

- Topics

1. Stack
2. Queue
3. Trees
4. Hashing
5. Graphs

Stacks : Basic Ops

Array
Linked list
Infix Postfix
Hanoi
Function Calls

Queue : Basic Ops

Arr
LL
Apps
Types

Trees : Binary tree

Traversal
BST
AVL
B-TREE , HEAP , HASH

Graphs : BFS

DFS

MST

Topological sort

PRIM

KRUSKAL



• Stacks

Array Implementation

Program :-

```
#include <stdio.h>
#include <stdlib.h>
#define N 5;
```

```
int stack[N];
int top = -1;
```

```
int isempty() {
    return top == -1;
}
```

```
int isfull() {
    return top == N-1;
}
```

```
void push() {
```

```
    int x;
    printf("Enter data: ");
    scanf("%d", &x);
```

```
    if (isfull()) {
        printf("Overflow");
    }
```

```
    else {
        top++;
        stack[top] = x;
    }
```

```
}
```

```
void pop() {
```

```
    int item;
```

```
    if (isempty()) {
        printf("Underflow");
    }
```

```
    else {
```

```
        item = stack[top];
        top--;
        printf("%d deleted", item);
    }
```

```
void display() {
```

```
    int i
```

```
    for (int i=top; i>=0; i--) {
        printf("%d\n", stack[i]);
    }
```

```
int main() {
```

```
:
```

```
}
```

Linked List Implementation

Program :-

```
# include <stdio.h>
# include <stdlib.h>

Struct node {
    int data ;
    Struct node * next;
}
Struct node * top = 0
```

```
void push (int x) {
```

```
    Struct node * newnode ;
    newnode = (Struct node *) malloc (sizeof (Struct node));
    newnode -> data = x ;
    newnode -> next = top ;
    top = newnode ;
}
```

```
void pop () {
```

```
    Struct node * temp ;
    temp = top ;
    if ( top == -1 ) {
        printf (" Underflow ");
    }
    else {
```

```
        printf ("%d deleted ", top -> data );
    }
```

```
    top = top -> next
```

```
    free (temp);
}
```

```
}
```

```
void display () {
```

```
    Struct node * temp
    temp = top
```

```

if ( top == 0 ) {
    printf( " empty " );
}
else {
    while ( temp != 0 ) {
        printf( "%d \n" temp->data );
        temp = temp->next
    }
}

```

3

```
int main () {
```

3

Infix to postfix

Infix to Postfix Conversion

- ① Print Operands as they arrive
- ② If stack is empty or contains a left parenthesis on top, push the incoming operator onto the stack
- ③ If incoming symbol is '(', push it onto stack
- ④ If incoming symbol is ')', pop the stack & print the operators until left parenthesis is found.
- ⑤ If incoming symbol has higher precedence than the top of the stack, push it on the stack.
- ⑥ If incoming symbol has lower precedence than the top of the stack, pop & print the top. Then test the incoming operator against the new top of the stack.
- ⑦ If incoming operator has equal precedence with the top of the stack, use associativity rule.
- ⑧ At the end of the expression, pop & print all operators of stack.

⇒ associativity [L to R] then pop & print the top of the stack & then push the incoming operator
 ⇒ [R to L] then push the incoming operator

①	() {} []	→ R-L
②	^	→ L-R
③	* /	→ L-R
④	+	→ L-R

Postfix evaluation

Begin
 for each character in postfix expr, do
 if operand is encountered, push it onto stack
 else if operator is encountered, pop 2 elements
 A → top element
 B → next to top element
 result = B operator A
 push result onto stack
 return element of stack top
 End

Hanoi

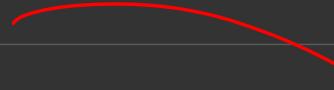
```

START
Procedure Hanoi(disk, source, dest, temp)

IF disk == 1, THEN
    move disk from source to dest
ELSE
    Hanoi(disk - 1, source, temp, dest) // Step 1
    move disk from source to dest // Step 2
    Hanoi(disk - 1, temp, dest, source) // Step 3
END IF

END Procedure
STOP

```

- Queue 

deletion from front & insertⁿ from rear

Array Implementation

Program :-

```
# include <stdio.h>
# define N 5
int queue [N];
int front = -1;
int rear = -1;
```

```
void enqueue (int x)
```

```
if (rear == N-1) {
    printf("Overflow");
}
else if (front == -1 && rear == -1) {
    front = rear = 0
    queue [rear] = x;
}
else {
    rear++;
    queue [rear] = x;
}
```

```
void dequeue () {
```

```
if (front == -1 && rear == -1) {
    printf("Underflow");
}
else if (front == rear) {
    front = rear = -1;
}
else {
    printf ("%d deleted ", queue [front]);
    front++;
}
```

```

void display () {
    if ( rear == -1 && front == -1 ) {
        printf( " Underflow " );
    }
    else {
        for ( int i = front ; i <= rear ; i++ ) {
            printf( "%d\n" , queue [ i ] );
        }
    }
}

```

```

int main () {
}

```

Linked list implementation

Program :-

```

#include <stdlib.h>
#include <stdio.h>

struct Node {
    int data;
    struct Node * next;
};

struct Node * front = 0;
struct Node * rear = 0;

void enqueue ( int x ) {
    struct Node * newnode;
    newnode = ( struct node * ) malloc ( sizeof ( struct Node * ) );
    newnode -> data = x;
    newnode -> next = 0;

    if ( front == 0 && rear == 0 ) {
        front = rear = newnode;
    }
    else {
        rear -> next = newnode;
        rear = newnode;
    }
}

```

```
void dequeue() {
    struct Node *temp;
    temp = front;
    if (front == 0 && rear == 0) {
        printf (" Underflow ");
    }
    else {
        printf ("%d deleted ", front->data);
        front = front->next;
        free (temp);
    }
}
```

```
void display () {
    struct Node *temp;
    temp = front;
    if (front == 0 && rear == 0) {
        printf (" Underflow ");
    }
    else {
        while (temp != 0) {
            printf ("%d \n ", temp->data);
            temp = temp->next;
        }
    }
}
```

```
int main () {
}
```

Circular Queue

Program :-

```
#include <stdio.h>
#define MAX_SIZE 5 // Change this to any desired maximum

typedef struct {
    int queue[MAX_SIZE];
    int front;
    int rear;
} CircularQueue;

// Initialize the queue
void initializeQueue(CircularQueue *cq) {
    cq->front = -1;
    cq->rear = -1;
}

// Function to check if the Circular Queue is empty
int is_empty(CircularQueue *cq) {
    return cq->front == -1;
}

// Function to check if the Circular Queue is full
int is_full(CircularQueue *cq) {
    return (cq->rear + 1) % MAX_SIZE == cq->front;
}

// Function to add an element to the Circular Queue
const char* enqueue(CircularQueue *cq, int data) {
    if (is_full(cq)) {
        return "Queue is full";
    }
    if (is_empty(cq)) {
        cq->front = cq->rear = 0;
    } else {
        cq->rear = (cq->rear + 1) % MAX_SIZE;
    }
    cq->queue[cq->rear] = data;
    return "Enqueued element";
}

// Function to remove an element from the Circular Queue
const char* dequeue(CircularQueue *cq) {
    if (is_empty(cq)) {
        return "Queue is empty";
    }
    int data_to_dequeue = cq->queue[cq->front];
    if (cq->front == cq->rear) {
        cq->front = cq->rear = -1; // Queue is now empty
    } else {
        cq->front = (cq->front + 1) % MAX_SIZE;
    }
    printf("Dequeued element: %d\n", data_to_dequeue);
    return "Dequeued element";
}

// Function to get the front element of the Circular Queue
const char* peek_front(CircularQueue *cq) {
    if (is_empty(cq)) {
        return "Queue is empty";
    }
    printf("Front element: %d\n", cq->queue[cq->front]);
    return "Front element retrieved";
}

// Function to get the rear element of the Circular Queue
const char* peek_rear(CircularQueue *cq) {
    if (is_empty(cq)) {
        return "Queue is empty";
    }
    printf("Rear element: %d\n", cq->queue[cq->rear]);
    return "Rear element retrieved";
}

// Function to get the rear element of the Circular Queue
const char* peek_rear(CircularQueue *cq) {
    if (is_empty(cq)) {
        return "Queue is empty";
    }
    printf("Rear element: %d\n", cq->queue[cq->rear]);
    return "Rear element retrieved";
}

int main() {
    CircularQueue cq;
    initializeQueue(&cq);

    // Testing the circular queue operations
    printf("%s\n", enqueue(&cq, 10));
    printf("%s\n", enqueue(&cq, 20));
    printf("%s\n", enqueue(&cq, 30));
    printf("%s\n", peek_front(&cq));
    printf("%s\n", peek_rear(&cq));
    printf("%s\n", dequeue(&cq));
    printf("%s\n", dequeue(&cq));
    printf("%s\n", dequeue(&cq));
    printf("%s\n", dequeue(&cq)); // Should indicate queue is empty
    printf("%s\n", dequeue(&cq));

    return 0;
}
```


• Trees

• Binary Tree Representation

Program :-

```
#include <stdio.h>
#include <stdlib.h>
```

```
struct node {
    int data,
    struct node * left, * right ;
};
```

```
struct node * create () {
```

```
    int x ;
```

```
    struct node * newnode ;
```

```
newnode = (struct node *) malloc ( sizeof (struct node*) ) ;
```

```
printf (" Enter data & -1 if no node : " );
```

```
scanf ("%d ", &x) ;
```

```
if (x == -1) {
```

```
    return 0 ;
```

```
}
```

```
else {
```

```
    newnode -> data = x ;
```

```
    printf (" Enter left child of %d ", x) ;
```

```
    newnode -> left = create () ;
```

```
    printf (" Enter right child of %d ", x) ;
```

```
    newnode -> right = create () ;
```

```
    return newnode ;
```

```
}
```

```
int main () {
```

```
    struct node * root ;
```

```
    root = 0 ;
```

```
    root = create () ;
```

```
}
```

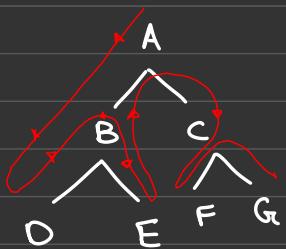
• Tree Traversal

1. Preorder Traversal

L (Root , left , right)

- Here , first we traverse the root
- Then go to left subtree n go on
- In left subtree , first the left child then right child
- Then the right subtree

eg



order of : A → B → D → E → C → F → G,
traversal

2. Inorder Traversal (left , root , right)

- Here go to the left-child of left-most subtree
- The root and the right sub-tree

eg

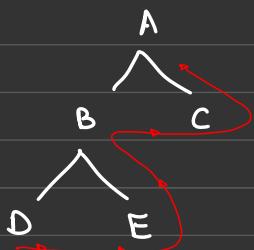


Order D → B → E → A → C

3. Postorder traversal

- Here first the left-child of left-most subtree
- Then the right child
- Then parent of left subtree
- The left child of right subtree then the right child n parent
- At last , root

eg



Order : D → E → B → C → A

Program :-

```
#include <stdio.h>
#include <stdlib.h>

struct node {
    int data;
    struct node * left, * right;
};

struct node * create () {
    // Same as the the prog above //
}

void preorder (struct node * root) {
    if (root == NULL) {
        return;
    }
    else {
        printf ("%d", root->data);
        preorder (root->left);
        preorder (root->right);
    }
}

void inorder (struct node * root) {
    if (root == NULL) {
        return;
    }
    else {
        inorder (root->left);
        printf ("%d", root->data);
        inorder (root->right);
    }
}

void postorder (struct node * root) {
    if (root == NULL) {
        return;
    }
    else {
        postorder (root->left);
        postorder (root->right);
    }
}
```

```
    printf ("%d", root->data);  
}  
}
```

```
int main () {  
  
    struct node * root = NULL;  
    root = create ();  
  
    printf ("Preorder Traversal : ");  
    preorder (root);  
  
    printf ("Inorder Traversal : ");  
    inorder (root);  
  
    printf ("Postorder Traversal : ");  
    postorder (root);  
  
    return 0;  
}
```

• Height of Binary tree

• Function :-

```
int calch (struct node * root) {  
    if (root == NULL) {  
        return -1;  
    }  
    else {  
        int lh = calch (root->left);  
        int rh = calch (root->right);  
  
        return 1 + (lh > rh ? lh : rh);  
    }  
}
```

```
int main () {
```

```
    int h = calch (root);  
}
```

• Binary Search Tree (BST)

- Here, the left child is less than parent/root node
- Right child greater than parent / child

Program :-

```
#include <stdio.h>
#include <stdlib.h>
```

```
struct node {
    int data;
    struct node *left, *right;
}
```

```
struct node *createnode (int data) {
    struct node *newnode;
    newnode = (struct node *) malloc (sizeof (struct node *));
    newnode -> data = data;
    newnode -> left = newnode -> right = 0;
    return newnode;
}
```

}

```
struct node *insert (struct node *root, int data) {
```

```
    if (root == 0) {
        return createnode (data);
    }
```

else {

```
    if (data < root -> data) {
```

```
        root -> left = insert (root -> left, data);
    }
```

}

else {

```
    root -> right = insert (root -> right, data);
}
```

}

return root;

}

3

[if data <
root then
left else
right]

```
struct node * search (struct node * root , int data) {
```

```
    if (root == 0) {  
        return root;  
    }
```

```
    else {  
        if ( data < root->data) {  
            return search (root->left , data);  
        }  
        else {  
            return search (root->right , data);  
        }  
    }
```

[if data < root->data
then search left
otherwise search right]

3 3 3

```
struct node * delete (struct node * root , int data) {
```

```
    struct node * temp;
```

```
    if (root == 0) {  
        return 0;  
    }
```

3

```
    else {
```

```
        if ( data < root->data) {  
            root->left = delete (root->left , data);  
        }
```

3

```
        else if ( data > root->data) {
```

```
            root->right = delete (root->right , data);  
        }
```

3

```
        else {
```

```
            if ( root->left == 0) {
```

```
                temp = root->right
```

```
                free (root);
```

```
                return temp;
```

3

Case - 1

```
            else if ( root->right == 0) {
```

```
                temp = root->right
```

```
                free (root);
```

```
                return temp;
```

3

Case - 2

```
            else { temp = root->right
```

```
                while (temp && temp->left != 0) {
```

```
                    temp = temp->left
```

Case - 3

```

root->data = temp->data;
root->right = delete (root->right, temp->data);
}
}

return root;
}

```

```

void inorderdisp (struct node *root) {
    if (root != 0) {
        inorderdisp (root->left);
        print ("%d ", root->data);
        inorderdisp (root->right);
    }
}

```

}

```

int main () {
    struct node *root = 0;

```

```

        // Creating the BST by inserting nodes
        root = insert(root, 50);
        root = insert(root, 30);
        root = insert(root, 20);
        root = insert(root, 40);
        root = insert(root, 70);
        root = insert(root, 60);
        root = insert(root, 80);

        printf("BST in-order traversal before deletion: ");
        inorderTraversal(root);
        printf("\n");

        // Search for a node
        int searchValue = 40;
        if (search(root, searchValue)) {
            printf("Node %d found in the BST.\n", searchValue);
        } else {
            printf("Node %d not found in the BST.\n", searchValue);
        }

        // Delete a node
        root = deleteNode(root, 20);
        printf("BST in-order traversal after deleting 20: ");
        inorderTraversal(root);
        printf("\n");

        root = deleteNode(root, 30);
        printf("BST in-order traversal after deleting 30: ");
        inorderTraversal(root);
        printf("\n");
    }

```

return 0;

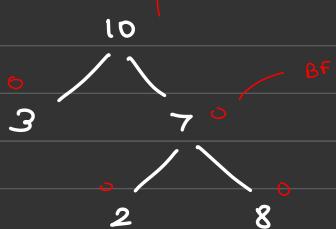
}

• AVL Trees

- It is a BST
- Here there is a BF (Balanced factor)
- $BF = \text{height of } (L_{\text{subtree}} - R_{\text{subtree}})$

L only $\{-1, 0, 1\}$

eg



An AVL tree causes imbalance, when any one of the following conditions occur:

case 1 :-

An insertion into the left subtree of the left child of node α .

case 2 :-

An insertion into the right subtree of the left child of node α .

case 3 :-

An insertion into the left subtree of the right child of node α . ↑

case 4 :-

An insertion into the right subtree of the right child of node α .

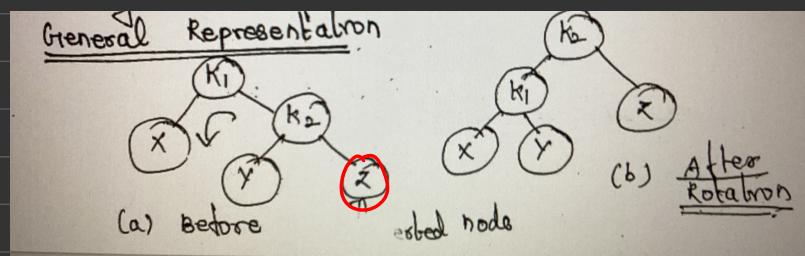
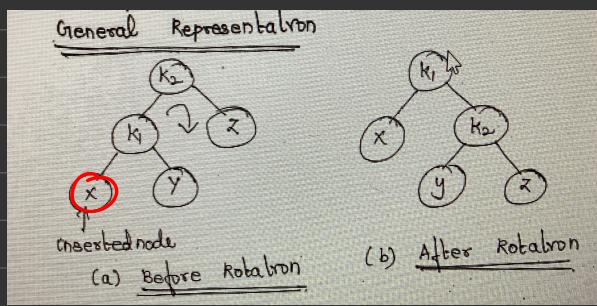
These imbalances can be overcome by

- (1) Single Rotation
- (2) Double Rotation

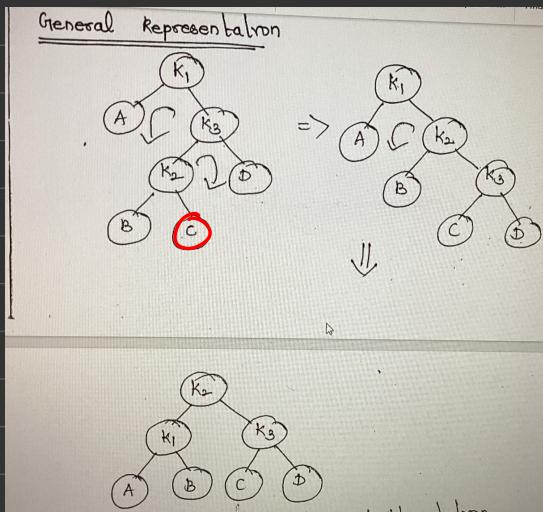
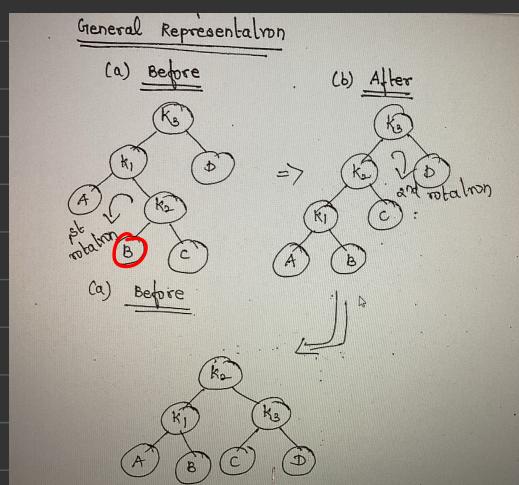
case 1 & case 4 \Rightarrow Single Rotation: $(L-L / R-R)$

case 2 & case 3 \Rightarrow Double Rotation $(L-R / R-L)$

• Single rotation (case -1 , 4)



• Double Rotation (Case -2 , 3)



• B-trees

↳ extension of BST

- Can have more than 2 child
- Has order m ($5, 3, 4 \dots$)
- Has more than one key

Every node has max. m children
 Min. children:- leaf $\rightarrow 0$
 root $\rightarrow 2$
 internal nodes $\rightarrow \lceil \frac{m}{2} \rceil$

Every node has max. $(m-1)$ keys
 Min. keys:- root node $\rightarrow 1$
 all other nodes $\rightarrow \lceil \frac{m}{2} \rceil - 1$

Skipped HEAP

N

HASHING



• Graphs

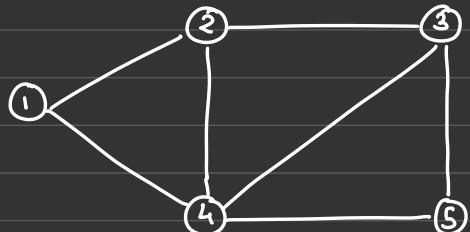


To ways to represent :-

1. Adjacent Matrix
2. Adjacent list

• Adjacent Matrix

eg

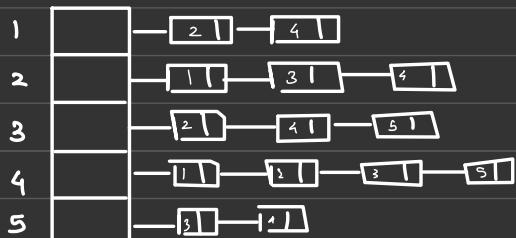


— [here there are no loops
i.e.]



	1	2	3	4	5
1	0	1	0	1	0
2	1	0	1	1	0
3	0	1	0	1	1
4	1	1	1	0	1
5	0	0	1	1	0

• Adjacent list



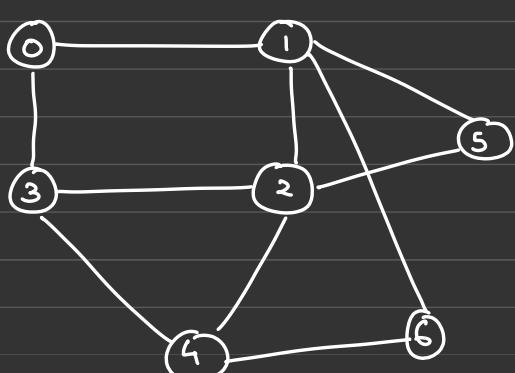
Complexity .. $(n+2e)$

• Graph Traversal

Two types : 1. BFS (Breadth first Search)
2. DFS (Depth first Search)

• BFS

eg



Step : 1. Take any node as root node
2. follow Queue Structure

eg Take 0 as root node



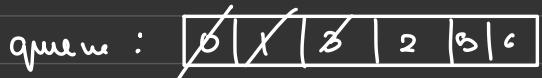
= 0

Step - 3 Go for adjacent most nodes of 0



result : 0 1

Step - 4 : Go for adjacent (uninserted, unvisited) nodes of '1'



result : 0 1 3

Step - 4 : Similar to other adj nodes of '3'



result : 0 1 3 2

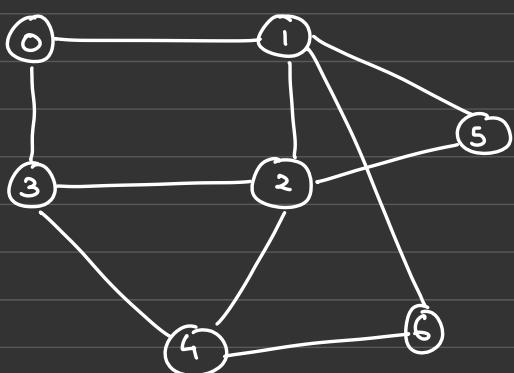
:

result : 0 1 3 2 5 6 4

• DFS

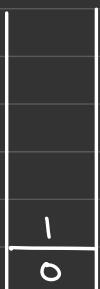
It follows Stack Structure

eg :



Step - 1 : Take 0 as root node

Stack :



res : 0, 1

Step - 2 : Take a adj vertex of '0' , let's say '1' , then take any of its adj vertex n go on

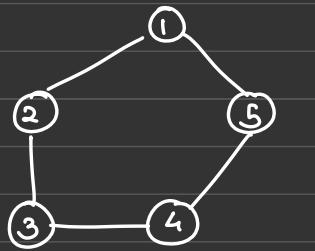
:

result : 0, 3, 2, 4, 6,

Note : When u go deep n find vertices already visited , then u gotta back-track but also pop that element n then go back

• Minimum Spanning tree

eg



$G = (V, E)$

$G' = (V', E')$ [Spanning tree]

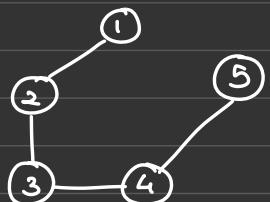
* A graph can have
>1 spanning tree

Relation :

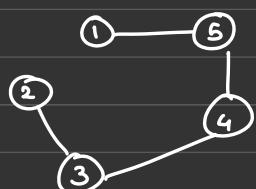
$$V' = V$$

$$\begin{aligned} E' &= \text{Subset } E \\ &= |V| - 1 \end{aligned}$$

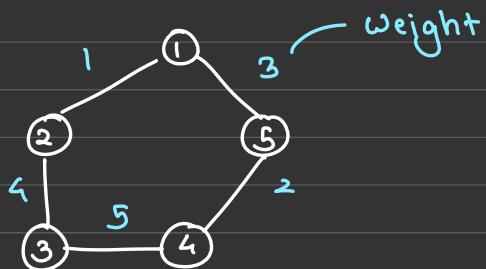
ST :



or



MST



[Here, the ST with less weight is MST]

• Topological Sorting

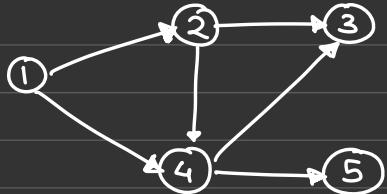
It's a linear ordering of vertices, every directed edge ab , it shld go from vertex a to b in order

eg To eat bread-jam

- 1 Take bread out
- 2 Apply jam
- 3 To eat
- 4 Eat

L shld be
DAG (directed acyclic graph)

eg



— [* It shld be always DAG]

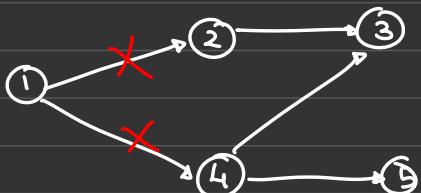
IN° [toward it]

OUT° [away]

eg IN° of $\begin{matrix} 1 \\ 2 \end{matrix}$ = 0
 IN° of $\begin{matrix} 3 \\ 4 \end{matrix}$ = 1

Step - 1 : Choose the vertex with $\text{IN}^\circ = 0$

2 : Now, delete all edges out going to that vertex,



Now IN° of $\begin{matrix} 2 \\ 4 \end{matrix}$ = 0
 IN° of $\begin{matrix} 3 \\ 5 \end{matrix}$ = 1

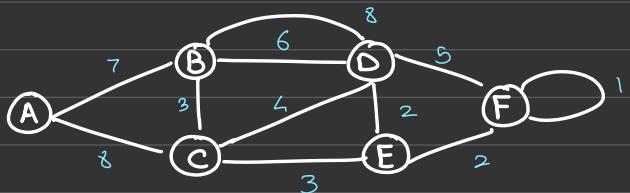
(updated)

Step - 3 : Repeat Step 1 then Step 2

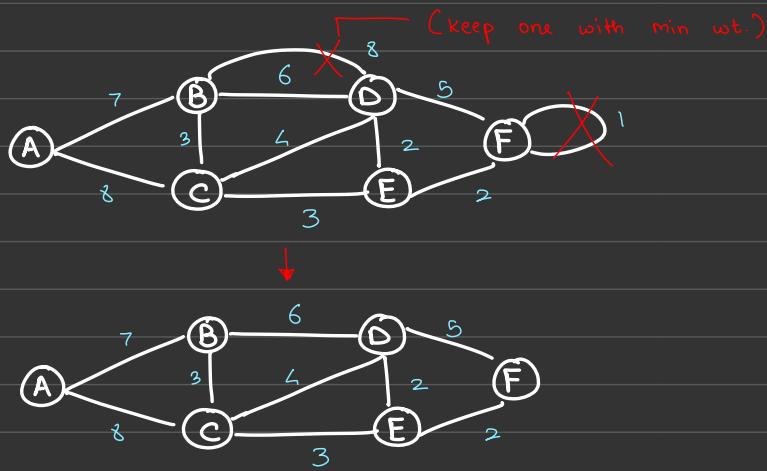
result : 1, 2, 4, 3, 5

• Prim's Algorithm for MST

eg



Step - 1 : Remove all loops & parallel edges

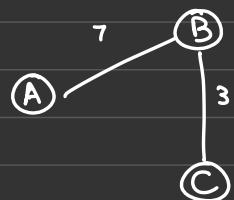


Step - 2 : Take any node as root, let's say **(A)**

Step - 3 : Take edge from **(A)**, one with min. wt

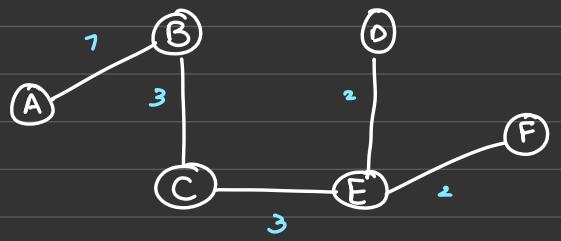


Step - 4: Now, check adj edges from **(B)**, one with minimum weight, *but also make sure to compare with **(A)**'s remaining edge*



:

Step - 5 : Go on ...

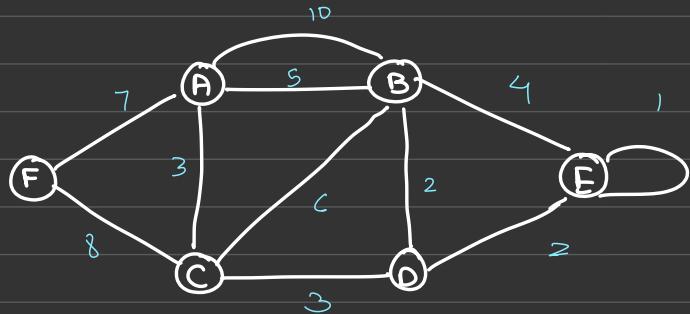


[Do it till u use all vertices n then stop]

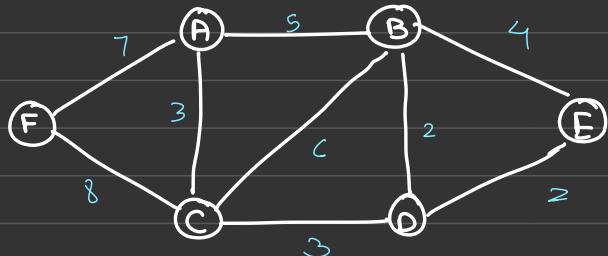
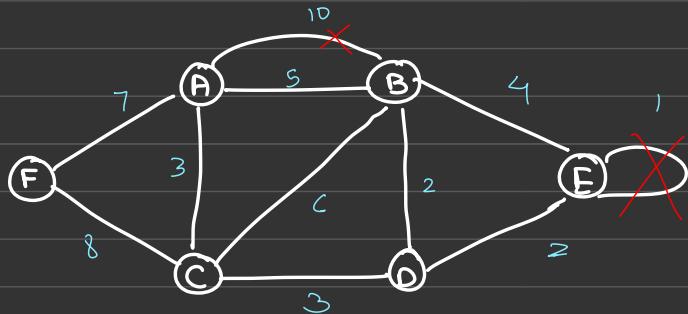
\downarrow
[MST]

• Kruskal's Algorithm for MST

eg



Step - 1 . Remove all loops n parallel edges



Step - 2 : Arrange all edges in inc order of their weight

$$BD = 2$$

$$DE = 2$$

$$AC = 3$$

$$CD = 3$$

$$BE = 4$$

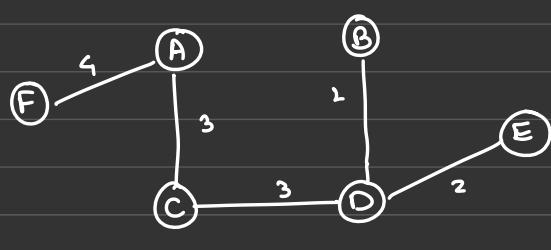
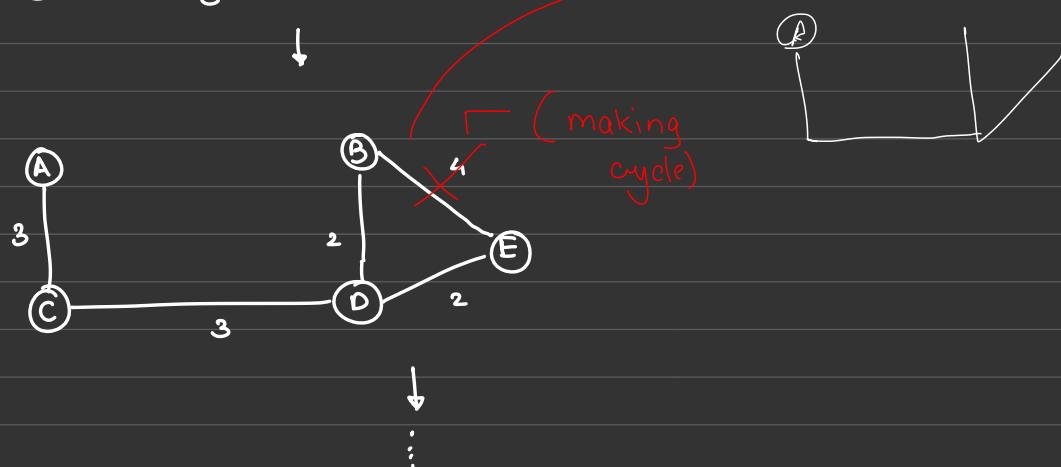
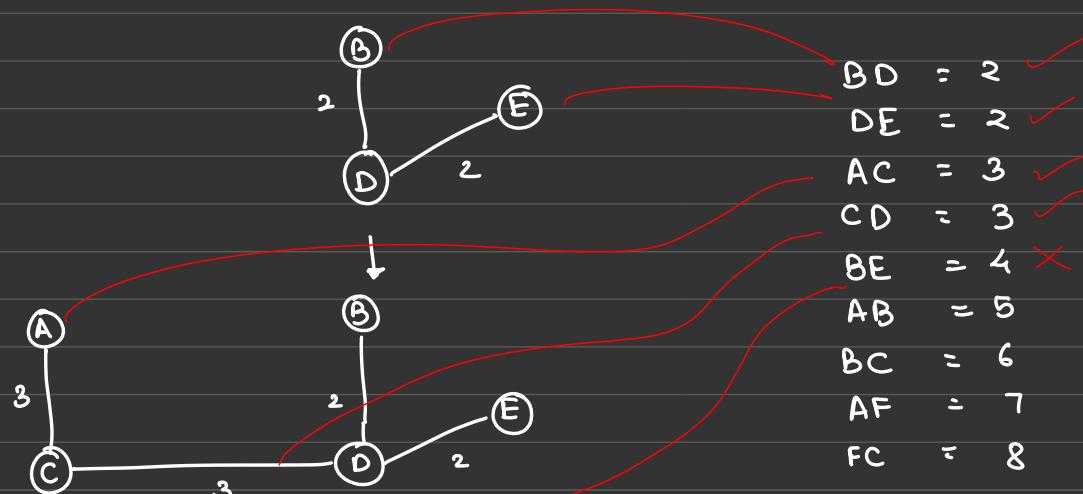
$$AB = 5$$

$$BC = 6$$

$$AF = 7$$

$$FC = 8$$

Step - 3 : Choose one with min wt. n star connecting
(* make sure it does not contain cycle)



MST

[To check
 $V' = V$
 i.e. $6 = 6$
 $E' = V - 1$
 $= 6 - 5$
 $= 5$