

Dr.
09/5/22

Deep Learning :-

Used for

1. Artificial neural network [ANN] [Regression/classification]
 2. Convolution neural networks [CNN] [computer vision]
[image classification]
 3. Recurrent neural network [RNN] [Time series analysis]
- and
- long short term memory

[LSTM]

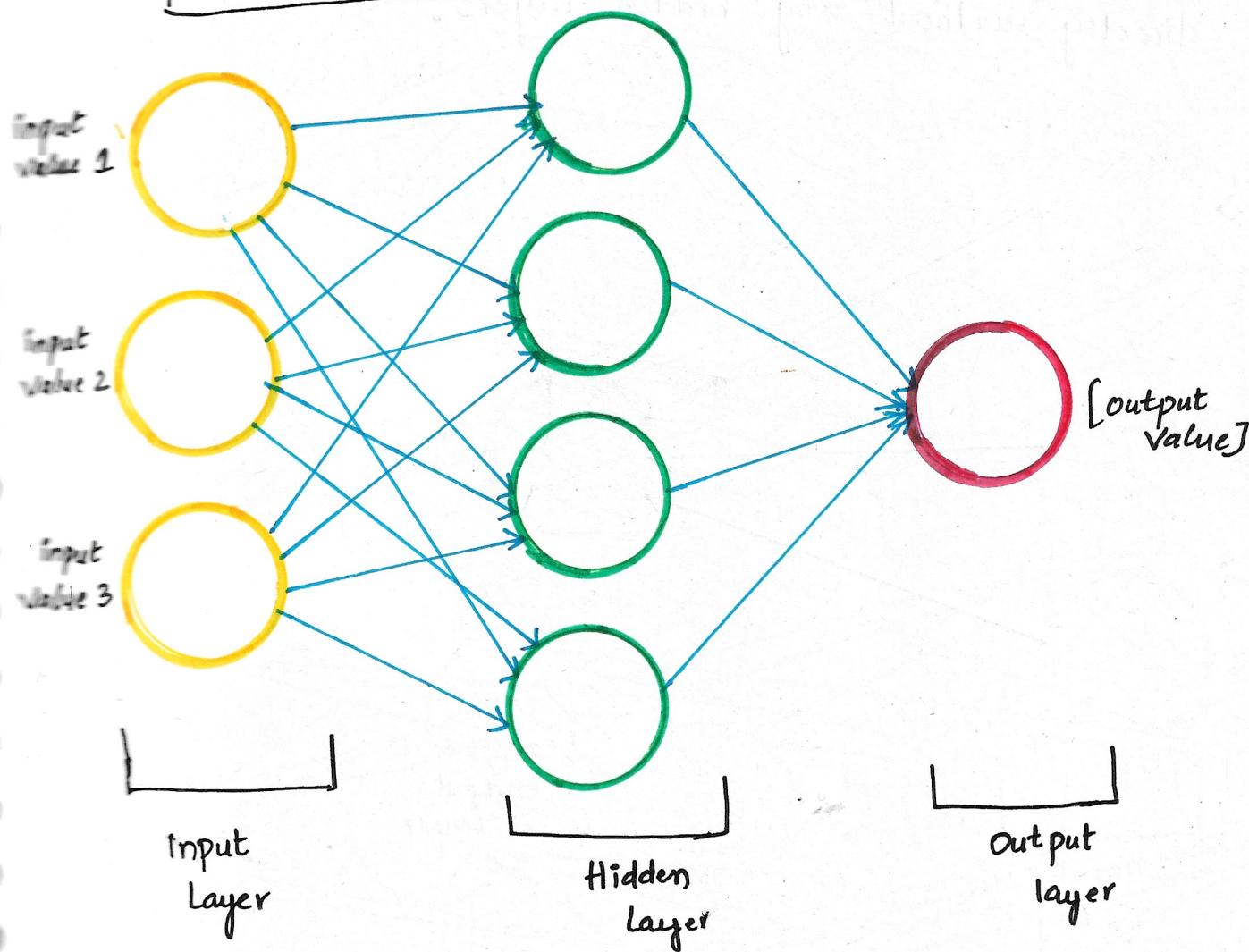
1. Artificial neural network

* Artificial intelligence :- application which can do its own task with out any human intervention

Ex:- netflix app

- * self driving cars
- * amazon application
- * Sofia (robot)

Neural network :- Connecting the neurons making as one connection is known as "Neural network".



Ex:-

x_1	x_2	x_3	y
-	-	-	-
-	-	-	-
-	-	-	-

Here, we have

- * Three input layers :

n_1, n_2, n_3

- * One output layer :

" y "

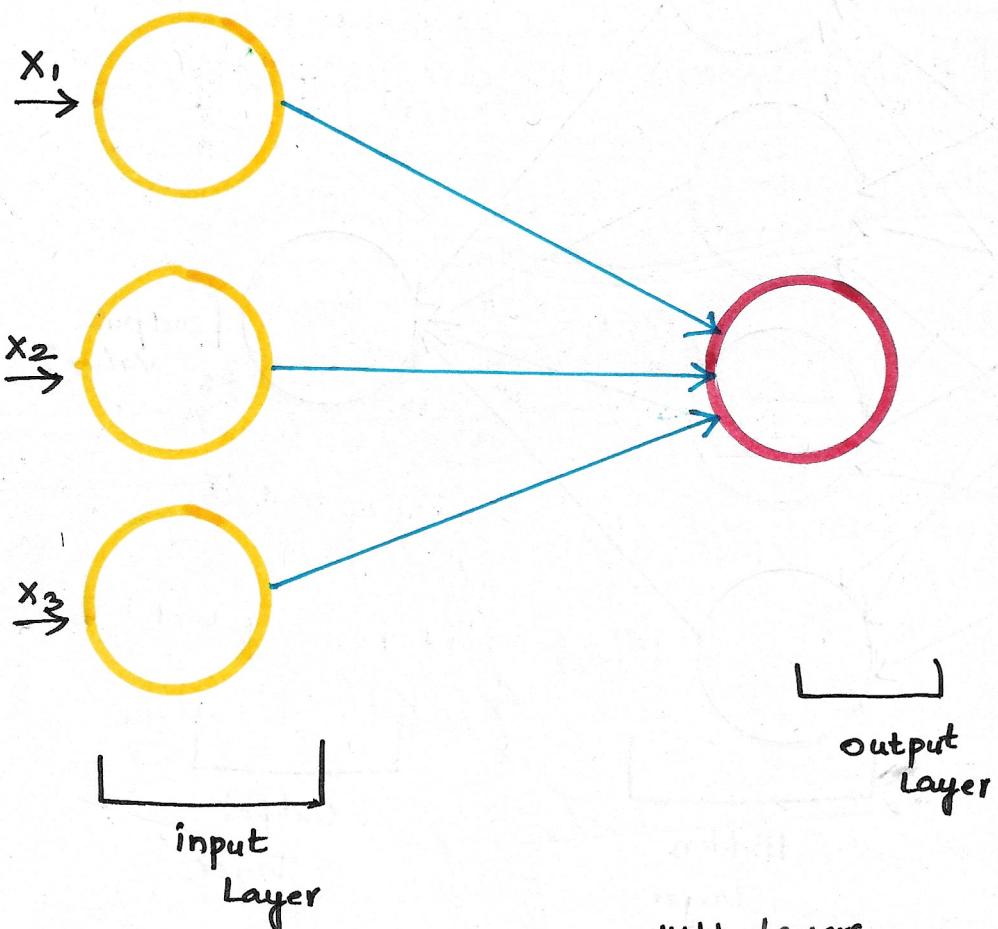
" y " can be

continuous
discrete

binary
multiclass.

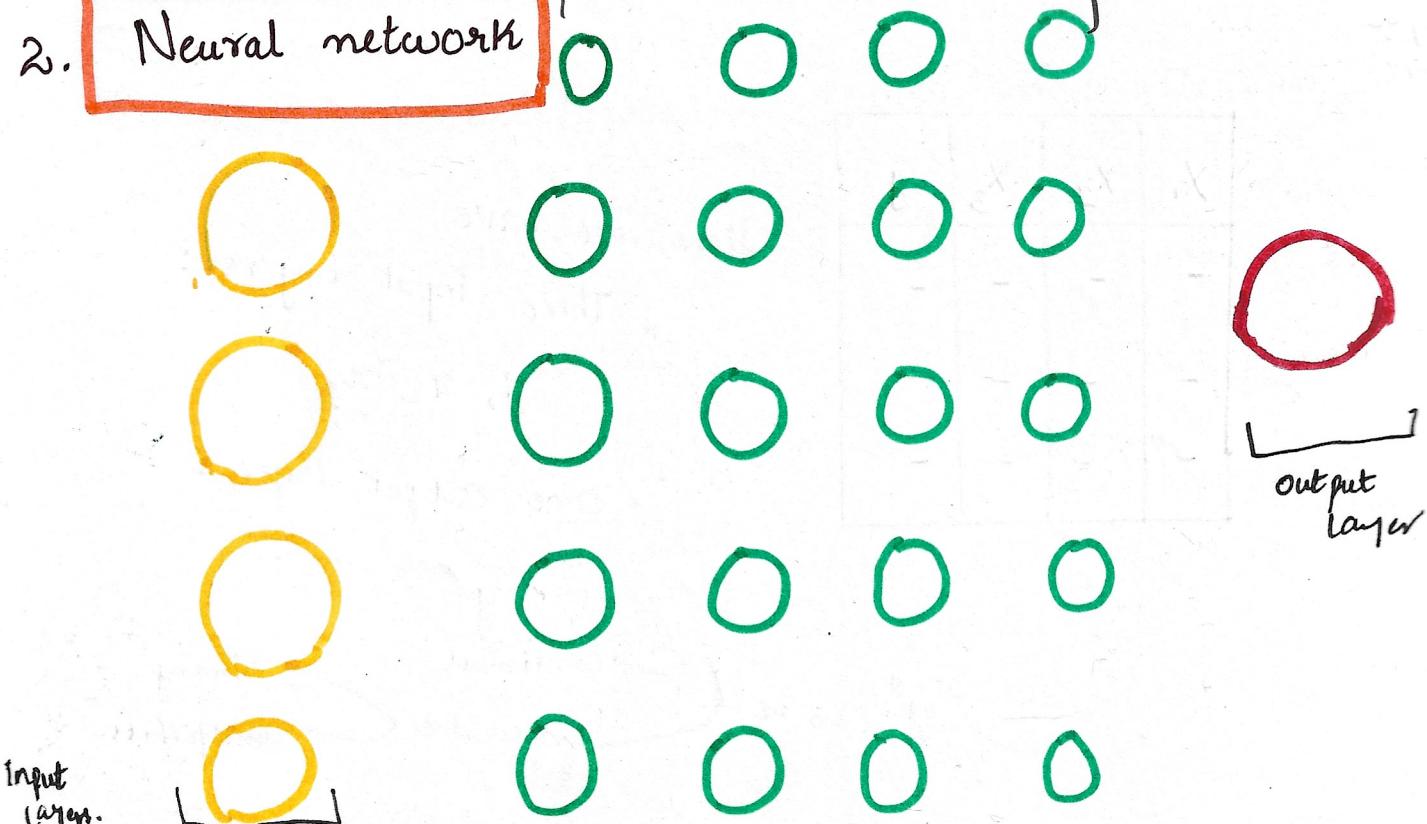
1. **Perceptron** :- Connecting Input layer to Output layers

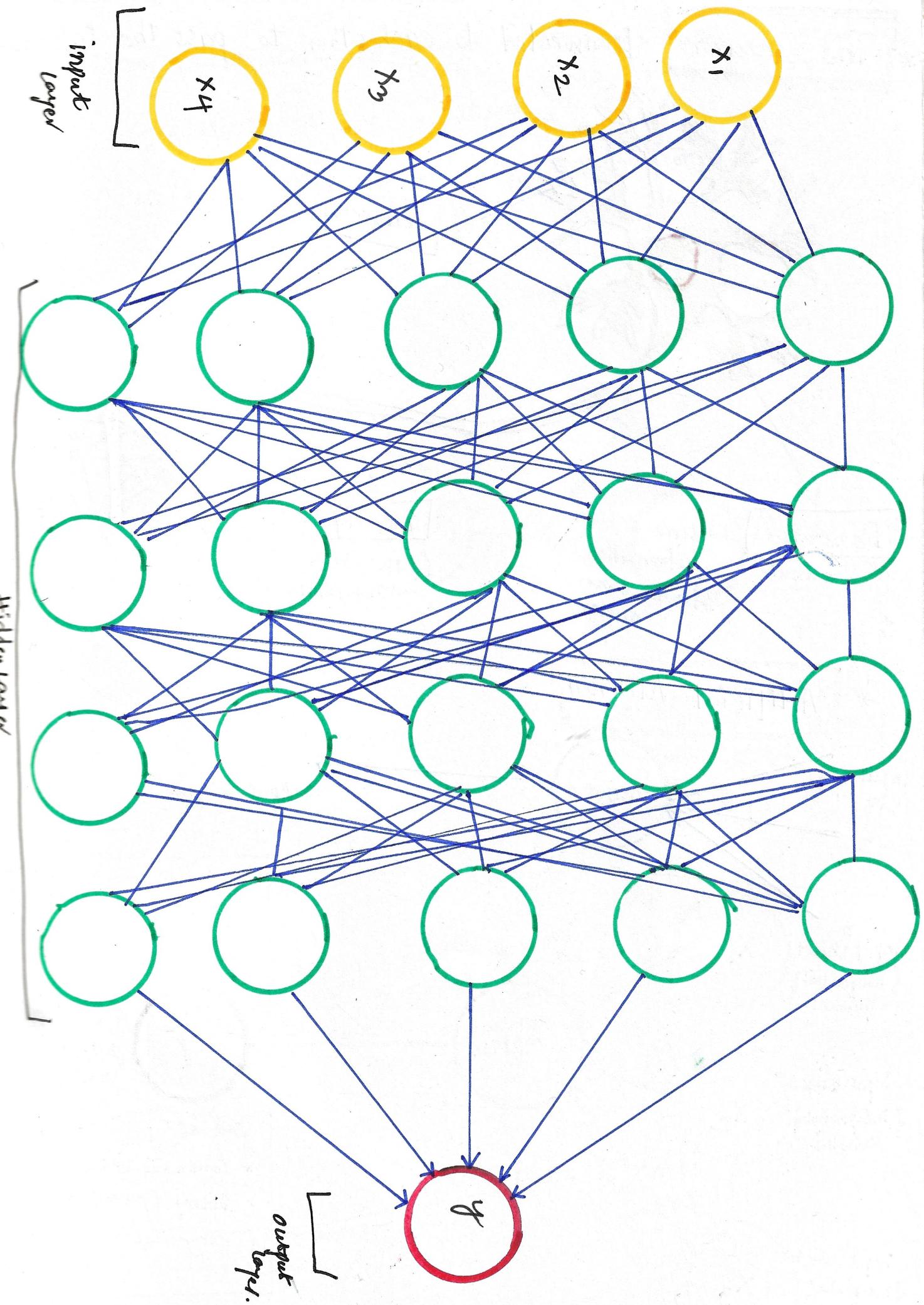
directly without any hidden layers.



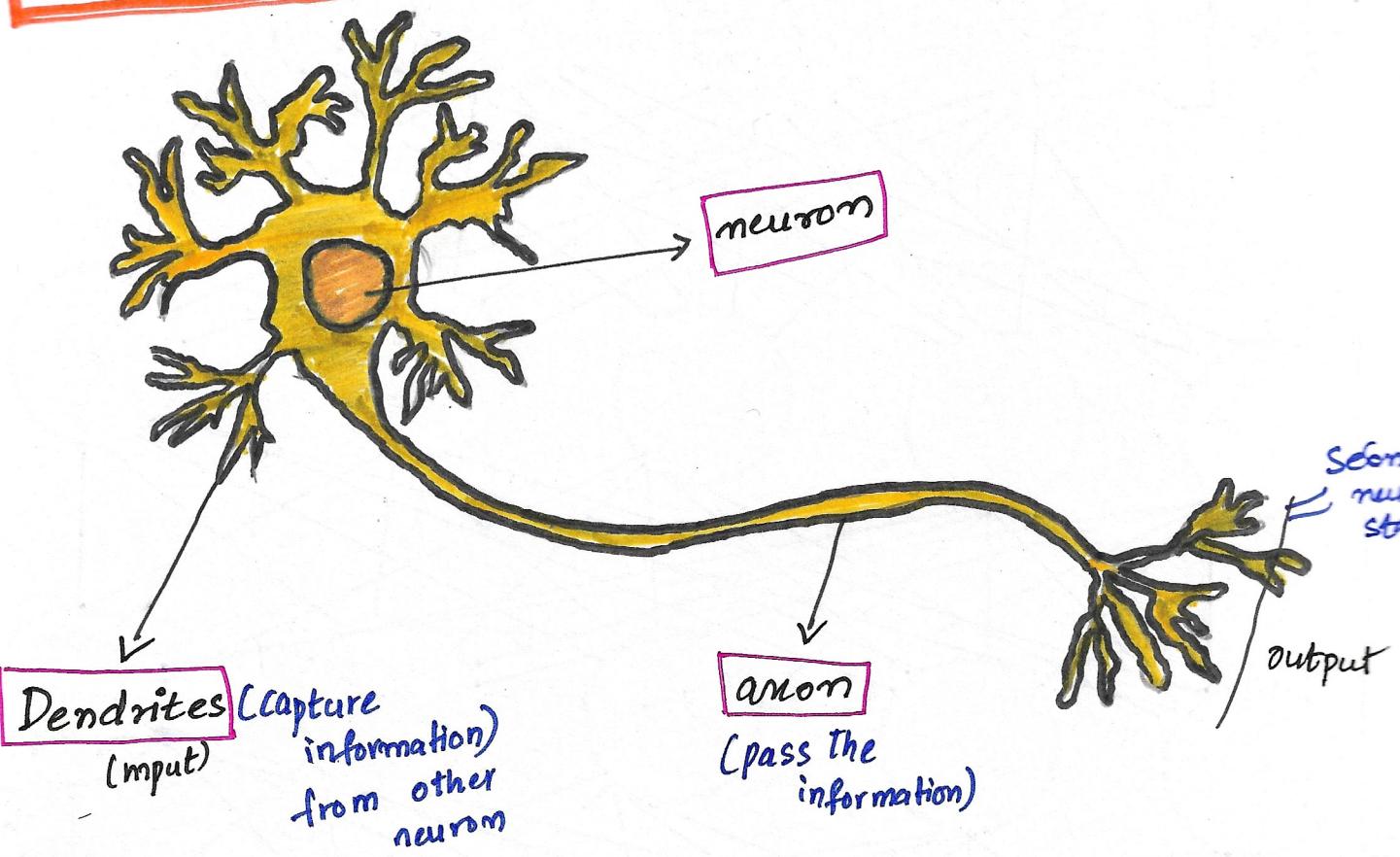
2. **Neural network**

Hidden Layers

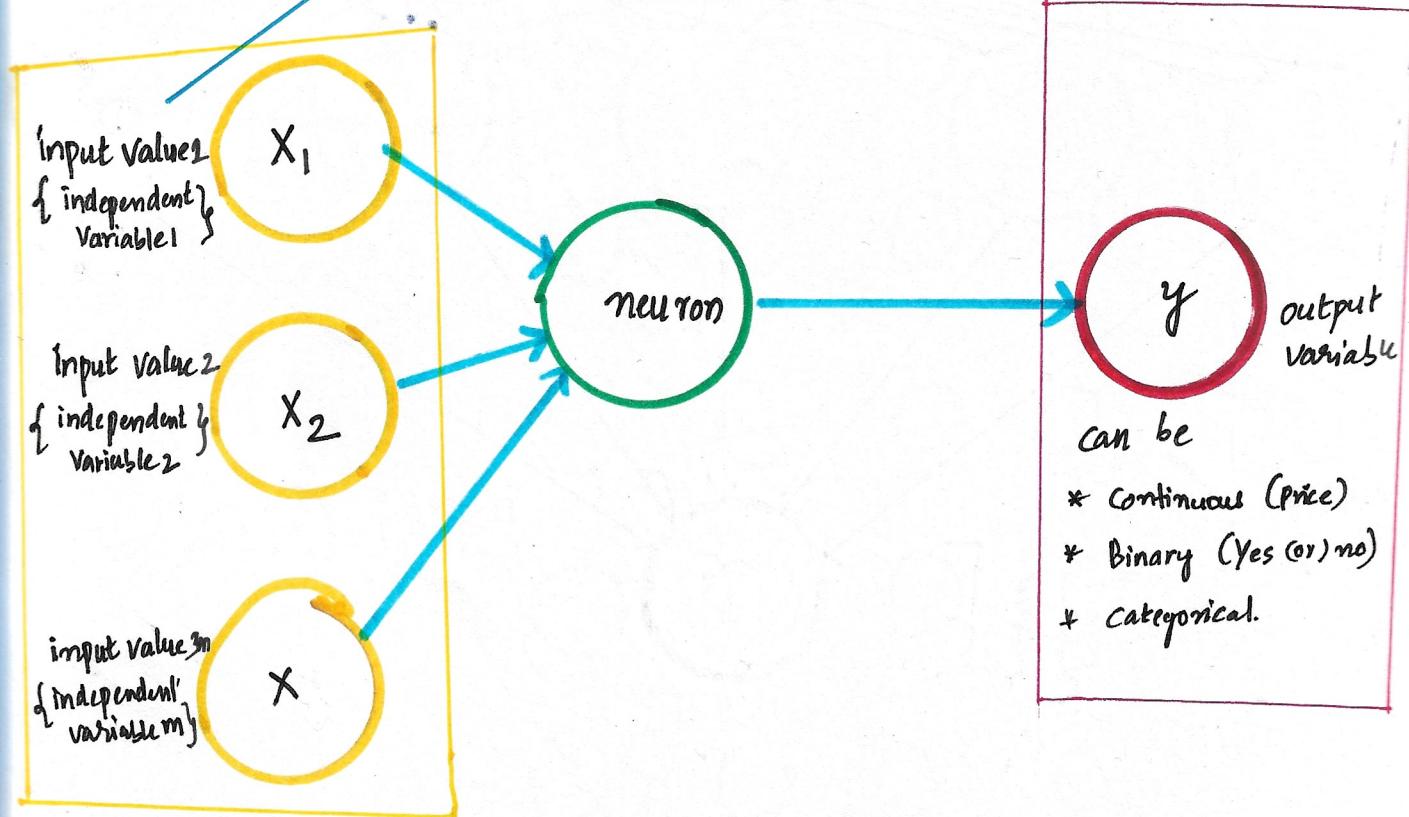




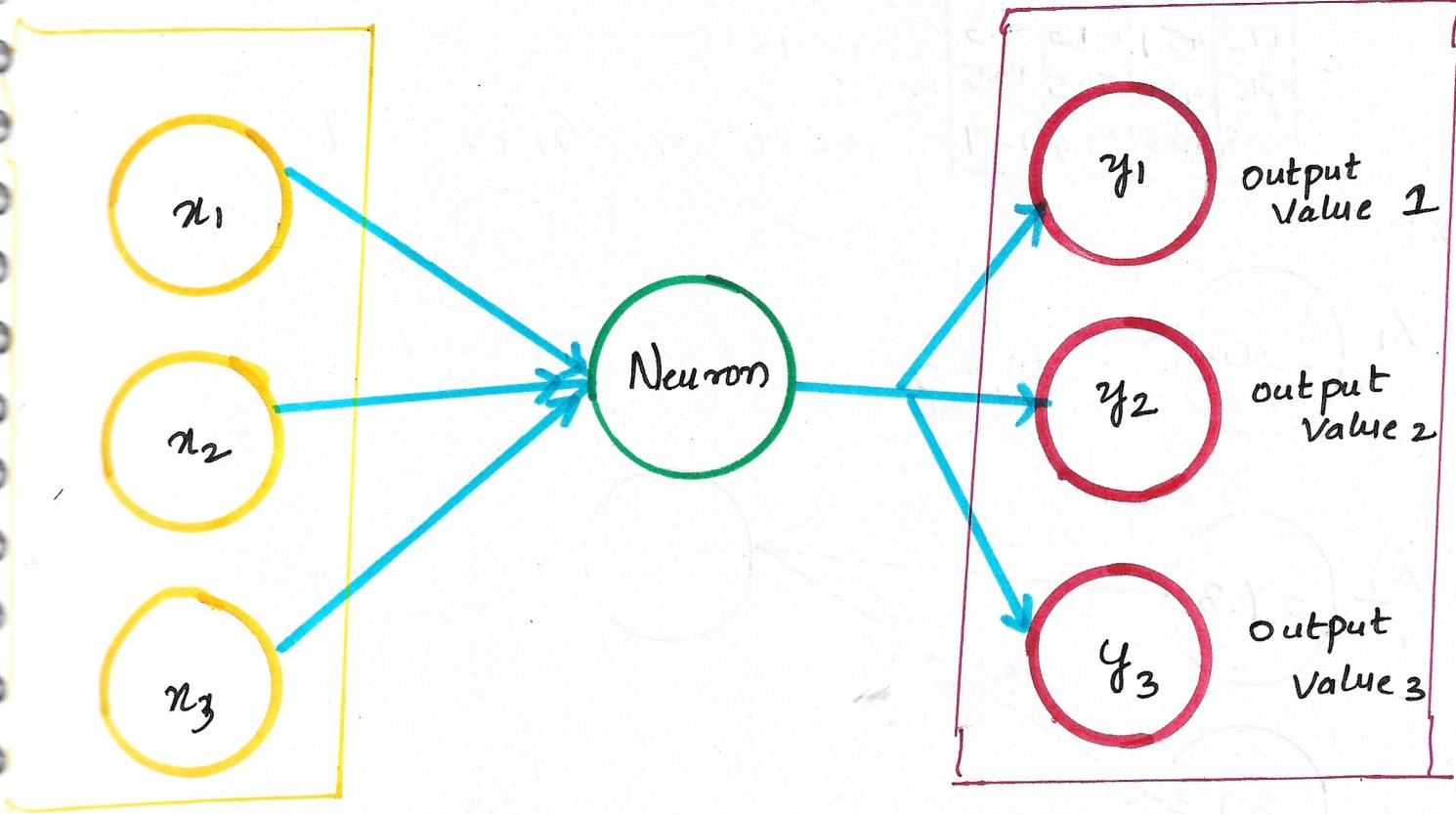
* The neuron connected to each other to pass the information



* Artificial Neuron



- * Binary classification \rightarrow o/p neuron \Rightarrow 1 neuron
- * Regression \rightarrow output neuron \Rightarrow 1 neuron
- * Multiclassification \rightarrow output neuron \Rightarrow no. of categories (6) classes.
Ex:- Penguin
Age, chi, Gentoo



* Weights

Machine learning: $\beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3 = (y - \hat{y})_{\text{min}}$

deep learning: $b + w_1 x_1 + w_2 x_2 + w_3 x_3 = (y - \hat{y})_{\text{min}}$

$\sum w_i x_i + b$

It can be written as

Ex:- Linear Regression.

X_1	X_2	X_3	y
TV	Radio	news paper	Sales
230.1	37.8	69.2	22.1
44.5	39.3	45.1	10.4
17.2	45.9	69.3	9.3
151.5	41.3	58.5	18.5
180.8	10.8	58.4	12.9

we consider weights

Ex:- Equation ($2x+5 = y$)

initialization of value

$$x = 100 \Rightarrow 2(100) + 5$$

$$\hat{y} \quad y \quad \text{error}$$

$$205 \quad 9 \quad -196$$

$$x = 99 \Rightarrow 2(99) + 5$$

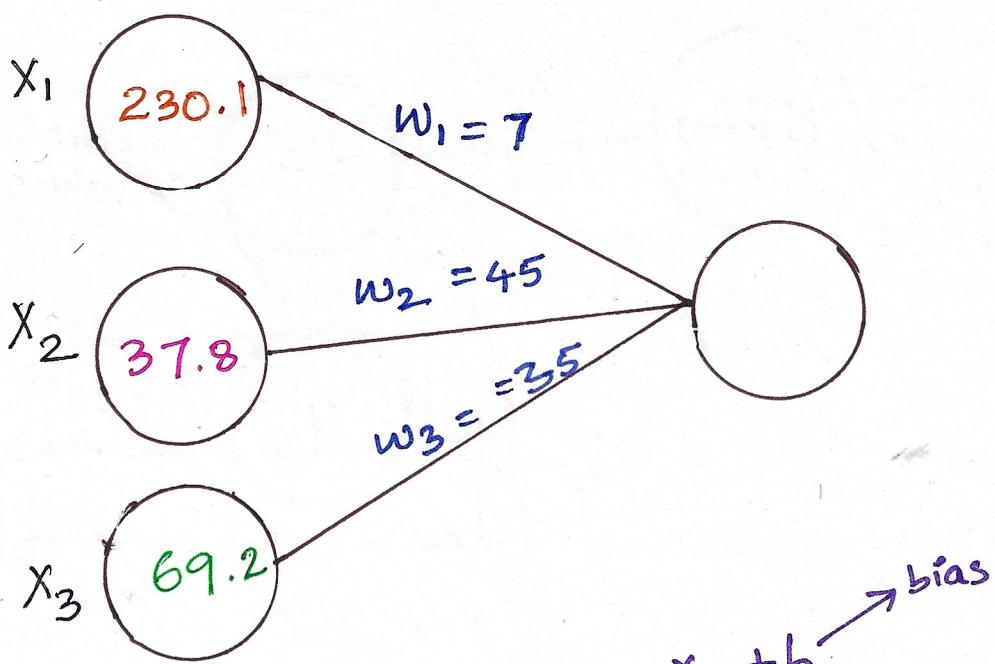
$$203 \quad 9 \quad -194$$

$$x = 98 \Rightarrow \dots$$

$$\vdots$$

$$x = 2 \Rightarrow 2(2) + 5 \quad 9 \quad 9 \quad 0$$

Ex:-



$$* w_1 x_1 + w_2 x_2 + w_3 x_3 + b$$

$$* [7 \times 230] + [45 \times 37] + [35 \times 69] + 100$$

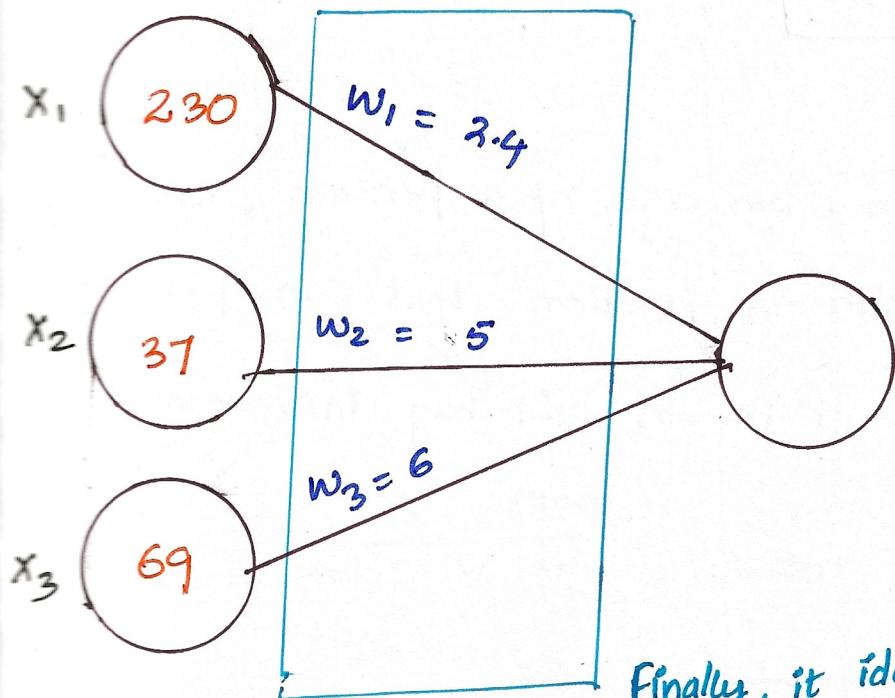
$$\hat{y} = 5790.$$

y	\hat{y}	$y - \hat{y}$
22.1	5790	5767.9

So, $(y - \hat{y})$ largest amount
of difference is there,

- Weights will be readjusted

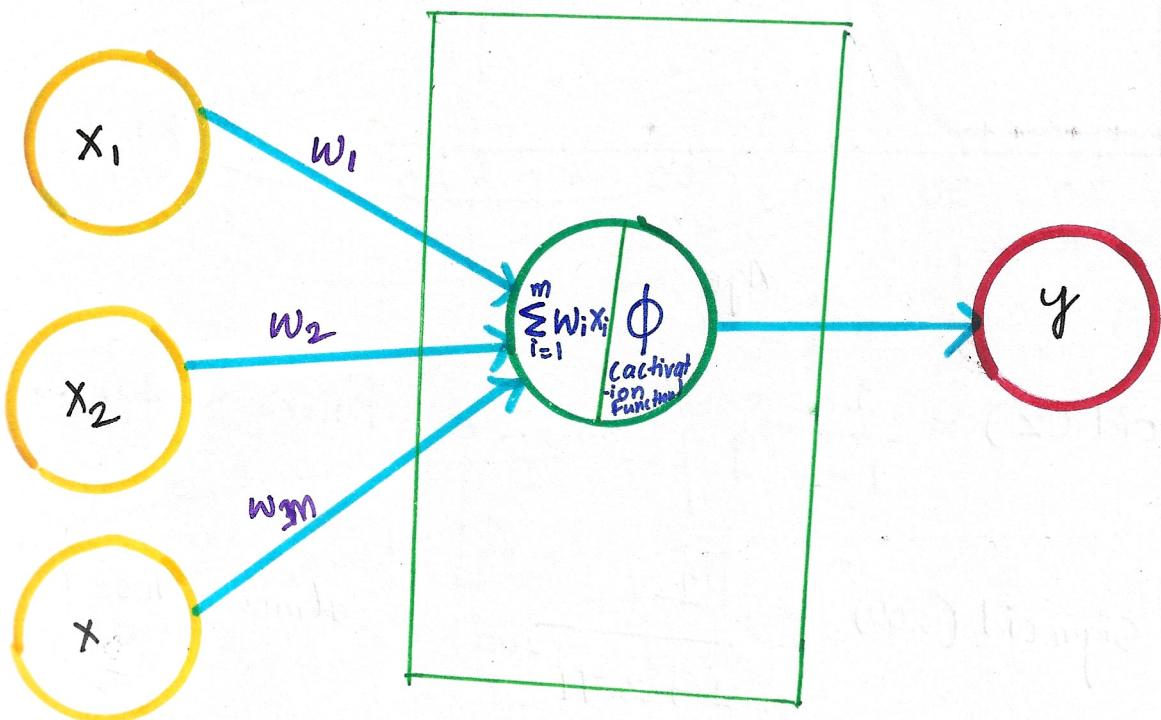
* weights will be adjusted



Finally, it identifies the best weights which gives sum of square errors to minimum.

Here, it's identifying only weights.
 $(SSE)_{min}$.

Steps in neuron

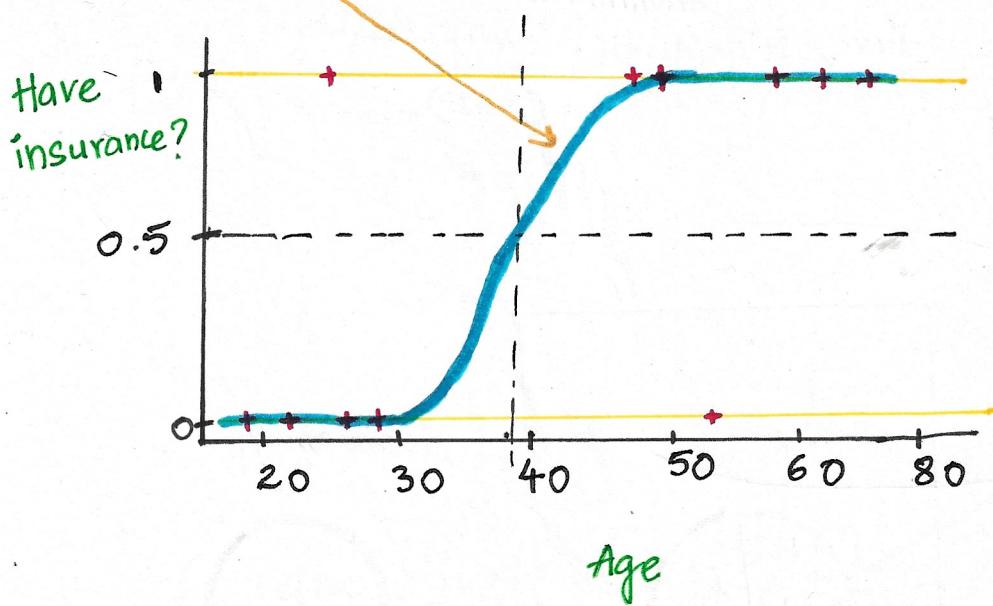


Ex:- **Binary classification.**

age	have-insurance
22	0
25	0
47	1
52	0
46	1
56	1
:	:

Given, an age of a person, come up with a function that can predict if person will buy insurance (or) not.

* **Sigmoid** or **Logit function**.



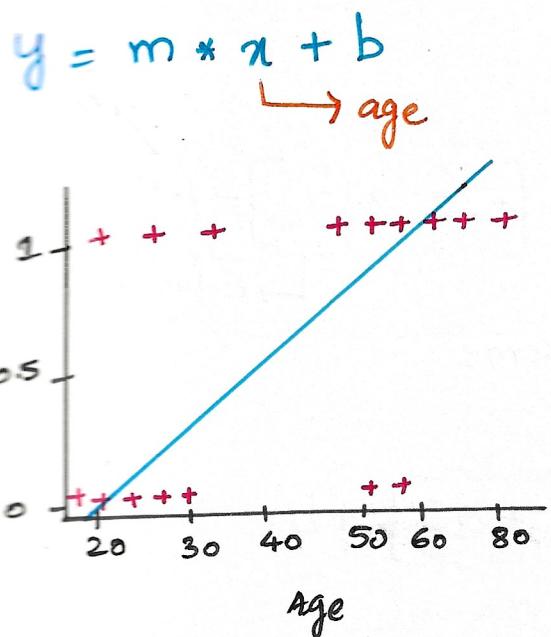
* **Sigmoid (z)** =
$$\frac{1}{1 + e^{-y}}$$
 $\therefore e = \text{Euler's number} \sim 2.71828$

$\therefore 200$ • Sigmoid (200) =
$$\frac{1}{1 + 2.71^{-200}} = \text{almost close to } 1$$

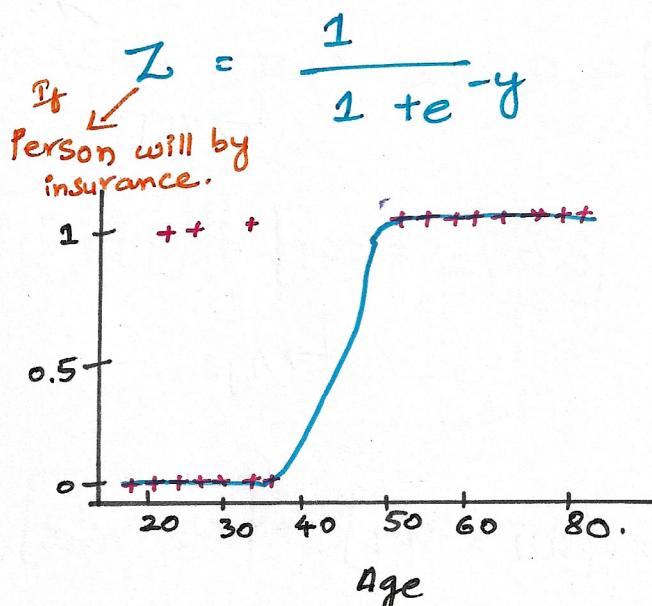
• Sigmoid (-200) =
$$\frac{1}{1 + 2.71^{+200}} = \text{almost close to } 0$$

* Sigmoid function converts input into range $0 \rightarrow 1$.

STEP : 1



Step : 2



$$y = 0.042 * x - 1.53$$

↓ Age.

• Steps :-

$$y = 0.042 * x - 1.53$$

$$Z = \frac{1}{1 + e^{-y}}$$

- value < 0.5 = Person will not buy
- value > 0.5 = Person will buy insurance.

Age = 35

$$y = 0.042 * 35 - 1.53$$

$$= -0.06$$

$$Z = \frac{1}{1 + 2.71}^{0.06}$$

$$= 0.48 \rightarrow 0.48$$

Age = 43

$$y = 0.042 * 43 - 1.53$$

$$= 0.216$$

$$Z = \frac{1}{1 + 2.71}^{-0.216}$$

$$= 0.568 \rightarrow 0.57$$

$$y = 0.042 * x - 1.53$$

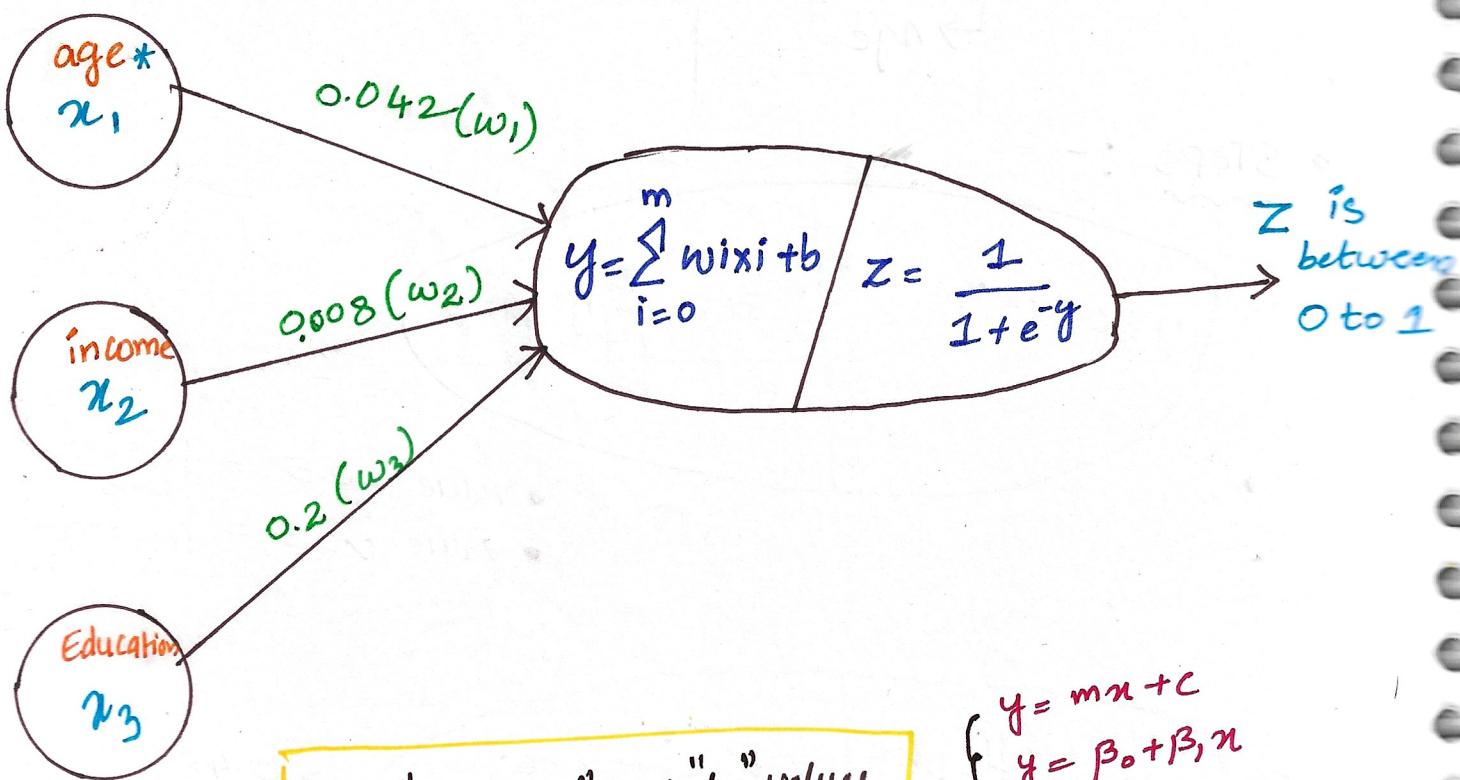
$\hookrightarrow \text{age}$

$$y = [0.042 * x_1] + [0.008 * x_2] + [0.2 * x_3] - 1.53$$

$\hookrightarrow \text{Age}$ $\hookrightarrow \text{income}$ $\hookrightarrow \text{Education}$

$$y = [w_1 * x_1] + [w_2 * x_2] + [w_3 * x_3] + b$$

$$y = \sum_{i=0}^m w_i x^i + b$$



* "weights" and "b" values

can be
+ve, -ve

$$\begin{cases} y = mx + c \\ y = \beta_0 + \beta_1 x \\ y = w_i x_i + b \end{cases}$$

all are same (but change in notation)

Ex:-

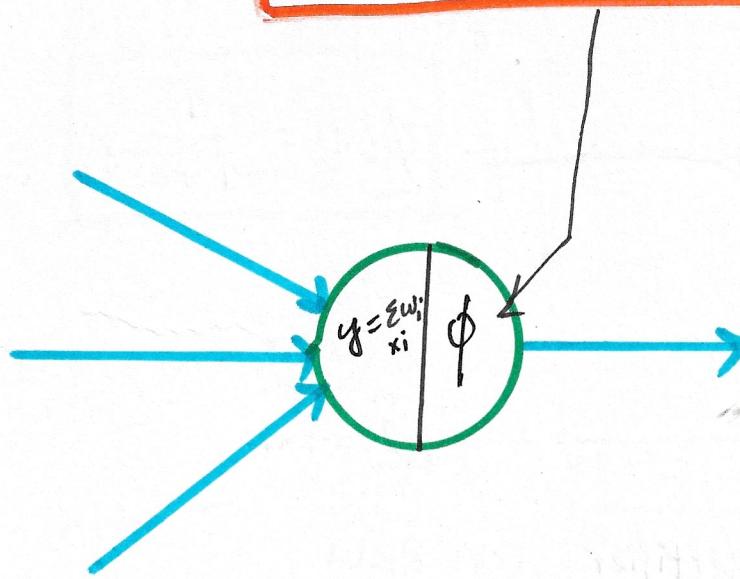
x	y
1	7
2	17
3	27
4	37
5	47

$$\therefore y = 10x - 3$$

$$= [w, x_1 + b] \rightarrow \\ = 10[x] + [-3]$$

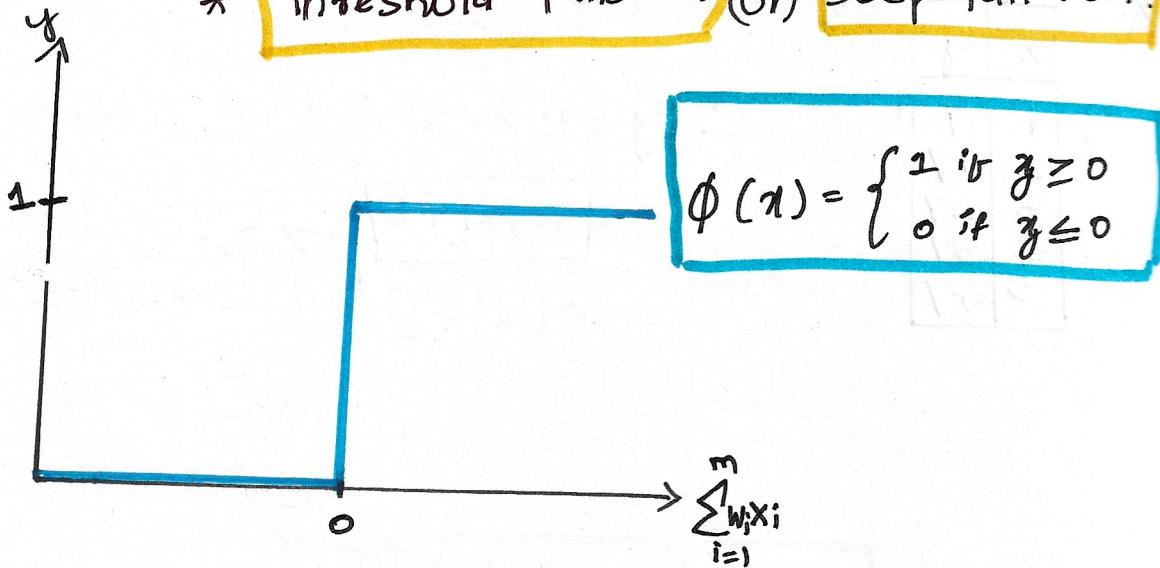
w, b
can be (+ve) or (-ve)

Activation function

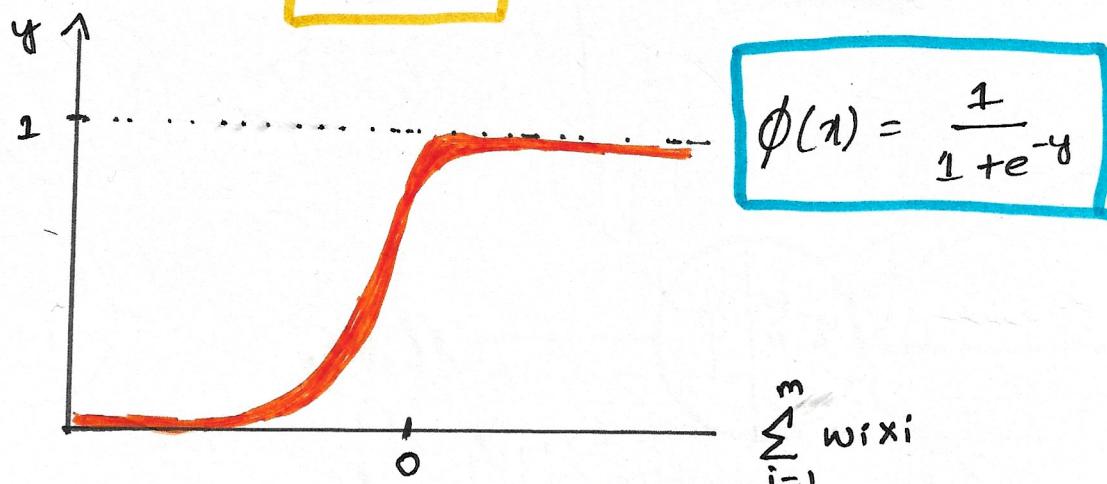


1. Threshold Function (or) step functions
2. sigmoid Function
3. rectifier (or) relu.
4. Hyperbolic Tangent (tanh)

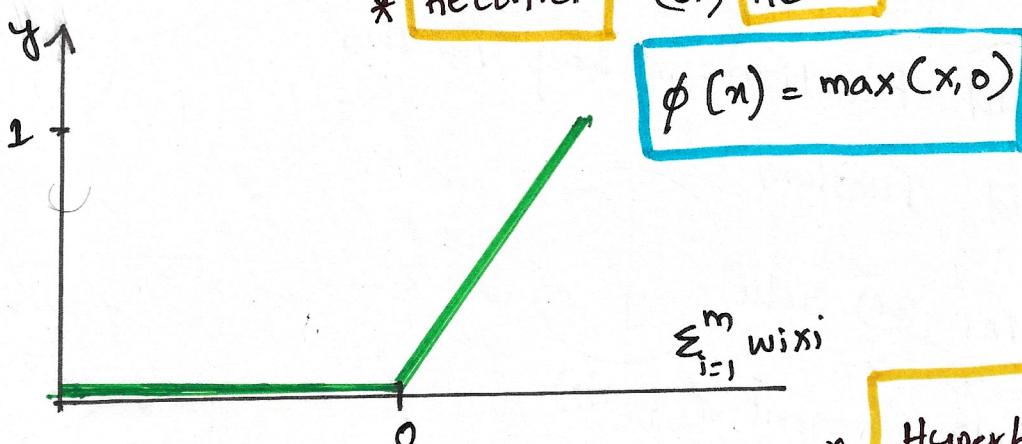
* Threshold function (or) Step function.



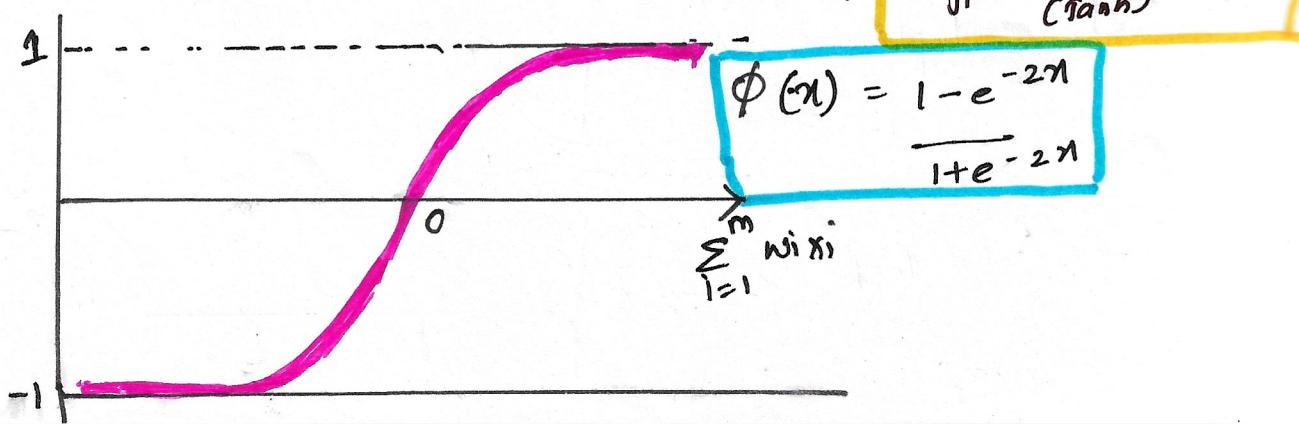
* Sigmoid



* Rectifier
(or) Relu



* Hyperbolic Tangent (Tanh)



* Threshold function (or) Step function

$$\phi(x) = \begin{cases} 1 & \text{if } y \geq 0 \\ 0 & \text{if } y \leq 0 \end{cases}$$

* Sigmoid function

$$\phi(x) = \frac{1}{1+e^{-x}}$$

$$\Rightarrow \frac{e^x}{1+e^x}$$

* Rectifier (or) Relu

• Relu = Rectifier Linear Unit.

$$\phi(x) = \max(x, 0)$$

* Tanh (or) hyperbolic Tangent

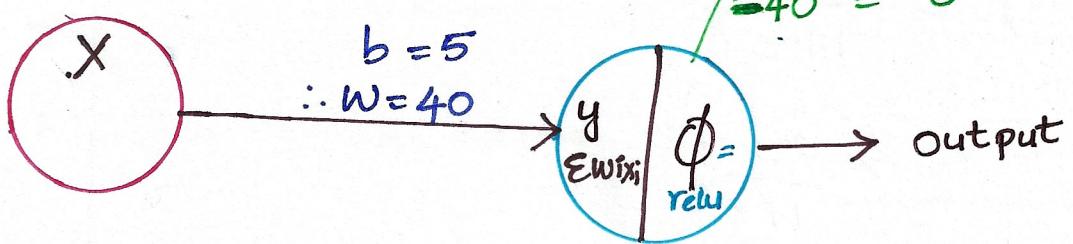
$$\phi(x) = \frac{1-e^{-2x}}{1+e^{-2x}}$$

Ex:- Regression \rightarrow Relu

x	y	\hat{y}	$y - \hat{y}$
1	11	45	-
2	12	85	-
3	13	125	-
4	14	165	-
5	15	205	-

$$\mathcal{E}(y - \hat{y})^2 = -$$

$$\begin{aligned}\hat{y} &= 45 \\ &= 0\end{aligned}$$

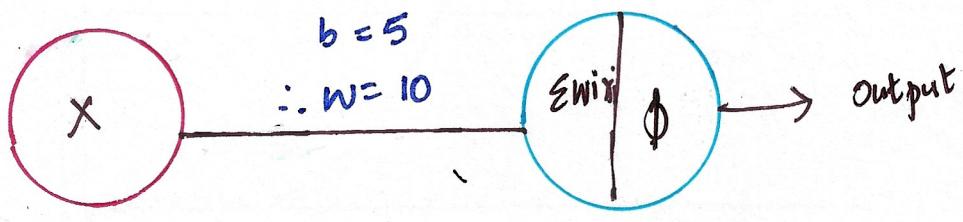
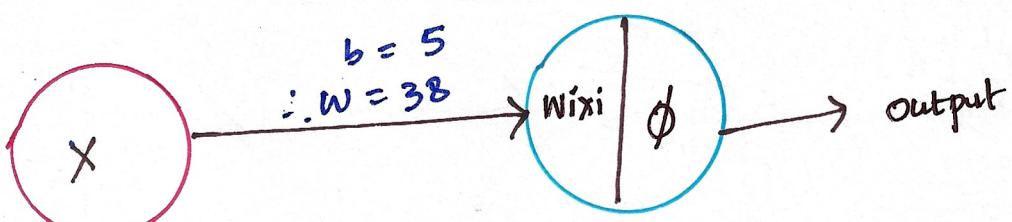
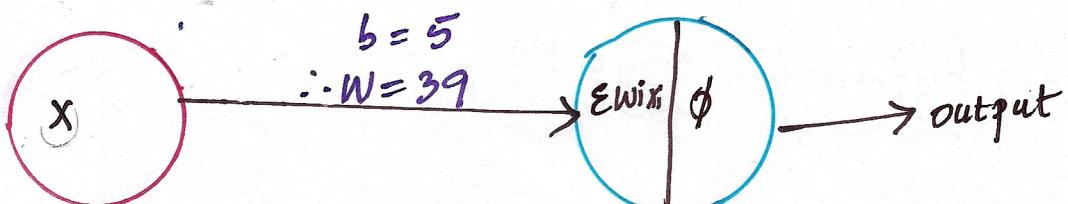


$$\therefore \hat{y} = w\pi + b$$

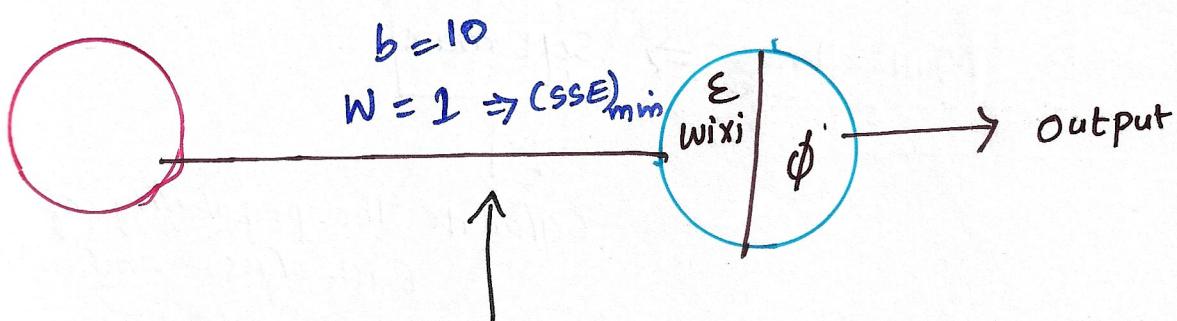
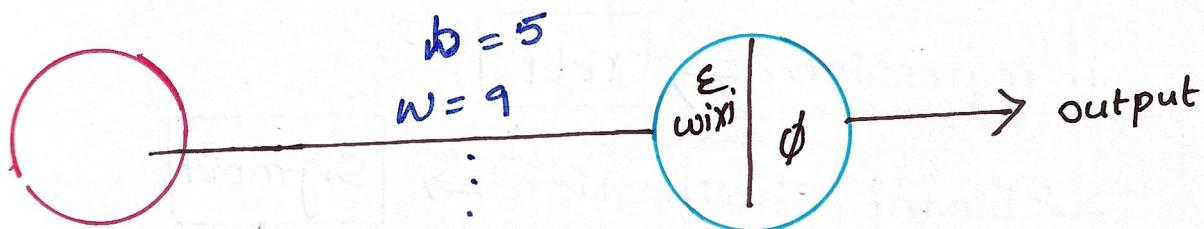
$$x=1, \hat{y} = 40(1) + 5 = 45$$

$$x=2, \hat{y} = 40(2) + 5 = 85$$

* **adjusting weights**



* after that it changes "bias" $\Rightarrow b$



$$\therefore y = wx + b$$

$$\Rightarrow y = 1(x) + 10$$

iterations :- try & errors [loop] ^{apply}
For better answer.

important Points

- no. of **input** Neurons = no. of input features.

- no. of **Output** Neurons = • Regression :- 1
• binary class :- 1

- Multiclass :- no. of categories

* Activation function of Output Neuron :

1. regression \Rightarrow Relu
2. binary classification \Rightarrow Sigmoid
3. Multiclass \Rightarrow Softmax

calculate the probability of each class. and which of them having highest probability we consider into that class.

DT:- 9/05/22
Rufy
09/05/22
5:30pm.

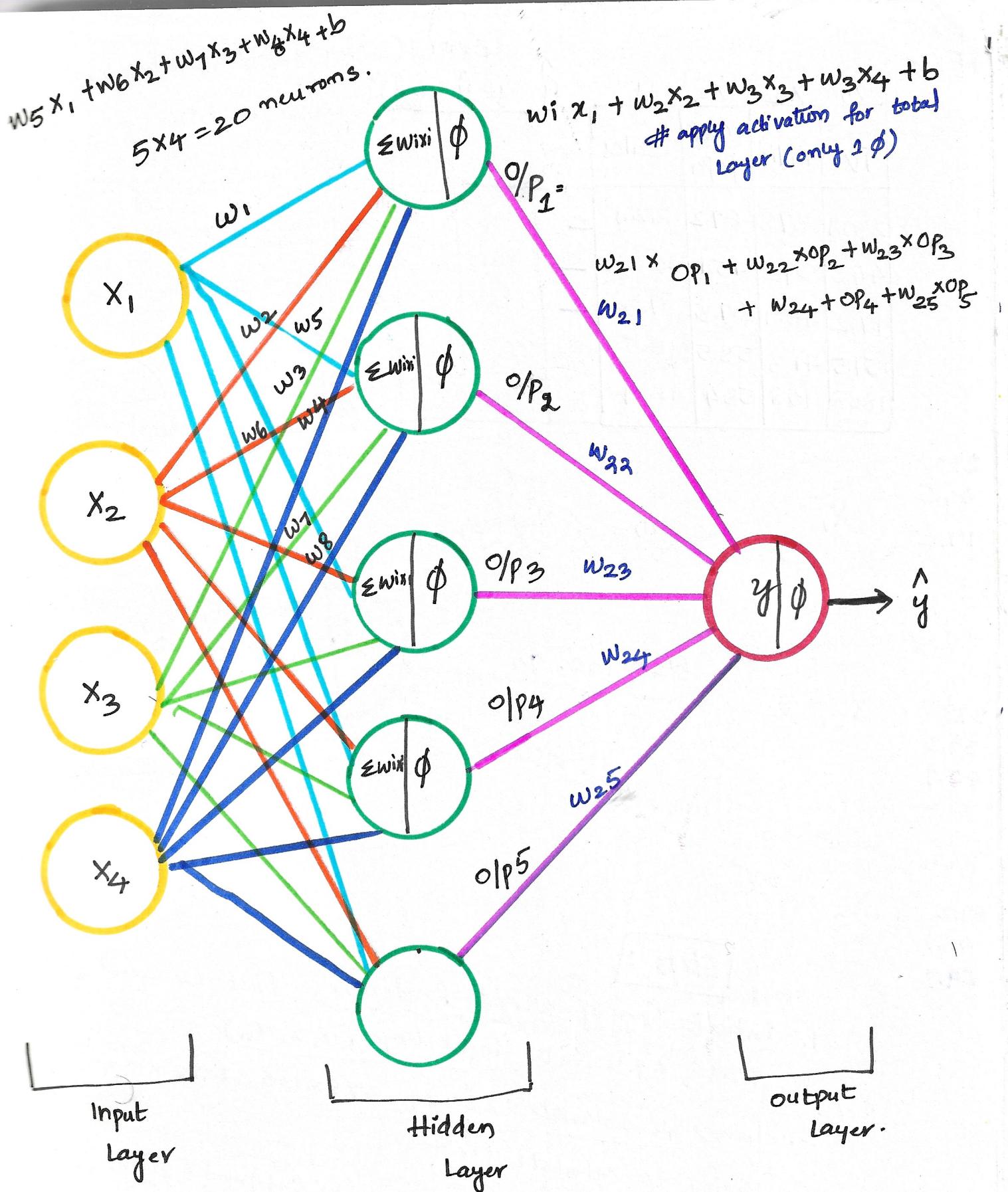
Ex :- drug(x), drug(y), drug(z)

$P(\text{drug } x)$
 $\text{prob}(\text{drug } y)$
 $\text{prob}(\text{drug } z)$] highest

How do neural network work ?

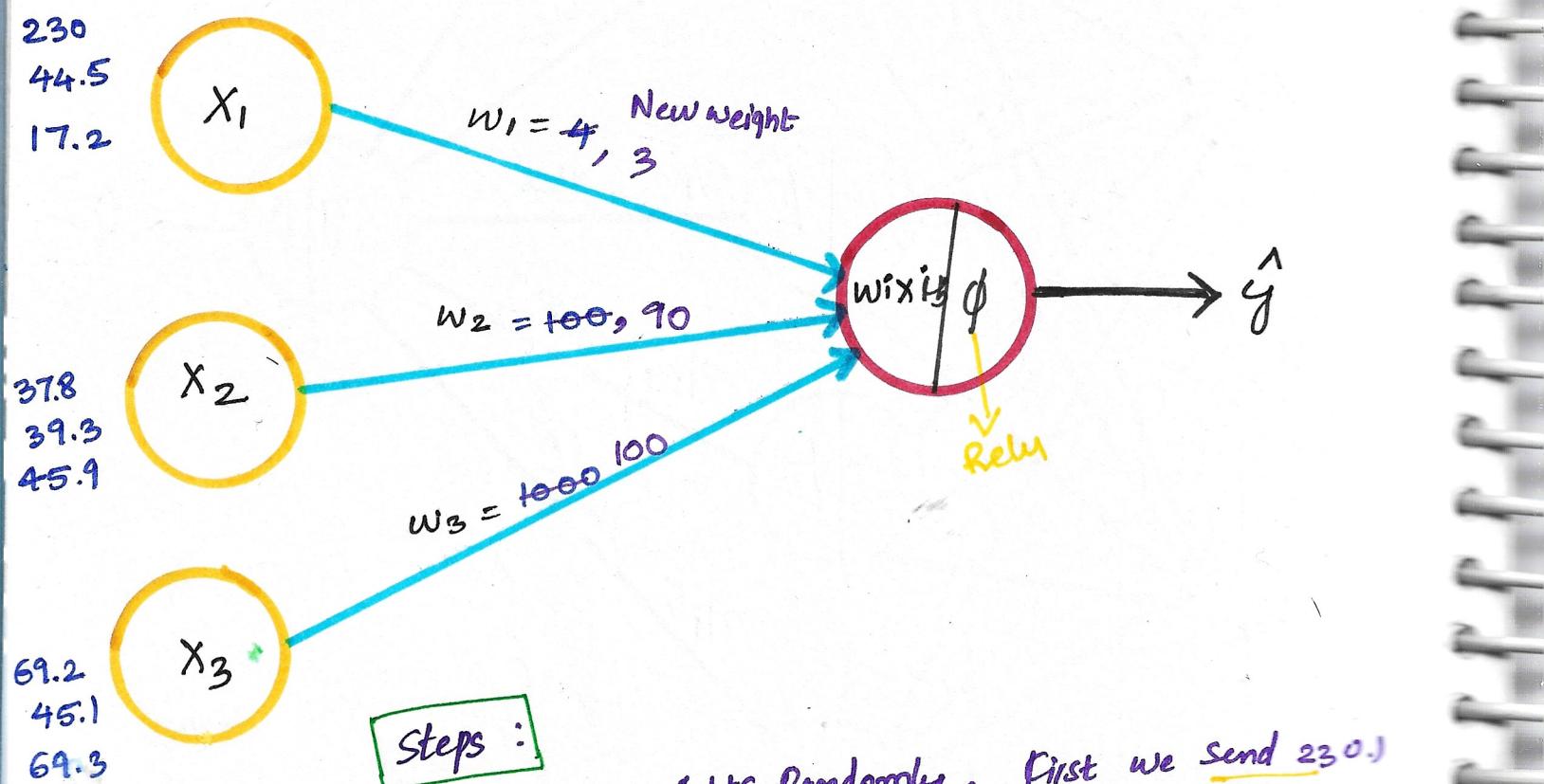
We can Take as per choice, Hidden Layers.
in Neural network

and same hidden layers, we can Take as many as no. of neurons in the neural network.



Ex:-

	X_1	X_2	X_3	y	\hat{y}	Error $(y - \hat{y})^2$
TV	Radio	news paper	Sales			
230.1	37.8	69.2	22.1	—		
44.5	39.3	45.1	10.4	—		
17.2	45.9	69.3	9.3	—		
151.5	41.3	58.5	18.5			
180.8	10.8	58.4	12.9			



Steps :

1. Initialization of weights Randomly, First we send 230, 37.8, 69.2 into input layer (x_1, x_2, x_3) with weight $230 \times 4, 37.8 \times 100, 69.2 \times 1000$ and
2. Then, we calculate $230 \times 4, 37.8 \times 100, 69.2 \times 1000$ and going to calculate (\hat{y}) .
3. In the neuron, we calculate $(w_i x_i + b)$ and $(\phi)(ReLU)$ and output is predicted (\hat{y}) .
4. Similarly same as first, we continue with all data. --
5. Then, it calculate Error $(y - \hat{y})^2$
6. After that, it calculate $(y - \hat{y})^2$ (predicted - Actual)².

7. at last, we want $(SSE)_{\min}$.

8. In order to reduce Error, the weights will recapdate To 3, 90, 100

9. again, it will do some pattern, in loop. (In forward & Backward).

10. Finally it make weights such that, it gives $(SSE)_{\min}$. till that, it process.

Ex:-

clear Example of updating weights

$$2x + 5 = 8$$

$$\begin{array}{c} \hat{y} \\ | \\ y \end{array} \quad \begin{array}{c} y \\ | \\ 8 \end{array} \quad \begin{array}{c} \hat{y} \\ | \\ y - \hat{y} \end{array}$$

$$x = 100$$

$$2(100) + 5 = 205 \quad 8 \quad -197$$

$$x = 105$$

As "x" value increasing, Error also increasing.
so, we decrease "x".

$$2(105) + 5 = 215 \quad 8 \quad -207$$

$$x = 95$$

$$2(95) + 5 = 195 \quad 8 \quad -187$$

as "x" value decreasing, Error also decreasing.

$$\frac{dx}{\Delta x} = 5 \quad (\text{change in } x = 5)$$

$$x = 90$$

$$x = 85$$

$$x = 80$$

:

$$x = 5$$

$$x = 0$$

$$\begin{aligned} x &= 1 \\ x &= 2 \\ x &= 1.5 \end{aligned}$$

$$2(5) + 5 = 15 \quad 8 \quad -7$$

$$2(0) + 5 = 5 \quad 8 \quad 3$$

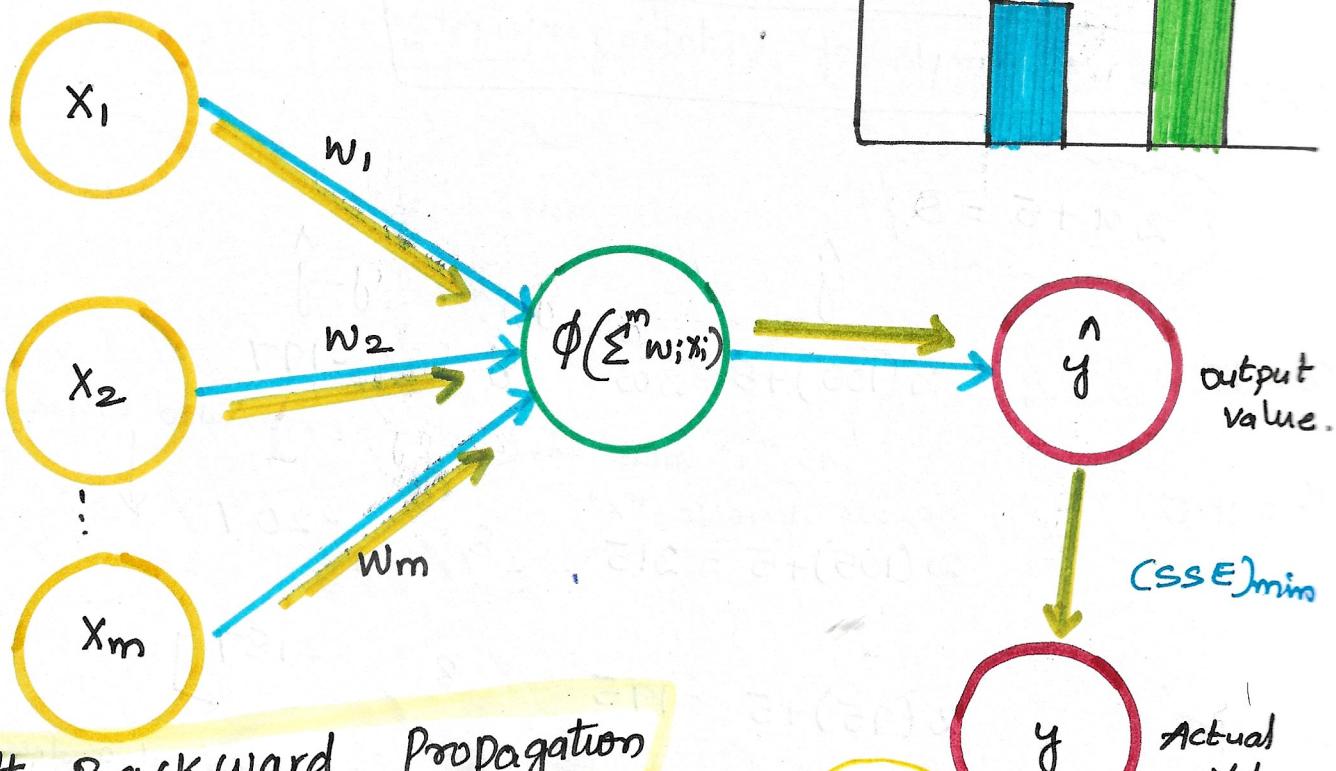
so, The Error is in between -5 & 3

We updated:
till we get minimum value

How do neural networks Learn ?

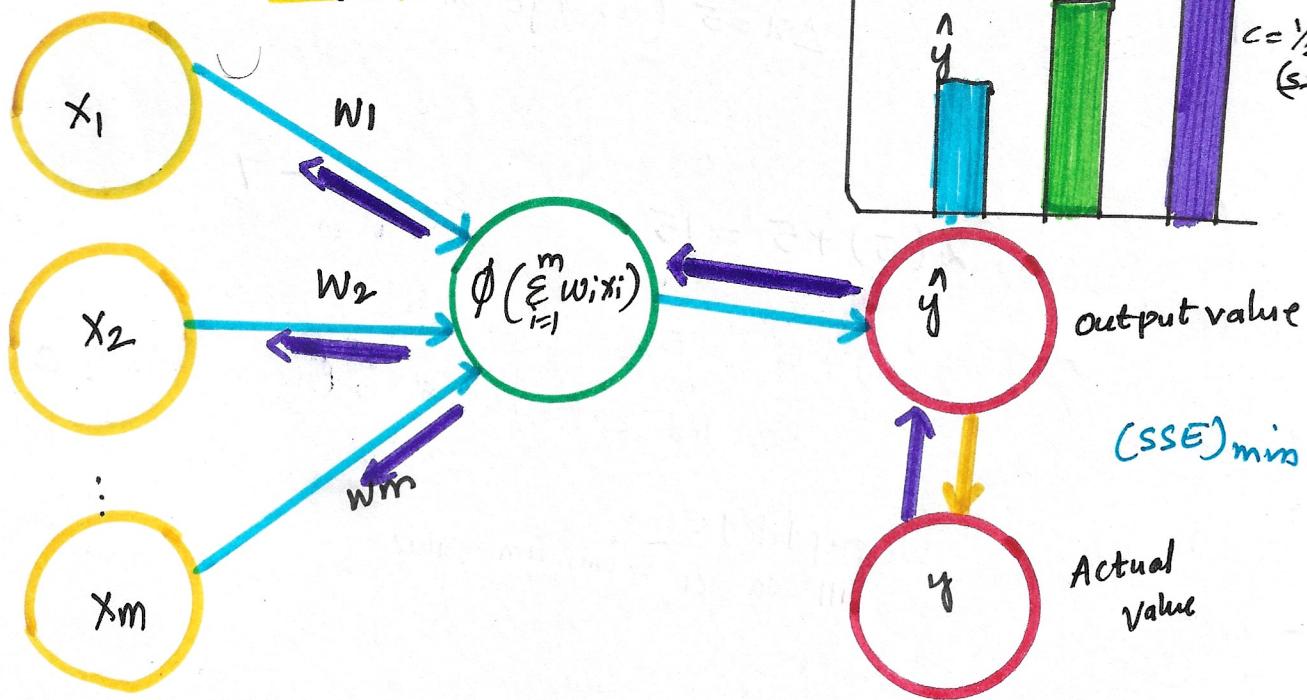
Neural networks learn based on connections.

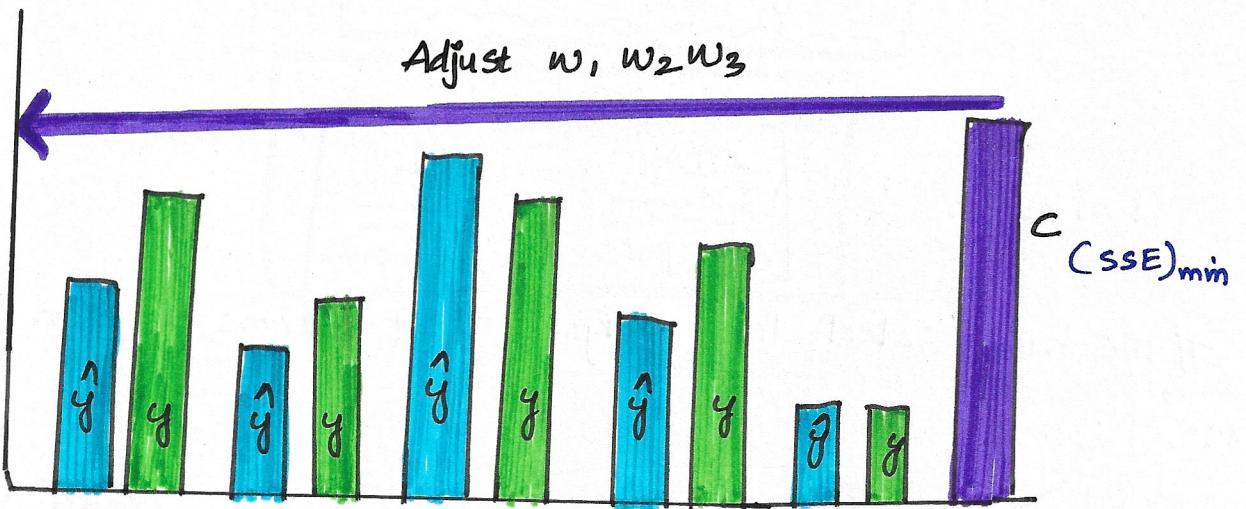
Forward propagation



Backward Propagation

For minimum Error, we have to update weights.





forward propagation :

First, calculating $\sum w_i x_i + b$ and calculating the output variable in the forward direction is known as forward propagation.

backward propagation :

Adjusting (or) updating the weights, coming backward direction is known as backward propagation. initially, weights are assigned randomly, and from that we update weights. The weights will be updated in a way that $(SSE)_{\min}$

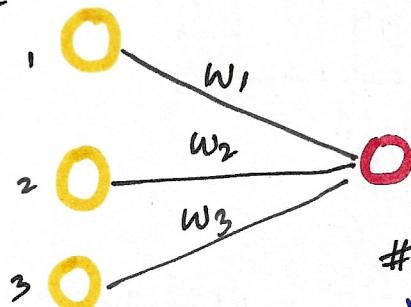
Weight initialization

1. Uniform

$$= \left[\frac{-1}{\sqrt{\text{inputs}}}, \frac{+1}{\sqrt{\text{inputs}}} \right]$$

we have select the weights, that forms, uniform distribution.

Ex:-

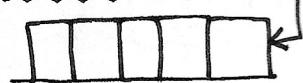


$$\left[\frac{-1}{\sqrt{3}}, \frac{+1}{\sqrt{3}} \right]$$

Backend code.
np.random.uniform()

we have select values
in these Only.

These weights should form
uniform distribution.



2. Xavier Uniform

$$U \left[-\sqrt{\frac{6}{\text{intout}}}, +\sqrt{\frac{6}{\text{intout}}} \right]$$

Xavier normal

$$N \left[0, \sqrt{\frac{2}{\text{intout}}} \right]$$

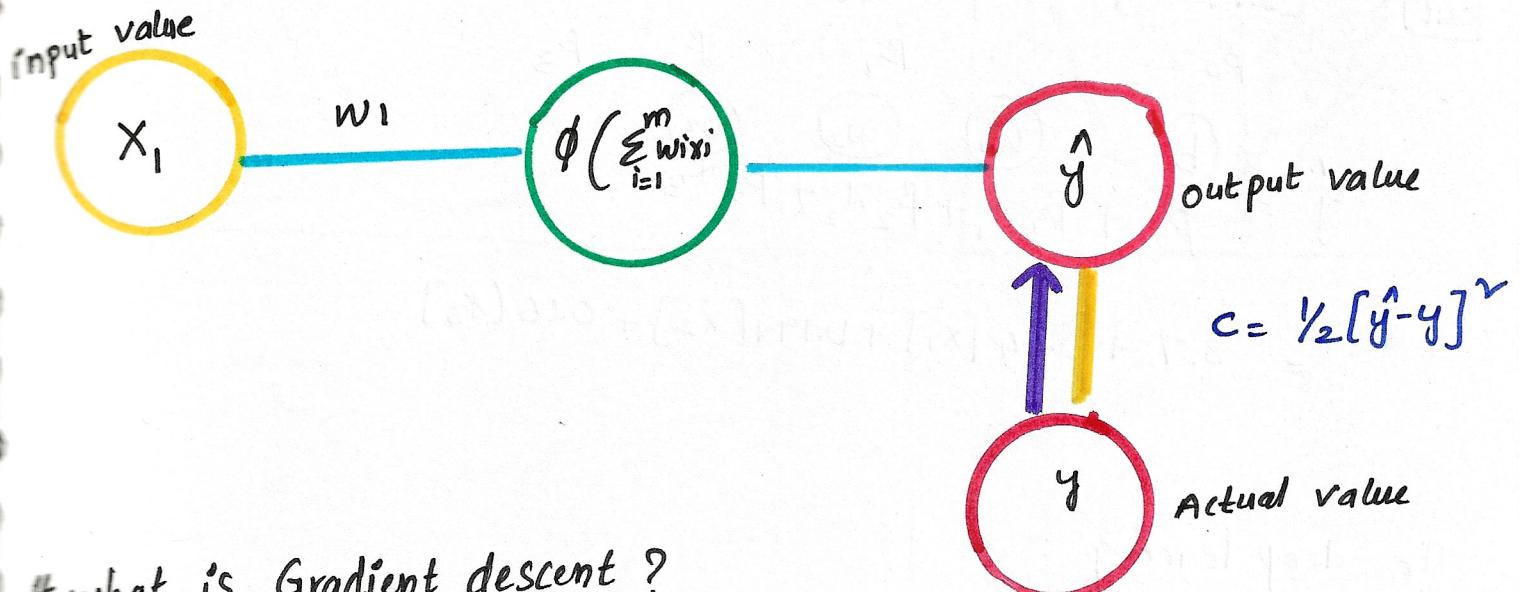
He - int Uniform

$$U \left[-\sqrt{\frac{6}{\text{in}}}, +\sqrt{\frac{6}{\text{in}}} \right]$$

He - int normal

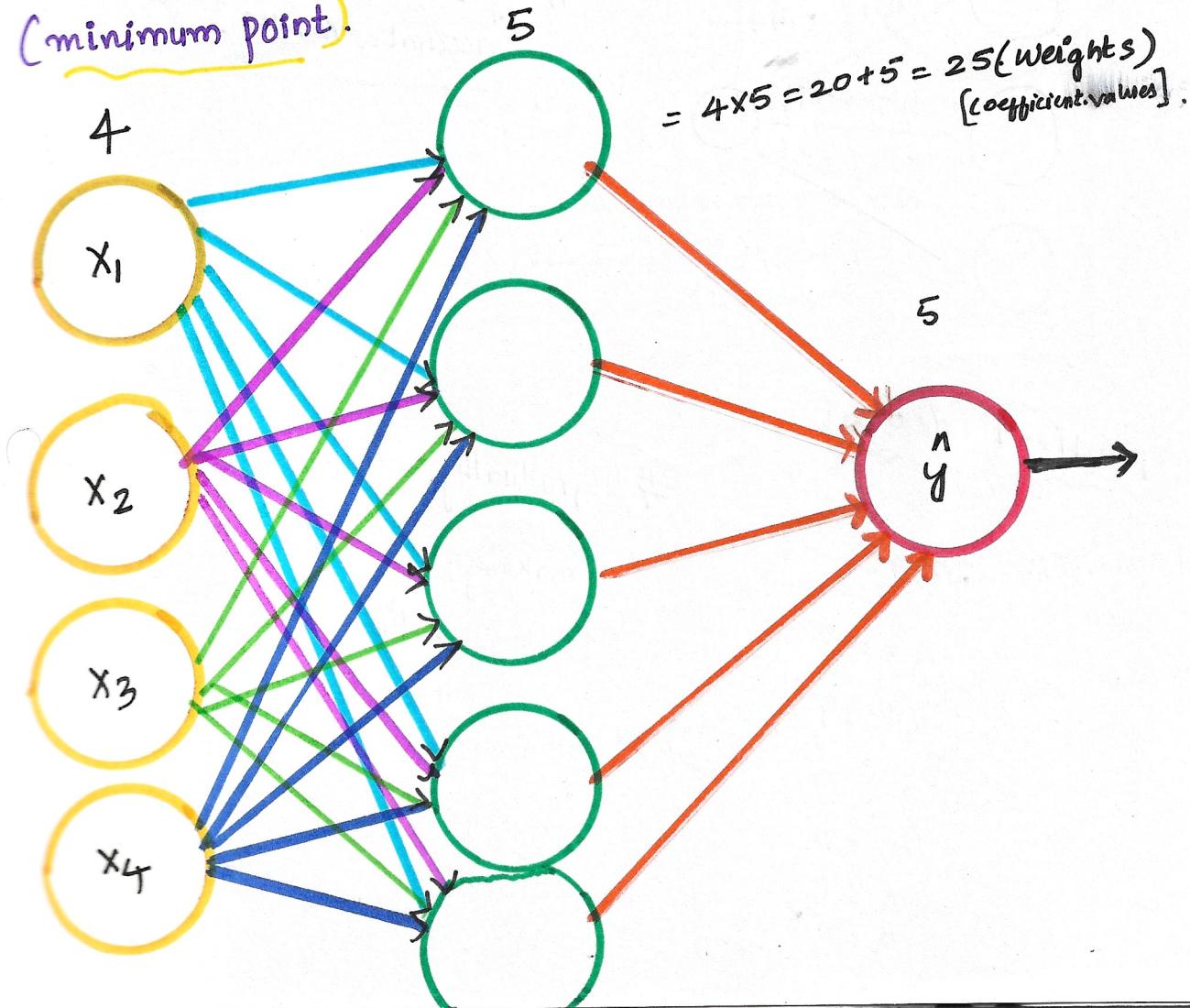
$$N \left[0, \sqrt{\frac{2}{\text{int}}} \right]$$

Gradient Descent



what is Gradient descent ?

Gradually decreasing and identifying the Local minima
(minimum point).



In machine learning:

Ex:- In multiple, linear regression

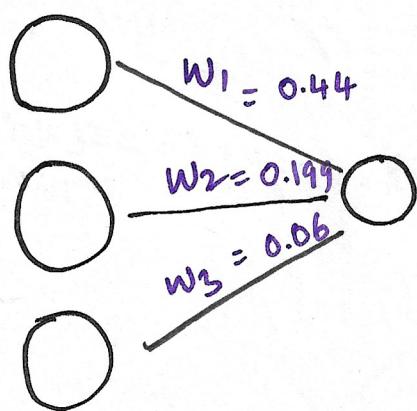
model.intercept — , model.coef —

[out]: (2.708), array (0.44, 0.199, 0.006)
 $\beta_0 \quad \beta_1 \quad \beta_2 \quad \beta_3$

$$\hat{y} = b + w_1 x_1 + w_2 x_2 + w_3 x_3$$

$$= 2.7 + 0.44[x_1] + 0.199[x_2] + 0.06[x_3]$$

In deep learning:



By Using this Technique, it gives
"accurate results".

Gradient descent

$$\text{Ex:- } 2x + 5 = 8$$

$$x = 100$$

$$x = 99$$

:

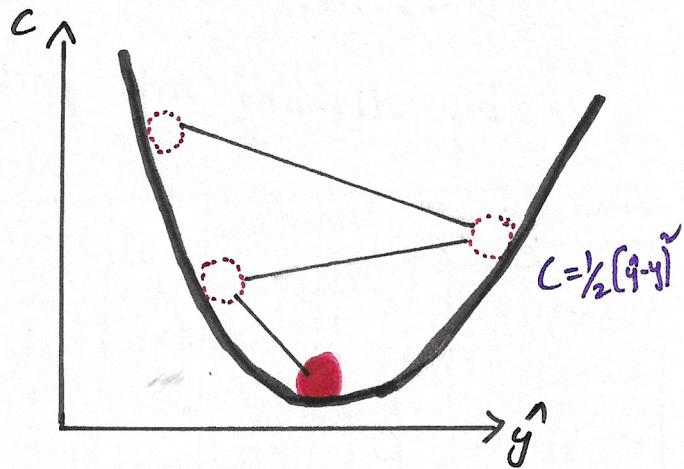
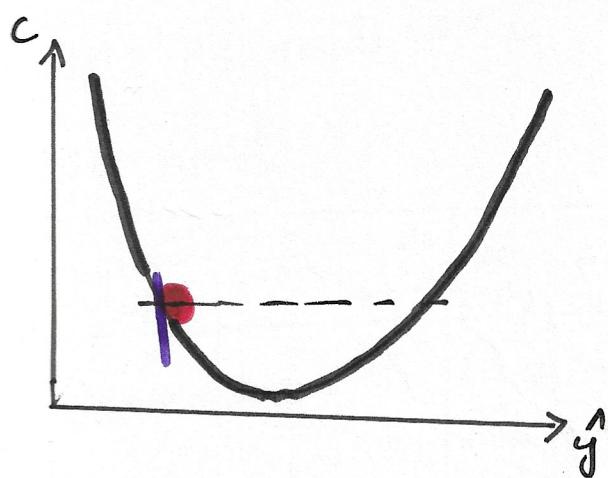
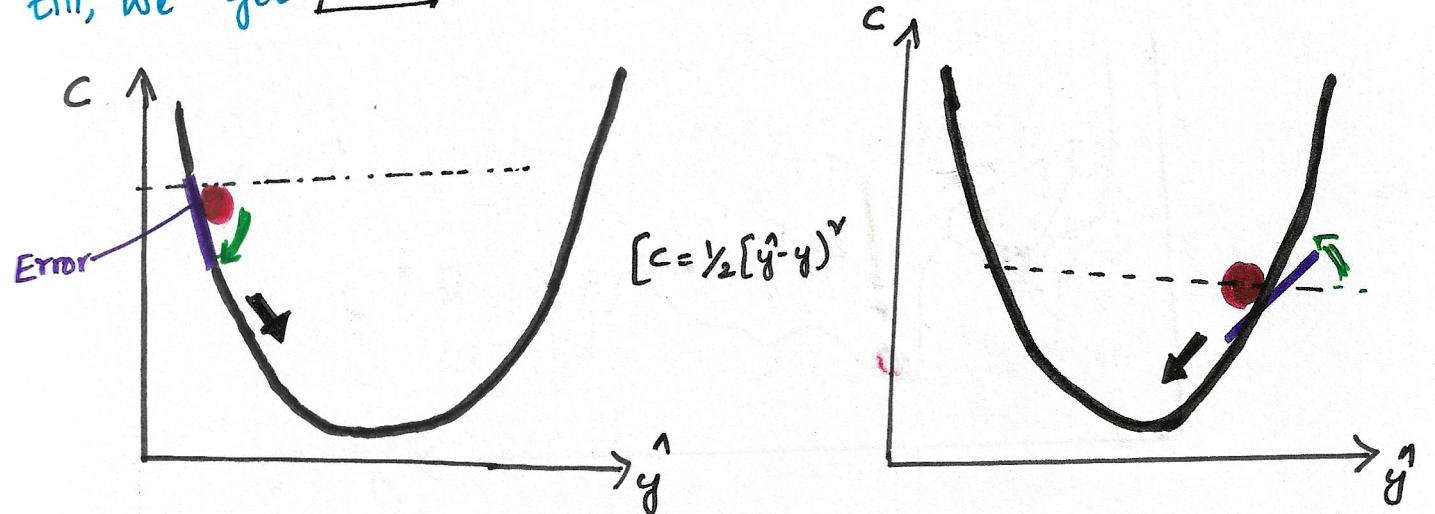
$$x = 0$$

$$x = 1$$

$$x = 1.5$$

Gradually reducing weights. and
making Error as minimum
Value.

By applying different "x" values and identifying the "perfect "x" value till, we get error as "0" \Rightarrow gradient decent



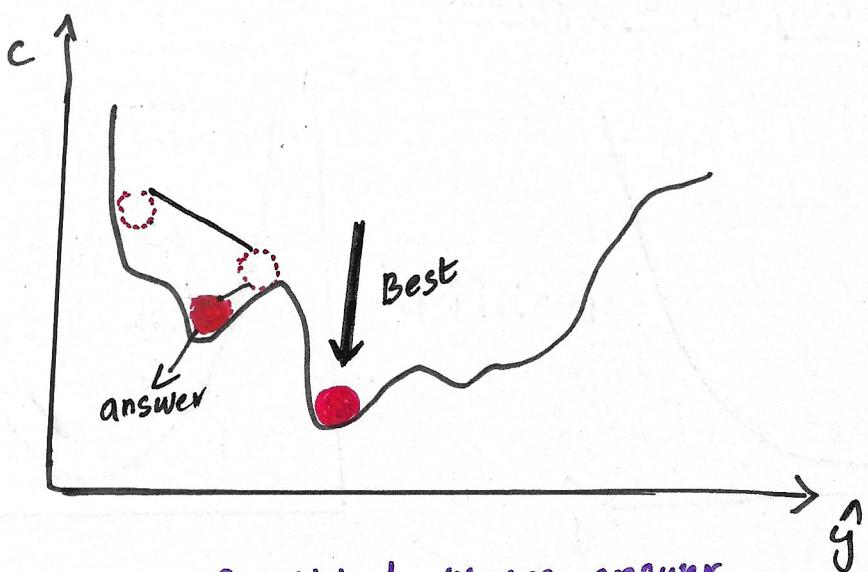
Stochastic Gradient Descent

- * Local minima

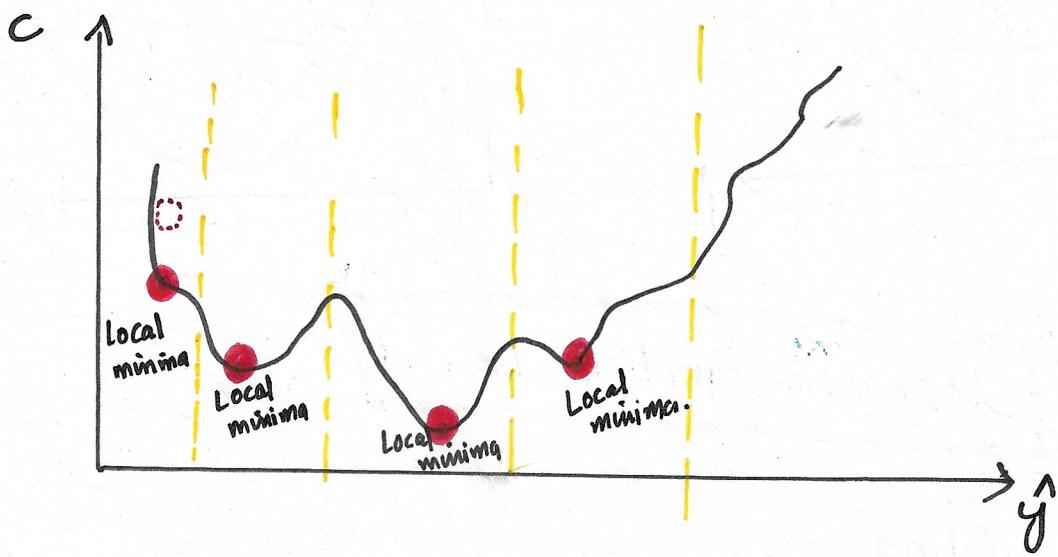
- * Global minima

EX:- • Every state 1^{st} ranker (local minima)

• All india ranker 1^{st} ranker (global minima)



Here, we predicted wrong answer,
But, there is another curve. So, how we find that?
by dividing into parts.



Identifying the Global minima is called
"Stochastic Gradient Descent"

Entire data we divide into parts (or) batches. Each part
We are identifying the "Local minima" and from
that overall identify "Global minima".
↓
"Error".

~~09/05/22
10:00pm~~

Dt: 10/5/22
10:00 AM

ANN - Classification backend.

Code :- on Tensorflow, Keras.

Tensorflow, CNTKs, theano
Google Microsoft Facebook

PIP install tensorflow
PIP install keras

```
import numpy as np  
import pandas as pd  
import tensorflow as tf  
import keras
```

from tensorflow import keras.

df = pd.read_csv ("churn-modelling.csv")

df.head()

Row no.	customer id	Surname	Credit Score	Geo graphy	Gender	Age	Tenure	Balance	num of Products	Has card	is active member	Estimated Salary
1	1563469	Hargrave	619	France	Female	42	2	0.00	1	1	1	101348
2	15647311	Hill	608	Spain	Female	41	1	83807	1	0	1	112542
3	15619304	Onio	502	France	Female	42	8	159660	3	1	0	113931.5
4	15101354	Bonni	699	France	Female	39	1	0.00	2	0	0	93826.63
5	15137889	Mitchell	850	Spain	female	43	2	125510	1	1	1	79084.10

df.info()

[out]: RangeIndex : 10000 entries , 0 to 9999

Nonnull columns

Dtype.

Data columns.

int64

-0- Row number

10000 Non null

+ Customer id

1000 Non null

int64

0	3. Credit score	10000 non null	int64
1	2. Surname	10000 non null	Object
categorical data	4. Geography	10000 non-null	object] Convert to object numeric
2	5. Gender	"	int64
3	6. Age	"	int64
4	7. Tenure	"	float64
5	8. Balance	"	int64
6	9. No. of Products	"	int64
7	10. HasCrCard	"	int64
8	11. Is Active member	"	int64
9	12. Estimated Salary	"	float64
10	13. Exited	"	int64

we can use drop function also [x & y]

$x = df.iloc[:, 3:13].values$

$y = df.iloc[:, 13].values$

$\begin{matrix} : \downarrow & 3:13 & C:13 \\ \text{all} & 3, 12 & \downarrow \\ & \text{only} & 13 \text{ column} \end{matrix}$

$x.shape$

[Out]: (10000, 10)

$y.shape$

[Out]: (10000,)

Original Data

13 input —> 3 drop (row no.
customer id, surname)
10 inputs —> 1 column

natural
ordinal data (sequence)

encoding [Categorical data]

from sklearn.preprocessing import

Label Encoder

$x[:, 2]$

[Out]: array(['Female', 'Female', ... 'male', 'Female']).

```
# label encoder = LabelEncoder()
# x[:, 2] = labelencoder.fit_transform(x[:, 2])
# changed to numerical.
# x[:, 2]
out: array [0, 0, 0, ..., 0, 1, 0]

# one hot encoding (nominal data = Geography (column)) # we can use get-dummies.
from sklearn.preprocessing import OneHotEncoder
from sklearn.compose import ColumnTransformer
** from sklearn.compose import ColumnTransformer
    L transforms data.

# x[:, 1]
out: array ([ "France", "Spain", "France", ..., "France", "Germany" ]).
    dtype=object.

# ct = ColumnTransformer([["encoder", OneHotEncoder(), [1]],
#                         remainder = "passthrough")
# x = np.array(ct.fit_transform(x))

# changed to numerical
# x[:, 1]
out: array ([0.0, 0.0, 0.0, ..., 0.0, 1.0, 0.0]).
```

train-test

```
from sklearn.model_selection import train_test_split
```

```
# n_train, n-test, y-train, y-test = train-test-split (x, y,  
test_size=0.2, random_state=29)
```

Shape.

```
# x-train.shape, x-test.shape, y-train.shape, y-test.shape.
```

```
[Out]: (8000, 12), (2000, 12), (8000), (2000,)
```

↳ after applying dummies it converts into 12 columns.

Scaling

```
from sklearn.preprocessing import StandardScaler
```

```
# sc = StandardScaler()
```

```
# x-train = sc.fit_transform(x-train)
```

```
# x-test = sc.fit_transform(x-test)
```

MODELLING

initializing The ANN

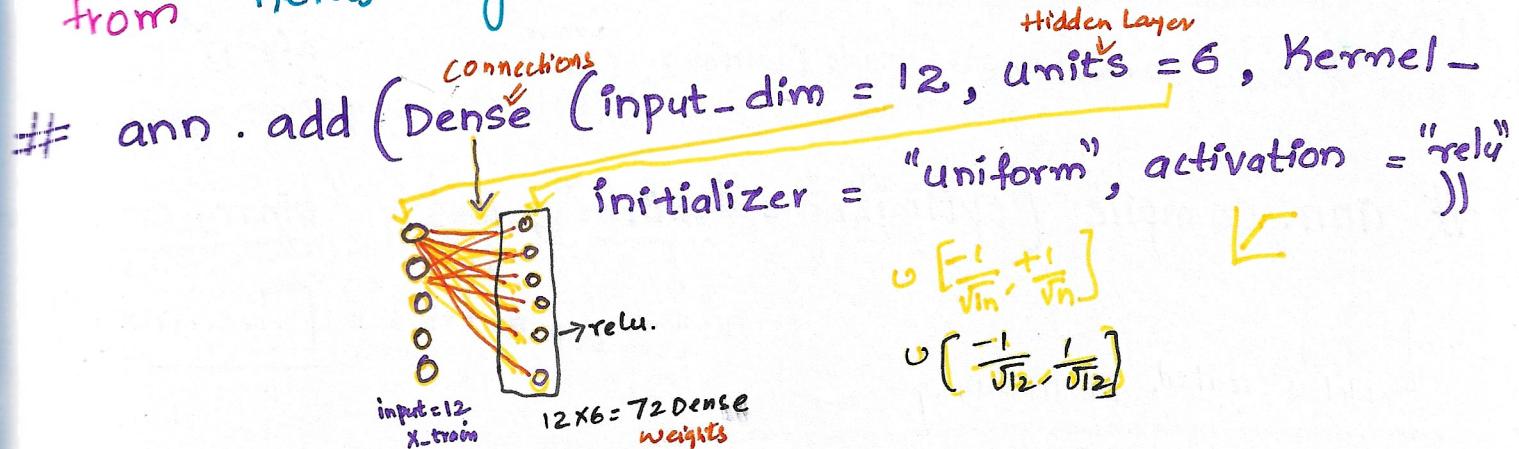
```
from keras.models import Sequential
```

```
# ann = Sequential()
```

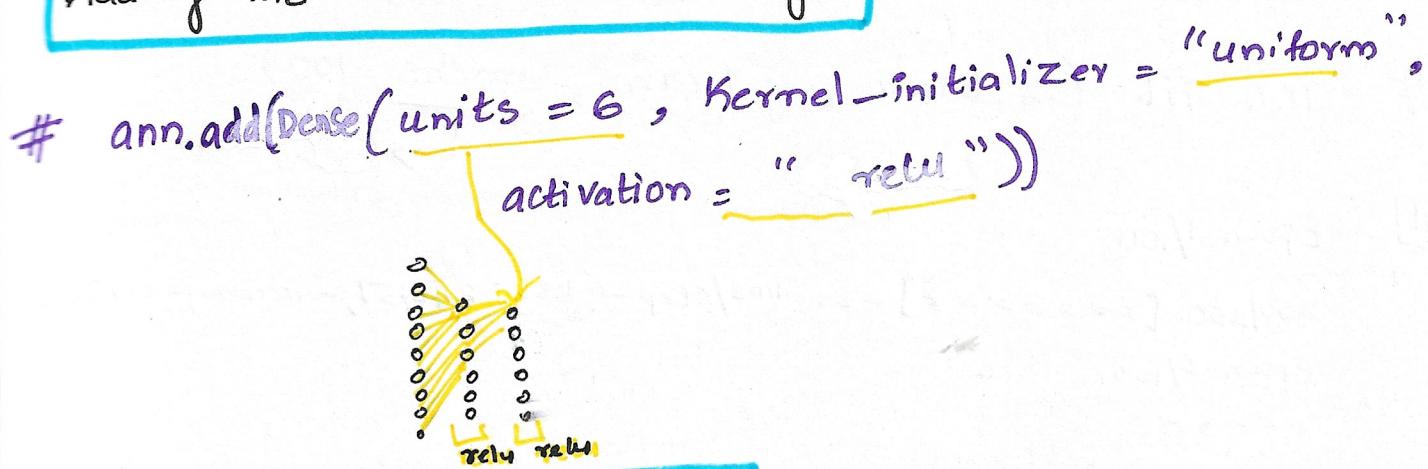


Adding The input Layer and first hidden Layer.

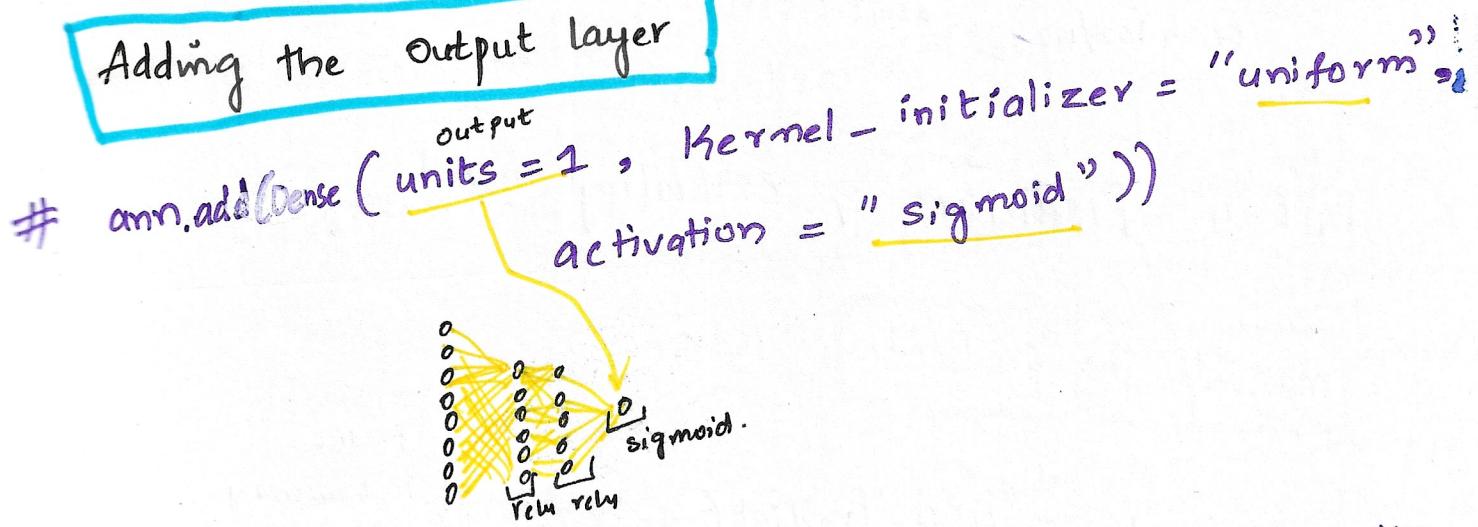
from Keras.layers import Dense.



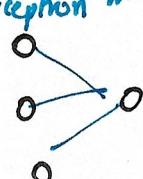
Adding the second hidden Layer.



Adding the output layer



Ex:- Perception model.



(ann.add(Dense(input_dim = 3, units = 1, Kernel_initializer = "uniform", activation = "relu")))

Part-3 Training the ANN

Compiling the ANN

past: Connection is made (wiring), current
EX: $E(y - \hat{y})^2$
regression = "mean_squared_error"

ann.compile (optimizer = "adam", loss = "binary_Crossentropy",
Gradient descent, metrics = ["accuracy"])

↑ model is created, fit the data ↓

training the ANN on training Set

ann.fit (x-train, y-train, epochs = 100)
no. of iteration.
(backward, forward directions)

Out

Epoch 1/100

250/250 [=====] - 2s 1ms/step - loss: 0.6657, accuracy: 0.7830

Epoch 2/100

.....

.....

Epoch 100/100 acc: 0.838

Part-4 Predictions & Evaluating model

making the predictions

y-Pred = ann.Predict(x-test) # Test accuracy.

$y_{\text{Pred}} = (\hat{y}_{\text{Pred}} > 0.5)$

Predict

Evaluating the model

```
from sklearn.metrics import Confusion_matrix, accuracy_score  
# print ("Test Accuracy:", accuracy_score(y-test, y-Pred))  
# Confusion-matrix (y-test, y-Pred)  
[ut]: Test accuracy : 08455  
array([[ 1536,  59  
       [ 250, 155]]])
```

Cross validate the model

```
# user defined function.  
def build_cross_classifier():  
    ann (or) anything we can use input layer  
    classifier = Sequential()  
    classifier.add(Dense(input_dim=12, units=6, kernel_initializer="uniform", activation="relu"))  
    classifier.add(Dense(units=6, kernel_initializer="uniform", activation="relu"))  
    classifier.add(Dense(units=1, kernel_initializer="uniform", activation="sigmoid"))  
    classifier.compile(optimizer="adam", loss="binary_crossentropy", metrics=["Accuracy"])  
    return classifier
```

classifier

```
from Keras.wrappers.Scikit_Learn import KerasClassifier
```

```
# classifier = KerasClassifier (build_fn = build_cross_classifier)
```

User defined function

, batch_size = 10 , epochs = 100

if stochastic descent
batch

iterations

Cross-validation

```
from sklearn.model_selection import cross_val_score
```

```
# accuracies = cross_val_score (estimator = classifier ,  
X = x_train , y = y_train , cv=5)
```

out : Epoch 1/100

640/640 [=====] - 1s 605us/step - loss: 0.4922, - acc: 0.7997

Epoch 2/100

640/640 [=====] - 0s 617us/step - loss: 0.4296, - acc: 0.8003

- - - - -

- - - - -

- - - - -

- - - - -

Epoch 100/100

640/640 [=====] 1s 885us/step - loss: 0.4003, - acc: 0.8342

160/160 [=====] 0s 666us/step - loss: 0.4110, - acc: 0.8375]

```
# print(accuracies)
```

```
# accuracies.mean()
```

(0.8237, 0.8343, 0.8362, 0.8362, 0.8374)

out
0.83362

⇒ Hyperparameter Tuning

Part-5 - Improving and Tuning the ANN

This can be done by 3 options

1. Hyperparameter tuning

2. Regularization (L_1 & L_2) to reduce overfitting if needed (for regression problems)

3. Dropout

Hyperparameter tuning can be done for identifying no. of hidden layers & no. of neurons in each hidden layer.

- Layers = $[[20], [10], [30], [40]] \rightarrow$ 1 hidden layer with different options of no. of neurons in hidden layer
- Layers = $[[20], [40, 20], [45, 30, 15]] \rightarrow$ Multiple hidden layers with different options of no. of neurons.

Hyperparameter tuning can be done for identifying best activation function for hidden layers.

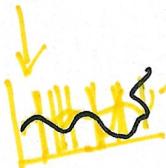
- activations = ["relu", "sigmoid"]

Hyperparameter tuning can be done for identifying optimizers

- Optimizer = ["adam", "rmsprop"]
gradient descent ↴
↳ stochastic gradient descent

Hyper parameter tuning for batchsize for building / training model.

- batch size = [10, 16, 32, 64, 128, 256]



Code: tuning:-

```
def build_classifier(mainoptimizer):  
    classifier = Sequential()  
    classifier.add(Dense(input_dim=12, units=6, kernel_initializer="uniform",  
                         activation="relu"))  
    classifier.add(Dense(units=6, kernel_initializer="uniform",  
                         activation="relu"))  
    classifier.add(Dense(units=1, kernel_initializer="uniform",  
                         activation="sigmoid"))  
    classifier.compile(optimizer=mainoptimizer, loss="binary-  
                           crossentropy", metrics=["accuracy"])  
  
    return classifier  
  
# classifier = KerasClassifier(build_fn=build_classifier)  
# parameters = {"batch_size": [10, 32], "epochs": [50, 100],  
#               "optimizer": ["adam", "rmsprop"]}
```

```
from sklearn.model_selection import GridSearchCV  
# grid = GridSearchCV (estimator = classifier, param_grid =  
# Parameters, scoring = "accuracy", cv=5)  
  
# grid_result = grid.fit (x-train, y-train)  
  
[out]: Epoch 1/100  
200/200 [=====] - os 7110s/step - loss: 0.5877, accu. 0.7997  
Epoch 2/100  
200/200 [=====] - os 630us/step - loss: 0.4592 - acc - 0.8003  
- - - - -  
- - - - -  
- - - - -  
- - - - -  
Epoch 100/100  
200/200 [=====] - os 830us/step - loss: 0.6392, acc - 84]
```

```
# grid_result . best_params -  
[out]: {"batch_size": 32, "epochs": 50, "optimizer": "adam"}
```

best accuracy

grid_result . best_score -

[out]: 0.844125

```
# y-pred = grid_result . predict (x-test)  
# y-pred = (y-Pred > 0.5)
```

accuracy, confusion-matrix

```
from sklearn.metrics import Confusion_matrix, accuracy_score.
```

print ("test accuracy": , accuracy_score(y-test, y-pred))

```
# Confusion_matrix(y-test, y-Pred)
```

[out]: Test accuracy : 0.8405

```
array([[1530, 65]  
[ 254, 151]],
```

✓
10.105122
5:30 PM.