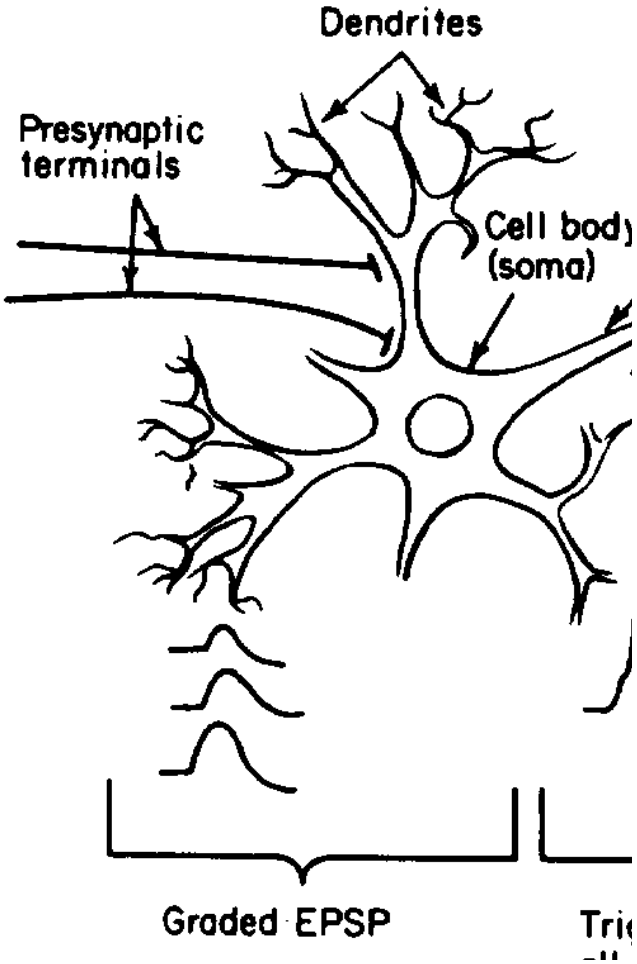
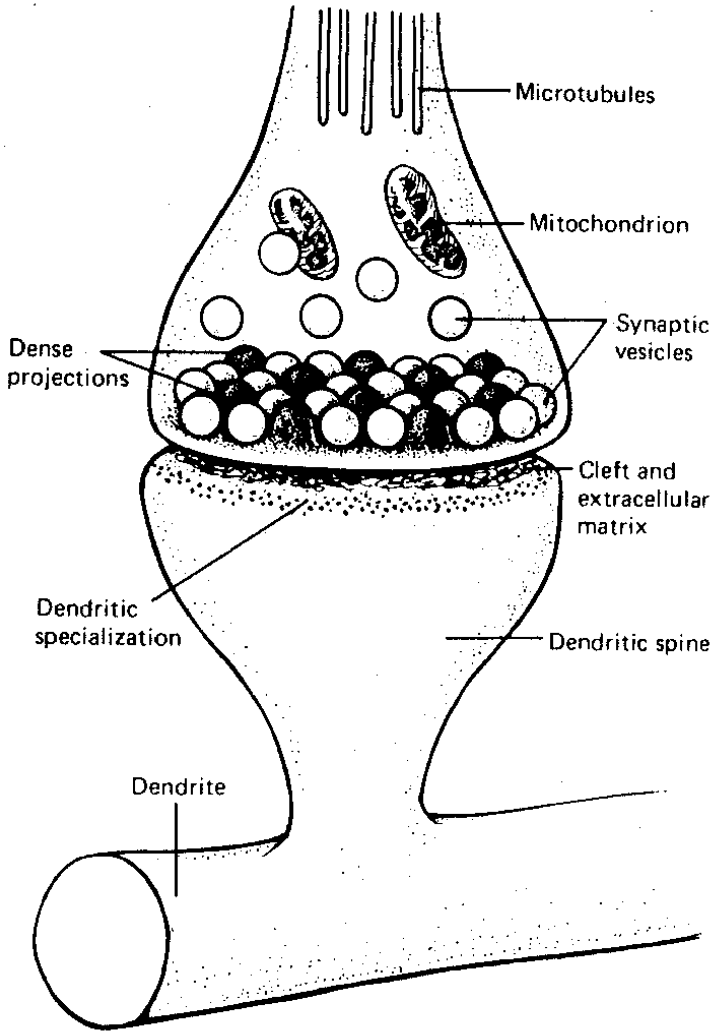
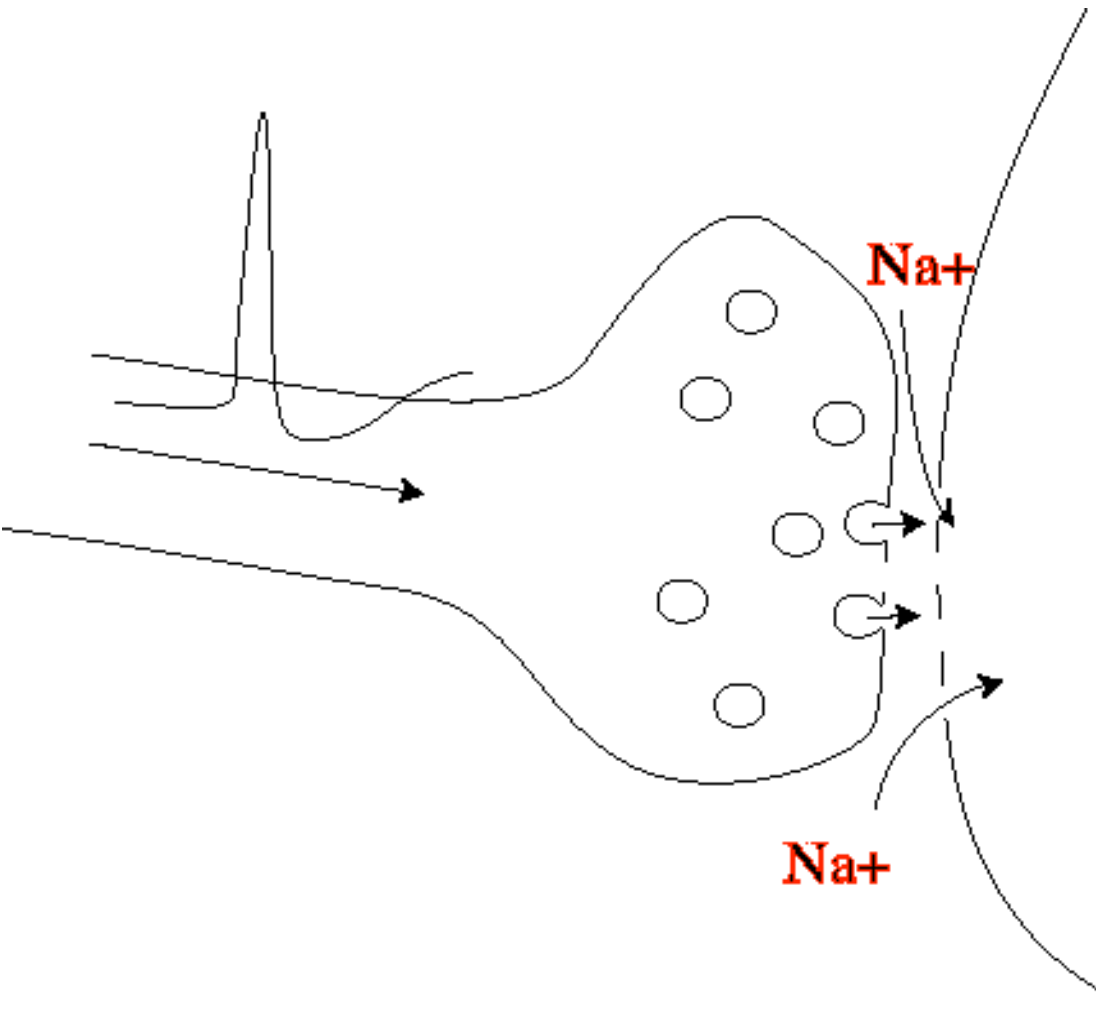
Neurons to networks

How do synapses transform inputs?





Excitatory synapse



Input spike

→ Neurotransmitter release i.e. glutamate

binds to/opens Na channels

Change in synaptic conductance

→ Na+ influx

voltage becomes more positive in post synaptic cell

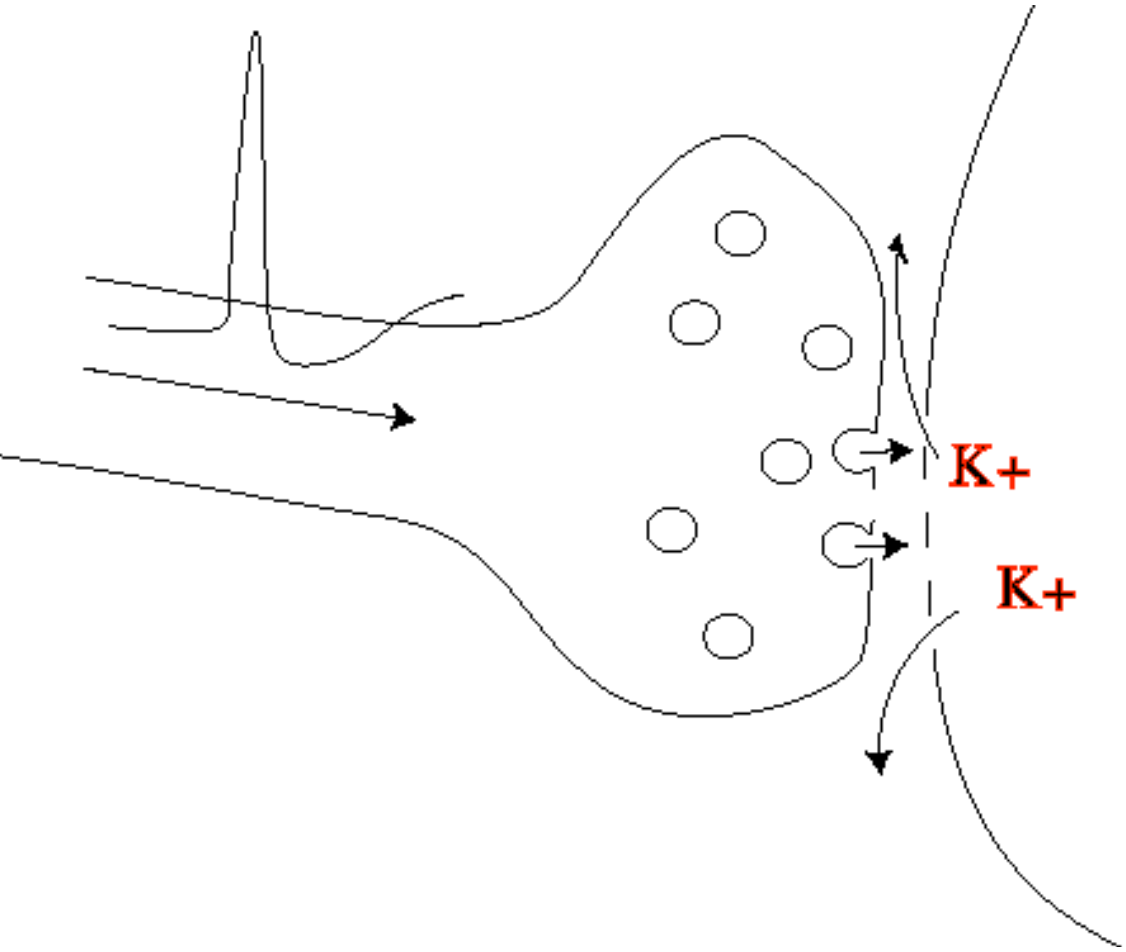
→ Depolarization due to EPSP

(excitatory postsynaptic potential)

E.g. AMPA synapse

Vocab: Depolarization means make V less neg = more positive

Inhibitory synapse



Input spike

→ Neurotransmitter release

GABA

binds to/opens K channels

Change in synaptic conductance

K+ leaves cell

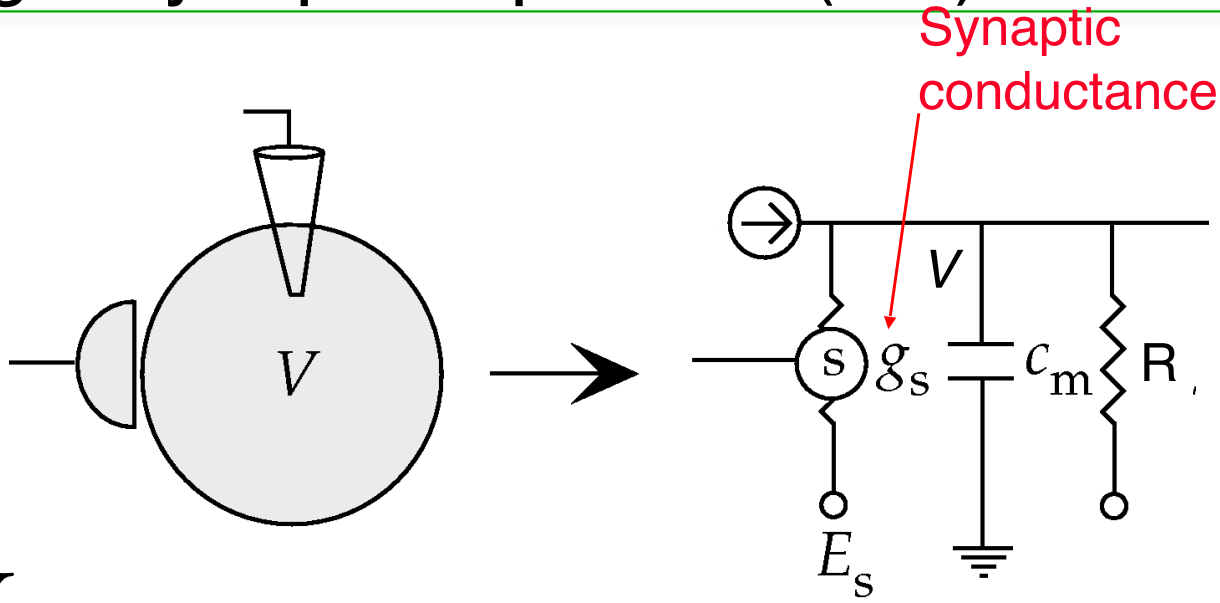
V becomes more negative

→ Hyperpolarization due to IPSP

(inhibitory postsynaptic potential)

Vocab: hyperpolarization means make V more negative

Modeling a synaptic input to a (RC) neuron



$$C\frac{dV}{dt} = g_L(E_L - V) + g_s(t)[E_s - V]$$

$g_s(t)$ synaptic conductance

E_s synaptic reversal potential

$E_s > V_{threshold} \rightarrow$ Excitatory

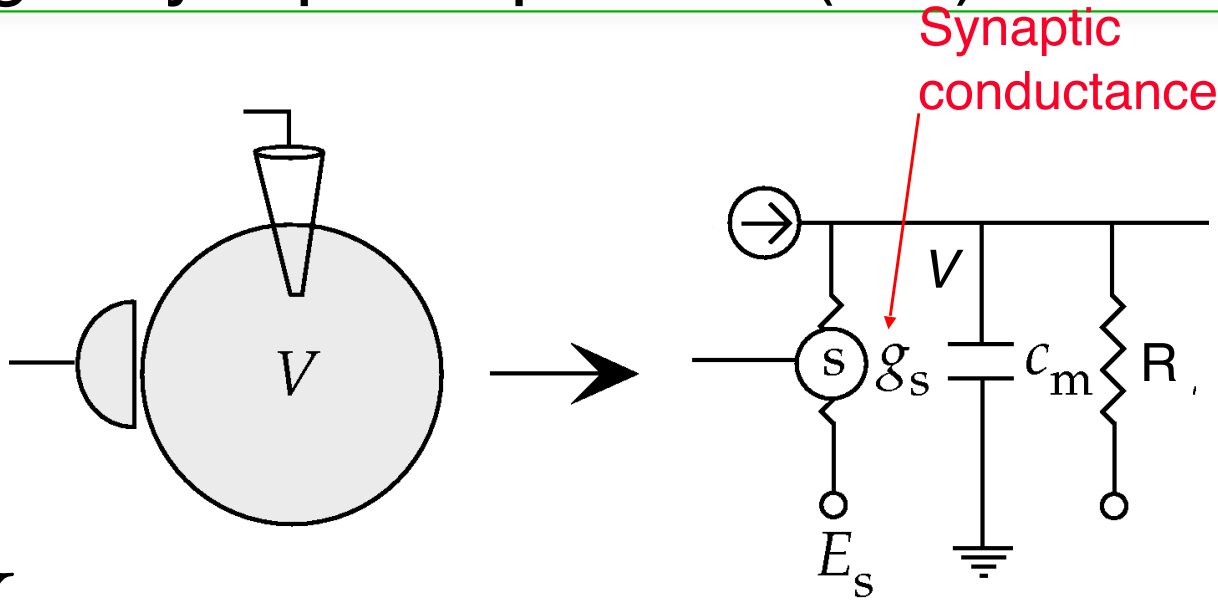
below the steady state potential

$E_s < E_L \rightarrow$ Inhibitory

$E_s \approx E_L \rightarrow$ Shunting

can alter time constant, making V relax back to its rest point faster (kind of inhibitory response, harder to create AP)

Modeling a synaptic input to a (RC) neuron



$$C\frac{dV}{dt} = g_L(E_L - V) + g_s(t)[E_s - V]$$

$g_s(t)$ synaptic conductance

$$g_s = g_{s,max} P_{rel} P_s$$

← Probability of postsynaptic channel opening (= fraction of channels opened)

fraction of channels opened in response to a release of a specific amount of NTs

max conductance based on number of channels avaliable

Probability of transmitter release given an input spike

some neurotransmitter vesicles do not successfully fuse with plasma membrane and release neurotransmitters in response to a spike; what proportion of vesicles successfully fuse?

Basic synapse model

Assume $P_{rel} = 1$ (for now)

What does a single spike input do to P_s?

Kinetic model:

open at a rate alpha

$$\text{closed} \xrightarrow{\alpha_s} \text{open}$$

$$\text{open} \xrightarrow{\beta_s} \text{closed}$$

close at a rate Beta.

$$\frac{dP_s}{dt} = \alpha_s(1 - P_s) - \beta_s P_s$$

Fraction of channels open

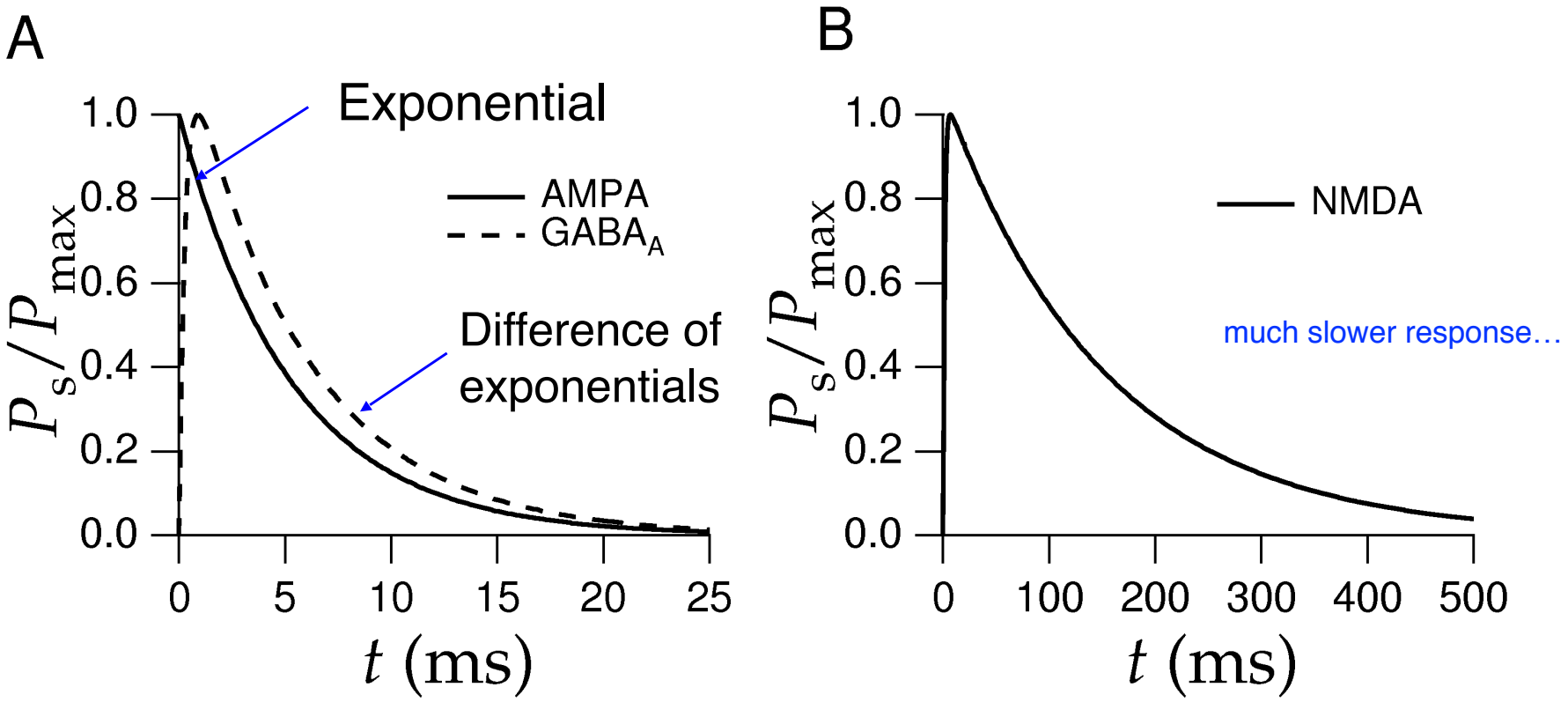
Opening rate

Fraction of channels closed

Closing rate

Where: $\alpha_s(V(t), Ca(t), \ldots)$ $\beta_s(V(t), Ca(t), \ldots)$

Synaptic filters

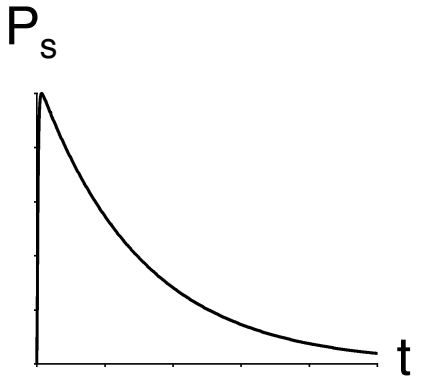


A difference of exponentials model better fits biological data for GABA, NMDA synapse types

Simplified synaptic models

Difference of exponentials:

$$P_s(t) = \text{const} \cdot P_{\max}\left(e^{-\frac{t}{\tau_1}} - e^{-\frac{t}{\tau_2}}\right)$$

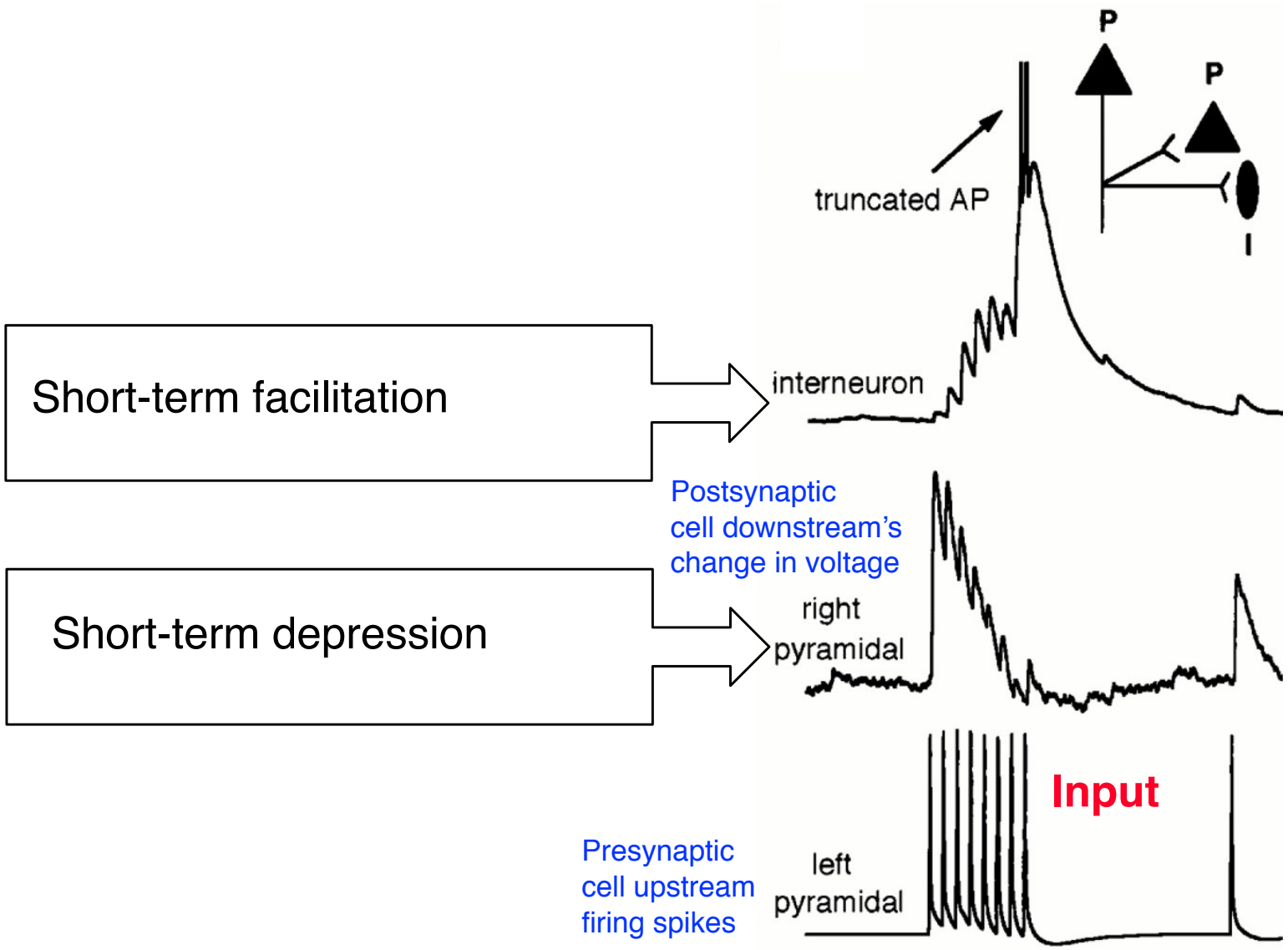


Alpha function:

$$P_s(t) = \text{const} \cdot \frac{t}{\tau_{peak}} e^{-\frac{t}{\tau_{peak}}}$$

What happens with a sequence of input spikes?

- Biological synapses are dynamic!

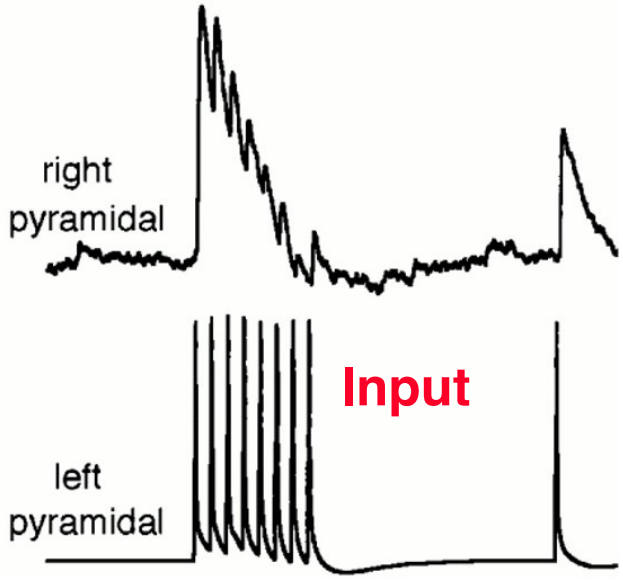


(Markram & Tsodyks, 1998)

Short-term synaptic plasticity: describe this via P_rel

Recall definition of synaptic conductance:

$$g_s = g_{s,\max} P_{rel} P_s$$



Idea: Specify how P_{rel} changes as a function of consecutive input spikes

$$\tau_P \frac{dP_{rel}}{dt} = P_0 - P_{rel}$$

Between input spikes, P_{rel} decays exponentially back to P_0

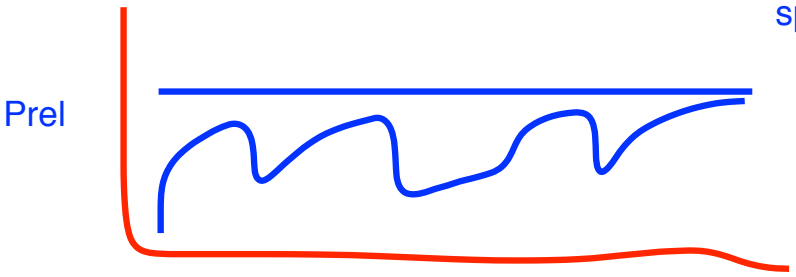
If input spike:

Fd < 1; causes Prel to drop in response to a spike

$$P_{rel} \rightarrow f_D P_{rel}$$

depression: decrement P_{rel}

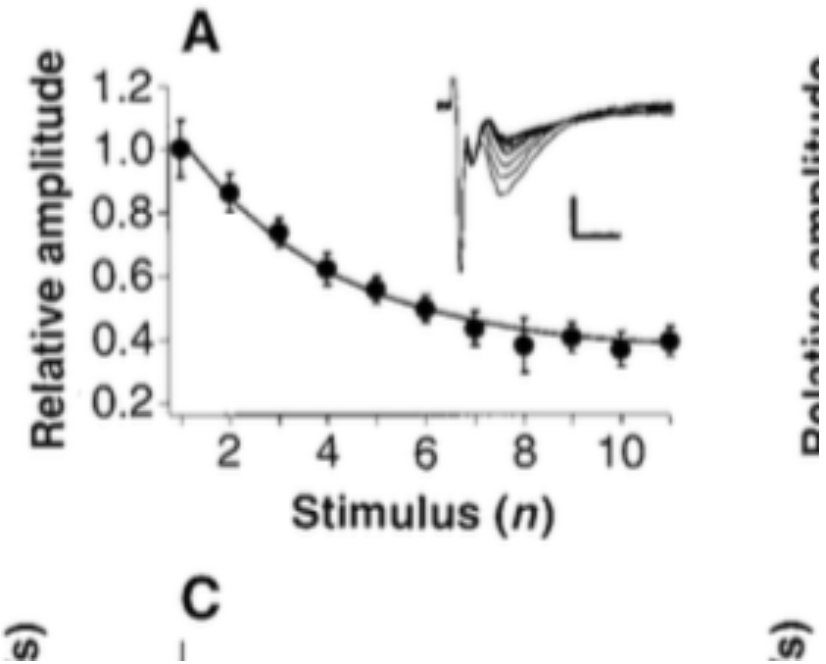
spike causes a drop in Prel



[sketch on board]

Abbott et al 1997

Fig. 1. Experimental results and fits of the model for synaptic depression. (**A**) Depression of synaptic responses during repetitive stimulation. Filled circles indicate normalized average field potential amplitudes evoked by 11 consecutive stimuli at 20 Hz. Error bars are stan-



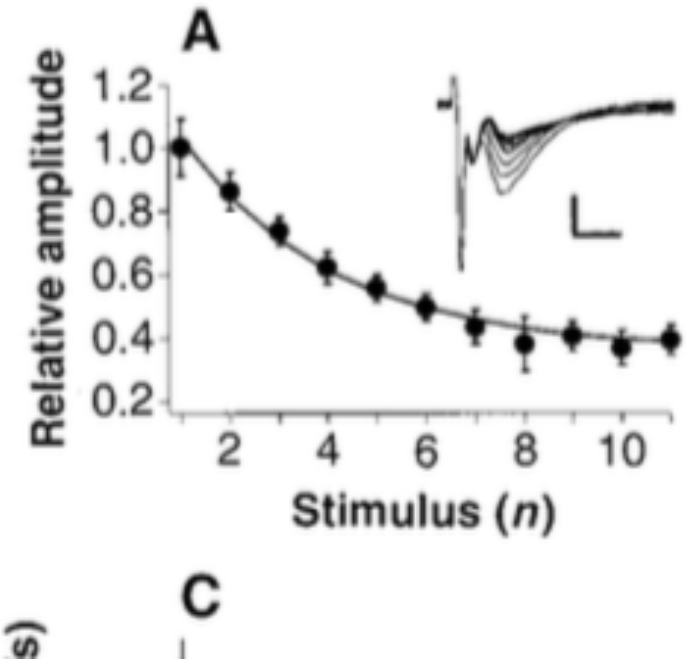
Lab exercise:

Write a code that implements the Abbott et al mechanism for synaptic depression.

Drive the synapse with spikes occurring regularly at 20 Hz, as in Fig. 1A of Abbott et al '97. Can you reproduce that figure?

Hint: this should be a few lines of code.

Fig. 1. Experimental results and fits of the model for synaptic depression. (**A**) Depression of synaptic responses during repetitive stimulation. Filled circles indicate normalized average field potential amplitudes evoked by 11 consecutive stimuli at 20 Hz. Error bars are stan-



Impact of synaptic depression

Key result (a few lines of calculation, see (7) in paper [ESB notes]):

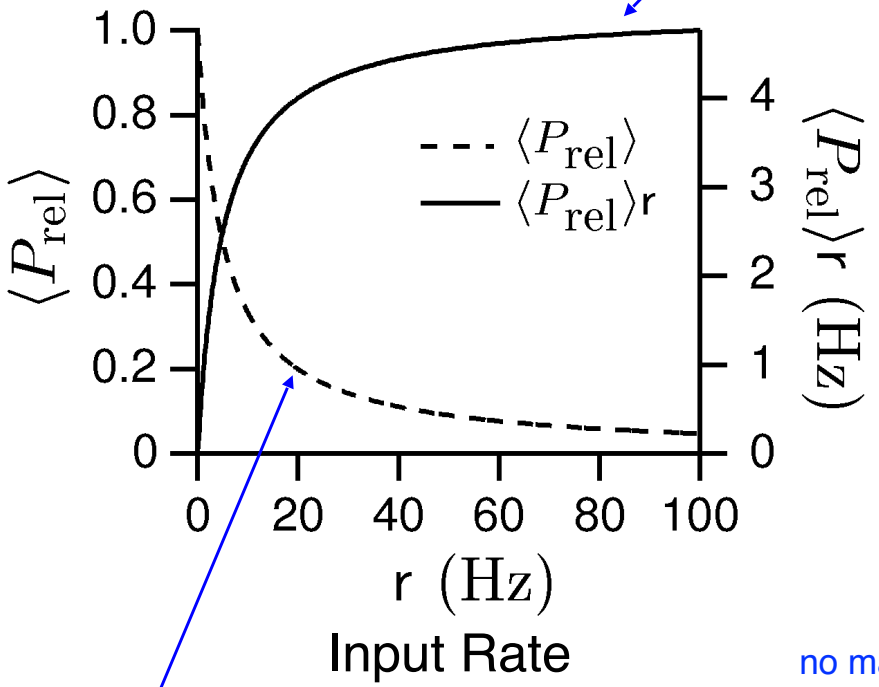
If synapse receives input spikes at rate r, then the **steady state value** of

$$P_{rel}(r) \sim 1/r$$

Prel as a function of r = k/r

Consequences of synaptic depression: steady state

average transmission rate



average release probability

At steady state,

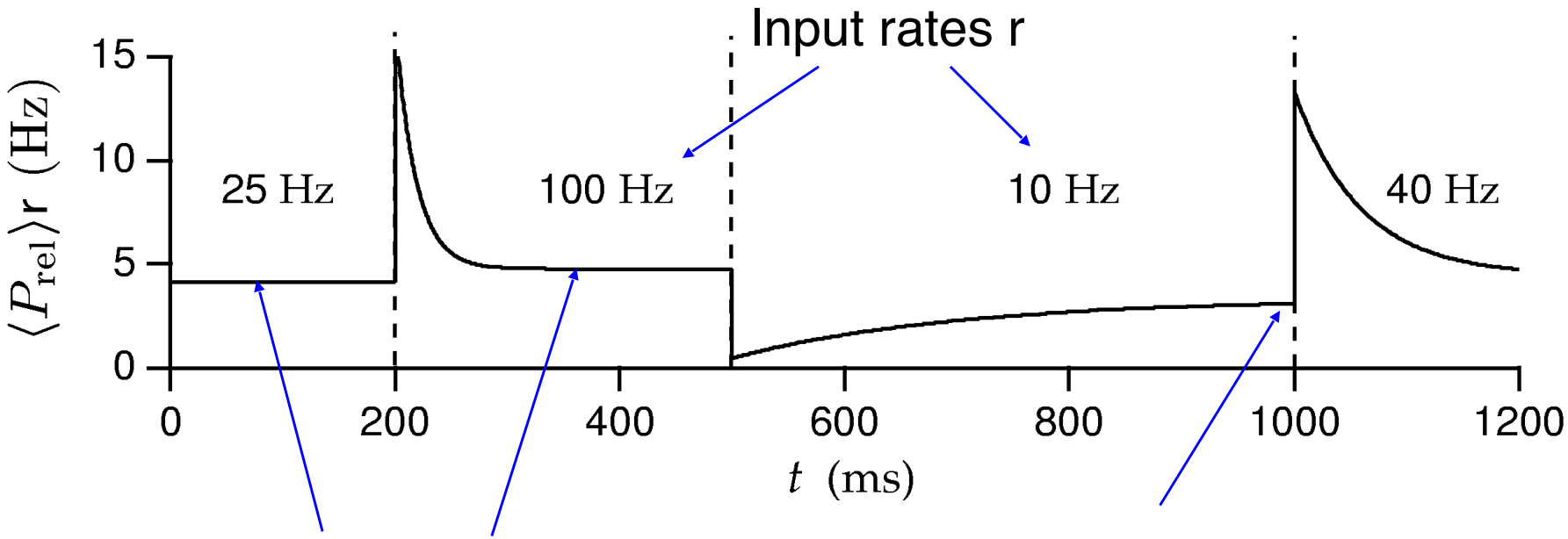
$$P_{rel}(r) \times r \approx \text{const for large } r$$

Constant synaptic input for Wide range of inputs!

Steady-state gain control

no matter what upstream cell is doing, does not change steady state rate of downstream cells

Consequences of synaptic depression: dynamic response



Steady-state transmission rates are similar for different rates

Transient inputs are amplified relative to steady-state inputs

cell gets insane amount of signals coming in; adaptation. Gets used to a stable amount of noise

<u>In fact: an equal-percent change from baseline gives an equal transient response.</u>

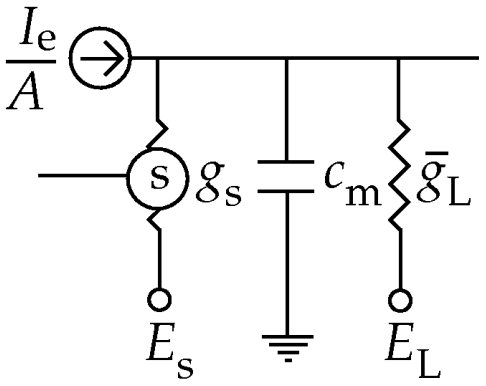
Who cares? Abbott et al 97: Neuron gets inputs from 1000's of upstream cells, each of which fires at 1-200 Hz. How can we be responsive to all?

Synaptic depression yields "gain control" to satisfy this.
vs. Adaptation or inhibition, does so in an INPUT-SPECIFIC way!

Extending the model to include facilitation

Recall definition of synaptic conductance:

$$g_s = g_{s,\max} P_{rel} P_s$$



If input spike:

$$P_{rel} \rightarrow f_D P_{rel}$$

depression: decrement P_{rel}

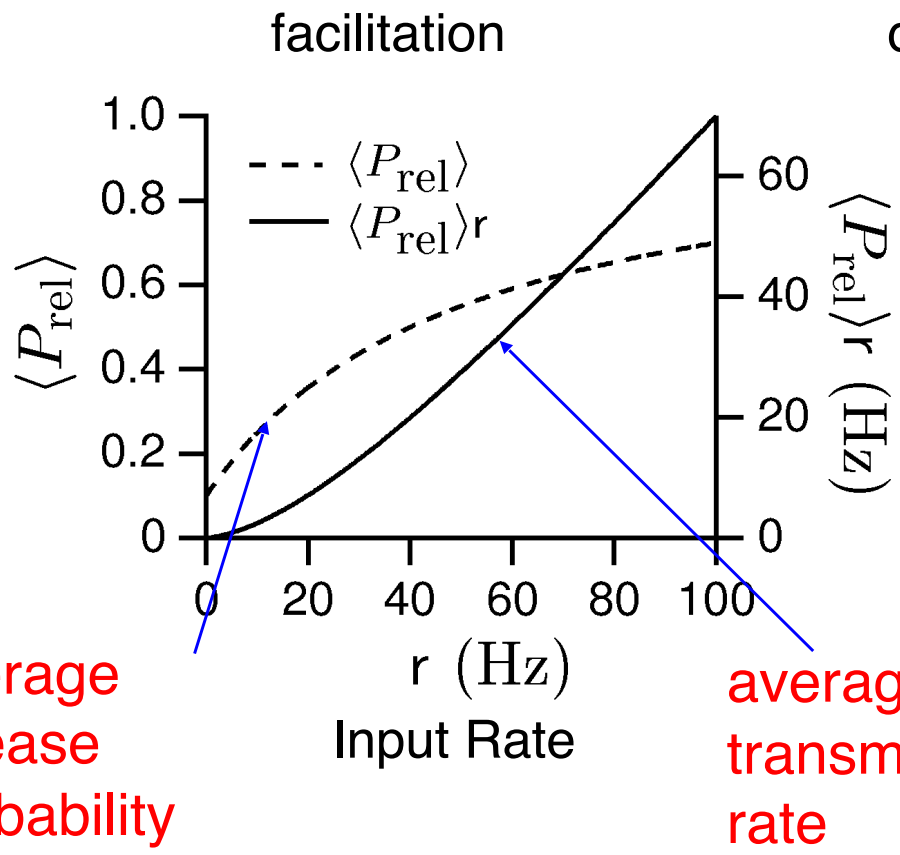
$$P_{rel} \rightarrow P_{rel} + f_F (1 - P_{rel})$$

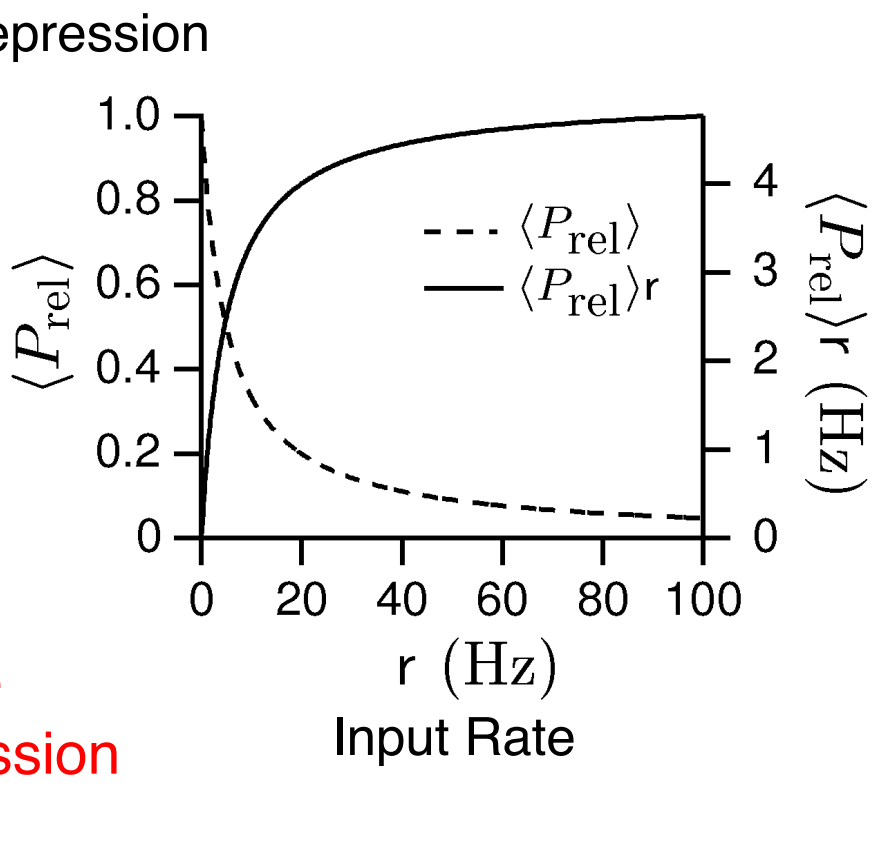
facilitation: increment P_{rel}

Between input spikes, P_{rel} still decays exponentially back to P_0

Abbott et al 1997

Effects of synaptic facilitation & depression



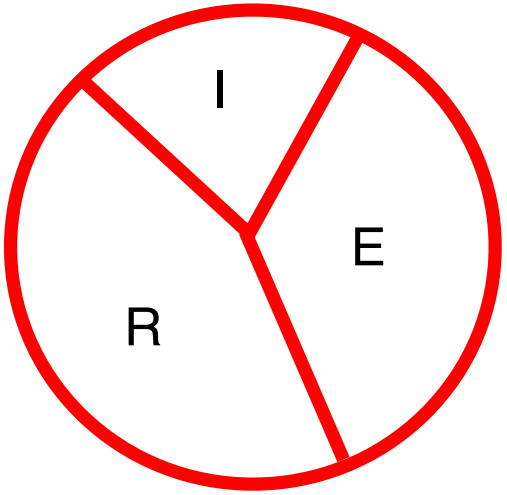


average release probability

average transmission rate

More detailed plasticity model

- Incoming spike activates a fraction of recovered resources R to become effective (E)
- Amount of effective resources E govern size of $g_s(t)$
- Effective resources rapidly inactivate (msec)
- Inactivated recover (100s of msec)
- E(t) determines postsynaptic current



t_{AP} : time of spike
at all spike times
jump R by $-U_{SE} * R(t_{AP})$

$$\frac{dR}{dt} = \frac{I}{\tau_{rec}} - U_{SE} \cdot R \cdot \delta(t - t_{AP})$$

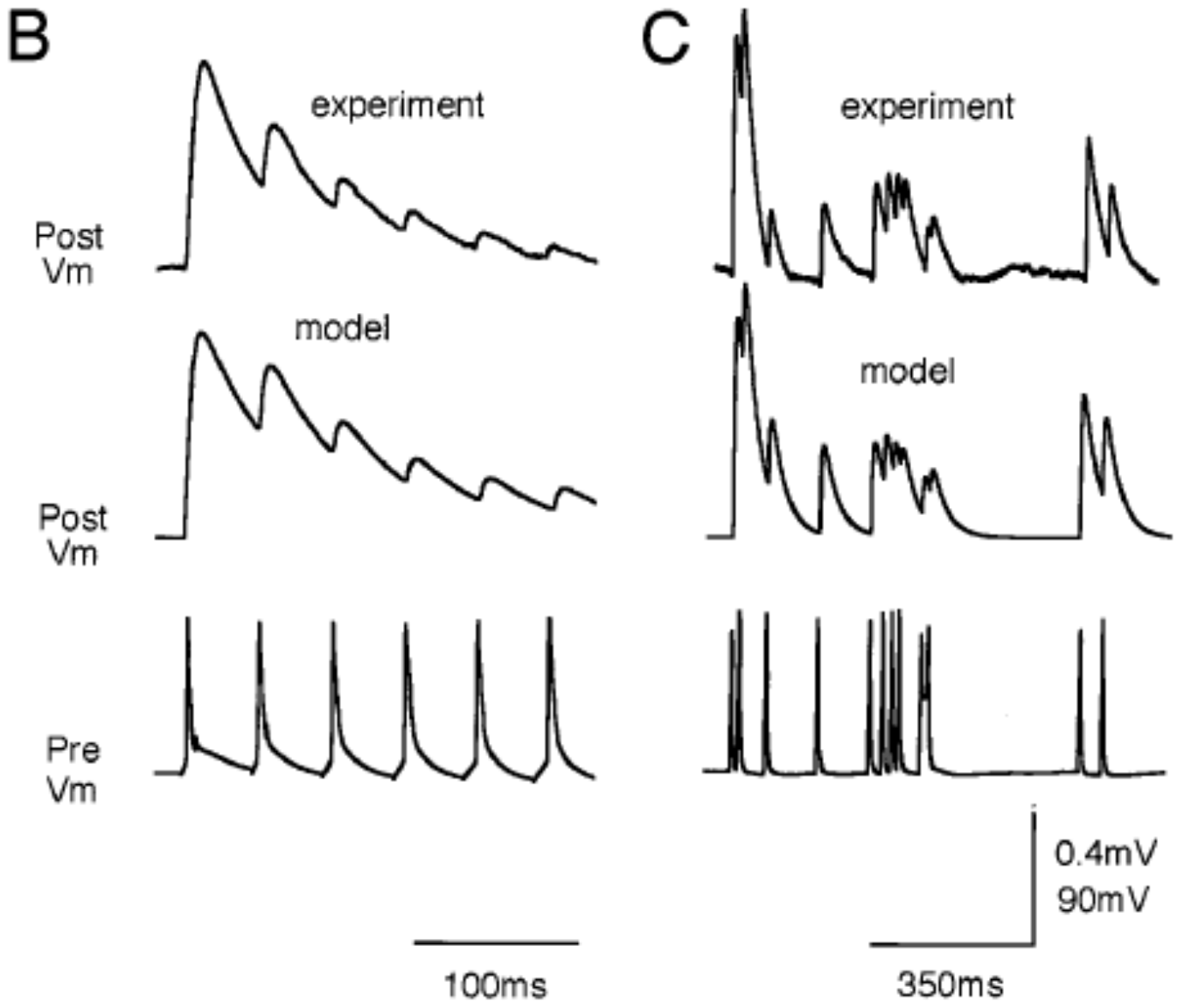
$$\frac{dE}{dt} = -\frac{E}{\tau_{inact}} + U_{SE} \cdot R \cdot \delta(t - t_{AP})$$

similar meaning

$$I = 1 - R - E,$$

Markram and Tsodyks, PNAS 1997

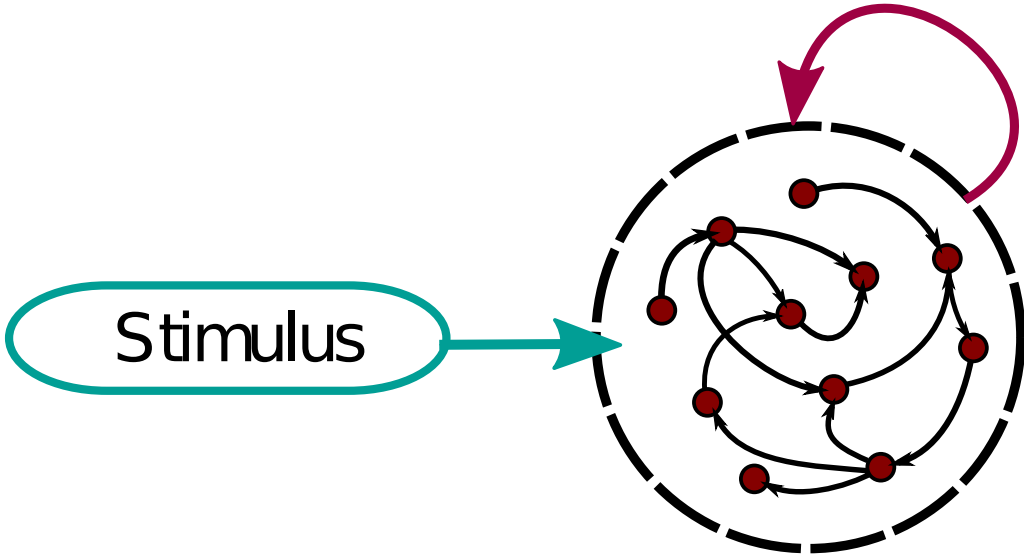
Match between model and experiment



Summary:

Synapses provide an additional layer of dynamics and computation, beyond that occurring in single neurons!

Network computation via simplified “firing rate” models



W, connection weight matrix

W_ij = weight from j to i

neuron (or neural population) i fires with rate $r_i(t)$

neuron (or neural population) i receives input

$$input_i = stim_i(t) + \sum_j W_{ij} r_j(t)$$

all the firing rates of cells j are multiplied by the weight from j to i

cell i is our specific cell of interest.

DYNAMICS: rates approach steady states f(input)

$$\tau \frac{dr_i}{dt} = f(input_i) - r_i$$