

CountPairs specs

countpairs

We'll say that a "pair" in a string is two instances of a char separated by a char. So "AxA" the A's make a pair. Pairs can overlap, so "AxAxA" contains 3 pairs -- 2 for A and 1 for x. Recursively compute the number of pairs in the given string.

a pair is two instances of a char separated by a char

```
countPairs("A") = 0
countPairs("xA") = 0
countPairs("AxA") = 1
countPairs("AxxA") = 0
countPairs("Ax0xA") = 1
countPairs("AxAxA") = 3
countPairs("xAxA") = 2
countPairs("aaaa") = 2
```

first find an integer n that identifies the problem. For example: in hanoi the n was the number of disks. in the addarray problem it was the current index in the array. what would be a good n for this problem?

Express the solution of the the problem for n using the solution for n-1.

Provide a solution for the base case. That could be for the smallest n you want to consider.

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step1. find an n that defines the problem. for example in hanoi the n is the number of disks, in factorial the n is the number of which we are computing the factorial.

step2. assume that we have a solution for n-1

step3. put the solution for n in terms of n-1

step4. solve the problem for the base case (e.g. n = 1)

lets apply the steps to the factorial.

here is the factorial function:

```
f(n) = n * n-1 * n-2 * n-3 ..... 1
f(2) = 2
f(3) = 6
f(4) = 24 ....
```

step 1: the n is the n from f(n)

step2: i have the solution for f(n-1)

step3: $f(n) = n * f(n-1)$

step4: $f(1) = 1$ this is the base case

```
static int f(int n) {  
    if (n == 1)  
        return 1;  
    else  
        return n * f(n-1);  
}
```

for the pairs problem:

step1: the n is going to be the length of the string

step2: if length str is n-1 then countPairs(str) returns the correct nr of pairs

step3: if I had the solution for a str of length n-1 could I use it to build the solution for n

```
given a String str of length n  
firstChar = str.charAt(0)  
strMinusTheFirstChar = str.substring(1)
```

what is the relationship between A and xAxAx
A is equal to the second char of the strMinusTheFirstChar

```
secondCharofShortStr = strMinusTheFirstChar.charAt(1)
```

```
can I express the solution of countPairs("xAxAx") in terms of countPairs("xAxAx")  
let pp = countPairs(strMinusTheFirstChar)
```

```
if firstChar == secondCharofShortStr then return pp + 1  
else  
    return pp
```

step4: base case: length is 2

```
if length == 2 return 0
```