

```
1 import components.naturalnumber.NaturalNumber;
2 import components.naturalnumber.NaturalNumber2;
3 import components.simplewriter.SimpleWriter;
4 import components.simplewriter.SimpleWriter1L;
5
6 /**
7  * Program with implementation of {@code NaturalNumber} secondary operation
8  * {@code root} implemented as static method.
9  *
10 * @author Vaishnavi Kasabwala
11 *
12 */
13 public final class NaturalNumberRoot {
14
15     /**
16      * Private constructor so this utility class cannot be instantiated.
17      */
18     private NaturalNumberRoot() {
19     }
20
21     /**
22      * Updates {@code n} to the {@code r}-th root of its incoming value.
23      *
24      * @param n
25      *         the number whose root to compute
26      * @param r
27      *         root
28      * @updates n
29      * @requires  $r \geq 2$ 
30      * @ensures  $n^r \leq \#n < (n + 1)^r$ 
31      */
32     public static void root(NaturalNumber n, int r) {
33         assert n != null : "Violation of: n is not null";
34         assert r >= 2 : "Violation of: r >= 2";
35
36         //constants
37         NaturalNumber one = new NaturalNumber2(1);
38         NaturalNumber two = new NaturalNumber2(2);
39
40         //NaturalNumber Variables
41         NaturalNumber low = new NaturalNumber2(0);
42         NaturalNumber high = new NaturalNumber2(n);
43         high.add(one);
44
45         NaturalNumber guess = new NaturalNumber2(0);
46
47         // temporary value for power function
48         NaturalNumber temp = new NaturalNumber2(0);
49
50         NaturalNumber value = new NaturalNumber2(high);
51         value.subtract(low);
52
53         while (value.compareTo(one) > 0) {
54
55             // guess
56             guess.copyFrom(high);
57             guess.add(low);
```

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58         guess.divide(two);
59
60         // temp ^ r
61         temp.copyFrom(guess);
62         temp.power(r);
63
64         // replace bounds
65         if (n.compareTo(temp) < 0) {
66             high.copyFrom(guess);
67         } else {
68             low.copyFrom(guess);
69         }
70
71         value.copyFrom(high);
72         value.subtract(low);
73     }
74
75     //update n
76     n.copyFrom(low);
77 }
78
79 /**
80  * Main method.
81  *
82  * @param args
83  *     the command line arguments
84  */
85 public static void main(String[] args) {
86     SimpleWriter out = new SimpleWriter1L();
87
88     final String[] numbers = { "0", "1", "13", "1024", "189943527", "0",
89                               "1", "13", "4096", "189943527", "0", "1", "13", "1024",
90                               "189943527", "82", "82", "82", "82", "82", "9", "27", "81",
91                               "243", "143489073", "2147483647", "2147483648",
92                               "9223372036854775807", "9223372036854775808",
93                               "618970019642690137449562111",
94                               "162259276829213363391578010288127",
95                               "170141183460469231731687303715884105727" };
96     final int[] roots = { 2, 2, 2, 2, 2, 3, 3, 3, 3, 3, 15, 15, 15, 15, 15,
97                          2, 3, 4, 5, 15, 2, 3, 4, 5, 15, 2, 2, 3, 3, 4, 5, 6 };
98     final String[] results = { "0", "1", "3", "32", "13782", "0", "1", "2",
99                               "16", "574", "0", "1", "1", "1", "3", "9", "4", "3", "2", "1",
100                              "3", "3", "3", "3", "3", "46340", "46340", "2097151", "2097152",
101                              "4987896", "2767208", "2353973" };
102
103     for (int i = 0; i < numbers.length; i++) {
104         NaturalNumber n = new NaturalNumber2(numbers[i]);
105         NaturalNumber r = new NaturalNumber2(results[i]);
106         root(n, roots[i]);
107         if (n.equals(r)) {
108             out.println("Test " + (i + 1) + " passed: root(" + numbers[i]
109                        + ", " + roots[i] + ") = " + results[i]);
110         } else {
111             out.println("**** Test " + (i + 1) + " failed: root("
112                        + numbers[i] + ", " + roots[i] + ") expected <"
113                        + results[i] + "> but was <" + n + ">");
114         }
115     }

```

```
115     }
116
117     out.close();
118 }
119
120 }
```