

```
1 import components.naturalnumber.NaturalNumber;
2 import components.naturalnumber.NaturalNumber2;
3 import components.simplewriter.SimpleWriter;
4 import components.simplewriter.SimpleWriter1L;
5
6 /**
7  * Program with implementation of {@code NaturalNumber} secondary operation
8  * {@code root} implemented as static method.
9  *
10 * @author Vaishnavi Kasabwala
11 *
12 */
13 public final class NaturalNumberRoot {
14
15     /**
16      * Private constructor so this utility class cannot be instantiated.
17      */
18     private NaturalNumberRoot() {
19     }
20
21     /**
22      * Updates {@code n} to the {@code r}-th root of its incoming value.
23      *
24      * @param n
25      *         the number whose root to compute
26      * @param r
27      *         root
28      * @updates n
29      * @requires  $r \geq 2$ 
30      * @ensures  $n^r \leq \#n < (n + 1)^r$ 
31      */
32     public static void root(NaturalNumber n, int r) {
33         assert n != null : "Violation of: n is not null";
34         assert r >= 2 : "Violation of: r >= 2";
35
36         NaturalNumber two = new NaturalNumber2(2);
37
38         NaturalNumber low = new NaturalNumber2(0);
39         NaturalNumber high = new NaturalNumber2(n);
40
41         // create the guess variable
42         NaturalNumber guess = new NaturalNumber2(high);
43         guess.add(low);
44         guess.divide(two);
45
46         NaturalNumber temp = new NaturalNumber2(high);
47         temp.power(1 / r);
48
49         while (guess.compareTo(temp) != 0) {
50             //guess
51             guess.copyFrom(high);
52             guess.add(low);
53             guess.divide(two);
54
55             if (guess.compareTo(temp) < 0) {
56                 low.copyFrom(guess);
57             } else
```

```

58         high.copyFrom(guess);
59     }
60 }
61
62 // Update n
63 n.copyFrom(guess);
64 }
65
66 /**
67  * Main method.
68  *
69  * @param args
70  *      the command line arguments
71  */
72 public static void main(String[] args) {
73     SimpleWriter out = new SimpleWriter1L();
74
75     final String[] numbers = { "0", "1", "13", "1024", "189943527", "0",
76                               "1", "13", "4096", "189943527", "0", "1", "13", "1024",
77                               "189943527", "82", "82", "82", "82", "9", "27", "81",
78                               "243", "143489073", "2147483647", "2147483648",
79                               "9223372036854775807", "9223372036854775808",
80                               "618970019642690137449562111",
81                               "162259276829213363391578010288127",
82                               "170141183460469231731687303715884105727" };
83     final int[] roots = { 2, 2, 2, 2, 2, 3, 3, 3, 3, 3, 15, 15, 15, 15, 15,
84                           2, 3, 4, 5, 15, 2, 3, 4, 5, 15, 2, 2, 3, 3, 4, 5, 6 };
85     final String[] results = { "0", "1", "3", "32", "13782", "0", "1", "2",
86                               "16", "574", "0", "1", "1", "1", "3", "9", "4", "3", "2", "1",
87                               "3", "3", "3", "3", "3", "46340", "46340", "2097151", "2097152",
88                               "4987896", "2767208", "2353973" };
89
90     for (int i = 0; i < numbers.length; i++) {
91         NaturalNumber n = new NaturalNumber2(numbers[i]);
92         NaturalNumber r = new NaturalNumber2(results[i]);
93         root(n, roots[i]);
94         if (n.equals(r)) {
95             out.println("Test " + (i + 1) + " passed: root(" + numbers[i]
96                       + ", " + roots[i] + ") = " + results[i]);
97         } else {
98             out.println("*** Test " + (i + 1) + " failed: root("
99                       + numbers[i] + ", " + roots[i] + ") expected <"
100                      + results[i] + "> but was <" + n + ">");
101         }
102     }
103
104     out.close();
105 }
106
107 }

```