Puzzle Engine Library AP Exam

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June 10, 2019

Listing 1: CMakeLists.txt

```
cmake_minimum_required(VERSION 3.10)
project(PuzzleEngine CXX)

set(CMAKE_CXX_STANDARD 17)
set(CMAKE_CXX_STANDARD_REQUIRED ON)
set(CMAKE_CXX_EXTENSIONS OFF)

set(CMAKE_CXX_EXTENSIONS OFF)

set(CMAKE_CXX_FLAGS_DEBUG "${CMAKE_CXX_FLAGS_DEBUG} -fsanitize=undefined -fsanitize=address")
set(CMAKE_LINK_FLAGS_DEBUG "${CMAKE_LINK_FLAGS_DEBUG} -fsanitize=undefined -fsanitize=address")
add_executable(frogs frogs.cpp)
add_executable(crossing crossing.cpp)
add_executable(family family.cpp)
```

Listing 2: reachability.hpp

```
* The reachability header file library.
    * Author: Christopher Hansen Nielsen
    * Mail: chni15@student.aau.dk, Student Number: 20154154
    * Written and compiled on a windows machine.
    * g++ -std=c++17 -pedantic -Wall -DNDEBUG -03 -o frogs frogs.cpp
    * g++ -std=c++17 -pedantic -Wall -DNDEBUG -03 -o crossing crossing.cpp
    * g++ -std=c++17 -pedantic -Wall -DNDEBUG -03 -o family family.cpp
   #ifndef PUZZLEENGINE_REACHABILITY_HPP
   #define PUZZLEENGINE_REACHABILITY_HPP
   #include <vector>
   #include <list>
   #include <functional>
18 #include <iostream>
   #include <algorithm>
   #include <typeinfo>
  // This enum is used to handle the support for different search orders except for cost order. It
 ⇒is implemented
  // as part of requirement 5.
   enum search_order_t {
25
       breadth_first, depth_first
26
  // This struct is the basis for keeping track of the solution when traversing the states. When
 ⇒it is used, it holds a
29 // pointer to the parent node as well as a copy of the state.
30 template<class StateTypeT>
31 struct trace_node {
```

```
trace_node *parentState;
32
       StateTypeT selfState;
33
   };
34
35
  // This function is used to pass on the transition generator function from the respective
 →puzzles. It is implemented
  // as part of requirement 2.
37
   template<class StateTypeT>
   std::function<std::list<std::function<void(StateTypeT &)>>(StateTypeT &)>
   successors(std::list<std::function<void(StateTypeT &)>> transitions(const StateTypeT &state)) {
40
       return transitions;
41
   }
42
  // This class holds all the information about a given state space. It utilizes two template
 →types StateTypeT and
   // CostTypeT. These are the basis of the generic implementation as part of requirements 8 and 9.
   template<class StateTypeT, class CostTypeT = std::nullptr_t>
   class state_space_t {
47
   private:
48
       StateTypeT _startState;
49
       CostTypeT _initialCost;
       std::function<std::list<std::function<void(StateTypeT &)>>(StateTypeT &)> _transitionFunctions;
51
       std::function<bool(const StateTypeT &)> _invariantFunction;
52
       std::function<CostTypeT(const StateTypeT &state, const CostTypeT &cost)> _costFunction;
       bool _isCostEnabled; // used explicitly to determine whether or not a cost have been specified.
55
       template<class ValidationFunction>
56
       std::list<StateTypeT> solveOrder(ValidationFunction isGoalState, search_order_t order);
58
       template<class ValidationFunction>
59
       std::list<StateTypeT> solveCost(ValidationFunction isGoalState);
60
   public:
62
       // This is the first constructor for the class, which handles calls from the frogs.cpp
63
       // and crossing.cpp instantiation.
64
       state_space_t(const StateTypeT startInputState,
                     std::function<std::list<std::function<void(StateTypeT &)>>(StateTypeT &)>
  →transFunctions,
                     bool invariantFunc(const StateTypeT &) = [](
67
                              const StateTypeT &state) { return true; }) : _startState(startInputState),
                                                                           _transitionFunctions(
69
                                                                                   transFunctions),
70
                                                                           _invariantFunction(invariantFunc),
71
                                                                           _isCostEnabled(false){
73
74
       // This the second and overloaded constructor for the class. This handles calls from the
 → family.cpp.
       state_space_t(const StateTypeT startInputState, const CostTypeT costInput,
76
                     std::function<std::list<std::function<void(StateTypeT &)>>(StateTypeT &)>
 →transFunctions,
                     bool invariantFunc(const StateTypeT &) = [](
78
                              const StateTypeT &state) { return true; },
79
                     std::function<CostTypeT(const StateTypeT &state, const CostTypeT &cost)>
 →costFunc = [](
                              const StateTypeT &state, const CostTypeT &cost)
81
                                      { return CostTypeT{0, 0}; }) : _startState(
82
                                                                           startInputState),
83
                                                                       _initialCost(
                                                                               costInput),
85
                                                                       _transitionFunctions(
86
```

```
transFunctions),
                                                                        _invariantFunction(
                                                                                invariantFunc),
89
                                                                        _costFunction(
90
                                                                                costFunc),
                                                                        _isCostEnabled(
                                                                                true) {
93
        }
        template<class ValidationFunction>
96
        std::list<StateTypeT> check(ValidationFunction isGoalState, search_order_t order =
  →search_order_t::breadth_first);
99
   // This function is called from the different puzzle files and returns a solution if found. It
100
  →introduces a new template
   // ValidationFunction that handles the goal predicate function. It also takes an order, which is
  →defaulted to
   // breadth first if nothing else is specified.
   // It returns a list of states.
   template<class StateTypeT, class CostTypeT>
   template<class ValidationFunction>
   std::list<StateTypeT> state_space_t<StateTypeT, CostTypeT>::check(ValidationFunction
  →isGoalState, search_order_t order) {
        std::list<StateTypeT> solution;
107
108
        if (_isCostEnabled) { // Here we check if the cost method is specified, and calls the
109
  ⇒solveCost if true.
            solution = solveCost(isGoalState);
110
        } else { // Otherwise we call the solveOrder method with the order provided.
111
            solution = solveOrder(isGoalState, order);
112
114
        // Returns the list of states. Implemented as part of requirement 4.
115
        return solution;
116
   }
117
118
   // The method is used when solving the state space based on a given cost. It takes in
119
  →isGoalState which is a predicate
   // that is used to determine whether a solution have been found.
   // It returns a list of states. It is implemented as part of requirement 7.
   template<class StateTypeT, class CostTypeT>
   template<class ValidationFunction>
    std::list<StateTypeT> state_space_t<StateTypeT, CostTypeT>::solveCost(ValidationFunction
  →isGoalState) {
        StateTypeT currentState;
125
        CostTypeT itCost{_initialCost}, newCost;
        trace_node<StateTypeT> *traceState {};
127
        std::list<StateTypeT> passed, solution;
128
        std::list<std::pair<CostTypeT, trace_node<StateTypeT> *>> waiting;
129
130
        // The method utilizes a waiting list that contains a pair of cost and a trace_node. The
131
   →cost is used to determine
        // which element should be popped from the list next.
132
        waiting.push_back(std::make_pair(itCost, new trace_node<StateTypeT>{nullptr, _startState}));
133
134
        while (!waiting.empty()) {
135
            // Here we take the first element from the list and then pop it.
136
            currentState = waiting.front().second->selfState;
            traceState = waiting.front().second;
138
            itCost = waiting.front().first;
139
```

```
waiting.pop_front();
            // Here we check if the goal state has been reached. This is implemented as part of
142
  →reauirement 3.
            if (isGoalState(currentState)) {
143
                // If a goal is found, we use the traceState to traverse back up through the tree of
   →trace_nodes
                // until the parentState is NULL. For each node we push the state to the solution list.
145
146
                while (traceState->parentState != NULL) {
                    solution.push_front(traceState->selfState);
147
                    traceState = traceState->parentState;
148
                }
149
150
                solution.push_front(traceState->selfState); // Adds the start state to the solution
151
  ⇔trace.
                return solution;
152
            }
153
154
            // Here we check if the currentState is part of the passed list.
155
            if (!(std::find(passed.begin(), passed.end(), currentState) != passed.end())) {
156
                // If it is not, we push it to the list, and generate the transitions via the
   →_transitionFunctions which
                // is a member of the state_space_t class.
158
                passed.push_back(currentState);
                auto transitions = _transitionFunctions(currentState);
160
161
                for (auto transition: transitions) {
162
                    // For each transition, we then generate the successor
                    auto successor{currentState};
164
                    transition(successor);
165
166
                    // Prevents invalid states being added to waiting via an invariant predicate.
  →This is implemented as
                    // part of requirement 6.
168
                    if (!_invariantFunction(successor)) {
169
                         continue;
                    }
171
                    newCost = _costFunction(successor, itCost);
172
                    waiting.push_back(std::make_pair(newCost, new trace_node<StateTypeT>{traceState,
  →successor}));
174
                if (!transitions.empty()) { // Prevents sorting if no new transitions have been found.
175
                    // Here we sort the waiting list based on the cost for each pair in the list.
176
                    waiting.sort([](const std::pair<CostTypeT, trace_node<StateTypeT> *> &a,
                                     std::pair<CostTypeT, trace_node<StateTypeT> *> &b) { return
  →a.first < b.first; });</pre>
179
            }
180
        }
181
182
        return solution;
    }
184
185
    // The method is used when solving the state space based on a given order. It takes in
  →isGoalState which is a predicate
   // that is used to determine whether a solution have been found. It also takes an order, which
  ⇒specifies how the
188 // solution should be found. The method is very similar to solveCost in functionality.
   // It returns a list of states.
    template<class StateTypeT, class CostTypeT>
    template<class ValidationFunction>
```

```
std::list<StateTypeT>
    state_space_t<StateTypeT, CostTypeT>::solveOrder(ValidationFunction isGoalState, search_order_t
  →order) {
        StateTypeT currentState;
194
        trace_node<StateTypeT> *traceState {};
195
        std::list<StateTypeT> passed, solution;
196
        std::list<trace_node<StateTypeT> *> waiting;
197
198
        // As solveOrder does not utilize a cost, waiting is just a list of trace_nodes.
        waiting.push_back(new trace_node<StateTypeT>{nullptr, _startState});
200
201
        while (!waiting.empty()) {
202
            switch (order) { // We switch on the order to determine what element should be accessed
  →and popped from waiting.
                case breadth_first:
204
                     currentState = waiting.front()->selfState;
205
                     traceState = waiting.front();
206
                     waiting.pop_front();
207
                     break:
208
                case depth_first:
209
                     currentState = waiting.back()->selfState;
                     traceState = waiting.back();
211
                     waiting.pop_back();
212
                     break;
                default:
                     std::cout << "Order not supported" << std::endl;</pre>
215
                     break:
216
            }
            if (isGoalState(currentState)) {
218
                while (traceState->parentState != NULL) {
219
                     solution.push_front(traceState->selfState);
220
                     traceState = traceState->parentState;
222
223
                solution.push_front(traceState->selfState); // Adds the start state to the solution
224

→ trace.

                 return solution;
225
            }
226
            if (!(std::find(passed.begin(), passed.end(), currentState) != passed.end())) {
227
                passed.push_back(currentState);
                auto transitions = _transitionFunctions(currentState);
229
230
                for (auto transition: transitions) {
231
                     auto successor{currentState};
232
                     transition(successor);
233
234
                     if (!_invariantFunction(successor)) { // Prevents invalid states being added to
  →waiting.
                         continue;
236
237
                     waiting.push_back(new trace_node<StateTypeT>{traceState, successor});
239
            }
240
        }
241
        return solution;
243
    }
244
245
   // The following hash override is implemented in order to compile family.cpp. It is, however,
  →never used and should
247 // not be used at all. Gives a warning when compiling the program.
```

```
template<class StateType, size_t typeSize>
struct std::hash<std::array<StateType, typeSize>> {
    std::size_t operator()(const array<StateType, typeSize> &key) const {
        return NULL;
    }
}

therefore typeSize is typeSize
```

Listing 3: frogs.cpp

```
* Solution to a frog leap puzzle:
    * http://arcade.modemhelp.net/play-4863.html
    * Author: Marius Mikucionis <marius@cs.aau.dk>
    * Compile and run:
    * g++ -std=c++17 -pedantic -Wall -DNDEBUG -03 -o frogs frogs.cpp && ./frogs
    */
   #include "reachability.hpp" // your header-only library solution
   #include <iostream>
   #include <list>
11
   //#include <functional> // std::function
   enum class frog_t { empty, green, brown };
14
   using stones_t = std::vector<frog_t>;
15
16
   std::list<std::function<void(stones_t&)>> transitions(const stones_t& stones) {
       auto res = std::list<std::function<void(stones_t&)>>{};
18
       if (stones.size()<2)</pre>
19
           return res;
20
       auto i=0u;
21
       while (i < stones.size() && stones[i]!=frog_t::empty) ++i; // find empty stone</pre>
22
       if (i==stones.size())
           return res; // did not find empty stone
       // explore moves to fill the empty from left to right (only green can do that):
25
       if (i > 0 \&\& stones[i-1] == frog_t::green)
26
           res.push_back([i](stones_t& s){ // green jump to next
27
                              s[i-1] = frog_t::empty;
                              s[i]
                                    = frog_t::green;
                          });
30
       if (i > 1 && stones[i-2]==frog_t::green)
           res.push_back([i](stones_t& s){ // green jump over 1
                              s[i-2] = frog_t::empty;
33
                              s[i] = frog_t::green;
34
                          });
35
       // explore moves to fill the empty from right to left (only brown can do that):
36
       if (i < stones.size()-1 && stones[i+1]==froq_t::brown) {</pre>
37
           res.push_back([i](stones_t& s){ // brown jump to next
                              s[i+1] = frog_t::empty;
                              s[i] = frog_t::brown;
                          });
41
42
       if (i < stones.size()-2 && stones[i+2]==frog_t::brown) {</pre>
           res.push_back([i](stones_t& s){ // brown jump over 1
                              s[i+2]=frog_t::empty;
45
                              s[i]=frog_t::brown;
                          });
       return res;
49
   }
50
```

```
std::ostream& operator<<(std::ostream& os, const stones_t& stones) {</pre>
        for (auto&& stone: stones)
53
            switch (stone) {
54
            case frog_t::green: os << "G"; break;</pre>
55
            case frog_t::empty: os << "_"; break;</pre>
            case frog_t::brown: os << "B"; break;</pre>
            default: os << "?"; break; // something went terribly wrong</pre>
            }
        return os;
    }
61
62
    std::ostream& operator<<(std::ostream& os, const std::list<const stones_t*>& trace) {
63
        for (auto stones: trace)
            os << "State of " << stones->size() << " stones: " << *stones << '\n';
65
        return os:
66
    }
67
68
    void show_successors(const stones_t& state, const size_t level=0) {
69
        // Caution: this function uses recursion, which is not suitable for solving puzzles!!
70
71
        // 1) some state spaces can be deeper than stack allows.
        // 2) it can only perform depth-first search
        // 3) it cannot perform breadth-first search, cheapest-first, greatest-first etc.
73
        auto trans = transitions(state); // compute the transitions
        std::cout << std::string(level*2, ' ')</pre>
                   << "state " << state << " has " << trans.size() << " transitions";</pre>
76
        if (trans.empty())
77
            std::cout << '\n';
78
        else
            std::cout << ", leading to:\n";</pre>
80
        for (auto& t: trans) {
81
            auto succ = state; // copy the original state
            t(succ); // apply the transition on the state to compute successor
            show_successors(succ, level+1);
84
        }
85
86
    }
    void explain(){
88
        const auto start = stones_t{{ frog_t::green, frog_t::green, frog_t::empty,
89
                                        frog_t::brown, frog_t::brown }};
90
        std::cout << "Leaping frog puzzle start: " << start << '\n';</pre>
        show_successors(start);
92
        const auto finish = stones_t{{ frog_t::brown, frog_t::brown, frog_t::empty,
93
                                         frog_t::green, frog_t::green }};
94
        std::cout << "Leaping frog puzzle start: " << start << ", finish: " << finish << '\n';
        // Added type specification to the template.
96
        auto space = state_space_t<stones_t >(start, successors<stones_t>(transitions));// define
  ⇒state space
        // explore the state space and find the solutions satisfying goal:
98
        std::cout << "--- Solve with default (breadth-first) search: ---\n";</pre>
99
        auto solutions = space.check([&finish](const stones_t& state){ return state==finish; });
100
        for (auto&& trace: solutions) { // iterate through solutions:
            std::cout << "Solution: a trace of " << trace.size() << " states\n";</pre>
102
            std::cout << trace; // print solution</pre>
103
        }
104
    }
105
106
    void solve(size_t frogs, search_order_t order = search_order_t::breadth_first){
107
        const auto stones = frogs*2+1; // frogs on either side and 1 empty in the middle
108
        auto start = stones_t(stones, frog_t::empty); // initially all empty
        auto finish = stones_t(stones, frog_t::empty); // initially all empty
110
        while (frogs-->0) { // count down from frogs-1 to 0 and put frogs into positions:
111
```

```
start[frogs] = frog_t::green;
                                                               // green on left
            start[start.size()-frogs-1] = frog_t::brown;
                                                              // brown on right
            finish[frogs] = frog_t::brown;
                                                               // brown on left
114
            finish[finish.size()-frogs-1] = frog_t::green; // green on right
115
        }
116
        std::cout << "Leaping frog puzzle start: " << start << ", finish: " << finish << '\n';
117
        // Added type specification to the template.
118
        auto space = state_space_t<stones_t >(std::move(start), successors<stones_t>(transitions));
119
        auto solutions = space.check(
            [finish=std::move(finish)](const stones_t& state){ return state==finish; },
121
            order):
122
        // Introduced a change in print to adhere to my solution
123
        std::cout << "Solution: trace of " << solutions.size() << " states\n";</pre>
124
        for (auto&& trace: solutions) {
125
            std::cout << trace << std::endl;</pre>
126
        }
127
    }
128
129
    int main(){
130
        //explain();
131
        std::cout << "--- Solve with depth-first search: ---\n";</pre>
132
        solve(2, search_order_t::depth_first);
133
        std::cout << "--- Solve with breadth-first search: ---\n";</pre>
134
        solve(2); // 20 frogs may take >5.8GB of memory
135
136
    }
    /** Sample output:
137
    Leaping frog puzzle start: GG_BB
138
    state GG_BB has 4 transitions, leading to:
      state G_GBB has 2 transitions, leading to:
140
        state _GGBB has 0 transitions
141
142
        state GBG_B has 2 transitions, leading to:
          state GB_GB has 2 transitions, leading to:
            state _BGGB has 1 transitions, leading to:
144
              state B_GGB has 0 transitions
145
            state GBBG_ has 1 transitions, leading to:
146
              state GBB_G has 0 transitions
          state GBGB_ has 1 transitions, leading to:
148
            state GB_BG has 2 transitions, leading to:
149
              state _BGBG has 1 transitions, leading to:
150
                 state B_GBG has 1 transitions, leading to:
                   state BBG_G has 1 transitions, leading to:
152
                     state BB_GG has 0 transitions
153
              state GBB_G has 0 transitions
154
      state _GGBB has 0 transitions
155
      state GGB_B has 2 transitions, leading to:
156
        state G_BGB has 2 transitions, leading to:
157
          state _GBGB has 1 transitions, leading to:
            state BG_GB has 2 transitions, leading to:
159
              state B_GGB has 0 transitions
160
              state BGBG_ has 1 transitions, leading to:
161
                 state BGB_G has 1 transitions, leading to:
                   state B_BGG has 1 transitions, leading to:
163
                     state BB_GG has 0 transitions
164
          state GB_GB has 2 transitions, leading to:
165
            state _BGGB has 1 transitions, leading to:
              state B_GGB has 0 transitions
167
            state GBBG_ has 1 transitions, leading to:
168
              state GBB_G has 0 transitions
169
        state GGBB_ has 0 transitions
170
      state GGBB_ has 0 transitions
171
    Leaping frog puzzle start: GG_BB, finish: BB_GG
172
```

```
--- Solve with default (breadth-first) search: ---
   Solution: a trace of 9 states
   State of 5 stones: GG_BB
   State of 5 stones: G_GBB
   State of 5 stones: GBG_B
   State of 5 stones: GBGB_
   State of 5 stones: GB_BG
179
   State of 5 stones: _BGBG
   State of 5 stones: B_GBG
   State of 5 stones: BBG_G
   State of 5 stones: BB_GG
183
   --- Solve with depth-first search: ---
  Leaping frog puzzle start: GG_BB, finish: BB_GG
   Solution: trace of 9 states
   State of 5 stones: GG_BB
187
   State of 5 stones: GGB_B
   State of 5 stones: G_BGB
   State of 5 stones: _GBGB
   State of 5 stones: BG_GB
191
   State of 5 stones: BGBG_
   State of 5 stones: BGB_G
   State of 5 stones: B_BGG
   State of 5 stones: BB_GG
196 Leaping frog puzzle start: GGGG_BBBB, finish: BBBB_GGGG
   Solution: trace of 25 states
   State of 9 stones: GGGG_BBBB
198
   State of 9 stones: GGG_GBBBB
  State of 9 stones: GGGBG_BBB
  State of 9 stones: GGGBGB_BB
202 State of 9 stones: GGGB_BGBB
   State of 9 stones: GG_BGBGBB
203
   State of 9 stones: G_GBGBGBB
   State of 9 stones: GBG_GBGBB
   State of 9 stones: GBGBG_GBB
206
   State of 9 stones: GBGBGBG_B
  State of 9 stones: GBGBGBGB_
   State of 9 stones: GBGBGB_BG
210 State of 9 stones: GBGB_BGBG
211 State of 9 stones: GB_BGBGBG
   State of 9 stones: _BGBGBGBG
   State of 9 stones: B_GBGBGBG
   State of 9 stones: BBG_GBGBG
215 State of 9 stones: BBGBG_GBG
216 State of 9 stones: BBGBGBG_G
217 State of 9 stones: BBGBGB_GG
218 State of 9 stones: BBGB_BGGG
   State of 9 stones: BB_BGBGGG
   State of 9 stones: BBB_GBGGG
   State of 9 stones: BBBBG_GGG
221
   State of 9 stones: BBBB_GGGG
222
223
```

Listing 4: crossing.cpp

```
* **
2 * Solution to river crossing puzzle with a goat, a cabbage and a wolf.
3 * Author: Marius Mikucionis <marius@cs.aau.dk>
4 * Compile and run:
5 * g++ -std=c++17 -pedantic -Wall -DNDEBUG -O3 -o crossing crossing.cpp && ./crossing
6 */
7 #include "reachability.hpp" // your header-only library solution
```

```
#include <functional> // std::function
   #include <list>
   #include <array>
11
   #include <iostream>
13
   enum actor_t { cabbage, goat, wolf }; // names of the actors
14
   enum class pos_t { shore1, travel, shore2}; // names of the actor positions
15
   using actors_t = std::array<pos_t,3>; // positions of the actors
17
   auto transitions(const actors_t& actors) {
18
       auto res = std::list<std::function<void(actors_t&)>>{};
19
       for (auto i=0u; i<actors.size(); ++i)</pre>
            switch(actors[i]) {
21
            case pos_t::shore1:
22
                res.push_back([i](actors_t& actors){ actors[i] = pos_t::travel; });
            case pos_t::travel:
25
                res.push_back([i](actors_t& actors){ actors[i] = pos_t::shore1; });
26
                res.push_back([i](actors_t& actors){ actors[i] = pos_t::shore2; });
27
            case pos_t::shore2:
29
                res.push_back([i](actors_t& actors){ actors[i] = pos_t::travel; });
30
            }
       return res;
33
   }
34
35
   bool is_valid(const actors_t& actors) {
36
       // only one passenger:
37
       if (std::count(std::begin(actors), std::end(actors), pos_t::travel)>1)
38
            return false;
       // goat cannot be left alone with wolf, as wolf will eat the goat:
40
       if (actors[actor_t::goat]==actors[actor_t::wolf] && actors[actor_t::cabbage]==pos_t::travel)
41
            return false;
42
       // goat cannot be left alone with cabbage, as goat will eat the cabbage:
       if (actors[actor_t::goat]==actors[actor_t::cabbage] && actors[actor_t::wolf]==pos_t::travel)
44
            return false:
45
       return true;
46
   }
48
   std::ostream& operator<<(std::ostream& os, const pos_t& pos) {</pre>
49
       switch(pos) {
50
       case pos_t::shore1: os << "1"; break;</pre>
51
       case pos_t::travel: os << "~"; break;</pre>
52
       case pos_t::shore2: os << "2"; break;</pre>
53
       default: os << "?"; break; // something went terribly wrong</pre>
       }
55
       return os;
56
57
   }
   std::ostream& operator<<(std::ostream& os, const actors_t& actors) {</pre>
59
       return os << actors[actor_t::cabbage]</pre>
60
                  << actors[actor_t::goat]
61
                  << actors[actor_t::wolf];
62
   }
63
64
   std::ostream& operator<<(std::ostream& os, std::list<const actors_t*>& trace) {
65
       auto step = 0u;
66
       for (auto* actors: trace)
67
            os << step++ << ": " << *actors << '\n';
68
```

```
return os;
    }
70
71
    void solve(){
72
        auto state_space = state_space_t<actors_t>(
73
            actors_t{},
                                                  // initial state
            successors<actors_t>(transitions), // successor generator
75
                                                  // invariant over all states
            &is_valid);
        auto solution = state_space.check(
             [](const actors_t& actors){ // all actors should be on the shore2:
78
                 return std::count(std::begin(actors), std::end(actors), pos_t::shore2)==actors.size();
79
            });
80
        // Introduced a change in print to adhere to my solution
        std::cout << "# CGW" << std::endl;</pre>
82
        int it = 0;
83
        for (auto&& trace: solution)
            std::cout << it << ": " << trace << std::endl;</pre>
    }
86
87
    int main(){
        solve();
    }
90
91
    /** Sample output:
    # CGW
    0: 111
    1: 1~1
    2: 121
    3: ~21
    4: 221
    5: 2~1
    6: 211
    7: 21~
    8: 212
102
    9: 2~2
103
    10: 222
    */
105
```

Listing 5: family.cpp

```
/**
    * Reachability algorithm implementation for river-crossing puzzle:
    * https://www.funzug.com/index.php/flash-games/japanese-river-crossing-puzzle-game.html
    * Author: Marius Mikucionis <marius@cs.aau.dk>
    * Compile using:
    * g++ -std=c++17 -pedantic -Wall -DNDEBUG -03 -o family family.cpp && ./family
    * Inspect the solution (only the traveling part):
    * ./family | grep trv | grep '~~~'
   #include "reachability.hpp" // your header-only library solution
11
12
   #include <iostream>
13
   #include <vector>
   #include <list>
   #include <array>
   #include <functional> // std::function
   #include <algorithm> // all_of
   /** Model of the river crossing: persons and a boat */
20
   struct person_t {
21
       enum { shore1, onboard, shore2 } pos = shore1;
```

```
enum { mother, father, daughter1, daughter2, son1, son2, policeman, prisoner };
   };
24
25
   struct boat_t {
26
        enum { shore1, travel, shore2 } pos = shore1;
27
        uint16_t capacity{2};
28
        uint16_t passengers{0};
29
   };
30
31
   struct state_t {
        boat_t boat;
32
        std::array<person_t,8> persons;
33
   };
34
35
   /** less-than operators for std::map */
36
   bool operator<(const person_t& p1, const person_t& p2) {</pre>
37
        if (p1.pos < p2.pos)</pre>
            return true;
        else if (p2.pos < p1.pos)</pre>
40
            return false; // p2 < p1
41
42
        return false; // equal
   }
44
   bool operator<(const boat_t& b1, const boat_t& b2) {</pre>
45
        if (b1.pos < b2.pos)</pre>
46
            return true;
        else if (b2.pos < b1.pos)</pre>
48
            return false;
49
        if (b1.passengers < b2.passengers)</pre>
            return true;
51
        else if (b2.passengers < b1.passengers)</pre>
52
            return false;
        if (b1.capacity < b2.capacity)</pre>
            return true;
55
        else if (b2.capacity < b1.capacity)</pre>
56
57
            return false;
        return false;
   }
59
60
   bool operator<(const state_t& s1, const state_t& s2) {</pre>
61
        if (s1.boat < s2.boat)</pre>
            return true;
63
        if (s2.boat < s1.boat)</pre>
64
            return false; // s2 < s1
65
        for (auto i=0u; i<s1.persons.size(); ++i)</pre>
            if (s1.persons[i] < s2.persons[i])</pre>
67
                 return true;
            else if (s2.persons[i] < s1.persons[i])</pre>
                 return false;
        return false; // s2 == s1
71
   }
72
   /** equality operations for std::unordered_map */
74
   bool operator==(const person_t& p1, const person_t& p2) {
75
        return (p1.pos == p2.pos);
76
   }
78
   bool operator==(const boat_t& b1, const boat_t& b2) {
79
        return (b1.pos == b2.pos) &&
80
            (b1.capacity == b2.capacity) &&
81
            (b1.passengers == b2.passengers);
82
   }
83
```

```
bool operator==(const state_t& s1, const state_t& s2) {
         return (s1.boat == s2.boat) && (s1.persons == s2.persons);
86
    }
87
    /** hash operations for std::unordered_map */
89
    namespace std {
90
        template <>
91
         struct hash<person_t> {
             std::size_t operator()(const person_t& key) const {
93
                  return std::hash<decltype(key.pos)>{}(key.pos);
94
             }
95
        };
        template <>
97
         struct hash<boat_t> {
98
             std::size_t operator()(const boat_t& key) const {
                 auto h_pos = std::hash<decltype(key.pos)>{};
100
                 auto h_int = std::hash<decltype(key.capacity)>{};
101
                 return ((((h_pos(key.pos) << 1) ^</pre>
102
                             h_int(key.capacity)) << 1) ^</pre>
103
                          h_int(key.passengers));
             }
105
        };
106
        template <>
108
         struct hash<state_t> {
109
             std::size_t operator()(const state_t& key) const {
110
                  return (std::hash<boat_t>{}(key.boat) << 1) ^</pre>
111
                      std::hash<decltype(key.persons)>{}(key.persons); // assumes hash over container
112
             }
113
        };
114
    }
115
116
    std::ostream& operator<<(std::ostream& os, const person_t& p) {</pre>
117
        os << '{';
118
         switch (p.pos) {
119
        case person_t::shore1: os << "sh1"; break;</pre>
120
         case person_t::onboard: os << "~~"; break;</pre>
121
         case person_t::shore2: os << "SH2"; break;</pre>
122
        default: os << "???" ; break; // something went terribly wrong</pre>
124
         return os << '}';
125
    }
126
127
    std::ostream& operator<<(std::ostream& os, const boat_t& b) {</pre>
128
        os << '{':
129
        switch (b.pos) {
130
        case boat_t::shore1: os << "sh1"; break;</pre>
131
        case boat_t::travel: os << "trv"; break;</pre>
132
         case boat_t::shore2: os << "SH2"; break;</pre>
133
        default: os << "???" ; break; // something went terribly wrong</pre>
134
135
        return os << ',' << b.passengers << ',' << b.capacity << '}';
136
    }
137
138
139
    std::ostream& operator<<(std::ostream& os, const state_t& s){</pre>
140
         return os << s.boat << ','
141
                    << s.persons[person_t::mother] << ','
142
                    << s.persons[person_t::father] << ','</pre>
143
                    << s.persons[person_t::daughter1] << ','
144
```

```
<< s.persons[person_t::daughter2] << ','</pre>
145
                   << s.persons[person_t::son1] << ',
                   << s.persons[person_t::son2] << '</pre>
147
                   << s.persons[person_t::policeman] << ','
148
                   << s.persons[person_t::prisoner];</pre>
149
    }
150
151
152
     * Returns a list of transitions applicable on a given state.
       transition is a function modifying a state
154
155
    std::list<std::function<void(state_t&)>>
156
    transitions(const state_t& s) {
157
        auto res = std::list<std::function<void(state_t&)>>{};
158
        switch (s.boat.pos) {
159
        case boat_t::shore1:
        case boat_t::shore2:
161
             if (s.boat.passengers>0) // start traveling
162
                 res.push_back([](state_t& state){    state.boat.pos = boat_t::travel; });
163
            break;
164
        case boat_t::travel:
165
             res.emplace_back([](state_t& state){ // arrive to shore1
166
                                   state.boat.pos = boat_t::shore1;
167
                                   state.boat.passengers = 0;
                                   for (auto& p: state.persons)
169
                                        if (p.pos == person_t::onboard)
170
                                            p.pos = person_t::shore1;
171
                               });
172
             res.emplace_back([](state_t& state){
                                                        // arrive to shore2
173
                                   state.boat.pos = boat_t::shore2;
174
                                   state.boat.passengers = 0;
                                   for (auto& p: state.persons)
                                        if (p.pos == person_t::onboard)
177
                                            p.pos = person_t::shore2;
178
                               });
179
            break;
180
        }
181
        for (auto i=0u; i<s.persons.size(); ++i) {</pre>
182
             switch (s.persons[i].pos) {
             case person_t::shore1: // board the boat on shore1:
                 if (s.boat.pos == boat_t::shore1)
185
                     res.push_back([i](state_t& state){
186
                                         state.persons[i].pos = person_t::onboard;
187
                                         state.boat.passengers++;
188
                                    });
189
                 break:
190
             case person_t::shore2: // board the boat on shore2:
                 if (s.boat.pos == boat_t::shore2)
192
                     res.push_back([i](state_t& state){
193
                                         state.persons[i].pos = person_t::onboard;
194
                                         state.boat.passengers++;
195
                                    });
196
                 break;
197
             case person_t::onboard:
                 if (s.boat.pos == boat_t::shore1) // leave the boat to shore1
                      res.push_back([i](state_t& state){
200
                                         state.persons[i].pos = person_t::shore1;
201
                                         state.boat.passengers--;
202
                                    });
203
                 else if (s.boat.pos == boat_t::shore2) // leave the boat to shore2
204
                     res.push_back([i](state_t& state){
205
```

```
state.persons[i].pos = person_t::shore2;
                                        state.boat.passengers--;
                                   });
208
                break:
209
            }
210
211
        return res;
212
    }
213
214
    bool river_crossing_valid(const state_t& s) {
215
        if (s.boat.passengers > s.boat.capacity) {
216
            log(" boat overload\n");
217
    //
            return false;
218
219
        if (s.boat.pos == boat_t::travel) {
220
            if (s.persons[person_t::daughter1].pos == person_t::onboard) {
                if (s.boat.passengers==1 ||
222
                     (s.persons[person_t::daughter2].pos == person_t::onboard) ||
223
                     (s.persons[person_t::son1].pos == person_t::onboard) ||
224
                     (s.persons[person_t::son2].pos == person_t::onboard) ||
225
                     (s.persons[person_t::prisoner].pos == person_t::onboard)) {
    //
                     log(" d1 travel alone\n");
227
                     return false;
228
                }
            } else if (s.persons[person_t::daughter2].pos == person_t::onboard) {
230
                if (s.boat.passengers==1 ||
231
                     (s.persons[person_t::daughter1].pos == person_t::onboard) ||
232
                     (s.persons[person_t::son1].pos == person_t::onboard) ||
                     (s.persons[person_t::son2].pos == person_t::onboard) ||
234
                     (s.persons[person_t::prisoner].pos == person_t::onboard)) {
235
    11
                     log(" d2 travel alone\n");
236
                     return false;
238
            } else if (s.persons[person_t::son1].pos == person_t::onboard) {
239
                if (s.boat.passengers==1 ||
240
                     (s.persons[person_t::daughter1].pos == person_t::onboard) ||
                     (s.persons[person_t::daughter2].pos == person_t::onboard) ||
242
                     (s.persons[person_t::son2].pos == person_t::onboard) ||
243
                     (s.persons[person_t::prisoner].pos == person_t::onboard)) {
244
                     log(" s1 travel alone\n");
                     return false;
246
                }
247
            } else if (s.persons[person_t::son2].pos == person_t::onboard) {
248
                if (s.boat.passengers==1 ||
249
                     (s.persons[person_t::daughter1].pos == person_t::onboard) ||
250
                     (s.persons[person_t::daughter2].pos == person_t::onboard) ||
251
                     (s.persons[person_t::son1].pos == person_t::onboard) ||
                     (s.persons[person_t::prisoner].pos == person_t::onboard)) {
253
                     log(" s2 travel alone\n");
    11
254
                     return false;
255
                }
            }
257
            if (s.persons[person_t::prisoner].pos != s.persons[person_t::policeman].pos) {
258
                auto prisoner_pos = s.persons[person_t::prisoner].pos;
                if ((s.persons[person_t::daughter1].pos == prisoner_pos) ||
                     (s.persons[person_t::daughter2].pos == prisoner_pos) ||
261
                     (s.persons[person_t::son1].pos == prisoner_pos) ||
262
                     (s.persons[person_t::son2].pos == prisoner_pos) ||
263
                     (s.persons[person_t::mother].pos == prisoner_pos) ||
                     (s.persons[person_t::father].pos == prisoner_pos)) {
265
                     log(" pr with family\n");
   //
266
```

```
return false;
                 }
268
            }
269
            if (s.persons[person_t::prisoner].pos == person_t::onboard && s.boat.passengers<2) {</pre>
270
                 log(" pr on boat\n");
    //
271
                 return false;
272
            }
273
        }
274
        if ((s.persons[person_t::daughter1].pos == s.persons[person_t::father].pos) &&
             (s.persons[person_t::daughter1].pos != s.persons[person_t::mother].pos)) {
276
             log(" d1 with f(n");
    11
277
             return false:
278
        } else if ((s.persons[person_t::daughter2].pos == s.persons[person_t::father].pos) &&
                    (s.persons[person_t::daughter2].pos != s.persons[person_t::mother].pos)) {
280
    11
             log(" d2 with f(n");
281
             return false:
        } else if ((s.persons[person_t::son1].pos == s.persons[person_t::mother].pos) &&
283
                    (s.persons[person_t::son1].pos != s.persons[person_t::father].pos)) {
284
             log(" s1 with m\n");
285
    //
             return false;
286
        } else if ((s.persons[person_t::son2].pos == s.persons[person_t::mother].pos) &&
                    (s.persons[person_t::son2].pos != s.persons[person_t::father].pos)) {
288
             log(" s2 with m\n");
    //
289
             return false;
290
291
    //
        log(" OK\n");
292
        return true;
293
    }
294
295
    struct cost_t {
296
        size_t depth{0}; // counts the number of transitions
297
        size_t noise{0}; // kids get bored on shore1 and start making noise there
        bool operator<(const cost_t& other) const {</pre>
299
            if (depth < other.depth)</pre>
300
                 return true;
301
             if (other.depth < depth)</pre>
302
                 return false;
303
             return noise < other.noise;</pre>
304
        }
305
306
    };
307
    bool goal(const state_t& s){
308
        return std::all_of(std::begin(s.persons), std::end(s.persons),
309
                             [](const person_t& p) { return p.pos == person_t::shore2; });
310
    }
311
312
    template <typename CostFn>
314
    void solve(CostFn&& cost) { // no type checking: OK hack here, but not good for a library.
315
        // Overall there are 4*3*2*1/2 solutions to the puzzle
316
        // (children form 2 symmetric groups and thus result in 2 out of 4 permutations).
317
        // However the search algorithm may collapse symmetric solutions, thus only one is reported.
318
        // By changing the cost function we can express a preference and
319
        // then the algorithm should report different solutions
320
        auto states = state_space_t<state_t, cost_t>{
             state_t{}, cost_t{},
                                                 // initial state and cost
322
             successors<state_t>(transitions), // successor generator
323
            &river_crossing_valid,
                                                 // invariant over states
324
                                                 // cost over states
            std::forward<CostFn>(cost)};
325
        auto solutions = states.check(&goal);
326
        if (solutions.empty()) {
327
```

```
std::cout << "No solution\n";</pre>
        } else {
329
            // Introduced a change in print to adhere to my solution
330
            std::cout << "Solution:\n";</pre>
331
            std::cout << "Boat,
                                      Mothr,Fathr,Daug1,Daug2,Son1, Son2, Polic,Prisn\n";
            for (auto&& trace: solutions) {
333
                 std::cout << trace << '\n';
334
            }
335
336
        }
    }
337
338
    int main() {
339
        std::cout << "-- Solve using depth as a cost: ---\n";
340
        solve([](const state_t& state, const cost_t& prev_cost){
341
                   return cost_t{ prev_cost.depth+1, prev_cost.noise };
342
               }); // it is likely that daughters will get to shore2 first
        std::cout << "-- Solve using noise as a cost: ---\n";
344
        solve([](const state_t& state, const cost_t& prev_cost){
345
                   auto noise = prev_cost.noise;
346
                   if (state.persons[person_t::son1].pos == person_t::shore1)
347
                       noise += 2; // older son is more noughty, prefer him first
                   if (state.persons[person_t::son2].pos == person_t::shore1)
349
                       noise += 1:
350
                   return cost_t{ prev_cost.depth, noise };
               }); // son1 should get to shore2 first
352
        std::cout << "-- Solve using different noise as a cost: ---\n";</pre>
353
        solve([](const state_t& state, const cost_t& prev_cost){
354
                   auto noise = prev_cost.noise;
                   if (state.persons[person_t::son1].pos == person_t::shore1)
356
                       noise += 1;
357
                   if (state.persons[person_t::son2].pos == person_t::shore1)
358
                       noise += 2; // younger son is more distressed, prefer him first
                   return cost_t{ prev_cost.depth, noise };
360
               }); // son2 should get to the shore2 first
361
362
    /** Example solutions (shows only the states with travel):
363
    --- Solve using depth as a cost: ---
364
              Mothr, Fathr, Daug1, Daug2, Son1, Son2, Polic, Prisn
365
    {trv,2,2},{sh1},{sh1},{sh1},{sh1},{sh1},{sh1},{-~~},{-~~}
366
    {trv,1,2},{sh1},{sh1},{sh1},{sh1},{sh1},{sh1},{sh1},{~~~},{SH2}
    {trv,2,2},{sh1},{sh1},{~~~},{sh1},{sh1},{sh1},{~~~},{SH2}
368
    {trv,2,2},{sh1},{sh1},{SH2},{sh1},{sh1},{sh1},{~~~},{~~~}
369
    {trv,2,2},{~~~},{sh1},{SH2},{~~~},{sh1},{sh1},{sh1},{sh1},{sh1}
370
    {trv,1,2},{~~~},{sh1},{SH2},{SH2},{sh1},{sh1},{sh1},{sh1},
371
    {trv,2,2},{~~~},{~~~},{SH2},{SH2},{sh1},{sh1},{sh1},{sh1},
372
    {trv,1,2},{SH2},{~~~},{SH2},{SH2},{sh1},{sh1},{sh1},{sh1}
373
    {trv,2,2},{SH2},{sh1},{SH2},{SH2},{sh1},{sh1},{~~~},{~~~}
    {trv,1,2},{~~~},{sh1},{SH2},{SH2},{sh1},{sh1},{SH2},{SH2}
375
    {trv,2,2},{~~~},{~~~},{SH2},{SH2},{sh1},{sh1},{SH2},{SH2}
376
    {trv,1,2},{SH2},{~~~},{SH2},{SH2},{sh1},{sh1},{SH2},{SH2}
377
    {trv,2,2},{SH2},{~~~},{SH2},{SH2},{~~~},{sh1},{SH2},{SH2}
    {trv,2,2},{SH2},{SH2},{SH2},{SH2},{SH2},{SH2},{sh1},{~~~},{~~~}
379
    {trv,2,2},{SH2},{SH2},{SH2},{SH2},{SH2},{SH2},{~~~},{~~~},{sh1}
380
    {trv,1,2},{SH2},{SH2},{SH2},{SH2},{SH2},{SH2},{SH2},{sh1}
    {trv,2,2},{SH2},{SH2},{SH2},{SH2},{SH2},{SH2},{SH2},{~~~},{~~~}
    --- Solve using noise as a cost: ---
383
    Boat.
              Mothr, Fathr, Daug1, Daug2, Son1, Son2, Polic, Prisn
384
    {trv,2,2},{sh1},{sh1},{sh1},{sh1},{sh1},{sh1},{sh1},{-~~}
385
    {trv,1,2},{sh1},{sh1},{sh1},{sh1},{sh1},{sh1},{sh1},{-~~},{SH2}
    {trv,2,2},{sh1},{sh1},{sh1},{sh1},{~~~},{sh1},{~~~},{SH2}
387
    {trv,2,2},{sh1},{sh1},{sh1},{sh1},{sh1},{sh2},{sh1},{~~~},{~~~}
388
```

```
{trv,2,2},{sh1},{~~~},{sh1},{sh1},{SH2},{~~~},{sh1},{sh1}
    {trv,1,2},{sh1},{~~~},{sh1},{sh1},{SH2},{SH2},{sh1},{sh1}
390
    {trv,2,2},{~~~},{~~~},{sh1},{sh1},{SH2},{SH2},{sh1},{sh1}
391
    {trv,1,2},{~~~},{SH2},{sh1},{sh1},{SH2},{SH2},{sh1},{sh1}
392
    {trv,2,2},{sh1},{SH2},{sh1},{sh1},{SH2},{SH2},{~~~},{~~~}
    {trv,1,2},{sh1},{~~~},{sh1},{sh1},{SH2},{SH2},{SH2},{SH2},{SH2}
394
    {trv,2,2},{~~~},{~~~},{sh1},{sh1},{SH2},{SH2},{SH2},{SH2},
395
    {trv,1,2},{~~~},{SH2},{sh1},{sh1},{SH2},{SH2},{SH2},{SH2},
396
397
    {trv,2,2},{~~~},{SH2},{~~~},{sh1},{SH2},{SH2},{SH2},{SH2},{SH2}
    {trv,2,2},{SH2},{SH2},{SH2},{sh1},{SH2},{SH2},{~~~},{~~~}
398
    {trv,2,2},{SH2},{SH2},{SH2},{~~~},{SH2},{SH2},{~~~},{sh1}
399
    {trv,1,2},{SH2},{SH2},{SH2},{SH2},{SH2},{SH2},{SH2},{~~~},{sh1}
400
    {trv,2,2},{SH2},{SH2},{SH2},{SH2},{SH2},{SH2},{SH2},{~~~},{~~~}
401
    -- Solve using different noise as a cost: ---
402
              Mothr, Fathr, Daug1, Daug2, Son1, Son2, Polic, Prisn
403
    {trv,2,2},{sh1},{sh1},{sh1},{sh1},{sh1},{sh1},{sh1},{~~~},{~~~}
404
    {trv,1,2},{sh1},{sh1},{sh1},{sh1},{sh1},{sh1},{sh1},{~~~},{SH2}
405
    {trv,2,2},{sh1},{sh1},{sh1},{sh1},{sh1},{sh1},{~~~},{~~~},{SH2}
406
    {trv,2,2},{sh1},{sh1},{sh1},{sh1},{sh1},{sh1},{sh2},{~~~},{~~~}
407
    {trv,2,2},{sh1},{~~~},{sh1},{sh1},{~~~},{SH2},{sh1},{sh1}
408
    {trv,1,2},{sh1},{~~~},{sh1},{sh1},{SH2},{SH2},{sh1},{sh1}
    {trv,2,2},{~~~},{~~~},{sh1},{sh1},{SH2},{SH2},{sh1},{sh1}
410
    {trv,1,2},{~~~},{SH2},{sh1},{sh1},{SH2},{SH2},{sh1},{sh1}
411
    {trv,2,2},{sh1},{SH2},{sh1},{sh1},{SH2},{SH2},{~~~},{~~~}
413
    {trv,1,2},{sh1},{~~~},{sh1},{sh1},{SH2},{SH2},{SH2},{SH2},{SH2}
    {trv,2,2},{~~~},{~~~},{sh1},{sh1},{SH2},{SH2},{SH2},{SH2},{SH2}
414
    {trv,1,2},{~~~},{SH2},{sh1},{sh1},{SH2},{SH2},{SH2},{SH2},
415
    {trv,2,2},{~~~},{SH2},{~~~},{sh1},{SH2},{SH2},{SH2},{SH2},
    {trv,2,2},{SH2},{SH2},{SH2},{sh1},{SH2},{SH2},{~~~},{~~~}
417
    {trv,2,2},{SH2},{SH2},{SH2},{~~~},{SH2},{SH2},{~~~},{sh1}
418
    {trv,1,2},{SH2},{SH2},{SH2},{SH2},{SH2},{SH2},{SH2},{~~~},{sh1}
419
    {trv,2,2},{SH2},{SH2},{SH2},{SH2},{SH2},{SH2},{SH2},{~~~},{~~~}
420
     */
421
```