters a-z.
- The values of words are distinct.

遞歸 - DFS - Trie

```
// 時間複雜度 D(M(4*3^L), 空間複雜度 D(N)
// 利用 Trie 存放目標, DFS 去找尋答案
struct TrieNode
    unordered_map<char, TrieNode*> next;
    string word;
};
class Solution {
public:
    vector<string> findWords(vector<vector<char>>& board, vector<string>& words) {
       TrieNode root;
       // 製造 Trie
       for (const string& w : words)
       {
           TrieNode *p = &root;
           for (const char& c : w)
           {
```

```
if (p->next.find(c) == p->next.end())
                   p->next[c] = new TrieNode();
                p = p - next[c];
            }
            if (p->next.find(END_KEY) == p->next.end())
                p->next[END_KEY] = new TrieNode();
           p->next[END_KEY]->word = w;
        }
        // DFS 找尋答案
        vector<string> result;
        for (int i = 0; i < board.size(); i++)</pre>
        {
            for (int j = 0; j < board[0].size(); j++)
                if (root.next.find(board[i][j]) != root.next.end())
                   DFS(i, j, board, &root, result);
            }
        }
        return result;
    }
private:
   const vector<int> dirX{-1,0,1,0};
   const vector<int> dirY{0,-1,0,1};
   const char END_KEY = '$';
    const char VISITED_KEY = '#';
   void DFS(int i, int j, vector<vector<char>>& board
             , TrieNode *node, vector<string>& result)
    {
        const char letter = board[i][j];
        TrieNode *nextNode = node->next[letter];
        // 若找到答案
        if (nextNode->next.find(END_KEY) != nextNode->next.end())
        {
           result.push_back(nextNode->next[END_KEY]->word);
            // 剛除已找到的文字
           nextNode->next.erase(END_KEY);
        // 標為 visited
        board[i][j] = VISITED_KEY;
        // 擴展
        for (int x = 0; x < 4; x++)
            int newI = i + dirX[x];
            int newJ = j + dirY[x];
           // 若出了界限
            if (newI < 0 || newI >= board.size() || newJ < 0 || newJ >= board[0].size())
                continue;
            // 若新的字母是不需要的,包括了已經訪問的檢查
```

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```
if (nextNode->next.find(board[newI][newJ]) == nextNode->next.end())
                 continue;
             DFS(newI, newJ, board, nextNode, result);
         }
         // 復原
         board[i][j] = letter;
         // 删除空了的 TrieNode 加快找尋
         if (nextNode->next.size() == 0)
             node->next.erase(letter);
     }
 };
遞歸 - DFS - Trie - Array
 // 時間複雜度 O(M(4*3<sup>L</sup>), 空間複雜度 O(N)
 // 利用 Trie 存放目標, DFS 去找尋答案
 struct TierNode
     vector<TierNode*> next; // 這裏不同, 不是用 hash
     string word;
     TierNode()
         next.resize(26, nullptr);
     }
 };
 class Solution {
 public:
     vector<string> findWords(vector<vector<char>>& board, vector<string>& words) {
         TierNode root;
         // 製造 Tier
         for (const string& w : words)
         {
             TierNode *p = &root;
             for (const char& c : w)
             {
                 if (p->next[c-'a'] == nullptr)
                     p->next[c-'a'] = new TierNode();
                 p = p-\sum[c-'a'];
             p->word = w;
         }
         // DFS 找尋答案
         vector<string> result;
         for (int i = 0; i < board.size(); i++)</pre>
             for (int j = 0; j < board[0].size(); j++)
```

```
if (root.next[board[i][j]-'a'] != nullptr)
                   DFS(i, j, board, &root, result);
           }
       }
       return result;
    }
private:
   const vector<int> dirX{-1,0,1,0};
   const vector<int> dirY{0,-1,0,1};
   const char VISITED_KEY = '#';
   void DFS(int i, int j, vector<vector<char>>& board
             , TierNode *node, vector<string>& result)
    {
       const char letter = board[i][j];
       TierNode *nextNode = node->next[letter-'a'];
       // 若找到答案
       if (nextNode->word.size() != 0)
       {
           result.push_back(nextNode->word);
           // 剛除已找到的文字
           nextNode->word = "";
       // 標為 visited
       board[i][j] = VISITED_KEY;
       // 擴展
       for (int x = 0; x < 4; x++)
           int newI = i + dirX[x];
           int newJ = j + dirY[x];
           // 若出了界限
           if (newI < 0 || newI >= board.size() || newJ < 0 || newJ >= board[0].size())
               continue:
           // 若已經訪問過
           if (board[newI][newJ] == VISITED_KEY) // 這裏不同, 分開了出來檢查
               continue;
           // 若新的字母是不需要的
           if (nextNode->next[board[newI][newJ]-'a'] == nullptr)
               continue;
           DFS(newI, newJ, board, nextNode, result);
       }
       // 復原
       board[i][j] = letter;
   }
};
```

18.12 Word Squares 467

18.12 Word Squares

描述

Given a set of words (without duplicates), find all word squares you can build from them.

A sequence of words forms a valid word square if the kth row and column read the exact same string, where $0 \le k < max(numRows, numColumns)$.

For example, the word sequence ["ball", "area", "lead", "lady"] forms a word square because each word reads the same both horizontally and vertically.

```
b a l l
a r e a
l e a d
l a d y
```

- There are at least 1 and at most 1000 words.
- All words will have the exact same length.
- Word length is at least 1 and at most 5.
- Each word contains only lowercase English alphabet a-z.

```
Example 1:
Input:
["area", "lead", "wall", "lady", "ball"]
Output:
  [ "wall",
    "area"
    "lead",
    "lady"
  ],
  [ "ball",
    "area",
    "lead".
    "lady"
  ]
]
Explanation:
The output consists of two word squares.
The order of output does not matter (just the order of words in each word square matters).
  Example 2:
["abat", "baba", "atan", "atal"]
Output:
  [ "baba",
```

```
"abat",
     "baba",
     "atan"
   ],
   [ "baba",
     "abat",
     "baba",
     "atal"
   ]
 ٦
 Explanation:
 The output consists of two word squares.
 The order of output does not matter (just the order of words in each word square matters).
遞歸 - DFS
 // 時間複雜度 O(), 空間複雜度 O(N)
 // 會超時
 class Solution {
 public:
     vector<vector<string>> wordSquares(vector<string>& words) {
         vector<vector<string>> result;
         if (words.size() == 0) return result;
         for (const string& w : words)
         {
             vector<string> wordSquare{w};
             DFS(words, 1, wordSquare, result);
         return result;
     }
 private:
     void DFS(const vector<string>& words, int step
               , vector<string>& wordSquare, vector<vector<string>>& result)
     {
         if (step == wordSquare[0].size())
         {
             // 求得答案
             result.push_back(wordSquare);
         else if (step > wordSquare[0].size())
             return;
         else
         {
             // 擴展
             string prefix;
             for (const string& w : wordSquare)
                 prefix += w.substr(step, 1);
             for (const auto& nei : GetNeiByPrefix(prefix, words))
             {
                 wordSquare.push_back(nei);
```

```
DFS(words, step+1, wordSquare, result);
                 wordSquare.pop_back();
             }
         }
     }
     vector<string> GetNeiByPrefix(const string& prefix, const vector<string>& words)
         vector<string> result; result.reserve(words.size());
         for (const string& w : words)
             if (w.find(prefix) == 0) result.push_back(w);
         return result;
     }
 };
遞歸 - DFS - Hash
 // 時間複雜度 O(N*26^L), 空間複雜度 O(N*L) L is the length of a single word
 class Solution {
 public:
     vector<vector<string>> wordSquares(vector<string>& words) {
         vector<vector<string>> result;
         if (words.size() == 0) return result;
         CreatePrefixMap(words); // 利用 hash table 加快
         for (const string& w : words)
         {
             vector<string> wordSquare{w};
             DFS(words, 1, wordSquare, result);
         return result:
     }
 private:
     unordered_map<string, set<string>> m_prefixMap;
 private:
     void CreatePrefixMap(const vector<string>& words)
     {
         for (const string& w : words)
             string prefix;
             int count = 0;
             for (int i = 0; i < w.size()-1; i++)
             {
                 prefix += w[i];
                 m_prefixMap[prefix].insert(w);
         }
     void DFS(const vector<string>& words, int step
               , vector<string>& wordSquare, vector<vector<string>>& result)
```

```
{
         if (step == wordSquare[0].size())
         {
             // 求得答案
             result.push_back(wordSquare);
         else if (step > wordSquare[0].size())
             return;
         else
         {
             // 擴展
             string prefix;
             for (const string& w : wordSquare)
                 prefix += w.substr(step, 1);
             for (const auto& nei : GetNeiByPrefix(prefix, words))
                 wordSquare.push_back(nei);
                 DFS(words, step+1, wordSquare, result);
                 wordSquare.pop_back();
             }
         }
     }
     set<string> GetNeiByPrefix(const string& prefix, const vector<string>& words)
         auto it = m_prefixMap.find(prefix);
         if (it == m_prefixMap.end()) return set<string>(); // 若找不到
         return it->second;
     }
 }:
遞歸 - DFS - Trie
 // 時間複雜度 O(N*26^L), 空間複雜度 O(N*L) L is the length of a single word
 struct Trie
     vector<Trie*> m_next;
     vector<int> m_wordIndex;
     Trie() { m_next.resize(26, nullptr); }
 };
 class Solution {
 public:
     vector<vector<string>> wordSquares(vector<string>& words) {
         vector<vector<string>> result;
         if (words.size() == 0) return result;
         CreateTrie(words); // 利用 hash table 加快
         vector<string> wordSquare;
         for (const string& w : words)
```

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```
wordSquare.push_back(w);
            DFS(words, 1, wordSquare, result);
            wordSquare.pop_back();
        return result;
    }
private:
    Trie m_root;
private:
    void CreateTrie(const vector<string>& words)
    {
        int wordIndex = 0;
        for (const string& w : words)
            Trie *cur = &m_root;
            for (const char& c : w)
                const char cc = c - 'a';
                if (cur->m_next[cc] == nullptr)
                    cur->m_next[cc] = new Trie();
                cur = cur->m_next[cc];
                cur->m_wordIndex.push_back(wordIndex);
            wordIndex++;
        }
    }
    void DFS(const vector<string>& words, int step
             , vector<string>& wordSquare, vector<vector<string>>& result)
    {
        if (step == wordSquare[0].size())
        {
            // 求得答案
            result.push_back(wordSquare);
        }
        else
            Trie *cur = &m_root;
            // 利用 Trie 來找到岩的 prefix
            for (const string& s : wordSquare)
                const char cc = s[step] - 'a';
                if (cur->m_next[cc] == nullptr) return;
                cur = cur->m_next[cc];
            // 擴展
            for (const auto& nei : cur->m_wordIndex)
                // 由 index 找回文字
                wordSquare.push_back(words[nei]);
                DFS(words, step+1, wordSquare, result);
                wordSquare.pop_back();
```

```
}
};
```

18.13 Android Unlock Patterns

描述

Given an Android 3x3 key lock screen and two integers m and n, where $1 \le m \le n \le 9$, count the total number of unlock patterns of the Android lock screen, which consist of minimum of m keys and maximum n keys.

Rules for a valid pattern:

- Each pattern must connect at least m keys and at most n keys.
- · All the keys must be distinct.
- If the line connecting two consecutive keys in the pattern passes through any other keys, the other keys
 must have previously selected in the pattern. No jumps through non selected key is allowed.
- The order of keys used matters.

图 18-1 Android Unlock Patterns

遞歸 - DFS - vector 版

```
// 時間複雜度 O(N!), 空間複雜度 O(N)
class Solution {
public:
   int numberOfPatterns(int m, int n) {
       int result = 0;
       // 使用了 vector, 此方法最慢, 對比使用 integer
       vector<bool> used(9, false);
       for (int len = m; len <= n; len++)
           result += DFS(-1, len, used);
       return result;
   }
private:
   // index: 為是次選中的下標 last: 為上次選中的下標
   // IsValid: 是在檢驗, 由 last index 走到 index 是否合法
   bool IsValid(int index, int last, const vector<bool>& used)
       // 若果此下標已被使用
       if (used[index]) return false;
       // 若果此下標是第一次被選用
       if (last == -1) return true:
       // 若果是鄰近的移動, 或日字移動法
       if ((index + last) % 2 == 1) return true;
       // 若果是大斜角走, 要先檢查居中下標
       int mid = (index + last) / 2;
       if (mid == 4) return used[mid];
       // 處理鄰近斜角移動
       if ((index % 3 != last % 3) && (index / 3 != last / 3))
           return true;
       // 剩下的移動選擇都不是相鄰的
       return used[mid];
   }
   int DFS(int last, int len, vector<bool>& used)
       if (len == 0)
           return 1;
       int sum = 0;
       for (int i = 0; i < 9; i++)
       {
           if (IsValid(i, last, used))
           {
              used[i] = true;
               sum += DFS(i, len - 1, used);
              used[i] = false;
           }
       return sum;
   }
};
```

遞歸 - DFS - int 版

```
// 時間複雜度 O(N!), 空間複雜度 O(N)
 // 快很多的版本. 因為用了 int 來代替 vector. 用來記錄使用情況
 class Solution {
 public:
     int numberOfPatterns(int m, int n) {
        // 使用 int 來記錄已使用的情況
        return count(m, n, 0, 1, 1);
     }
 private:
     int count(int m, int n, int used, int i2, int j2) {
        int number = m <= 0;</pre>
        if (!n) return 1;
        for (int i=0; i<3; i++) {
            for (int j=0; j<3; j++) {
               // 求得下一個下標. 和標示使用
                int I = i2 + i, J = j2 + j, used2 = used | (1 << (i*3 + j));
               // 當 used2 == used, 代表重覆使用下標
               // 所以只有當 used2 變大了才會繼續
               // I % 2 和 J % 2 的檢查包括了所有小斜步和日字步
               // 那後的 (I*3 + J)/2 會檢查大斜步的居中下標和餘下的所有步法
                if (used2 > used && (I % 2 || J % 2 || used2 & (1 << (I/2*3 + J/2))))
                   number += count(m-1, n-1, used2, i, j);
            }
        }
        return number;
     }
 };
遞歸 - DFS - int 版
 // 時間複雜度 O(N!), 空間複雜度 O(N)
 // 快很多的版本, 因為用了 int 來代替 vector, 用來記錄使用情況
 class Solution {
 public:
     int numberOfPatterns(int m, int n) {
        int result = 0;
        int used = 0;
        for (int len = m; len <= n; len++)
            result += DFS(-1, len, used);
        return result;
     }
 private:
     // index: 為是次選中的下標 last: 為上次選中的下標
     // IsValid: 是在檢驗, 由 last index 走到 index 是否合法
     bool IsValid(int index, int last, const int& used)
     {
        // 若果此下標已被使用
        if (used & 1 << index) return false;</pre>
        // 若果此下標是第一次被選用
```

```
if (last == -1) return true;
       // 若果是鄰近的移動, 或日字移動法
       if ((index + last) % 2 == 1) return true;
       // 若果是大斜角走, 要先檢查居中下標
       int mid = (index + last) / 2;
       if (mid == 4) return used & 1 << mid;
       // 處理鄰近斜角移動
       if ((index % 3 != last % 3) && (index / 3 != last / 3))
           return true;
       // 剩下的移動選擇都不是相鄰的
       return used & 1 << mid;
   int DFS(int last, int len, int& used)
       if (len == 0)
           return 1;
       int sum = 0;
       for (int i = 0; i < 9; i++)
           if (IsValid(i, last, used))
           {
               used |= 1 << i;
               sum += DFS(i, len - 1, used);
               used \&= ~(1 << i);
           }
       }
       return sum;
   }
};
```

18.14 Fenwick Tree or Binary Indexed Tree

描述

We may use this tree to calculate the sum of the prefix of a given array. Mean while we can update the value of the array and the tree in logN time.

Code

```
// 時間複雜度 O(NLogN), 空間複雜度 O(N)
// Learn from https://www.youtube.com/watch?v=CWDQJGaN1gY
class FenwickTree
{
public:
    FenwickTree() {}
    ~FenwickTree() {}

    vector<int> CreateTree(const vector<int>& input)
    {
        vector<int> binaryIndexedTree(input.size()+1);
        for (size_t i = 1; i <= input.size(); i++)</pre>
```

```
{
            UpdateBinaryIndexedTree(binaryIndexedTree, input[i-1], i);
        return binaryIndexedTree;
    int GetSum(const vector<int>& binaryIndexedTree, int index)
    {
        index++;
        int sum = 0;
        while (index > 0)
            sum += binaryIndexedTree[index];
            index = GetParent(index);
        return sum;
    }
private:
    void UpdateBinaryIndexedTree(vector<int>& binaryIndexedTree, int val, int index)
        while (index < binaryIndexedTree.size())</pre>
            binaryIndexedTree[index] += val;
            index = GetNext(index);
    }
    /**
     * To get parent
     * 1) 2's complement to get minus of index
     * 2) AND this with index
     * 3) Subtract that from index
     */
    int GetParent(int index)
    {
        return index - (index & -index);
    }
    /**
     * To get next
     * 1) 2's complement of get minus of index
     * 2) AND this with index
     * 3) Add it to index
     */
    int GetNext(int index)
    {
        return index + (index & -index);
    }
};
int main(int argc, char *argv[])
    vector<int> input{1,2,3,4,5,6,7};
    FenwickTree ft;
    vector<int> binaryIndexedTree = ft.CreateTree(input);
    assert(1 == ft.GetSum(binaryIndexedTree, 0));
    assert(3 == ft.GetSum(binaryIndexedTree, 1));
```

```
assert(6 == ft.GetSum(binaryIndexedTree, 2));
assert(10 == ft.GetSum(binaryIndexedTree, 3));
assert(15 == ft.GetSum(binaryIndexedTree, 4));
assert(21 == ft.GetSum(binaryIndexedTree, 5));
assert(28 == ft.GetSum(binaryIndexedTree, 6));
return 0;
}
```

18.15 Count of Smaller Numbers After Self

描述

You are given an integer array nums and you have to return a new counts array. The counts array has the property where counts[i] is the number of smaller elements to the right of nums[i].

Example:

```
Input: [5,2,6,1]
Output: [2,1,1,0]
Explanation:
To the right of 5 there are 2 smaller elements (2 and 1).
To the right of 2 there is only 1 smaller element (1).
To the right of 6 there is 1 smaller element (1).
To the right of 1 there is 0 smaller element.
```

Note: Please read more about FenwickTree from example FenwickTree.

Code

```
// 時間複雜度 D(NLogN), 空間複雜度 D(N)
// The idea of this solution is similar to the monotonic stack
class Solution {
public:
    vector<int> countSmaller(vector<int>& nums)
    {
        // Relative indexing.
        // This is the key to achieve true O(n(\log(n))).
        set<int> unique_elements;
        for (const int& i : nums) unique_elements.insert(i);
        // 由細至大配上 id
        unordered_map<int,int> index;
        int id = 0;
        for (const auto& e : unique_elements) index[e] = id++;
        // Fenwick Tree
        vector<int> ft(id+1);
        vector<int> result;
        // 由尾至頭歷遍
        for (int i = nums.size()-1; i >= 0; --i)
```

```
// 記低出現過的下標
            ftIncrement(ft, index[nums[i]]);
            // 數一數較細的下標出現過的次數
            result.push_back(ftPrefixSum(ft, index[nums[i]]));
        reverse(result.begin(),result.end());
        return result;
    }
private:
    // Insert into Fenwick tree
    // O(log(n))
    void ftIncrement(vector<int> &ft, int index)
    {
        // 0 index -> 1 index
        ++index;
        while (index < ft.size())</pre>
            ft[index] += 1;
            index += (index&-index);
    }
    // Get sum from [0,index) in a Fenwick tree.
    // O(log(n))
    int ftPrefixSum(vector<int> &ft, int index)
        // 0 index -> 1 index but excluding index
        int sum = 0;
        while (index > 0)
            sum += ft[index];
            index -= (index&-index);
        return sum;
};
```

18.16 Coin Change

描述

You are given coins of different denominations and a total amount of money amount. Write a function to compute the fewest number of coins that you need to make up that amount. If that amount of money cannot be made up by any combination of the coins, return -1.

```
Example 1:
Input: coins = [1, 2, 5], amount = 11
Output: 3
Explanation: 11 = 5 + 5 + 1

Example 2:
Input: coins = [2], amount = 3
Output: -1
```

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Note: You may assume that you have an infinite number of each kind of coin.

DP

```
設狀態為 f(i), 表示 i 最少的 coins 數目
                      f(i) = min(f(i - coins[j]) + 1) \&\&coins[j] < i
 // 時間複雜度 O(n*k), 空間複雜度 O(n)
 class Solution {
 public:
     int coinChange(vector<int>& coins, int amount) {
          if (coins.size() == 0) return -1;
          sort(coins.begin(), coins.end());
          vector<int> f(amount+1, INT MAX);
          f[0] = 0;
          for (int i = coins[0]; i < f.size(); i++)</pre>
              for (int j = 0; j < coins.size(); j++)
                  if (coins[j] > i) break;
                  if (f[i-coins[j]] == INT MAX) continue;
                  f[i] = min(f[i], f[i-coins[j]] + 1);
              }
          }
         return f[amount] == INT_MAX ? -1 : f[amount];
     }
 };
DFS
 // 時間複雜度 O(n*k), 空間複雜度 O(n)
 class Solution {
 public:
     int coinChange(vector<int>& coins, int amount) {
          if (coins.size() == 0) return -1;
          sort(coins.begin(), coins.end());
          vector<int> counts(amount+1, 0);
          counts[0] = 0;
          DFS(coins, amount, counts);
          return counts[amount] == INT_MAX ? -1 : counts[amount];
     }
 private:
     int DFS(vector<int>& coins, int amount, vector<int>& counts)
          if (amount < 0) return -1;
          if (amount == 0) return 0;
```

18.17 Min Stack

描述

Design a stack that supports push, pop, top, and retrieving the minimum element in constant time.

- push(x) Push element x onto stack.
- pop() Removes the element on top of the stack.
- top() Get the top element.
- getMin() Retrieve the minimum element in the stack.

Example 1:

```
Input
["MinStack","push","push","getMin","pop","top","getMin"]
[[],[-2],[0],[-3],[],[],[]]

Output
[null,null,null,-3,null,0,-2]

Explanation
MinStack minStack = new MinStack();
minStack.push(-2);
minStack.push(0);
minStack.push(-3);
minStack.getMin(); // return -3
minStack.pop();
minStack.top(); // return 0
minStack.getMin(); // return -2
```

Note: You may assume that you have an infinite number of each kind of coin.

Stack and Min Stack

```
// 時間複雜度 O(1), 空間複雜度 O(n) class MinStack {
```

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```
public:
      MinStack(){
      void push(int x)
          if(s1.empty())
              s1.push(x);
              minStack.push(x);
          }
          else
          {
              if(x < minStack.top())</pre>
                  s1.push(x);
                  minStack.push(x);
              }
              else
                  s1.push(x);
                  minStack.push(minStack.top());
          }
      }
      void pop()
          s1.pop();
          minStack.pop();
      }
      int top()
      {
          return s1.top();
      int getMin()
          return minStack.top();
      }
 private:
      stack<int> s1; // 一個正常 stack
      stack<int> minStack; // 一個 min stack
 };
Stack and Pair
 // 時間複雜度 O(1), 空間複雜度 O(n)
 class MinStack {
 public:
      /** initialize your data structure here. */
      MinStack() {
      }
```

```
void push(int x) {
        if (m cache.empty())
            m_cache.emplace(x, x);
        else
            m_cache.emplace(x, min(m_cache.top().second, x));
    }
    void pop() {
        m_cache.pop();
    }
    int top() {
        return m cache.top().first;
    }
    int getMin() {
        return m_cache.top().second;
    }
private:
    stack<pair<int,int>> m_cache;
}:
```

18.18 Guess the Word

描述

This problem is an interactive problem new to the LeetCode platform.

We are given a word list of unique words, each word is 6 letters long, and one word in this list is chosen as secret.

You may call master.guess(word) to guess a word. The guessed word should have type string and must be from the original list with 6 lowercase letters.

This function returns an integer type, representing the number of exact matches (value and position) of your guess to the secret word. Also, if your guess is not in the given wordlist, it will return -1 instead.

For each test case, you have 10 guesses to guess the word. At the end of any number of calls, if you have made 10 or less calls to master guess and at least one of these guesses was the secret, you pass the testcase.

Besides the example test case below, there will be 5 additional test cases, each with 100 words in the word list. The letters of each word in those testcases were chosen independently at random from 'a' to 'z', such that every word in the given word lists is unique.

```
Example 1:
Input: secret = "acckzz", wordlist = ["acckzz", "ccbazz", "eiowzz", "abcczz"]

Explanation:

master.guess("aaaaaa") returns -1, because "aaaaaa" is not in wordlist.
master.guess("acckzz") returns 6, because "acckzz" is secret and has all 6 matches.
master.guess("ccbazz") returns 3, because "ccbazz" has 3 matches.
```

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```
master.guess("eiowzz") returns 2, because "eiowzz" has 2 matches.
master.guess("abcczz") returns 4, because "abcczz" has 4 matches.
```

We made 5 calls to master.guess and one of them was the secret, so we pass the test case.

Note: Any solutions that attempt to circumvent the judge will result in disqualification.

Minimax Strategy

```
// 時間複雜度 O(N^2), 空間複雜度 O(N^2)
// 使用了 minimax algorithm 來最大化地減少下一個需要嘗試的搜尋範圍
class Solution {
public:
    void findSecretWord(vector<string>& wordlist, Master& master) {
        int N = wordlist.size();
       m_H.resize(N, vector<int>(N));
       for (int i = 0; i < N; i++)
           for (int j = i; j < N; j++)
               int match = 0;
               for (int k = 0; k < 6; k++)
                   if (wordlist[i][k] == wordlist[j][k])
                       match++;
               }
               m_H[i][j] = m_H[j][i] = match;
           }
       }
       vector<int> possible;
       vector<bool> path(N, false);
       for (int i = 0; i < N; i++) possible.push_back(i);</pre>
       while (!possible.empty())
       {
            int guess = solve(possible, path);
            int matches = master.guess(wordlist[guess]);
            if (matches == wordlist[0].length()) return; // 找到答案
           // 找不到答案, 便需要找出下一個搜尋範圍
           vector<int> possible2;
           for (const int& j : possible)
               if (m_H[guess][j] == matches) possible2.push_back(j);
           possible = possible2;
           path[guess] = true;
   }
private:
   vector<vector<int>> m_H;
    int solve(const vector<int>& possible, const vector<bool>& path)
    {
```

```
if (possible.size() <= 2) return possible.front();</pre>
          int ansgrpSize = possible.size();
          int ansguess = -1;
          for (int guess = 0; guess < m_H.size(); guess++)</pre>
              if (!path[guess])
              {
                  vector<vector<int>> groups(7, vector<int>());
                  for (const int& j : possible)
                      if (j != guess)
                          groups[m_H[guess][j]].push_back(j);
                  }
                  int maxGroupSize = 0;
                  for (int i = 0; i < 7; i++)
                      if (groups[i].size() > maxGroupSize)
                          maxGroupSize = groups[i].size();
                  }
                  if (maxGroupSize < ansgrpSize)</pre>
                      ansgrpSize = maxGroupSize;
                      ansguess = guess;
              }
          }
         return ansguess;
     }
 };
Random Pick
 // 時間複雜度 O(N^2), 空間複雜度 O(N^2)
 class Solution {
 public:
     void findSecretWord(vector<string>& wordlist, Master& master) {
          string target = wordlist[rand() % wordlist.size()];
          int count = 10;
          while(count--) {
              int numMatch = master.guess(target);
              shrinkList(wordlist, target, numMatch);
              target = wordlist[rand() % wordlist.size()];
          }
     }
 private:
```

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```
void shrinkList(vector<string> & wordlist, const string & target, int numMatch) {
    vector<string> newList;
    for (auto & w : wordlist) {
        if (computeComm(w, target) == numMatch) {
            newList.push_back(w);
        }
    }
    wordlist = newList;
}

int computeComm(const string & s1, const string & s2) {
    int comm = 0;
    for (int i = 0; i < 6; ++i) {
        if (s1[i] == s2[i]) comm++;
    }
    return comm;
}</pre>
```

18.19 Bulls and Cows

描述

You are playing the following Bulls and Cows game with your friend: You write down a number and ask your friend to guess what the number is. Each time your friend makes a guess, you provide a hint that indicates how many digits in said guess match your secret number exactly in both digit and position (called "bulls") and how many digits match the secret number but locate in the wrong position (called "cows"). Your friend will use successive guesses and hints to eventually derive the secret number.

Write a function to return a hint according to the secret number and friend's guess, use A to indicate the bulls and B to indicate the cows.

Please note that both secret number and friend's guess may contain duplicate digits.

```
Example 1:
Input: secret = "1807", guess = "7810"
Output: "1A3B"

Explanation: 1 bull and 3 cows. The bull is 8, the cows are 0, 1 and 7.
    Example 2:
Input: secret = "1123", guess = "0111"
Output: "1A1B"

Explanation: The 1st 1 in friend's guess is a bull, the 2nd or 3rd 1 is a cow.
```

Note: You may assume that the secret number and your friend's guess only contain digits, and their lengths are always equal.

One pass One Hash map

```
// 時間複雜度 O(N), 空間複雜度 O(1)
class Solution {
public:
    string getHint(string secret, string guess) {
       // 利用正負數去代表 secret 和 guess 的出現來減少一個 hash map
       vector<int> counter(10, 0);
       int bulls = 0;
       int cows = 0;
       for (size_t i = 0; i < secret.size(); i++)</pre>
           const char& s = secret[i];
           const char& g = guess[i];
           if (s == g)
               bulls++;
           else
           {
               cows += (counter[s-'0'] < 0 ? 1 : 0) + (counter[g-'0'] > 0 ? 1 : 0);
               counter[s-'0']++; // 用正數代表 secret 出現
               counter[g-'0']--; // 用負數代表 guess 出現
           }
       }
       return to_string(bulls) + "A" + to_string(cows) + "B";
   }
};
```

第19章

Remake Data Structure

There are examples to try to remake those data strucutre in standard libraries for a practice purpose.

19.1 Smart Pointer

描述

Know more about smart pointer and reference counting.

分析

Nil

代碼

```
#include <iostream>
#include "DefaultMutex.h"
class ReferenceCount
public:
    ReferenceCount();
    ~ReferenceCount();
    void AddRef();
    int Release();
 private:
    int m_count;
    DefaultMutex m_mutex;
};
ReferenceCount::ReferenceCount()
{
    m_count = 0;
}
ReferenceCount::~ReferenceCount()
{
}
```

```
void ReferenceCount::AddRef()
    DefaultLock lock(m_mutex);
    m_count++;
}
int ReferenceCount::Release()
    DefaultLock lock(m_mutex);
    if (m_count > 0)
    {
        return --m_count;
    }
    else
    {
        m_count = 0;
        return m_count;
}
template<typename T>
class SmartPointer
 public:
    SmartPointer();
    SmartPointer(T* pData);
    SmartPointer(const SmartPointer<T>& smartPointer);
    template<typename U>
        SmartPointer(const SmartPointer<U>& smartPointer, T* pData);
    ~SmartPointer();
    T& operator* ();
    T* operator-> ();
    SmartPointer<T>& operator = (const SmartPointer<T>& smartPointer);
    T* Get();
    T* Get() const;
    template<typename> friend class SmartPointer; // with this friend, we can define the follow
 private:
    T* m_pData;
    ReferenceCount* m_pRC;
};
template<typename T>
SmartPointer<T> MakeSmartPointer();
template<typename T, typename U>
    SmartPointer<T> StaticCast(const SmartPointer<U>& smartPointer);
template<typename T, typename U>
    SmartPointer<T> DynamicCast(const SmartPointer<U>& smartPointer);
```

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```
// Start implementation
template<typename T>
SmartPointer<T>::SmartPointer()
   : m_pData(NULL), m_pRC(NULL)
{
   m_pRC = new ReferenceCount();
}
template<typename T>
SmartPointer<T>::SmartPointer(T* pData)
   : m_pData(pData), m_pRC(NULL)
{
   m_pRC = new ReferenceCount();
   m_pRC->AddRef();
}
template<typename T>
SmartPointer<T>::SmartPointer(const SmartPointer<T>& smartPointer)
   : m_pData(smartPointer.m_pData), m_pRC(smartPointer.m_pRC)
{
   m_pRC->AddRef();
}
template<typename T>
template<typename U>
SmartPointer<T>::SmartPointer(const SmartPointer<U>& smartPointer, T* pData)
   : m_pData(pData), m_pRC(smartPointer.m_pRC)
{
   m_pRC->AddRef();
}
template<typename T>
SmartPointer<T>::~SmartPointer()
   if (m_pRC->Release() == 0)
   {
       if (m_pData)
          delete m_pData;
       delete m_pRC;
   }
}
template<typename T>
T& SmartPointer<T>::operator* ()
{
   return *m_pData;
}
template<typename T>
```

```
T* SmartPointer<T>::operator-> ()
    return m_pData;
template<typename T>
SmartPointer<T>& SmartPointer<T>::operator = (const SmartPointer<T>& smartPointer)
    if (this != &smartPointer)
    {
        if (m_pRC->Release() == 0)
            if (m_pData)
                delete m_pData;
            delete m_pRC;
        }
        m_pData = smartPointer.m_pData;
        m_pRC = smartPointer.m_pRC;
        m_pRC->AddRef();
    }
    return *this;
}
template<typename T>
T* SmartPointer<T>::Get()
    return m_pData;
}
template<typename T>
T* SmartPointer<T>::Get() const
{
 return m_pData;
template<typename T>
SmartPointer<T> MakeSmartPointer()
    SmartPointer<T> smartPointer(new T());
    return smartPointer;
}
template<typename T, typename U>
SmartPointer<T> StaticCast(const SmartPointer<U>& smartPointer)
    T* p = static_cast<T*>(smartPointer.Get());
    return SmartPointer<T>(smartPointer, p);
}
template<typename T, typename U>
SmartPointer<T> DynamicCast(const SmartPointer<U>& smartPointer)
```

19.1 Smart Pointer 491

```
T* p = dynamic_cast<T*>(smartPointer.Get());
if (p)
    return SmartPointer<T>(smartPointer, p);
else
    return SmartPointer<T>();
}
```

相關題目

Nil

第 20 章

Database

Database questions

20.1 Combine Two Tables

描述

SQL Schema Table: Person

++					
-	Column Name	İ	Туре	 -	
1	PersonId FirstName LastName	 -	int varchar varchar	1	
+		+-		-+	

PersonId is the primary key column for this table.

Table: Address

++					
Column Name	Type				
AddressId PersonId	int				
City	varchar				
State	varchar				
++					

AddressId is the primary key column for this table.

Write a SQL query for a report that provides the following information for each person in the Person table, regardless if there is an address for each of those people:

outer join

```
// Note: Using where clause to filter the records will fail if there is
// no address information for a person because it will not display the name information.
SELECT
    FirstName, LastName, City, State
FROM
```

```
Person LEFT JOIN Address
ON
Person.PersonID = Address.PersonID
```

20.2 Second Highest Salary

描述

For example, given the above Employee table, the query should return 200 as the second highest salary. If there is no second highest salary, then the query should return null.

Write a SQL query to get the second highest salary from the Employee table.

sub-query and LIMIT clause

```
// Note: Use a sub-query to handle only one record in this table
SELECT
   (SELECT DISTINCT
        Salary
   FROM
        Employee
   ORDER BY Salary DESC
   LIMIT 1 OFFSET 1) AS SecondHighestSalary
.
```

IFNULL and LIMIT

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```
LIMIT 1 OFFSET 1),
NULL) AS SecondHighestSalary
```

20.3 Nth Highest Salary

描述

For example, given the above Employee table, the nth highest salary where n = 2 is 200. If there is no nth highest salary, then the query should return null.

Write a SQL query to get the nth highest salary from the Employee table.

IFNULL and LIMIT

```
CREATE FUNCTION getNthHighestSalary(N INT) RETURNS INT
BEGIN
SET N=N-1;
  RETURN (
      # Write your MySQL query statement below.
      select
          ifnull(
              (select distinct
                   salary
               from
                   employee
               order by salary desc
               limit N,1),
          null)
  );
END
```

20.4 Rank Scores

描述

SQL Schema

```
Create table If Not Exists Scores (Id int, Score DECIMAL(3,2))
Truncate table Scores
insert into Scores (Id, Score) values ('1', '3.5')
insert into Scores (Id, Score) values ('2', '3.65')
insert into Scores (Id, Score) values ('3', '4.0')
insert into Scores (Id, Score) values ('4', '3.85')
insert into Scores (Id, Score) values ('5', '4.0')
insert into Scores (Id, Score) values ('6', '3.65')
```

Write a SQL query to rank scores. If there is a tie between two scores, both should have the same ranking. Note that after a tie, the next ranking number should be the next consecutive integer value. In other words, there should be no "holes" between ranks.

Table: Scores

+		+-		+
-	Id	1	Score	1
+		+-		+
-	1	1	3.50	1
	2	1	3.65	
-	3	1	4.00	1
-	4	1	3.85	
-	5	1	4.00	
-	6	1	3.65	1
+		+-		+

For example, given the above Scores table, your query should generate the following report (order by highest score):

+		+-		+
-	score	1	Rank	1
+		+-		+
-	4.00	1	1	- 1
-	4.00		1	- 1
-	3.85		2	- 1
- [3.65		3	- 1
- [3.65		3	- 1
-	3.50		4	- 1
+		+-		+

Important Note: For MySQL solutions, to escape reserved words used as column names, you can use an apostrophe before and after the keyword. For example 'Rank'.

Dense_Rank

```
SELECT Score, dense_rank() OVER(ORDER BY Score DESC) AS `Rank` FROM Scores;
```

20.5 Consecutive Numbers

描述

```
Create table If Not Exists Logs (Id int, Num int) Truncate table Logs insert into Logs (Id, Num) values ('1', '1') insert into Logs (Id, Num) values ('2', '1') insert into Logs (Id, Num) values ('3', '1') insert into Logs (Id, Num) values ('4', '2') insert into Logs (Id, Num) values ('5', '1') insert into Logs (Id, Num) values ('6', '2') insert into Logs (Id, Num) values ('7', '2')
```

Write an SQL query to find all numbers that appear at least three times consecutively. Return the result table in any order. The query result format is in the following example:

Table: Logs

id is the primary key for this table.

Logs table:

```
+---+
| Id | Num |
+---+
| 1 | 1 | 1 |
| 2 | 1 |
| 3 | 1 |
| 4 | 2 |
| 5 | 1 |
| 6 | 2 |
| 7 | 2 |
```

Result table:

1 is the only number that appears consecutively for at least three times.

multiple table

```
SELECT DISTINCT
11.Num AS ConsecutiveNums
FROM
Logs 11,
Logs 12,
Logs 13
WHERE
11.Id = 12.Id - 1
```

```
AND 12.Id = 13.Id - 1
AND 11.Num = 12.Num
AND 12.Num = 13.Num
```

20.6 Employees Earning More Than Their Managers

描述

SQL Schema

```
Create table If Not Exists Employee (Id int, Name varchar(255), Salary int, ManagerId int) Truncate table Employee insert into Employee (Id, Name, Salary, ManagerId) values ('1', 'Joe', '70000', '3') insert into Employee (Id, Name, Salary, ManagerId) values ('2', 'Henry', '80000', '4') insert into Employee (Id, Name, Salary, ManagerId) values ('3', 'Sam', '60000', 'None') insert into Employee (Id, Name, Salary, ManagerId) values ('4', 'Max', '90000', 'None')
```

The Employee table holds all employees including their managers. Every employee has an Id, and there is also a column for the manager Id.

Table: Employee

Id	Name	Salary	++ ManagerId
1 2 3 4	Joe Henry Sam Max	70000 80000 60000 90000	4 NULL

Given the Employee table, write a SQL query that finds out employees who earn more than their managers. For the above table, Joe is the only employee who earns more than his manager.

```
+----+
| Employee |
+----+
| Joe |
```

multiple table

```
SELECT
a.Name AS 'Employee'
FROM
Employee AS a,
Employee AS b
WHERE
a.ManagerId = b.Id
AND a.Salary > b.Salary;
```

join

```
SELECT

a.NAME AS Employee

FROM Employee AS a JOIN Employee AS b

ON a.ManagerId = b.Id

AND a.Salary > b.Salary
.
```

20.7 Duplicate Emails

描述

```
SQL Schema
```

```
Create table If Not Exists Person (Id int, Email varchar(255))
Truncate table Person
insert into Person (Id, Email) values ('1', 'a@b.com')
insert into Person (Id, Email) values ('2', 'c@d.com')
insert into Person (Id, Email) values ('3', 'a@b.com')
```

Write a SQL query to find all duplicate emails in a table named Person.

Table: Person

For example, your query should return the following for the above table:

```
+----+
| Email |
+----+
| a@b.com |
```

Using GROUP BY and a temporary table

```
select Email from
(
  select Email, count(Email) as num
  from Person
  group by Email
) as statistic
where num > 1
;
```

Using GROUP BY and HAVING condition

```
select Email
from Person
group by Email
having count(Email) > 1;
```

20.8 Customers Who Never Order

描述

```
SQL Schema
```

```
Create table If Not Exists Customers (Id int, Name varchar(255))
Create table If Not Exists Orders (Id int, CustomerId int)
Truncate table Customers
insert into Customers (Id, Name) values ('1', 'Joe')
insert into Customers (Id, Name) values ('2', 'Henry')
insert into Customers (Id, Name) values ('3', 'Sam')
insert into Customers (Id, Name) values ('4', 'Max')
Truncate table Orders
insert into Orders (Id, CustomerId) values ('1', '3')
insert into Orders (Id, CustomerId) values ('2', '1')
```

Suppose that a website contains two tables, the Customers table and the Orders table. Write a SQL query to find all customers who never order anything.

Table: Customers.

```
+----+
| Id | Name |
+----+
| 1 | Joe |
| 2 | Henry |
| 3 | Sam |
| 4 | Max |
```

Table: Orders.

+-		+-		+
1	Id	1	${\tt CustomerId}$	1
+		+-		+
1	1	1	3	1
1	2	1	1	1
+-		+-		+

Using the above tables as example, return the following:

Not In

```
select customers.name as 'Customers'
from customers
where customers.id not in
(
    select customerid from orders
);
```

Left Join

```
SELECT Name AS 'Customers'
FROM Customers c
LEFT JOIN Orders o
ON c.Id = o.CustomerId
WHERE o.CustomerId IS NULL;
```

20.9 Department Highest Salary

描述

```
SQL Schema
```

```
Create table If Not Exists Employee (Id int, Name varchar(255), Salary int, DepartmentId int)
Create table If Not Exists Department (Id int, Name varchar(255))
Truncate table Employee
insert into Employee (Id, Name, Salary, DepartmentId) values ('1', 'Joe', '70000', '1')
insert into Employee (Id, Name, Salary, DepartmentId) values ('2', 'Jim', '90000', '1')
insert into Employee (Id, Name, Salary, DepartmentId) values ('3', 'Henry', '80000', '2')
insert into Employee (Id, Name, Salary, DepartmentId) values ('4', 'Sam', '60000', '2')
insert into Employee (Id, Name, Salary, DepartmentId) values ('5', 'Max', '90000', '1')
Truncate table Department
insert into Department (Id, Name) values ('1', 'IT')
insert into Department (Id, Name) values ('2', 'Sales')
```

The Employee table holds all employees. Every employee has an Id, a salary, and there is also a column for the department Id.

++-	+		+-	+
Id	Name	Salary	İ	DepartmentId
1 2 3 4 5	Joe Jim Henry Sam Max	70000 90000 80000 60000 90000	1 1 1 1	1 1 2 2 2 1 1
++-	+		+-	+

The Department table holds all departments of the company.

```
+---+---+
| Id | Name |
+---+----+
| 1 | IT |
```

```
| 2 | Sales |
```

Write a SQL query to find employees who have the highest salary in each of the departments. For the above tables, your SQL query should return the following rows (order of rows does not matter).

Department	+ Employee	++ Salary +
IT	Max	90000
IT	Jim	90000
Sales	Henry	80000

Join, In

20.10 Department Top Three Salaries

描述

```
SQL Schema
```

```
Create table If Not Exists Employee (Id int, Name varchar(255), Salary int, DepartmentId int)
Create table If Not Exists Department (Id int, Name varchar(255))
Truncate table Employee
insert into Employee (Id, Name, Salary, DepartmentId) values ('1', 'Joe', '85000', '1')
insert into Employee (Id, Name, Salary, DepartmentId) values ('2', 'Henry', '80000', '2')
insert into Employee (Id, Name, Salary, DepartmentId) values ('3', 'Sam', '60000', '2')
insert into Employee (Id, Name, Salary, DepartmentId) values ('4', 'Max', '90000', '1')
insert into Employee (Id, Name, Salary, DepartmentId) values ('5', 'Janet', '69000', '1')
insert into Employee (Id, Name, Salary, DepartmentId) values ('6', 'Randy', '85000', '1')
insert into Employee (Id, Name, Salary, DepartmentId) values ('7', 'Will', '70000', '1')
Truncate table Department
insert into Department (Id, Name) values ('1', 'IT')
insert into Department (Id, Name) values ('2', 'Sales')
```

Table: Employee

4.		٠.		_
 -	Column Name	-	Туре	 -
1		1		T
	Id	ı	int	ı
	Name	1	varchar	
1	Salary	1	int	
1	DepartmentId	1	int	
+-		+-		+

Id is the primary key for this table.

Each row contains the ID, name, salary, and department of one employee.

Table: Department

+-			+-	+
1	${\tt Column}$	Name	1	Type
+-			+-	+
-	Id		1	int
-	Name		1	varchar
+-			+-	+

Id is the primary key for this table.

Each row contains the ID and the name of one department.

A company's executives are interested in seeing who earns the most money in each of the company's departments. A high earner in a department is an employee who has a salary in the top three unique salaries for that department.

Write an SQL query to find the employees who are high earners in each of the departments.

Return the result table in any order.

The query result format is in the following example:

Employee table:

++			+
Id	Name	Salary	DepartmentId
++ 1	Henry Sam	60000 90000	1
6	Randy	85000	1
7	Will	70000	1
++			

Department table:

ㅗ.				
:			Name	Ī
+-		+-		+
1	1	1	IT	1
	2	1	Sales	
+.		٠.		-+

Result table:

```
+----+
 | Department | Employee | Salary |
 +----+
 +----+
 In the IT department:
 - Max earns the highest unique salary
 - Both Randy and Joe earn the second-highest unique salary
 - Will earns the third-highest unique salary
 In the Sales department:
 - Henry earns the highest salary
 - Sam earns the second-highest salary
 - There is no third-highest salary as there are only two employees
Join, sub-query
 SELECT
     d.Name AS 'Department', e1.Name AS 'Employee', e1.Salary
 FROM
     Employee e1
        JOIN
     Department d ON e1.DepartmentId = d.Id
     3 > (SELECT
            COUNT(DISTINCT e2.Salary)
        FROM
            Employee e2
        WHERE
            e2.Salary > e1.Salary
               AND e1.DepartmentId = e2.DepartmentId
        )
Join, dense rank
 SELECT d.NAME AS Department,
       a. NAME AS Employee,
       a. salary
 FROM (SELECT e.*,
               Dense_rank()
                OVER (
                  partition BY departmentid
                  ORDER BY salary DESC) AS DeptPayRank
        FROM
               employee e) a
       JOIN department d
```

```
ON a. departmentid = d. id WHERE deptpayrank <= 3;
```

20.11 Delete Duplicate Emails

描述

SOL Schema

```
Truncate table Person insert into Person (Id, Email) values ('1', 'john@example.com') insert into Person (Id, Email) values ('2', 'bob@example.com') insert into Person (Id, Email) values ('3', 'john@example.com')
```

Write a SQL query to delete all duplicate email entries in a table named Person, keeping only unique emails based on its smallest Id.

For example, after running your query, the above Person table should have the following rows:

```
+---+
| Id | Email | |
+---+
| 1 | john@example.com | | 2 | bob@example.com | |
```

Note:

Your output is the whole Person table after executing your sql. Use delete statement.

Delete, Where

```
DELETE p1 FROM Person p1,
    Person p2
WHERE
    p1.Email = p2.Email AND p1.Id > p2.Id;
```

20.12 Rising Temperature

描述

```
Create table If Not Exists Weather (Id int, RecordDate date, Temperature int)
Truncate table Weather
insert into Weather (Id, RecordDate, Temperature) values ('1', '2015-01-01', '10')
insert into Weather (Id, RecordDate, Temperature) values ('2', '2015-01-02', '25')
insert into Weather (Id, RecordDate, Temperature) values ('3', '2015-01-03', '20')
insert into Weather (Id, RecordDate, Temperature) values ('4', '2015-01-04', '30')
```

Table: Weather

+	
Column Name	Type
+	++
id	int
recordDate	date
temperature	int
+	++

4-----

id is the primary key for this table.

This table contains information about the temperature in a certain day.

Write an SQL query to find all dates' id with higher temperature compared to its previous dates (yester-day).

Return the result table in any order.

The query result format is in the following example:

Weather

++		
		Temperature
1	2015-01-01 2015-01-02 2015-01-03 2015-01-04	10 25 20 30
++	+	+

Result table:

```
+----+
| id |
+----+
| 2 |
| 4 |
```

In 2015-01-02, temperature was higher than the previous day $(10 \rightarrow 25)$. In 2015-01-04, temperature was higher than the previous day $(20 \rightarrow 30)$.

Join, Datediff

```
SELECT
   weather.id AS 'Id'
FROM
   weather
        JOIN
   weather w ON DATEDIFF(weather.recordDate, w.recordDate) = 1
        AND weather.Temperature > w.Temperature
;
```

Join, Subdate

```
select
    w1.id
from
    Weather w1
join
    Weather w2
οn
    subdate(w1.recordDate, 1) = w2.recordDate
    and w1. Temperature > w2. Temperature;
```

20.13 **Trips and Users**

描述

SQL Schema

```
Create table If Not Exists Trips (Id int, Client Id int, Driver Id int, City Id int, Status EN
Create table If Not Exists Users (Users Id int, Banned varchar(50), Role ENUM('client', 'drive
Truncate table Trips
insert into Trips (Id, Client_Id, Driver_Id, City_Id, Status, Request_at) values ('1', '1', '1
insert into Trips (Id, Client_Id, Driver_Id, City_Id, Status, Request_at) values ('2', '2', '1')
insert into Trips (Id, Client_Id, Driver_Id, City_Id, Status, Request_at) values ('3', '3',
insert into Trips (Id, Client_Id, Driver_Id, City_Id, Status, Request_at) values ('4', '4', '1
insert into Trips (Id, Client_Id, Driver_Id, City_Id, Status, Request_at) values ('5', '1', '1
insert into Trips (Id, Client_Id, Driver_Id, City_Id, Status, Request_at) values ('6', '2', '1
insert into Trips (Id, Client_Id, Driver_Id, City_Id, Status, Request_at) values ('7', '3', '1
insert into Trips (Id, Client_Id, Driver_Id, City_Id, Status, Request_at) values ('8', '2', '1
insert into Trips (Id, Client_Id, Driver_Id, City_Id, Status, Request_at) values ('9', '3', '1
insert into Trips (Id, Client_Id, Driver_Id, City_Id, Status, Request_at) values ('10', '4', '
Truncate table Users
insert into Users (Users_Id, Banned, Role) values ('1', 'No', 'client')
insert into Users (Users_Id, Banned, Role) values ('2', 'Yes', 'client')
insert into Users (Users_Id, Banned, Role) values ('3', 'No', 'client')
insert into Users (Users_Id, Banned, Role) values ('4', 'No', 'client')
insert into Users (Users Id, Banned, Role) values ('10', 'No', 'driver')
insert into Users (Users_Id, Banned, Role) values ('11', 'No', 'driver')
insert into Users (Users_Id, Banned, Role) values ('12', 'No', 'driver')
```

insert into Users (Users Id, Banned, Role) values ('13', 'No

' 1

Table: Trips

+	-+
Column Name	Type
+	-+
Id	int
Client_Id	int
Driver_Id	int
City_Id	int
Status	enum
Request_at	date
+	-++

Id is the primary key for this table.

The table holds all taxi trips. Each trip has a unique Id, while Client_Id and Driver_Id are for Status is an ENUM type of ('completed' , 'cancelled_by_driver' , 'cancelled_by_client').

Table: Users

Column Name	Type
Users_Id Banned Role	int

Users_Id is the primary key for this table.

The table holds all users. Each user has a unique Users_Id, and Role is an ENUM type of ('cli Status is an ENUM type of ('Yes', 'No').

Write a SQL query to find the cancellation rate of requests with unbanned users (both client and driver must not be banned) each day between "2013-10-01" and "2013-10-03".

The cancellation rate is computed by dividing the number of canceled (by client or driver) requests with unbanned users by the total number of requests with unbanned users on that day.

Return the result table in any order. Round Cancellation Rate to two decimal points.

The query result format is in the following example:

Trips table:

	_	Driver_Id	• –	Status	Request_at
1 2 3 4 5 6 7 8 9 10	1 2 3 4 1 2 3 2 3	10 11 12 13 10 11 12 12 10	1 1 6 6 1 6 6 12 12 12	completed cancelled_by_driver completed cancelled_by_client completed completed completed completed completed completed completed cancelled_by_driver	2013-10-01 2013-10-01 2013-10-01 2013-10-01 2013-10-02 2013-10-02 2013-10-03 2013-10-03 2013-10-03

Users table:

+	-+-		+-		-+
Users_Id	į	Banned	İ	Role	į
1		No	T.	client	1
2	1	Yes	I	client	1
3	1	No	I	client	1
4	1	No	I	client	1
10	1	No		driver	1
11	1	No	I	driver	1
12	1	No	١	driver	1
13	1	No	١	driver	1

```
Result table:
        | Cancellation Rate |
 +----+
  | 2013-10-01 | 0.33
  | 2013-10-02 | 0.00
  | 2013-10-03 | 0.50
 On 2013-10-01:
   - There were 4 requests in total, 2 of which were canceled.
   - However, the request with Id=2 was made by a banned client (User_Id=2), so it is ignored in
   - Hence there are 3 unbanned requests in total, 1 of which was canceled.
   - The Cancellation Rate is (1/3) = 0.33
 On 2013-10-02:
   - There were 3 requests in total, 0 of which were canceled.
   - The request with Id=6 was made by a banned client, so it is ignored.
   - Hence there are 2 unbanned requests in total, 0 of which were canceled.
   - The Cancellation Rate is (0 / 2) = 0.00
 On 2013-10-03:
   - There were 3 requests in total, 1 of which was canceled.
   - The request with Id=8 was made by a banned client, so it is ignored.
   - Hence there are 2 unbanned request in total, 1 of which were canceled.
   - The Cancellation Rate is (1 / 2) = 0.50
CASE WHEN, Extra Column
 SELECT
     t.Request at AS Day
      , ROUND(SUM(t.flag) / COUNT(t.Request_at), 2) AS "Cancellation Rate"
 FROM
      (
         SELECT
              , CASE WHEN Status!='completed' THEN 1 ELSE 0 END AS flag
         FROM
             Trips
         WHERE
                     Request_at >= '2013-10-01' AND Request_at <= '2013-10-03'</pre>
             AND Client_Id NOT IN (SELECT Users_Id FROM Users WHERE Banned='Yes')
             AND Driver_Id NOT IN (SELECT Users_Id FROM Users WHERE Banned='Yes')
     ) AS t
 GROUP BY
     t.Request_at
Extra Table
 WITH cte AS
```

SELECT

```
Client Id
      , Driver Id
      , Status
      , Request_at
     , CASE WHEN Status!='completed' THEN 1 ELSE 0 END AS flag
 FROM
     Trips
 WHERE
     Request_at >= '2013-10-01' AND Request_at <= '2013-10-03'</pre>
     AND Client_Id NOT IN (SELECT Users_Id FROM Users WHERE Banned='Yes')
     AND Driver_Id NOT IN (SELECT Users_Id FROM Users WHERE Banned='Yes')
 )
 SELECT
     Request_at AS Day
      , ROUND(SUM(flag) / COUNT(*), 2) AS 'Cancellation Rate'
 FROM
     cte
 GROUP BY
     Request_at
Extra Table, Faster
 WITH cte AS
 SELECT
      , CASE WHEN Status!='completed' THEN 1 ELSE 0 END AS flag
 FROM
     Trips
     Request_at >= '2013-10-01' AND Request_at <= '2013-10-03'</pre>
     AND Client_Id NOT IN (SELECT Users_Id FROM Users WHERE Banned='Yes')
     AND Driver_Id NOT IN (SELECT Users_Id FROM Users WHERE Banned='Yes')
 )
 SELECT
     Request_at AS Day
      , ROUND(SUM(flag) / COUNT(*), 2) AS 'Cancellation Rate'
 FROM
     cte
 GROUP BY
     Request_at
```

20.14 Game Play Analysis I

描述

Create table If Not Exists Activity (player_id int, device_id int, event_date date, games_play Truncate table Activity
insert into Activity (player_id, device_id, event_date, games_played) values ('1', '2', '2016insert into Activity (player_id, device_id, event_date, games_played) values ('1', '2', '2016insert into Activity (player_id, device_id, event_date, games_played) values ('2', '3', '2017insert into Activity (player_id, device_id, event_date, games_played) values ('3', '1', '2016insert into Activity (player_id, device_id, event_date, games_played) values ('3', '4', '2018-

Table: Activity

Column Name Type
player_id int
device_id int
event_date date
games_played int
++

(player_id, event_date) is the primary key of this table.

This table shows the activity of players of some game.

Each row is a record of a player who logged in and played a number of games (possibly 0) before

Write an SQL query that reports the first login date for each player.

The query result format is in the following example:

Activity table:

+			
player_id	device_id	event_date	games_played
1	2 3 1	2016-03-01 2016-05-02 2017-06-25 2016-03-02 2018-07-03	6
T			r+

Result table:

	ㅗ.		
player_id	ļ	first_login	ļ
+	+		+
1		2016-03-01	١
1 2		2017-06-25	1
3		2016-03-02	1
+	٠.		

GROUP BY, MIN

```
SELECT
    player_id,
    MIN(event_date) AS first_login
FROM
    activity
GROUP BY
```

```
player_id
```

20.15 Game Play Analysis II

描述

SQL Schema

Create table If Not Exists Activity (player_id int, device_id int, event_date date, games_played) Truncate table Activity insert into Activity (player_id, device_id, event_date, games_played) values ('1', '2', '2016-insert into Activity (player_id, device_id, event_date, games_played) values ('1', '2', '2016-insert into Activity (player_id, device_id, event_date, games_played) values ('2', '3', '2017-insert into Activity (player_id, device_id, event_date, games_played) values ('3', '1', '2016-insert into Activity (player_id, device_id, event_date, games_played) values ('3', '4', '2018-insert into Activity (player_id, device_id, event_date, games_played) values ('3', '4', '2018-

Table: Activity

+.	Column Name	-+- -	Туре	-+ -
T +	player_id device_id event_date games_played		int int date int	 -+

(player_id, event_date) is the primary key of this table.

This table shows the activity of players of some game.

Each row is a record of a player who logged in and played a number of games (possibly 0) before

Write an SQL query that reports the first login date for each player.

The query result format is in the following example:

Activity table:

player_id device_id event_date games_played
1

Result table:

+	
player_id	device_id
1	l 2
1 2	. – . I 3 I
3	1
+	++

```
GROUP BY, MIN
```

```
SELECT
   player_id
   , device_id
FROM
   activity
WHERE
   (player_id
    , event_date)
IN
   (SELECT
        player_id
        , MIN(event_date) AS event_date
   FROM
        activity
   GROUP BY player_id)
;
```

GROUP BY, Dense_Rank

```
SELECT
    player_id
    , device_id
FROM
    (SELECT
         player_id
         , device_id
         , DENSE_RANK() OVER (PARTITION BY player_id ORDER BY event_date) AS num
FROM
         activity) AS a
WHERE
         num = 1
.
```

20.16 Game Play Analysis III

描述

```
Create table If Not Exists Activity (player_id int, device_id int, event_date date, games_player Truncate table Activity insert into Activity (player_id, device_id, event_date, games_played) values ('1', '2', '2016-insert into Activity (player_id, device_id, event_date, games_played) values ('1', '2', '2016-insert into Activity (player_id, device_id, event_date, games_played) values ('2', '3', '2017-insert into Activity (player_id, device_id, event_date, games_played) values ('3', '1', '2016-insert into Activity (player_id, device_id, event_date, games_played) values ('3', '4', '2018-insert into Activity (player_id, device_id, event_date, games_played) values ('3', '4', '2018-insert into Activity (player_id, device_id, event_date, games_played) values ('3', '4', '2018-insert into Activity (player_id, device_id, event_date, games_played) values ('3', '4', '2018-insert into Activity (player_id, device_id, event_date, games_played) values ('3', '4', '2018-insert into Activity (player_id, device_id, event_date, games_played) values ('3', '4', '2018-insert into Activity (player_id, device_id, event_date, games_played) values ('3', '4', '2018-insert into Activity (player_id, device_id, event_date, games_played) values ('3', '4', '2018-insert into Activity (player_id, device_id, event_date, games_played) values ('3', '4', '2018-insert into Activity (player_id, device_id, event_date, games_played) values ('3', '4', '2018-insert into Activity (player_id, device_id, event_date, games_played) values ('3', '4', '2018-insert into Activity (player_id, device_id, event_date, games_played) values ('3', '4', '2018-insert into Activity (player_id, device_id, event_date, games_played) values ('3', '4', '2018-insert into Activity (player_id, device_id, event_date, games_played) values ('3', '4', '2018-insert into Activity (player_id, device_id, event_date, games_played) values ('3', '4', '2018-insert into Activity (player_id, device_id, event_date, games_played) values ('3', '4', '2018-insert into Activity (player_id, device_id, e
```

```
Table: Activity
```

```
+-----+
| Column Name | Type | +-----+
```

```
| player_id | int | device_id | int | event_date | date | games_played | int |
```

(player_id, event_date) is the primary key of this table.

This table shows the activity of players of some game.

Each row is a record of a player who logged in and played a number of games (possibly 0) before logging out on some day using some device.

Write an SQL query that reports for each player and date, how many games played so far by the player.

That is, the total number of games played by the player until that date. Check the example for clarity.

The query result format is in the following example:

Activity table:

+			
player_id	device_id	event_date	games_played
	2 3 1	2016-03-01 2016-05-02 2017-06-25 2016-03-02 2018-07-03	6 1 0

Result table:

+		L
player_id	event_date	games_played_so_far
1 1 3	2016-03-01 2016-05-02 2017-06-25 2016-03-02 2018-07-03	11
+		++

For the player with id 1, 5 + 6 = 11 games played by 2016-05-02, and 5 + 6 + 1 = 12 games played by 2017-06-25.

For the player with id 3, 0 + 5 = 5 games played by 2018-07-03.

Note that for each player we only care about the days when the player logged in.

SUM, Window Function