

人工智能实践 Artificial Intelligence Practice

DCS3015 Autumn 2022

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Lecture 8: Model-based RL

15th December 2022

Quick Recap

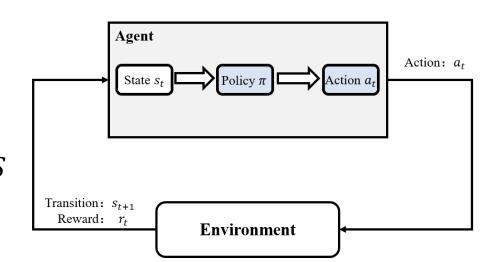


- \square States $S \in \mathbb{R}^s$
- \square Actions $A \in \mathbb{R}^a$
- \square Reward Function $R: S \times A \rightarrow \mathbb{R}$
- \square Transition Function $T: S \times A \rightarrow S$
- \square Discounted Factor $\gamma \in (0,1)$
- $\square \text{ Policy } \pi: S \to A$



$$\max_{\pi} \sum_{t=0}^{\infty} \gamma^t R(s_t, a_t)$$

Subject to $a_t = \pi(s_t), s_{t+1} = T(s_t, a_t)$



Quick Recap

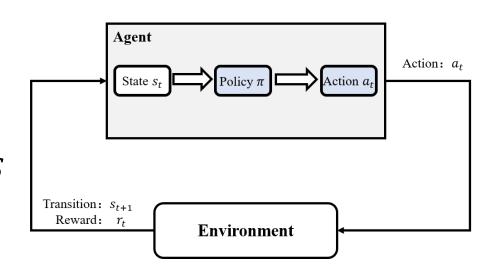


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Model-free RL vs. Model-based RL



Collect data

$$\mathcal{D} = \{s_t, a_t, r_{t+1}, s_{t+1}\}_{t=0}^T$$

Model-free: learn policy directly from data

$$\mathcal{D}
ightarrow \pi$$
 e.g. Q-learning, policy gradient

Model-based: learn model, then use it to learn or improve a policy

$$\mathcal{D} \to f \to \pi$$

Model-free RL vs. Model-based RL



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□ Why Model-based?	Model-free	Model-based
Asymptotic Performance	+	- / +
Computation	+	
Sample Efficiency		+
Exploration		+

Model-free RL vs. Model-based RL



Collect data

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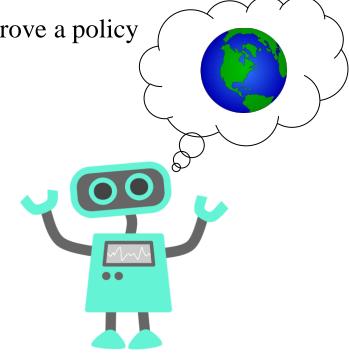
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□ What is a Model?



What is a Model?



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Model-based: learn model, then use it to learn or improve a policy

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What is a Model?

Definition: a model is a representation that **explicitly** encodes knowledge about the structure of the environment and task. state next, reward, terminate, infos = env.step(action)

A transition/dynamics model:

$$s_{t+1} = f_s(s_t, a_t)$$

A rewards model:

$$r_{t+1} = f_r(s_t, a_t)$$

A inverse transition/dynamics model:

$$a_t = f_s^{-1}(s_t, s_{t+1})$$

What is a Model?



Collect data

$$\mathcal{D} = \{s_t, a_t, r_{t+1}, s_{t+1}\}_{t=0}^T$$

Model-free: learn policy directly from data

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 Typically what is meant by the model in model-based RL

A inverse transition/dynamics model: $a_t = f_s^{-1}(s_t, s_{t+1})$

What is a Model?



Collect data

$$\mathcal{D} = \{s_t, a_t, r_{t+1}, s_{t+1}\}_{t=0}^T$$

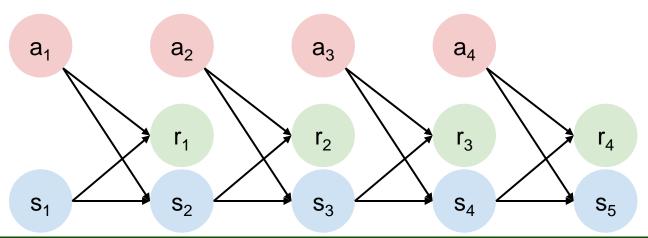
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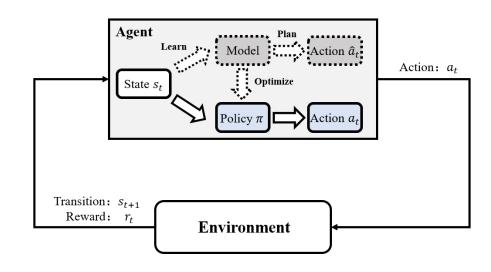
$$\mathcal{D} \to f \to \pi$$

□ What is a Model?





■ Model-based RL Process:



Run base policy $\pi_0(a_t|s_t)$ to collect data $\mathcal{D} = \{(s_t, a_t, s_{t+1})_i\}$

For _ do

Learn transition/dynamics model f(s, a)

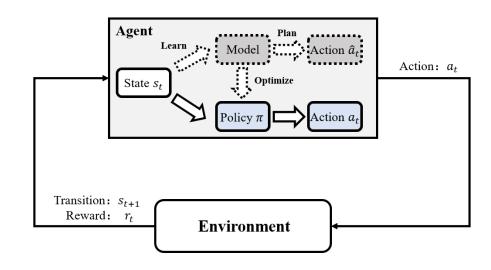
Use model f(s, a) to assist agent to update policy $\pi(a_t|s_t)$

Execute $\pi(a_t|s_t)$ and add the resulting data $\{(s_t, a_t, s_{t+1})_j\}$ to \mathcal{D}

End For



■ Model-based RL Process:



Run base policy $\pi_0(a_t|s_t)$ to collect data $\mathcal{D} = \{(s_t, a_t, s_{t+1})_i\}$

For _ do

Learn transition/dynamics model f(s, a)

Model Building

Use model f(s, a) to assist agent to update policy $\pi(a_t|s_t)$

Model Utilizing

Execute $\pi(a_t|s_t)$ and add the resulting data $\{(s_t, a_t, s_{t+1})_j\}$ to \mathcal{D}

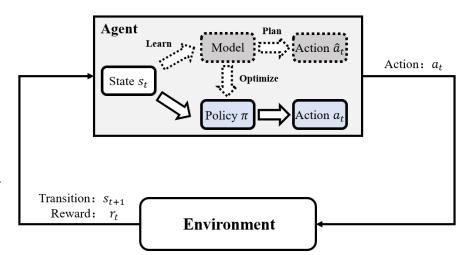
End For



■ Model Building

Collect data
$$\mathcal{D} = \{(s_t, a_t, s_{t+1})_i\}$$

Deterministic Model or **Probabilistic Model**

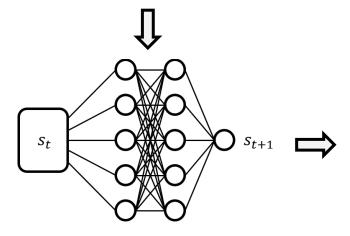


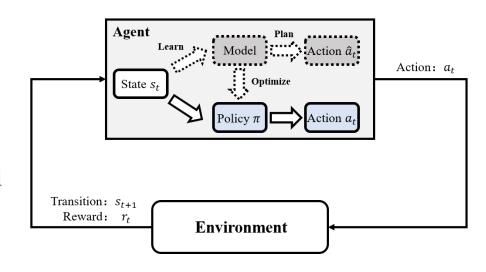


■ Model Building

Collect data
$$\mathcal{D} = \{(s_t, a_t, s_{t+1})_i\}$$

Deterministic Model or Probabilistic Model





Learn transition model f(s, a) to minimize **Mean** Squared Error (MSE):

$$\mathcal{L}_{MSE} = \mathbb{E}_{(s_t, a_t, s_{t+1}) \sim D} \left[f\left(s_t, a_t\right) - s_{t+1} \right]^2.$$

Incremental Predict:

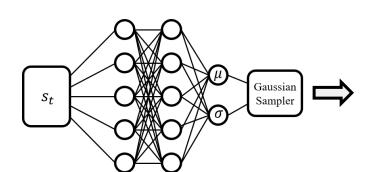
$$\hat{s}_{t+1} \sim s_t + f(s_t, a_t)$$

 $\hat{s}_{t+1} \sim f(s_t, a_t)$

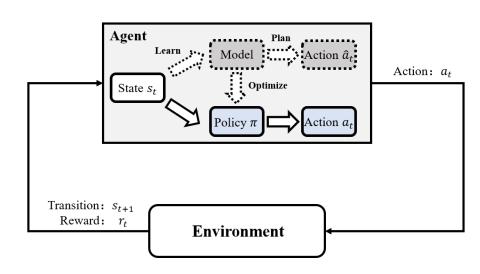


■ Model Building

Deterministic Model or **Probabilistic Model**



$$\hat{s}_{t+1} \sim \mathcal{N}\left(\mu(s_t, a_t), \sigma(s_t, a_t)\right)$$



Learn transition model f(s, a) to optimize **Negative Log Likelihood** (NLL)

$$\mathcal{L}_{NLL} = \mathbb{E}_{(s_t, a_t, s_{t+1}) \sim \mathcal{D}} \left(\frac{\left[\mu(s_t, a_t) - s_{t+1} \right]^2}{\sigma(s_t, a_t)} + \log \sigma(s_t, a_t) \right)$$

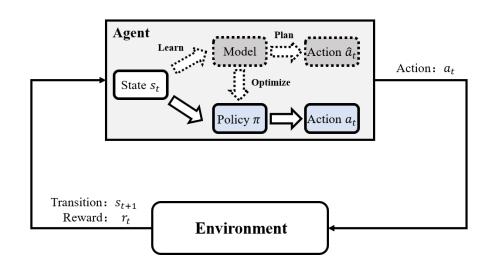


■ Model Building:

Collect data $\mathcal{D} = \{(s_t, a_t, s_{t+1})_i\}$

Learn transition model f(s, a) to minimize

$$\sum_{i} \|f(s_t, a_t) - s_{t+1}\|^2$$



□ Decision-Time Method (Plan):

$$(a_t, a_{t+1}, \dots, a_{t+\tau}, \dots, a_{t+T}) \sim Optimizer$$



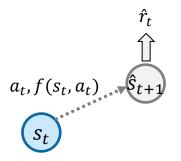
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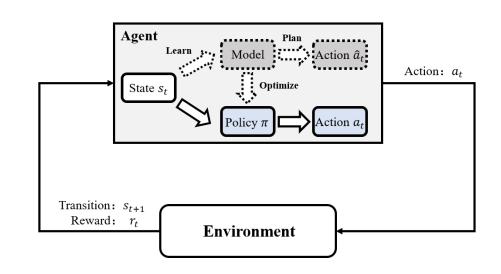
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□ Decision-Time Method (Plan):







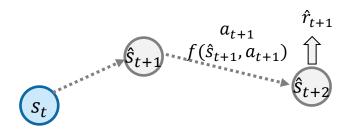
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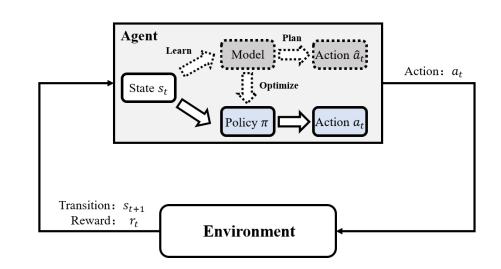
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□ Decision-Time Method (Plan):





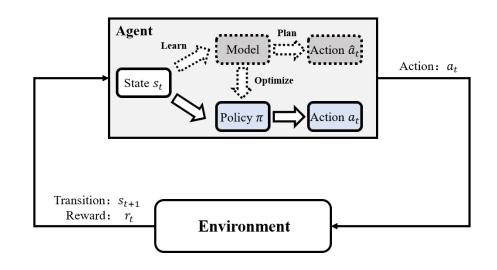


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Collect data $\mathcal{D} = \{(s_t, a_t, s_{t+1})_i\}$

Learn transition model f(s, a) to minimize

$$\sum_{i} \|f(s_t, a_t) - s_{t+1}\|^2$$



□ Decision-Time Method (Plan):

$$\hat{S}_{t}$$

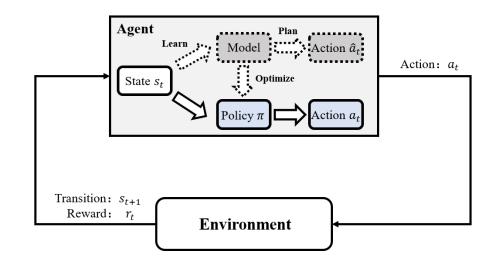


■ Model Building:

Collect data $\mathcal{D} = \{(s_t, a_t, s_{t+1})_i\}$

Learn transition model f(s, a) to minimize

$$\sum_{i} \|f(s_t, a_t) - s_{t+1}\|^2$$



□ Decision-Time Method (Plan):

$$\hat{S}_{t+1} \Rightarrow \sum_{\tau=t}^{t+T-1} \hat{r}(s_{\tau}, a_{\tau})$$

$$\hat{S}_{t+2} \Rightarrow \hat{S}_{t+2} \Rightarrow \hat{S}_{t+3} \Rightarrow \hat{S}_{t+1} \Rightarrow \hat{S}_{t+1} \Rightarrow \hat{S}_{t+1} \Rightarrow \hat{S}_{t+2} \Rightarrow \hat{S}_{t+3} \Rightarrow \hat{S}_$$

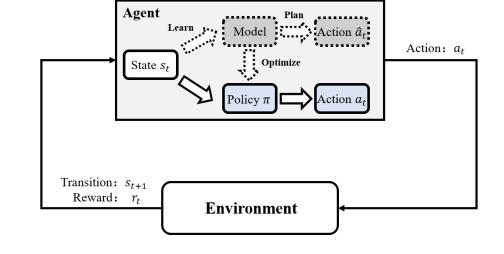


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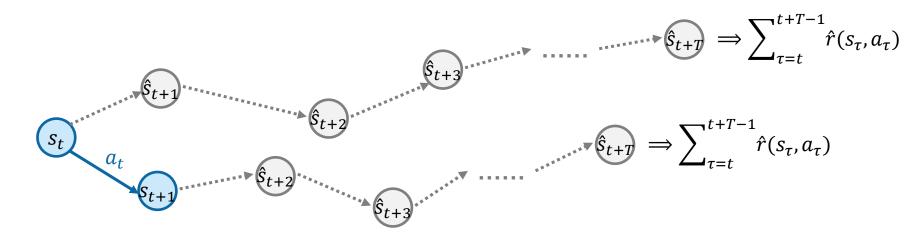
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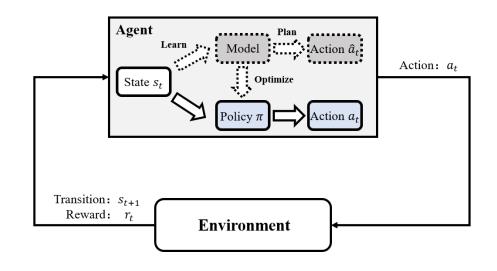


■ Model Building:

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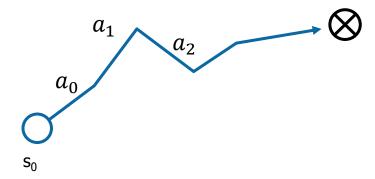
Learn transition model f(s, a) to minimize

$$\sum_{i} \|f(s_t, a_t) - s_{t+1}\|^2$$



□ Decision-Time Method (Plan):

Model Predictive Control (MPC) without Policy Function π



Trajectory Optimization with Action Sequence:

$$S_t \to a_t \to S_{t+1} \to a_{t+1} \to \cdots$$
$$J(a_0, ..., a_H) = \sum_{t=0}^{H} \gamma^t r_t$$



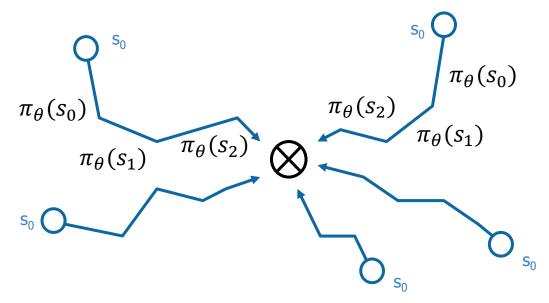
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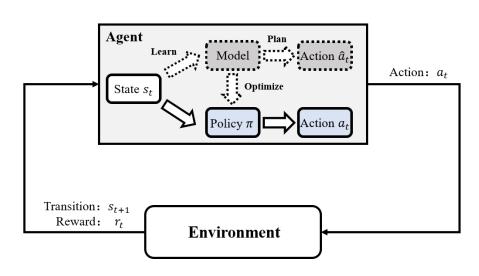
Collect data $\mathcal{D} = \{(s_t, a_t, s_{t+1})_i\}$

Learn transition model f(s, a) to minimize

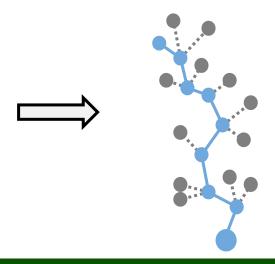
$$\sum_{i} \|f(s_t, a_t) - s_{t+1}\|^2$$

■ Background Method (Optimize):





Mix real and model-generated experience and apply additional policy updates.





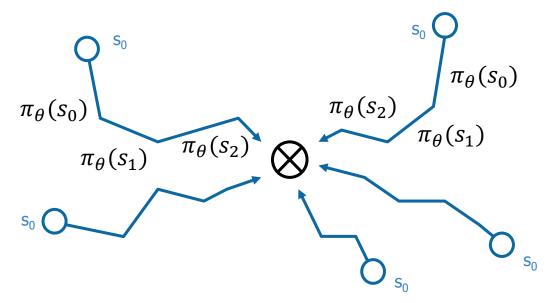
■ Model Building:

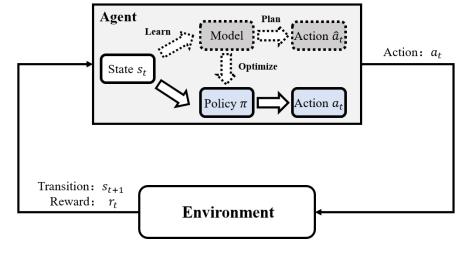
Collect data $\mathcal{D} = \{(s_t, a_t, s_{t+1})_i\}$

Learn transition model f(s, a) to minimize

$$\sum_{i} \|f(s_t, a_t) - s_{t+1}\|^2$$

□ Background Method (Optimize):





Policy Optimization with parameter θ :

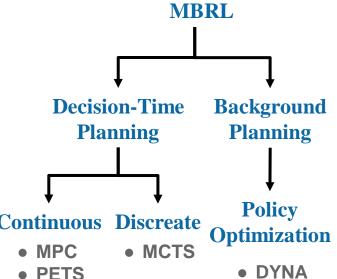
$$s_t \to \pi_{\theta}(s_t) \to s_{t+1} \to \pi_{\theta}(s_{t+1}) \to \cdots$$
$$J(\theta) = \mathbb{E}_{s_0}\left[\sum_{t=0}^{H} \gamma^t r_t\right], \quad a_t = \pi_{\theta}(s_t)$$



MBPO MAGE

□ Background vs. Decision-Time

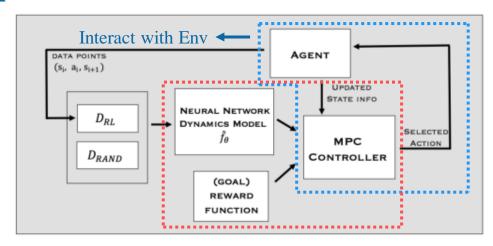
	Background	Decision-Time	N
Act without Learning		+	·
Unfamiliar situations		+	Decision-Time Planning
Computation	-		
Predictability Coherence	+		
Discrete and Continuous	+		Continuous DiscreaMPCMCT
			• PETS





■ MPC with Neural Network Model

- $\mathbf{D}_{RL} = \{(s_t, a_t, s_{t+1})_i\} \text{ to train neural network dynamic model.}$
- $\mathcal{D}_{RAND} = \{(a_1, a_2, ..., a_T)\} \text{ to store the sampled actions sequence.}$
- ☐ (Goal) Reward Function



- 1. Planning based on Model
- 2. Agent action selection



■ MPC with Neural Network Model

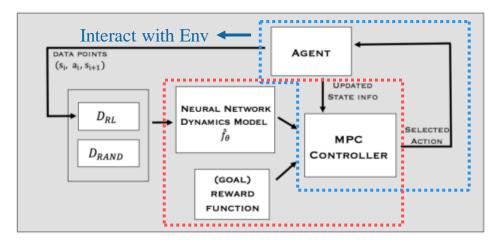
Algorithm 1 Model-based Reinforcement Learning 1: gather dataset \mathcal{D}_{RAND} of random trajectories 2: initialize empty dataset \mathcal{D}_{RL} , and randomly initialize f_{θ} 3: for iter=1 to max_iter do train $\hat{f}_{\theta}(\mathbf{s}, \mathbf{a})$ by performing gradient descent on Eqn. 2. using \mathcal{D}_{RAND} and \mathcal{D}_{RL} for t = 1 to T do 5: get agent's current state s_t 6: use f_{θ} to estimate optimal action sequence $\mathbf{A}_{t}^{(H)}$ 7: (Eqn. 4) execute first action \mathbf{a}_t from selected action sequence 8: $\mathbf{A}_{t}^{(H)}$ add $(\mathbf{s}_t, \mathbf{a}_t)$ to \mathcal{D}_{RL} 9:

Random Shooting (RS):

end for

11: end for

For
$$t = 1$$
 to T do:
 $random(a_t) \in A \rightarrow \mathcal{D}_{RAND}$



- 1. Planning based on Model
- $\hat{\mathbf{s}}_{t+1} = \mathbf{s}_t + \hat{f}_{\theta}(\mathbf{s}_t, \mathbf{a}_t)$ 2. Agent action selection

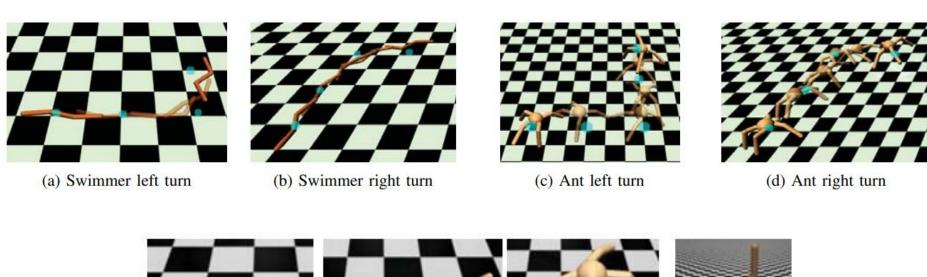
$$\mathcal{E}(\theta) = \frac{1}{|\mathcal{D}|} \sum_{(\mathbf{s}_t, \mathbf{a}_t, \mathbf{s}_{t+1}) \in \mathcal{D}} \frac{1}{2} \| (\mathbf{s}_{t+1} - \mathbf{s}_t) - \hat{f}_{\theta}(\mathbf{s}_t, \mathbf{a}_t) \|^2$$
 (1)

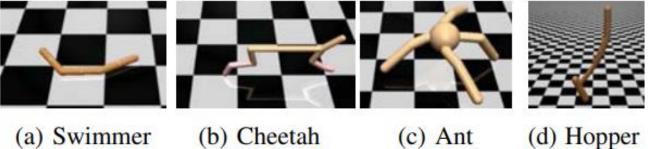
$$\mathbf{A}_{t}^{(H)} = \arg \max_{\mathbf{A}_{t}^{(H)}} \sum_{t'=t}^{t+H-1} r(\hat{\mathbf{s}}_{t'}, \mathbf{a}_{t'}) :$$

$$\hat{\mathbf{s}}_{t} = \mathbf{s}_{t}, \hat{\mathbf{s}}_{t'+1} = \hat{\mathbf{s}}_{t'} + \hat{f}_{\theta}(\hat{\mathbf{s}}_{t'}, \mathbf{a}_{t'}).$$
(3)



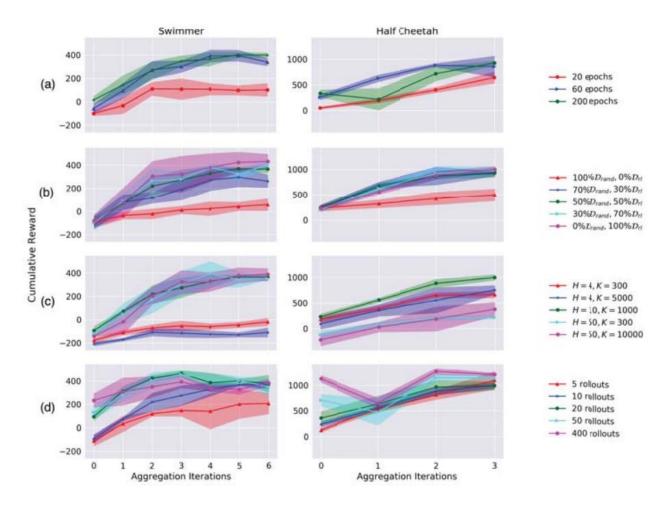
■ MPC with Neural Network Model







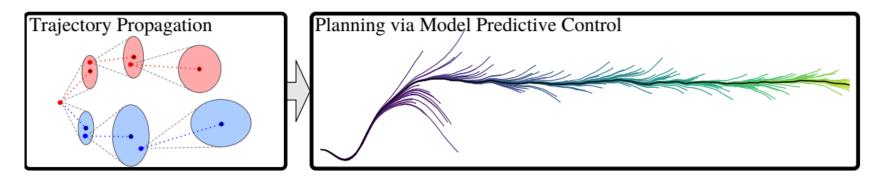
■ MPC with Neural Network Model



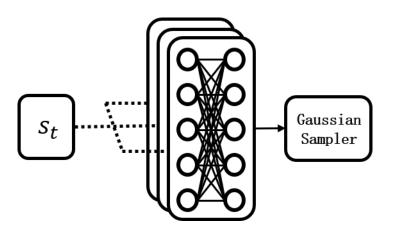
Nagabandi, Anusha, et al. "Neural network dynamics for model-based deep reinforcement learning with model-free fine-tuning.", ICRA. 2018.



☐ Probabilistic Ensemble with Trajectory Sampling (PETS)



- ☐ Probabilistic Model Networks to capture **aleatoric uncertainty**.
- Model Ensembles to capture **epistemic uncertainty**.



Model Ensemble Output:

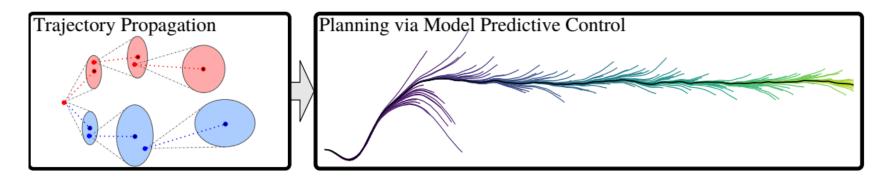
$$\hat{s}_{t+1} = random \left(f_1(s_t, a_t), f_2(s_t, a_t), ..., f_M(s_t, a_t) \right)$$

$$\hat{s}_{t+1} = \frac{1}{M} \sum_{j=1}^{M} f_j(s_t, a_t).$$

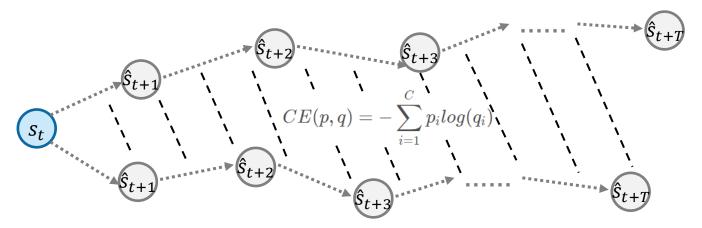
Chua, Kurtland, et al. "Deep reinforcement learning in a handful of trials using probabilistic dynamics models.", NIPS, 2018.



□ Probabilistic Ensemble with Trajectory Sampling (PETS)



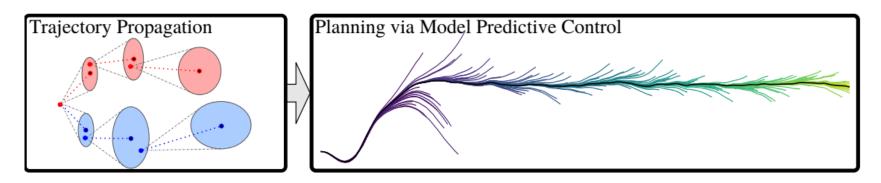
□ Cross Entropy Method (CEM) instead of Random Shooting (RS)



Chua, Kurtland, et al. "Deep reinforcement learning in a handful of trials using probabilistic dynamics models.", NIPS, 2018.



□ Probabilistic Ensemble with Trajectory Sampling (PETS)



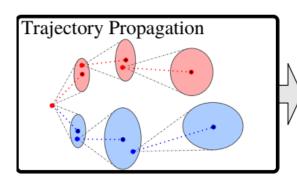
Algorithm 1 Our model-based MPC algorithm 'PETS':

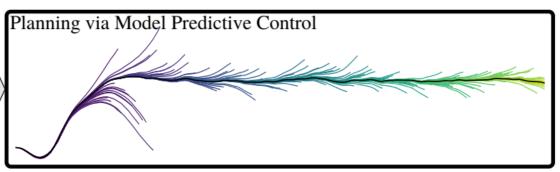
```
    Initialize data D with a random controller for one trial.
    for Trial k = 1 to K do
    Train a PE dynamics model f given D.
    for Time t = 0 to TaskHorizon do
    for Actions sampled a<sub>t:t+T</sub> ~ CEM(·), 1 to NSamples do
    Propagate state particles s<sup>p</sup><sub>τ</sub> using TS and f | {D, a<sub>t:t+T</sub>}.
    Evaluate actions as ∑<sup>t+T</sup><sub>τ=t-P</sub> ∑<sup>P</sup><sub>p=1</sub> r(s<sup>p</sup><sub>τ</sub>, a<sub>τ</sub>)
    Update CEM(·) distribution.
    Execute first action a<sup>*</sup><sub>t</sub> (only) from optimal actions a<sup>*</sup><sub>t:t+T</sub>.
    Record outcome: D ← D ∪ {s<sub>t</sub>, a<sup>*</sup><sub>t</sub>, s<sub>t+1</sub>}.
```

Chua, Kurtland, et al. "Deep reinforcement learning in a handful of trials using probabilistic dynamics models.", NIPS, 2018.

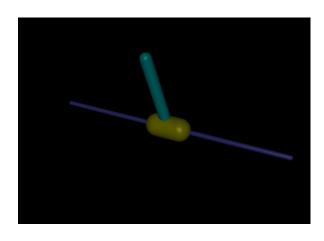


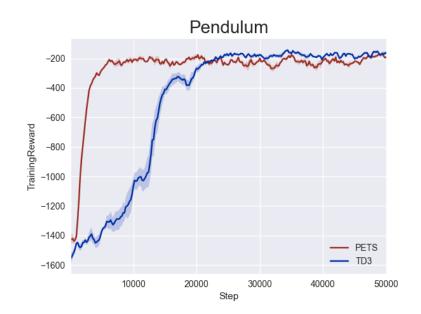
☐ Probabilistic Ensemble with Trajectory Sampling (PETS)





■ Experiments

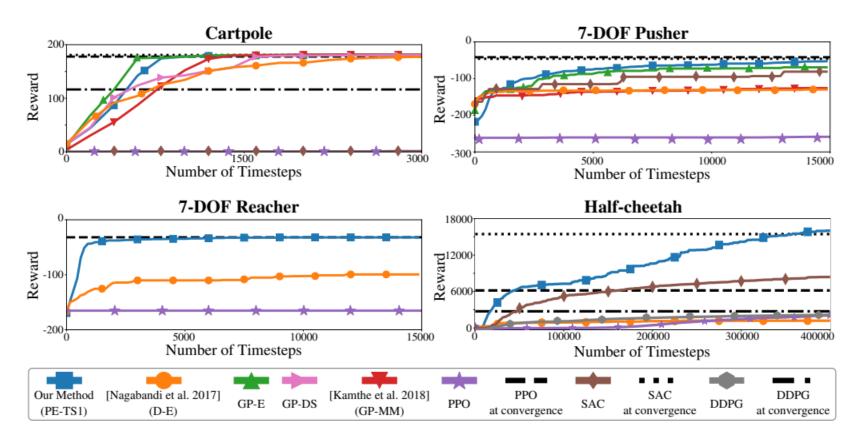






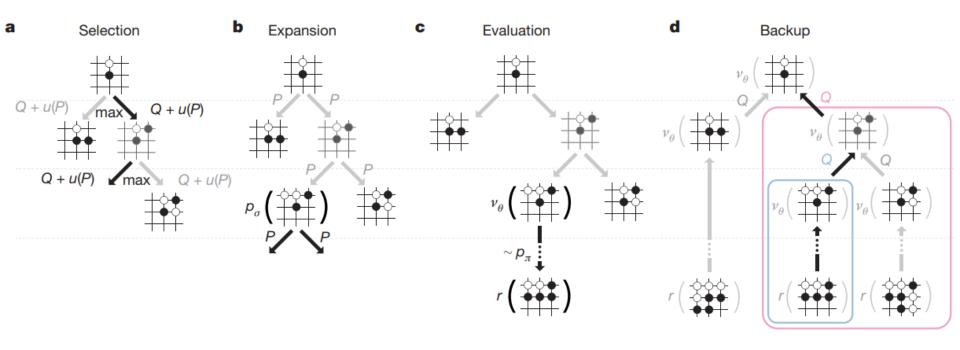
□ Probabilistic Ensemble with Trajectory Sampling (PETS)

■ Experiments





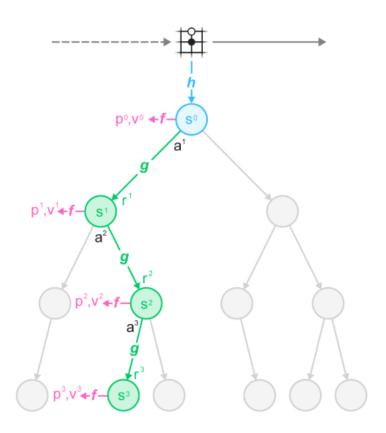
- **■** MuZero: Mastering Atari, Go and Chess
 - **■** Monte-Carlo Tree Search (MCTS) with Dynamics Model



Schrittwieser, Julian, et al. "Mastering atari, go, chess and shogi by planning with a learned model." Nature. 2020.



- **■** MuZero: Mastering Atari, Go and Chess
 - **■** Monte-Carlo Tree Search (MCTS) with Dynamics Model



- Representation Function: $s^0 = h_\theta(o_1, ..., o_n)$ to encode past observations.
- **D** Dynamic Function: r^k , $s^k = g_{\theta}(s^{k-1}, a^k)$
- lacktriangle Prediction Function: p^k , $v^k = f_{\theta}(s^k)$

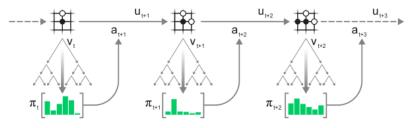
MCTS Backup:

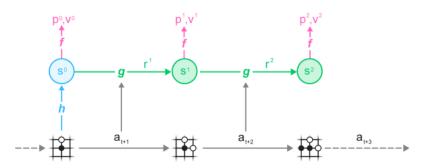
$$Q_{k+1}(s,a) = \frac{Q_k(s,a) \cdot N_k(s,a) + R}{N_k(s,a) + 1}$$
$$N_{k+1}(s,a) = N_k(s,a) + 1$$

Decision-Time



- **■** MuZero: Mastering Atari, Go and Chess
 - **■** Monte-Carlo Tree Search (MCTS) with Dynamics Model





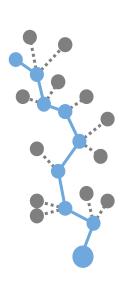
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- **Dyna-Q**
 - Mix real and model-generated experiences and apply for additional policy updates.



Tabular Dyna-Q

Initialize Q(s, a) and Model(s, a) for all $s \in S$ and $a \in A(s)$ Loop forever:

- (a) $S \leftarrow \text{current (nonterminal) state}$
- (b) $A \leftarrow \varepsilon$ -greedy(S, Q)
- (c) Take action A; observe resultant reward, R, and state, S' Update Q values with
- (d) $Q(S, A) \leftarrow Q(S, A) + \alpha [R + \gamma \max_a Q(S', a) Q(S, A)]$
- (e) $Model(S, A) \leftarrow R, S'$ (assuming deterministic environment)
- (f) Loop repeat n times:

 $S \leftarrow \text{random previously observed state}$

 $A \leftarrow$ random action previously taken in S

 $R, S' \leftarrow Model(S, A)$

 $Q(S, A) \leftarrow Q(S, A) + \alpha [R + \gamma \max_{a} Q(S', a) - Q(S, A)]$

Update O values with model transitions



- **■** Model-Based Policy Optimization (MBPO)
 - **□** Dyna-Q updates the policy with both real and model-generated transitions.
 - **□** How to guarantee the policy improvement if we only use the model-generated transitions?

Definition: Errors in the model can be exploited during policy optimization, resulting in large discrepancies between the predicted returns of the policy under the model and under the true dynamics.

$$\eta[\pi] \ge \hat{\eta}[\pi] - C.$$

 $\eta[\pi]$: the returns of the policy in true MDP; $\hat{\eta}[\pi]$: the returns under learned model.



- **■** Model-Based Policy Optimization (MBPO)
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Definition: Errors in the model can be exploited during policy optimization, resulting in large discrepancies between the predicted returns of the policy under the model and under the true dynamics.

$$\eta[\pi] \ge \hat{\eta}[\pi] - C.$$

The gap between true and model returns can be expressed in:

- **□** Generalization Error: $\epsilon_m = \mathbb{E}_{s,a\sim D_{env}}[D_{TV}(p(s'|s,a)||p_{\theta}(s'|s,a))]$
- **Policy Distribution**: $\epsilon_{\pi} = D_{TV}(\pi_D(s)||\pi(s))$



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The gap between:

$$|\eta_{1} - \eta_{2}| = |\sum_{s,a} (p_{1}(s,a) - p_{2}(s,a))r(s,a)|$$

$$= |\sum_{s,a} (\sum_{t} \gamma^{t} p_{1}^{t}(s,a) - p_{2}^{t}(s,a))r(s,a)|$$

$$= |\sum_{t} \sum_{s,a} \gamma^{t} (p_{1}^{t}(s,a) - p_{2}^{t}(s,a))r(s,a)|$$

$$\leq \sum_{t} \sum_{s,a} \gamma^{t} |p_{1}^{t}(s,a) - p_{2}^{t}(s,a)|r(s,a)$$

$$\leq r_{\max} \sum_{t} \sum_{s,a} \gamma^{t} |p_{1}^{t}(s,a) - p_{2}^{t}(s,a)|$$



- **Model-Based Policy Optimization (MBPO)**
 - Dyna-Q updates the policy with both real and model-generated transitions.
 - How to guarantee the policy improvement if we only use the modelgenerated transitions?

The gap between:

$$|\eta_1 - \eta_2| \le r_{\max} \sum_{t} \sum_{s,a} \gamma^t |p_1^t(s,a) - p_2^t(s,a)|$$

Lemma:

Lemma B.1 (TVD of Joint Distributions). Suppose we have two distributions $p_1(x,y) =$ $p_1(x)p_1(y|x)$ and $p_2(x,y) = p_2(x)p_2(y|x)$. We can bound the total variation distance of the joint as:

$$D_{TV}(p_1(x,y)||p_2(x,y)) \le D_{TV}(p_1(x)||p_2(x)) + E_{x \sim p_1}[D_{TV}(p_1(y|x)||p_2(y|x))]$$



- **■** Model-Based Policy Optimization (MBPO)
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The gap between:

$$|\eta_1 - \eta_2| \le r_{\text{max}} \sum_t \sum_{s,a} \gamma^t |p_1^t(s,a) - p_2^t(s,a)|$$

$$\epsilon_{m} = \max_{t} E_{s \sim \pi_{D,t}} \left[D_{TV} \left(p\left(s^{\prime}, r | s, a
ight) \| p_{ heta}\left(s^{\prime}, r | s, a
ight)
ight)
ight]$$

Lemma:

$$\max_s D_{TV}\left(\pi \| \pi_D\right) \leq \epsilon_{\pi}$$

Lemma B.2 (Markov chain TVD bound, time-varying). Suppose the expected KL-divergence between two transition distributions is bounded as $\max_t E_{s \sim p_1^t(s)} D_{KL}(p_1(s'|s)||p_2(s'|s)) \leq \delta$, and the initial state distributions are the same $-p_1^{t=0}(s) = p_2^{t=0}(s)$. Then the distance in the state marginal is bounded as:

$$D_{TV}(p_1^t(s)||p_2^t(s)) \le t\delta - - - \int_{\bullet}^{\bullet} \delta = \epsilon_m + \epsilon_{\pi}$$



- **■** Model-Based Policy Optimization (MBPO)
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The gap between:

$$|\eta_{1} - \eta_{2}| \leq r_{\max} \sum_{t} \sum_{s,a} \gamma^{t} |p_{1}^{t}(s,a) - p_{2}^{t}(s,a)| - - \frac{1}{2} \sum_{t} D_{TV}(p_{1}^{t}(s)||p_{2}^{t}(s)) \leq t(\epsilon_{m} + \epsilon_{\pi})$$

$$\leq 2r_{\max} \sum_{t} \gamma^{t} t(\epsilon_{m} + \epsilon_{\pi}) + \epsilon_{\pi}$$

$$\leq 2r_{\max} \left(\frac{\gamma(\epsilon_{\pi} + \epsilon_{m})}{(1 - \gamma)^{2}} + \frac{\epsilon_{\pi}}{1 - \gamma}\right)$$

The returns and model returns of the policy are bounded as:

$$\eta[\pi] \ge \hat{\eta}[\pi] - \underbrace{\left[\frac{2\gamma r_{\max}(\epsilon_m + 2\epsilon_\pi)}{(1-\gamma)^2} + \frac{4r_{\max}\epsilon_\pi}{(1-\gamma)}\right]}_{C(\epsilon_m, \epsilon_\pi)}$$



■ Model-Based Policy Optimization (MBPO)

- □ Dyna-Q updates the policy with both real and model-generated transitions.
- **□** How to guarantee the policy improvement if we only use the model-generated transitions?
- **□** H-steps Q-target objective:

Model-based Critic Loss Function:

$$Loss_{critic} = \frac{1}{2} (y - Q(s_t, a_t))^2$$

Dyna-Q one-step Q-target:

$$y = \hat{r}(s_t, a_t) + \gamma Q(\hat{s}_{t+1}, \hat{a}_{t+1})$$

Multi-steps Q-target:

$$y = \sum_{k=t}^{H-1} \gamma^{k-t} \hat{r}_k + \gamma^H Q(\hat{s}_H, \hat{a}_H)$$



- **■** Model-Based Policy Optimization (MBPO)
 - **□** Dyna-Q updates the policy with both real and model-generated transitions.
 - **□** How to guarantee the policy improvement if we only use the model-generated transitions?
 - **□** H-steps Q-target objective
 - **■** MBPO Algorithm:

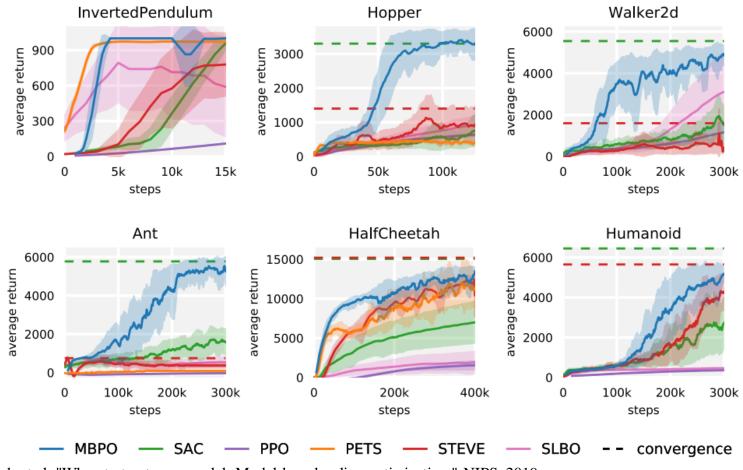
Algorithm 2 Model-Based Policy Optimization with Deep Reinforcement Learning

- 1: Initialize policy π_{ϕ} , predictive model p_{θ} , environment dataset \mathcal{D}_{env} , model dataset $\mathcal{D}_{\text{model}}$
- 2: **for** N epochs **do**
- 3: Train model p_{θ} on \mathcal{D}_{env} via maximum likelihood
- 4: **for** E steps **do**
- 5: Take action in environment according to π_{ϕ} ; add to \mathcal{D}_{env}
- 6: **for** M model rollouts **do**
- 7: Sample s_t uniformly from \mathcal{D}_{env}
- 8: Perform k-step model rollout starting from s_t using policy π_{ϕ} ; add to $\mathcal{D}_{\text{model}}$
- 9: **for** G gradient updates **do**
- 10: Update policy parameters on model data: $\phi \leftarrow \phi \lambda_{\pi} \hat{\nabla}_{\phi} J_{\pi}(\phi, \mathcal{D}_{\text{model}})$



□ Model-Based Policy Optimization (MBPO)

■ Experiments



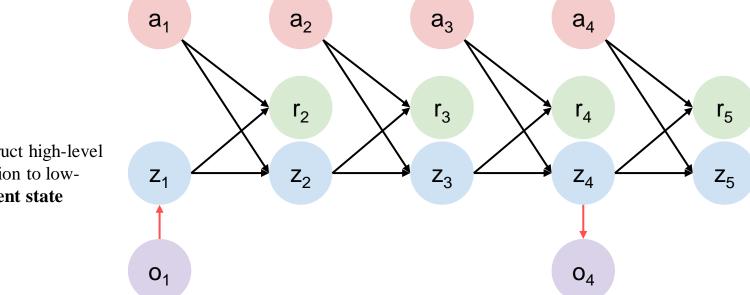
Janner, Michael, et al. "When to trust your model: Model-based policy optimization." NIPS, 2019.

Model-based RL with Images



Dreamer: Latent Imagination

Latent state-transition models



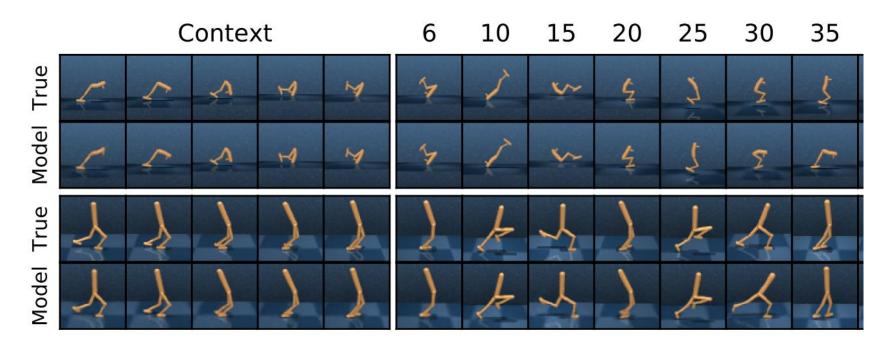
Reconstruct high-level observation to lowlevel latent state

Model-based RL with Images



☐ Dreamer: Latent Imagination

■ Latent state-transition models



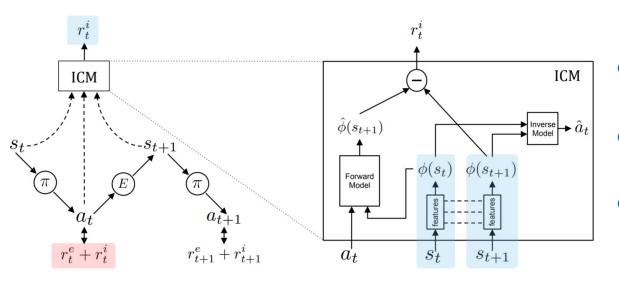
Hafner, Danijar, et al. "Dream to control: Learning behaviors by latent imagination." arXiv preprint arXiv:1912.01603 (2019).

Inverse Model



☐ Intrinsic Curiosity Module (ICM)

- Besides extrinsic reward, agent set **intrinsic reward** to express its familiarity with the true environment. (Curiosity Driven)
- \square Model Prediction: $f(s_t, a_t) \rightarrow s_{t+1}$
- Intrinsic Reward: $r_t^{in} \sim ||f(s_t, a_t) s_{t+1}||_2^2$



Forward Dynamics Model:

$$f_{\psi F}(\phi(s_t), a_t) \to \hat{\phi}(s_{t+1})$$

Inverse Model:

$$g_{\psi I}(\phi(s_t), \phi(s_{t+1})) \rightarrow \hat{a}_t.$$

Intrinsic Reward:

$$r_t^i = \|\hat{\phi}(s_{t+1}) - \phi(s_{t+1})\|_2^2$$

Deep Reinforcement Learning



谢谢!

中山大学计算机学院