

# Automated Verification of Stand-alone Solar Photovoltaic Systems

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## Abstract

With declining costs and increasing performance, the deployment of renewable energy systems is growing faster. In 2017, for the first time, the number of people without access to electricity dipped below 1 billion, but trends on energy access likewise fall short of global goals. Particular attention is given to stand-alone solar photovoltaic systems in rural areas or where grid extension is unfeasible. Tools to evaluate electrification projects are available, but they are based on simulations that do not cover all aspects of the design space. Automated verification using model checking has proven to be an effective technique to any kind of program verification. This paper marks the first application of software model checking to formally verify the design of a stand-alone solar photovoltaic system including solar panel, charge controller, battery, inverter, and electric load. Case studies, from real photovoltaic systems deployed in five different sites, ranging from 700W to 1,200W, were used to evaluate this proposed approach and to compare that with specialized simulation tools. Different verification tools were evaluated as well, in order to compare performance and soundness. Data from practical applications show the effectiveness of our approach, where specific conditions that lead to failures in a photovoltaic solar system are only detailed by the automated verification method.

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## 1. Introduction

Lack of access to clean and affordable energy is considered a core dimension of poverty [1]. Progress has been made worldwide; in particular, the number of people without electricity access fell below 1 billion threshold for the first  
5 time in 2017 [2]. The share of people without access to electricity from Africa is 58%, while 19% of the share comes from developing Asia, and 31% from Latin America [2]. Numbers from Brazil show the aim to electrify 270 isolated places and 2.7 million of people until 2023 [3]. Furthermore, there is a close relationship between the lack of energy and the low HDI (Human Development  
10 Index) of those localities [4].

In order to provide universal electricity for all, decentralized systems led by solar photovoltaic (PV) in off-grid and mini-grid systems will be the lowest-cost solution for three-quarters of the additional connections needed; and grid extension will be the standard especially in urban areas [2].

15 Only a niche market a few years ago, solar photovoltaic (PV) systems are now becoming a mainstream electricity provider, with an increase of approximately 50% from 2016 to 2017 in terms of new installations of PV [5]. However, this growth is not driven by isolated systems.

In order to simulate or evaluate a PV system there are a myriad of specialized  
20 tools available in the market, such as RETScreen, HOMER, PVWatts, SAM, and Hybrid2 [6, 7, 8, 9, 10]; and even general purpose simulation tools such as PSpice, Saber, or MATLAB/Simulink package [11, 12]. However, those tools are based on running experiments in simulation models. Simulation has the advantage of being cheap (if compared to test in real systems) and can be  
25 employed before the system design is concluded but it has the drawback of an incomplete coverage since the verification of all possible combinations and potential failures of a system is unfeasible [13].

Formal methods based on model checking offer a great potential to obtain a more effective and faster verification in the design process [13]. Any kind of system can be specified as computer programs using mathematical logic, which constitutes the intended (correct) behavior; then, one can try to give a formal proof or otherwise establish that the program meets its specification. In this study, a mathematical model of each component of a stand-alone PV system, as panel solar, charge controller, batteries, inverter, and electrical load is created. The behavior of each system component can be analyzed and observed with the support of those formal models, as a joint operation of the components, which in this case represents the operation of the solar PV system itself. The project requirements, as battery autonomy and power demand, besides weather conditions, as solar irradiance and ambient temperature, are translated as part of the computer program and automatically verified during the formal process. The model checking tool reports in which conditions a system does not meet the user requirements. A key benefit to this approach is that it helps in the detection of flaws in the design phase of system development, thereby considerably improving system reliability [14]. The implementation of the proposed tool is carried out by means of an algorithm written in language C, that is executed by three state-of-the-art model checkers to formally verifying PV designs, in order to evaluate performance and correctness: the C Bounded Model Checker (CBMC) [15], the Efficient SMT-based Bounded Model Checker (ESBMC) [16], and the Configurable Program Analysis Checker (CPAchecker).

In prior studies, the evaluation of PV systems w.r.t. user requirements were performed by simulation tools using MATLAB/Simulink [12, 17], or HOMER Pro [18]. Related to formal methods, studies were carried out toward the modeling of power smart grids [14] and solar panels [19]; however, those studies do not perform automated verification. In addition, recent research performed a formal study of PV farms, where the focus has been the interaction with the grid [20]; or to model a PV system and to verify the maximum power point of solar panels with the use of Jmodelica tool [21]. Both studies restrict to PV panels, and do not include batteries, inverters, and charge controllers.

This paper makes three original contributions. Firstly, we propose an algo-  
60 rithm written in language C that implements the automated verification method  
which formally checks the sizing and the operation of a given stand-alone PV  
system. Secondly, we evaluate the verification method by comparing three state-  
of-the-art model checkers in five real case studies. Thirdly, experimental results  
show that this proposed approach can find subtle design errors in stand-alone  
65 PV systems, which are not easily detected by other approaches based on simu-  
lation.

*Outline.* Section 2 gives the background about solar PV systems, design and  
validation of PV systems, and the mathematical modeling. Section 3 presents  
the automated verification technique. Section 4 shows how to perform the sizing  
70 of a stand-alone PV system. The methodology is presented in section 5. Sec-  
tion 6 is devoted to the results. Section 7 presents the conclusion and describes  
future work.

## 2. Solar Photovoltaic System

PV systems are classified into distinct types [22]. Specifically for remote  
75 rural areas of developing countries or places where the grid extension is not  
feasible, the most suitable configuration is the regulated stand-alone system  
with battery and AC load; this configuration is the focus of this study.

### 2.1. Design and Simulation of Solar PV systems

Here we evaluated the most popular tools available in the literature and  
80 summarized at Table 1: PVWatts, SAM, HOMER, RETScreen, and Hybrid2 [6,  
7, 8, 9, 10].

As highlights, only Hybrid2 does not have technical support; HOMER and  
Hybrid2 perform off-grid system with battery backup analysis. Additionally,  
HOMER and RETScreen include economical analysis or even optimization-  
85 sensitive analysis. However, commercial version of those tools, called RETScreen  
Expert and HOMER Pro, are available only for Microsoft Windows and the an-  
nual subscription typically range from US\$504.00 to US\$657.00.

Table 1: Comparative coverage of reference software

Characteristic	PVWatts	SAM	HOMER	RETScreen	Hybrid2
Support	X	X	X	X	
Off-grid systems			X	X	X
Hybrid systems			X	X	X
Photovoltaics	X	X	X	X	X
Batteries			X		X
Main technical (T) or economical(E)	T	T	E	E	T
Optimization			X	X	
Sensitive analysis			X	X	

In this study, only HOMER has the minimum features for a comparative with our proposed verification approach. That evaluation is presented in Section 6.3.

## 90 2.2. Component models for a stand-alone PV system

A stand-alone PV system is illustrated in Fig.1. The PV generator (panel or array) is a semiconductor device that can convert solar energy into DC electricity. For night hours or rainy days, we need to hold batteries, where power can be stored and used. The use of battery as a storage form implies the presence of  
95 a charge controller [23]. The PV arrays produce DC and therefore when the PV system contains an AC load, a DC/AC conversion is required (inverter). The AC load dictates the behavior of AC electrical load from the house that will be fed by the system.

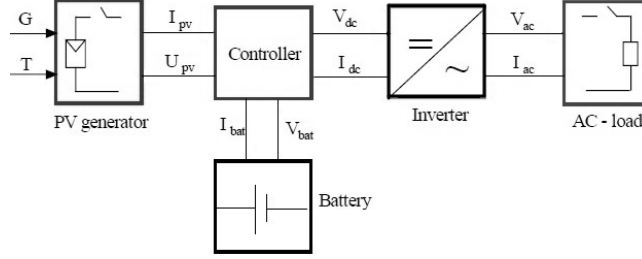


Figure 1: Block diagram for a typical stand-alone PV system [23].

### 2.3. PV generator model

100 A wide variety of models exists for estimation of power output of PV modules (and  $I-V$  or  $P-V$  curves). However, the present work will rely on the simplified model of 1-diode. It was demonstrated that it has a small error rate, between 0.03% and 4.68% from selected PV panels tested [24].

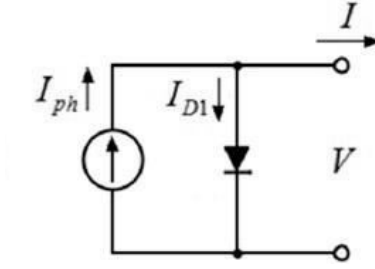


Figure 2: 1-diode equivalent PV cell/panel circuit model [25].

The 1-diode model, illustrated in Fig. 2, whose equation relates the output current,  $I$ , to the output voltage,  $V$ , is described by (1).

$$I = I_{ph} - I_{D1} = I_{ph} - I_0 \left[ \exp \left( \frac{V}{NaV_T} \right) \right], \quad (1)$$

105 where  $I_{ph}$  is the photocurrent delivered by the constant current source;  $I_0$  is the reverse saturation current corresponding to the diode;  $N$  is the number of series-connected cells;  $a$  is the ideality or quality factor ( $a = 1$  for ideal diodes and between 1 and 2 for real diodes);  $V_T$  is the thermal voltage ( $V_T = k_B T / q$ );  $k_B$  is the Boltzmann constant ( $1.3806503 \times 10^{-23} J/K$ );  $T$  the temperature of cell in Kelvin;  $q$  is absolute value of the electron's charge ( $-1.60217646 \times 10^{-19} C$ ).

The voltage and the current at the maximum power point tracking (MPPT), can be described by (2), (3), and (4) as follows [24]:

$$V_m = \frac{aNk_BT}{q} \ln \left( \frac{aNk_BT}{qI_0} \frac{I_{sc}}{V_{oc}} \right). \quad (2)$$

$$I_m = I_{ph} + I_0 - \frac{aNk_BT}{q} \left( \frac{I_{sc}}{V_{oc}} \right). \quad (3)$$

$$P_m = V_m I_m. \quad (4)$$

However, the photocurrent delivered by the constant current source ( $I_{ph}$ ) or even the reverse saturation current ( $I_0$ ) are not given by PV manufacturers. Therefore, (5) is used to calculate the photocurrent as function of irradiance and temperature [26]:

$$I_{ph} = \frac{G}{G_{ref}} [I_{ph,ref} + \mu_I (T - T_{ref})], \quad (5)$$

where the reference state (STC) of the cell is given by the solar irradiance  $G_{ref} = 1000W/m^2$  and the temperature  $T_{ref} = 298.15K (= 25^\circ C)$ ;  $\mu_I$  is the short-circuit current temperature coefficient ( $A/K$ ) (provided by PV manufacturers).  $I_{ph,ref}$  can be approximated to the reference short-circuit current [26] that is provided by PV manufacturers ( $I_{sc,ref}$ ). The cell temperature ( $T$ ) in degree Celsius is described by [27]:

$$T = T_{air} + \frac{NOCT - 20}{800} G, \quad (6)$$

110 where  $T_{air}$  is the ambient temperature,  $NOCT$  is the nominal operating cell temperature (in  $^\circ C$ ) that is found at the PV manufacturer's data-sheet [27], and  $G$  is the solar irradiance ( $W/m^2$ ) of the place where the PV system is deployed.

Furthermore, (7) permits the saturation current ( $I_0$ ) to be expressed as a  
115 function of the cell temperature as [26]

$$I_0 = \frac{I_{sc,ref} + \mu_I (T - T_{ref})}{\exp \left[ \frac{q(V_{oc,ref} + \mu_V (T - T_{ref}))}{aNk_BT} \right] - 1}, \quad (7)$$

where  $V_{oc,ref}$  is the reference open-circuit voltage and  $\mu_V$  is an open-circuit voltage temperature coefficient (V/K).

Using the maximum power point current (cf. (3)) and the saturation current in the reference temperature given by (7), the diode ideality factor [24] is determined by (8):

$$a = \frac{q(V_{m,ref} - V_{oc,ref})}{Nk_B T} \frac{1}{\ln \left( 1 - \frac{I_{m,ref}}{I_{sc,ref}} \right)}, \quad (8)$$

where  $V_{m,ref}$ ,  $V_{oc,ref}$ ,  $I_{m,ref}$ , and  $I_{sc,ref}$  are key cell values obtained under both actual cell temperature and solar irradiance conditions.

120 The PV generator model is now completely determined; it requires the actual cell temperature (or the air temperature), the actual solar irradiance and common data provided by manufacturers in data-sheets or manuals.

#### 2.4. The Battery Storage Model

Various models have been described in the literature and the most common ones are based on lead-acid batteries [28, 29]; that kind of battery has relative low cost and wide availability [28]. Here, the model adopted uses only manufacturer's data without empirical tests [28]. The discharge voltage equation is described by (9).

$$V_d = [2.085 - 0.12(1 - SOC)] - \frac{I}{C_{10}} \left( \frac{4}{1 + I^{1.3}} + \frac{0.27}{SOC^{1.5}} + 0.02 \right) (1 - 0.007\Delta T), \quad (9)$$

where  $C_{10}$  means 10h of rated capacity, which is standard on the manufacturer's data-sheet,  $\Delta T$  is temperature variation ( $\Delta T = T - T_{ref}$ ),  $SOC$  or state of charge indicates how much electric charge is stored in the cell at a given time. Mathematically, it is the ratio between the present capacity and the nominal capacity. If  $SOC = 1$ , then the battery is totally charged; and if  $SOC = 0$ , then the battery is fully discharged. The depth of discharge ( $DOD$ ) or the fraction of discharge, is  $DOC = 1 - SOC$ .

130



For the charging process, however, the parameters are described by (10) as

$$V_c = [2+0.16SOC] + \frac{I}{C_{10}} \left( \frac{6}{1+I^{0.86}} + \frac{0.48}{(1-SOC)^{1.2}} + 0.036 \right) (1-0.025\Delta T). \quad (10)$$

Note that SOC can be calculated easily at any point during the discharge period, thereby considering the current drained from batteries during a certain time period.

### 2.5. Charge Controller Model

135 The charge controller or controller is a set of items (DC-DC converter, MPPT, and switches) and can be defined as the responsible to manage the energy flow to PV system, batteries and loads by collecting information on the battery voltage and knowing the maximum and minimum values acceptable for the battery voltage. MPPT, or maximum power point tracking, is an electronic  
140 control mechanism that maintains the PV operating at the voltage of maximum power. Controllers aim to protect the battery (or batteries) against the excessive charge and discharge [29], improving its lifetime.

To protect the battery against an excessive charge, the PV arrays are disconnected from the system, when the terminal voltage increases above a certain  
145 threshold  $V_{max\_off}$  and when the current required by the load is less than the current delivered by the PV arrays [23]. PV arrays are connected again when the terminal voltage decreases below a certain value  $V_{max\_on}$ . In order to protect the battery against excessive discharge, the load is disconnected when the terminal voltage falls below a certain threshold  $V_{min\_off}$  and when the current  
150 required by the load is larger than the current delivered by the PV arrays [23]. The load is reconnected to the system, when the terminal voltage is above a certain value  $V_{min\_on}$ . The steps in the modeling of the controller process are summarized in Table 2.

The output power ( $P_{out}$ ) of controller is given by (11).

$$P_{in}\eta_c = P_{out}. \quad (11)$$

Table 2: Summary of the controller process (Source: [23])

Step	Constraint	Command
(1)	If $V > V_{max\_off}$ and $I_{load} < I_{pv}$	Disconnect PV array from the system
(2)	If command (1) is done and $V < V_{max\_on}$	Reconnect PV array to the system
(3)	If $V < V_{min\_off}$ and $I_{load} > I_{pv}$	Disconnect the load from the system
(4)	If command (3) is done and $V > V_{min\_on}$	Reconnect the load to the system

Assuming that the efficiency of the controller ( $\eta_c$ ) is a manufacturer's data, from (11) we compute (12).

$$V_{in}I_{in}\eta_c = V_{out}I_{out}, \quad (12)$$

where  $V_{in}$  is the voltage across the PV array,  $I_{in}$  is the output current of PV array,  $V_{out}$  is the DC bus voltage, and  $I_{out}$  is the output current from the converter.

## 2.6. The inverter model

The role of the inverter is to keep the voltage constant on the AC side, i.e., at the rated voltage, and to convert the input power  $P_{in}$  into the output power  $P_{out}$  with the best possible efficiency  $\eta_i$  as described by (13) [23]:

$$\eta_i = \frac{P_{out}}{P_{in}} = \frac{V_{AC}I_{AC}\cos\varphi}{V_{DC}I_{DC}}, \quad (13)$$

where  $I_{DC}$  is the current required by the inverter from the DC source to be able to keep the rated voltage on the AC side,  $V_{DC}$  is the input voltage to the inverter delivered by the DC source (PV panel or battery),  $V_{AC}$  and  $I_{AC}$  are the output voltage and current, respectively, and  $\cos\varphi$  can be obtained from the inverter's data-sheet.

### 2.7. Availability of Stand-alone PV Systems

Each stand-alone PV system, like any other power systems, has a specific level of availability. This reliability level impacts various issues, as system performance, production, feasibility, and investment. The availability of a stand-alone PV system can be defined as the percentage of time at which a power system is capable of meeting the load requirements [30]. The number of hours that the system is available, divided by 8,760 h, gives the annual system availability.

The system availability definition depends on how critical the load application is. For critical loads, 99% is considered acceptable. While in a ordinary house electrical load, 95% is considered acceptable. As an example, a system with 95% availability is expected to meet the load requirement of 8,322 h during an average year for the entire useful life of the system. An annual availability of 99% means that the system can operate the load for 8,672 h of the 8,760 h.

With that in mind, it is important to mention that even if a formal verification or a simulation shows that a PV system fails, it doesn't mean that the sizing is wrong. It is important to evaluate how critical the load application is and the horizon of evaluation. However this analysis can be useful, for example, to improve the sized battery autonomy.

## 3. Automated Verification Using Model Checking

Although simulation and testing explore possible behaviors and scenarios of a given system, they leave open the question of whether unexplored trajectories may contain a flaw. Formal verification conducts an exhaustive exploration of all possible behaviors; when a design is said to be “correct” by a formal verification method, it implies that all behaviors have been explored, and questions regarding adequate coverage or missed behavior becomes irrelevant [31]. Formal verification is a systematic approach that applies mathematical reasoning to obtain guarantees about the correctness of a system; one successful method in this domain is model checking [31]. Here we evaluate three state-of-the-art model checkers to formally verifying PV designs w.r.t. user requirements.

### 3.1. CBMC

The C Bounded Model Checker (CBMC) falsifies assertions in C programs or proves that they are safe if a completeness threshold is given [15]. CBMC implements a bit-precise translation of a C program, annotated with assertions and with loops unrolled up to a given depth, into a logical formula. If the formula is satisfiable, then a failing execution that leads to a violated assertion exists [15]. CBMC's verification flow can be summarized in three stages: (i) Front-end: scans, parses and type-checks C code; it converts control flow elements, such as *if* or *switch* statements, loops and jumps, into equivalent guarded *goto* statements, thus aiming to reduce verification effort; (ii) Middle-end: performs symbolic execution by eagerly unwinding loops up to a fixed bound, which can be specified by the user on a per-loop basis or globally, for all loops and finally; (iv) Back-end: supports SAT and SMT solvers to discharge verification conditions.

### 3.2. ESBMC

ESBMC (or Efficient SMT-based Bounded Model Checker) is a bounded and unbounded model checker for C programs [16], which supports the verification of LTL properties with bounded traces [32]. ESBMC's verification flow can be summarized in three stages: (i) a front-end that can read and compile C code, where the system formal specification is first handled; (ii) preprocessing steps to deal with code representation, control flow and unwinding of loops, and model simplification, thereby aiming to reduce verification effort; and finally (iii) the SMT solving stage, where all constraints and properties of the system are encoded into SMT and checked for satisfiability. ESBMC exploits the standardized input language of SMT solvers (SMT-LIB<sup>1</sup> logic format) to make use of a resource called *assertion stack* [33]. This enables ESBMC, and the respective solver, to learn from previous checks, thus optimizing the search procedure and potentially eliminating a large amount of formula state space to

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<sup>1</sup><http://smtlib.cs.uiowa.edu/>

be searched, because it solves and disregards data during the process, incrementally. This technique is called “incremental SMT” [34] and allows ESBMC to reduce the memory overhead, mainly when the verified system is complex and the computing platform does not have large amount of memory to deal with the entire design space state.

### 3.3. CPAChecker

Configurable program analysis (CPA) provides a conceptual basis for expressing different verification approaches in the same formal setting. The CPA formalism provides an interface for the definition of program analyses; consequently, the tool CPAChecker provides an implementation framework that allows the seamless integration of program analyses that are expressed in the CPA framework. The comparison of different approaches in the same experimental setting is intended to be easy and the experimental results is expected to be more meaningful [35]. Related to the architecture, the central data structure is a set of control-flow automata (CFA), which consist of control-flow locations and control-flow edges. The CPA framework provides interfaces to SMT solvers and interpolation procedures, such that the CPA operators can be written in a concise and convenient way [35]. Currently CPAChecker uses MathSAT as an SMT solver, and CSIsat and MathSAT as interpolation procedures [35]. The CPA algorithm performs the reachability analysis, and operates on an object of the abstract data type CPA, i.e., the algorithm applies operations from the CPA interface without knowing which concrete CPA it is analyzing. For most configurations, the concrete CPA will be a composite CPA, which implements the combination of different CPAs. In software verification, its usual to take a considerable amount of effort to convert a verification idea into actual experimental results — and CPAChecker aim to accelerate this process [35].

## 4. Stand-alone PV System Sizing and Verification

In addition to the verification tool being able to check a PV solar system, as if it were actually being used in the field, indicating the conditions that it does

not meet the system user requirements, it is possible to extend the tool, giving it the capacity to carry out the validation of the designed system (a.k.a. sizing check).  
 250

Therefore this is a additional feature included at this paper. The sizing check will be performed by the proposed tool, and it will indicate if there is an error of sizing before to perform the automated verification of the system. This stage ensures that the system meets the standard project steps related to worst monthly average solar energy [29]. Firstly, it is needed to correct the energy consumption estimated to the load ( $E_{consumption}$ ), which is carried out by (14), where the efficiency of batteries ( $\eta_b$ ), controller ( $\eta_c$ ), and the inverter ( $\eta_i$ ) are considered [29].

$$E_{corrected} = \frac{E_{consumption}}{\eta_b \eta_c \eta_i}. \quad (14)$$

Following, it is necessary to estimate the energy that can be produced for each panel, called  $E_p$ , in Wh, as defined by (15).

$$E_p = Solar\_Irradiance \times Panel\_Area \times \eta_p \times 1000, \quad (15)$$

where the solar irradiance is expressed in terms of  $kWh/m^2$  and depends on the site where the PV systems will be deployed, the PV panel area is given in  $m^2$  and corresponds to the size of one PV panel, and  $\eta_p$  represents the PV panel efficiency.  
 255

The total minimum number of needed solar panels ( $N_{TPmin}$ ) is computed by (16) and the check is performed using (17), where the sized number of panels ( $N_{TP}$ ) must be greater than the result from (16).

$$N_{TPmin} = \frac{E_{corrected}}{E_p}. \quad (16)$$

$$N_{TP} \geq N_{TPmin}. \quad (17)$$

Particularly, the total number of panels in series ( $N_{PSmin}$ ) and parallel ( $N_{PPmin}$ ) are given by (18) and (19), respectively. With the check performed by (20) and (21). Where  $V_{mppt,max}$  is the maximum operation voltage and

260  $V_{mppt,min}$  is the minimum operation voltage of the charge controller;  $V_{maxPower,TempMax}$  and  $V_{maxPower,TempMin}$  are the maximum power voltage from the PV module considering the maximum and minimum operational temperature, respectively;  $P_{total}$  is the total power demanded from the PV system and  $P_{max,ref}$  is the power supplied from one PV panel in *Watts*.

$$\frac{V_{mppt,min}}{V_{maxPower,TempMax}} \leq N_{PSmin} \leq \frac{V_{mppt,max}}{V_{maxPower,TempMin}}. \quad (18)$$

$$N_{PPmin} = \frac{P_{total}}{Number\ Panels\ Series \times P_{max,ref}}. \quad (19)$$

$$N_{PS} \geq N_{PSmin}. \quad (20)$$

$$N_{PP} \geq N_{PPmin}. \quad (21)$$

Related to the batteries, firstly must be defined the total capacity of the battery bank, as described by (22) as

$$C_{bank} = \frac{E_{corrected} \times autonomy}{V_{system} \times DOD}. \quad (22)$$

where the variable *autonomy* is a design definition;  $V_{system}$  is the DC voltage of the bus, and the other variables were discussed previously in Section 2.3 and 2.4. Secondly, the total (minimum) number of batteries is computed, as described by (23). Additionally, (24) performs the final sizing check, thus considering the number of batteries in series ( $N_{BS}$ ) and the number of batteries in parallel ( $N_{BP}$ ) that are established to the project.

$$N_{Btotal} = N_{BSmin} \times N_{BPmin} = \frac{V_{system}}{V_{bat}} \times \frac{C_{bank}}{1\ Battery\ Capacity}. \quad (23)$$

$$(N_{BS} \times N_{BP}) \geq N_{Btotal}. \quad (24)$$

Related to the charge controller, initially it must meet the voltage requirement of the PV system, as described by (25) to the charge controller voltage:

$$V_c = V_{system}. \quad (25)$$

Following, the short circuit reference information from the manufacturer's solar panel must be corrected to the cell temperature, as described by (26):

$$I_{sc,amb} = \frac{G}{G_{ref}} [I_{sc,ref} + \mu_I \times (T - 25)]. \quad (26)$$

The controller must meet the maximum current from the PV array given by (27) and (28).

$$I_{c,min} = I_{sc,amb} \times N_{PP}. \quad (27)$$

$$I_c \geq I_{c,min}. \quad (28)$$

The sizing project check of the inverter is carried out by means of three equations. Equation (29) ensures that the input voltage of the controller meets the system voltage. Equation (30) ensures that the output voltage of the controller meets the AC voltage of the load. Finally, (31) ensures that the controller can support the total demand of the load and the surge power. Where  $V_{in}DC$  is the nominal input voltage and  $V_{out}AC$  is the nominal output voltage of the inverter;  $MAX_{AC,ref}$  is the peak power that the inverter can support.

$$V_{in}DC = V_{system}. \quad (29)$$

$$V_{out}AC = V_{AC}. \quad (30)$$

$$[(Demand \leq P_{AC,ref}) \text{ and } (P_{surge} \leq MAX_{AC,ref})]. \quad (31)$$

265 Worth to mention that the charge controller, the battery, and the inverter have a nominal efficiency presented at data sheets, and those numbers are very close to 100%. However, based on empirical data, those efficiencies must be corrected, according to the loading of each component. If field or essay data is not available, considering that the proposed tools is aimed to be used prior



270 the deployment of the PV system at the field, it is recommended (at least) to  
correct the battery efficiency ( $\eta_b$ ) to 85%, keeping the remaining efficiencies as  
expressed by the manufacturers.

## 5. Proposed Automated Verification Method of PV Systems

275 The flowchart of the proposed automated verification method is illustrated  
in Fig. 3.

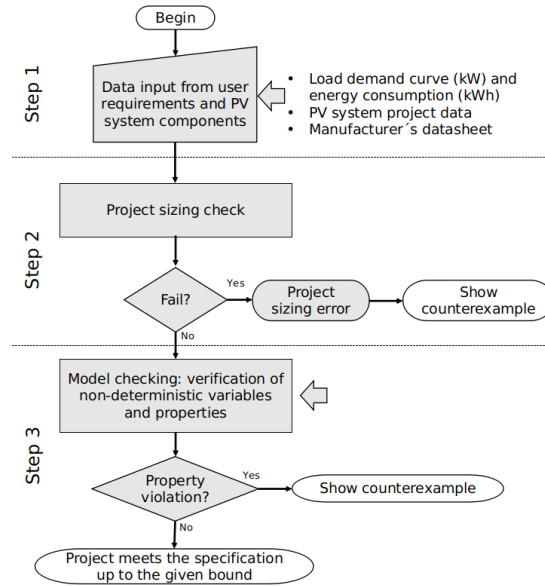


Figure 3: Flowchart of the proposed automated verification of PV systems.

In Step 1, the PV input data (e.g., load power demand and load energy consumption) and the formulae to check the sizing project, the mathematical model, the limits of the weather non-deterministic variables, are all written as an ANSI-C code [36]. In Step 2, the sizing check of the PV system takes place  
280 to make sure that the components were selected according to worst monthly average solar energy method [29]. The equations to check the PV sizing are present at Section 4. In Step 3, weather variables (e.g., solar irradiance and ambient temperature) will be systematically explored by our verification engine

based on maximum and minimum values from the site, where the PV system  
will be deployed. In addition, depending on one of the desired properties of  
the system such as battery autonomy, energy availability, or even system power  
supply, our verification engine is able to indicate a failure if those properties are  
not met; in this particular case, it provides a diagnostic counterexample that  
shows in which conditions the property violation occurred.

In a nutshell, the model checker will process the ANSI-C code with constraints and properties from the PV system that are provided by the user, and the tool will automatically verify if the PV system requirements are met. If it returns a failure (i.e., SAT), then the tool provides a counterexample, i.e., a sequence of states that leads to the property violation; this information can be used as a feedback to improve the PV system design. However, if the verification succeeds (i.e., UNSAT), there is no failure up to the bound  $k$ ; therefore, the PV system will present its intended behavior up to the bound  $k$ .

Algorithm 1 describes the pseudo-code used to perform the automated verification. The batteries are assumed to have SOC of 100% (Line 1), i.e., the batteries are charged. That is important because the system is said ready to use when the batteries are charged.

Information related to average temperature ( $T$ ) and solar irradiance ( $G$ ), maximum and minimum annual, are given to the algorithm in Lines 7 to 10 using non-deterministic variables from model checker to explore all possible states and the *assume* macro to constrain the non-deterministic values using a given range. In order to reduce the computational effort of the algorithm, every 24h-day was considered as a time-step of 1 hour, and it was split into two parts: (a) one where it is possible to occur PV generation, during daylight, with a duration in hours depending on each site (but dependent on the sun and weather conditions); and (b) one that includes all the remaining day (without any PV generation). Therefore, our approach depends on specific data about the solar irradiation levels to define the average amount of hours of PV generation.

After that, the model from PV generator is used in the function call of Line 7, to produce the voltage and current considering the states of  $G$  and  $T$ . With

315 respect to every hour considered, the conditional *if-else-endif* statements from Lines 8, 11, 13, 16 and 19, will perform the charge or discharge of batteries according to the value of different variables: if there is PV generation (which depends on  $G$  and  $T$ ), the updated state of charge from batteries, the house's load and the set-up information of the PV system.

320 Next, representing the time of the day where PV generation is not possible anymore, starting in Line 22, the algorithm will only discharge the batteries (using the 1 hour step) until a new charging process (at the next day) starts. Specific *assert* in Line 26 will check the state of charging from batteries, and they will violate the property if their levels reach the minimum that represents  
 325 a discharged battery; therefore, the PV system is unable to supply energy to the house. Nevertheless, if the verification engine does not fail, then we can conclude that the PV system does not need further corrections up to the given bounds.

## 6. Experimental Evaluation

### 330 6.1. Description of the Case Studies

We have performed five case studies to evaluate our proposed verification method: (a) four PV systems (three in series 325W PV panels, four 220 Ah batteries in a configuration with two series and two parallel with 48h autonomy, 700 W inverter with surge of 1,600W, charge controller with MPPT with  
 335 35A/150V of capacity) deployed in four different houses in an indigenous community (GPS coordinates 2°44'50.0"S 60°25'47.8"W) situated nearby Manaus (Brazil), with each house having a different power demand (house 1 = 253 W, house 2 = 263 W, house 3 = 283 W, and house 4 = 501 W); and (b) one case concerning a system deployed as an individual system in Manaus (GPS coordinates  
 340 3°4'20.208"S 60°0'30.168"W), supporting 915 W of the house's load (house 5 with four 325W PV panels in a configuration two series and two parallel, four 120Ah batteries in series and autonomy of just 6 h, 1,200 W inverter with surge of 1,600 W, charge controller with MPPT of 150V/35A).

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**Algorithm 1** Model checking algorithm for stand-alone PV

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```
1: declare min and max solar irradiation[24h], and temperature[24h]
2: declare case studies details : sizing and manufacturers data
3: sizing_check()
4: startPVgeneration  $\leftarrow$  findStartPVgeneration()
5: endPVgeneration  $\leftarrow$  findEndPVgeneration()
6: SOC  $\leftarrow$  100%
7: for 1st 24h loop to Nth 24h loop do
8:   for endPVgeneration + 1 to startPVgeneration - 1 do
9:     dischargeBattery in 1h()
10:    assert(SOC  $\geq$  SOC_min)
11:   end for
12:   for startPVgeneration to endPVgeneration do
13:     G  $\leftarrow$  nondet_uint() {G is non-deterministic variable}
14:     T  $\leftarrow$  nondet_uint() {T is non-deterministic variable}
15:     assume (Gmin  $\leq$  G  $\leq$  Gmax) {restricting G values}
16:     assume (Tmin  $\leq$  T  $\leq$  Tmax) {restricting T values}
17:     Imax, Vmax  $\leftarrow$  PVgenerationMODEL(G, T)
18:     {If-then-else sequence to imitate charge controller work}
19:     if (battery is empty) AND (PV is generating) then
20:       chargeBattery in 1h() {PV feed the house}
21:     else if (battery is empty) AND NOT(PV is generating) then
22:       FAIL with assert macro {Battery is empty and there is not PV generation}
23:     else if NOT(battery is empty) AND (PV is generating) then
24:       stop battery charge {PV feed the house}
25:     else if NOT(battery is empty) AND NOT(PV is generating) then
26:       dischargeBattery in 1h() {Battery feed the house}
27:     end if
28:     assert(SOC  $\geq$  SOC_min)
29:     hour  $\leftarrow$  hour + 1
30:   end for
31: end for
32: return ()
```

---

Note that the annual average temperature ( $T$ ) in Manaus is from 23°C to 32°C; and irradiance ( $G$ ) varies from 274 W/m<sup>2</sup> to 852 W/m<sup>2</sup> when there is sunlight (that information is provided in Lines 5 and 6 of Algorithm 1). Another characteristic of Manaus, based on historical weather data [37], is related to the fact that only during 8 hours of the day is possible to have PV generation, from 8:00h to 16:00h (that information is provided in Algorithm 1 as well).

## 6.2. Objectives and Setup

Our experimental evaluation aims to answer two research questions:

RQ1 (**soundness**) Does our approach provide correct results?

RQ2 (**performance**) How does our approach compare against other existing tools?

All experiments were conducted on an otherwise idle Intel octa core Xeon CPU E5-2640 with 2.4 GHz and 264 GB of RAM, running Ubuntu 18.04.1 LTS 64-bits. Concerning the verification engine, ESBMC v6.0.0 was used <sup>2</sup>. We have also used the SMT solver Boolector version 2.4.1 [38].

In order to evaluate the proposed verification method and its performance, we have considered five case studies and also compared its performance to the HOMER Pro tool. Experimental setup of HOMER Pro: Intel Core i5-4210 (4-cores), with 1.7 GHz and 4 GB of RAM, running Microsoft Windows 10; we have used HOMER Pro v3.12.0.

## 6.3. Results and Discussion

The description of our experimental results can be broken down into two parts: (a) the 1,200 W PV system (house 5) failed during the sizing check since the number of panels was *incorrectly* sized; in particular, the counterexample provided by our verification engine indicated 3 PV panels in parallel and the

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<sup>2</sup>The command-line used to perform the verification is: `$ esbmc filename.c --no-bounds-check --no-pointer-check --no-div-by-zero-check --unwind 300 --boolector`

actual project has 2 in series and 2 in parallel. This verification took approx-  
370 imately 0.57 hours to be performed. In order to validate this possible flaw, it  
was surveyed the owner of the 1,200 W system; we identified that, in fact, the  
system does not meet the battery autonomy most of the time (mainly when  
all loads are turned on), and this was double checked with the monitoring sys-  
tem from the charge controller from the manufacturer who showed that the  
375 maximum power or surge power were not exceeded, thus affirming RQ1; this  
behavior is expected since the system was purchased as an off-the-shelf solution  
and not as a customized design for the electrical charges of the house; (b) For  
the 700 W PV systems of houses 2, 3, and 4, the sizing check was successful  
during verification, but our verification engine has found flaws related to the  
380 battery autonomy, particularly when SOC reached a empty-battery level. Our  
verification engine identified those flaws (for those three houses) right after the  
first night-discharge cycle, i.e., before the solar system started to recharge the  
batteries. Our verification engine took approximately 5.1 hours to find this flaw  
in house 2; 5.8 hours for house 3, and 4.4 hours for house 4. These flaws were  
385 confirmed with the dwellers who own the systems by an interview process and  
from a local monitoring system with the Raspberry Pi controller: at least once  
a month is usual the system to turn off, normally in raining or clouds days,  
thereby reaching the situation described in Step 3 of Table 2, further affirming  
RQ1; after the sun rises, the systems returns to normal condition operation. One  
390 more time the flaws were not caused by misuse of the system by the dwellers.  
Fig. 4 shows the monitoring result for the load curve of house 2 from June to  
July of 2018 (5 weeks), without undesired peaks from power demand of even  
unexpected energy consumption. The house 1 had an inconclusive result with  
the automated verification, because the solver did not presented any result from  
395 the SMT verification.

The same five case studies were evaluated by HOMER Pro. The simulation  
results showed that the project restrictions were met by four 700 W PV systems  
(house 1, 2, 3 and 4), without any indication of sizing error or even performance  
related issues. The case study that was unsuccessful during simulation was the

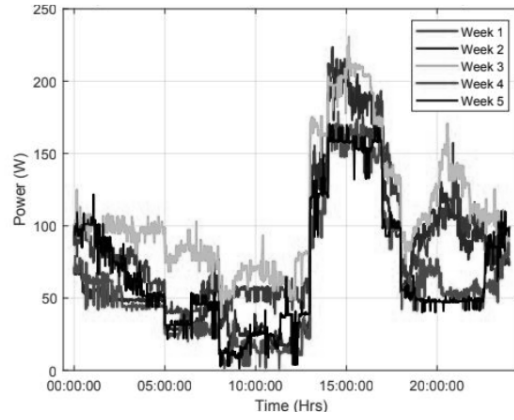


Figure 4: Five weeks monitored load curve from House 1.

1,200 W (house 5); however, without any indication about the failures of this PV system. All the simulations took less than 5 seconds (each) to be performed by HOMER Pro. Fig. 5 shows one of the screens presented by HOMER Pro software, specifically to house 1.

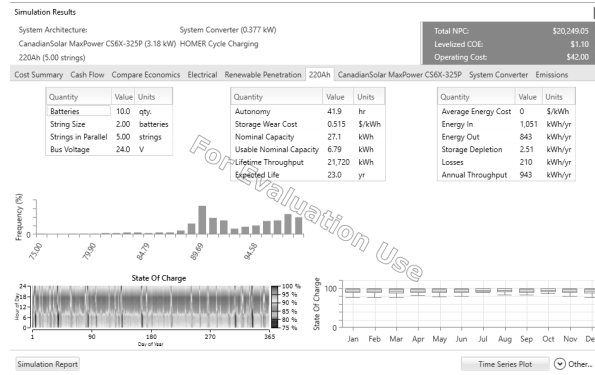


Figure 5: Homer simulation screen.

Despite the divergence of results for the houses 2, 3 and 4 w.r.t. our proposed approach, it is evident that the information collected from the dwellers and from the monitoring systems indicate that our approach provides the correct evaluation of the PV system, thus answering RQ2. House 5 presented flaws from both tools; however, only our approach indicated which design error was

responsible for the flaw (number of PV panels), further answering RQ2.

#### 410 6.4. Threats to Validity

We have reported a favorable assessment of the proposed method. Nevertheless, we have also identified three threats to the validity of our results that can further be assessed.

*Model precision:* each component of the PV system is mathematically modeled. A careful evaluation in a PV laboratory to validate the model could add  
415 more reliability to the results produced by our method.

*Time step:* The run-time complexity of our proposed method is an issue; the time step of one hour can be further reduced to approximate the algorithm to the real-world scenario, where a solar irradiance and ambient temperature  
420 can change in fractions of minutes.

*Case studies:* Our case studies are performed only in one municipality. A more complete evaluation can be performed if other places around the world could become case studies.

## 7. Conclusions and Future Work

425 We have described and evaluated an automated verification method to check whether a given PV system meets its specification using software model checking techniques. We have considered five case studies from real photovoltaic systems deployed in five different sites, ranging from 700 W to 1,200 W. Although this verification method takes longer than simulation methods, it is able to find  
430 specific conditions that lead to failures in a PV system previously validated by a commercial simulation tool. In particular, the proposed method was successful in finding sizing errors and indicating in which conditions a PV system can fail. As future work, the proposed method will be extended to start from a list of commercial equipment, where each equipment is verified and the final solution,  
435 which satisfies the project specification, is found, thus leading to an optimum sizing of PV systems. We will also consider other types of renewable energy



and even hybrid ones to allow our method to design and verify typical rural electrification.

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