Sandbox

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Chapter 1

Sandbox for playing with pandoc/slate

Normal table

Operation	Self	Peer	Host	All
Regular read	448.59	14.01	444.74	12.17
Regular write	442.98	16.21	16.18	12.17
Regular update	248.80	11.71	0.0028	6.00
Random read	6.78	1.43	2.39	4.04
Random write	6.63	1.14	3.47E-5	3.82
Random update	3.44	0.83	1.92E-5	2.08

Pretty wide table

Parts	Comp. cost	Comm.	Comp. to comm.	Scalak	oi M emory usage
Modularity optimization	10(E + V) /p	20V bytes	E/p : 2V	v	88E/p + 12V bytes
Graph contraction	5E / p + E'	8E' bytes	5E/p + E' : 8E'	Hard	16E' bytes
Louvain	10(E + V) / p	20V bytes	E/p: 2V	Okay	88E/p + 12V + 16E' bytes

Pretty wide table, with math

Parts	Comp. cost	Comm.	Comp. to comm.	Scalab	oi M gemory usage
Modularity optimization	10(E+V)/p	20V bytes	E/p:2V	Okay	88E/p + 12V bytes
Graph contraction	5E/p + E'	8E' bytes	$\begin{array}{l} 5E/p + E': \\ 8E' \end{array}$	Hard	16E' bytes
Louvain	10(E+V)/p	20V bytes	E/p: 2V	Okay	88E/p + 12V + 16E' bytes

JDO hacked version of above

Parts	Comp cost	Comm cost	Comp/comm ratio	Scalability	Memory usage (B)
Modularity optim. Graph contraction Louvain	10(E + V) /p	20V bytes	E/p: 2V	Okay	88E/p + 12V
	5E / p + E'	8E' bytes	5E/p + E': 8E'	Hard	16E'
	10(E + V) / p	20V bytes	E/p: 2V	Okay	88E/p + 12V + 16E'

and with math!

Parts	Comp cost	Comm cost	Comp/comm ratio	Scalability	Memory usage (B)
<i>U</i> 1	10(E+V)/p 5E/p+E'	20V bytes $8E'$ bytes	E/p : 2V 5E/p + E' : 8E'	Okay Hard	88E/p + 12V $16E'$
Louvain	10(E+V)/p	20V bytes	E/p:2V	Okay	88E/p + 12V + 16E'

Even wider table

Parts	Comp.	Comm.	Comp. to comm. ratio	Scalability	Memory usage
Wedge	dE/p				
generation					
Wedge	0	$aE/p \times 12$			
communication		bytes			
Wedge checking	aE/p x				
	log(d)				
AllReduce	2V	$2V \times 4$			
		bytes			
Triangle	(d + a x)	$aE/p \times 12$	\sim (d + a x	Okay	
Counting	$\log(d))E/p$	0 + 8V bytes	log(d)): 12a		
	+ 2V				
Scan Statistics	(d + a x)	12aE/p +	$\sim (d + a x)$	Okay	
(wedge checks)	$\log(d)$ E/p	8V bytes	log(d)): 12a		
	+ 2V +				
	V/p				
Scan Statistics	Vdd +	8V bytes	dd: 8	Perfect	
(intersection)	V/p				

	Comp.	Comm.	Comp. to		Memory
Parts	cost	cost	comm. ratio	Scalability	usage

Even wider table, with math!

	Comp.	Comm.	Comp. to		Memory
Parts	$\cos t$	cost	comm. ratio	Scalability	usage
Wedge generation	dE/p				
Wedge communication	0	$aE/p \times 12$ bytes			
Wedge checking	$aE/px\log$	$\zeta(d)$			
AllReduce	2V	$2V \times 4$ bytes			
Triangle	(d +	aE/px12 +	$(d + a \cdot \log(d))$:	Okay	
Counting	$ax \log(d))$ $2V$	E\$1/2+bytes	12a	-	
Scan Statistics (wedge checks)		12aE/p+ E%P+bytes	$(d+a\cdot\log(d)):$ 12a	Okay	
Scan Statistics (intersection)	, 1	8V bytes	dd:8	Perfect	

JDO hacked version of above

	Comp.	Comm. cost		
Parts	cost	(B)	Comp/comm ratio	Scalability
Wedge generation	dE/p			
Wedge	0	$aE/p \times 12$		
communication				
Wedge checking	aE/p x log(d)			
AllReduce	2V	$2V \times 4$		
Triangle Counting	$\begin{array}{l} (d + a x \\ log(d))E/p \\ + 2V \end{array}$	aE/p x 12 + 8V	$ \stackrel{\sim}{(d + a \times \log(d))} : $ 12a	Okay
Scan Statistics	$(d + a x \log(d))E/p$	12aE/p + 8V	\sim (d + a x log(d)) : 12a	Okay
(with wedge checks)	+ 2V + V/p			
Scan Statistics	Vdd + V/p	8V	dd: 8	Perfect
(with intersection)				

Table with line breaks

Application	Computation to communication ratio	Scalability	Implementation difficulty
Louvain	E/p : 2V	Okay	Hard
Graph SAGE	$\sim CF : min(C, 2p)x4$	Good	Easy
Random walk	Duplicated graph: infinity	Perfect	Trivial
	Distributed graph: 1:24	Very poor	Easy
Graph search: Uniform	1:24	very poor	Easy
Graph search: Greedy	Straight forward: d : 24 Pre-visit: 1:24	Poor very poor	Easy Easy
Graph search: Stochastic greedy	Straight forward: d : 24 Pre-visit: log(d) : 24	Poor very poor	Easy Easy
Geo location	Explicit movement: 25E/p:	Okay	Easy Easy
	4V UVM or peer access: 25:	Good	
Vertex nomination	$E: 8V \times min(d, p)$	Okay	Easy
Scan statistics	Duplicated graph: infinity	Perfect	Trivial
	Distributed graph: \sim (d + a * $\log(d)$) : 12	Okay	Easy
Sparse fused lasso	~ a:8	Less than okay	Hard
Graph projection	Duplicated graph : infinity Distributed graph : dE/p + E' : 6E'	Perfect Okay	Easy Easy
Local graph clustering	(6 + d)/p : 4	Good	Easy
Seeded graph matching Application	, ,, <u>,</u>		-
classification			

JDO hacked version of above

	Computation to		Implementation
Application	communication ratio	Scalability	diff.
Louvain	E/p: 2V	Okay	Hard
Graph SAGE	$\sim CF : min(C, 2p)x4$	Good	Easy
Random walk	Duplicated graph: infinity	Perfect	Trivial
Random walk	Distrib. graph: 1 : 24	Very poor	Easy
Graph search: Uniform	1:24	Very poor	Easy
Graph search: Greedy	Straightforward: d: 24	Poor	Easy
Graph search: Greedy	Pre-visit: 1:24	Very poor	Easy
G.S.: Stochastic greedy	Straightforward: d : 24	Poor	Easy
G.S.: Stochastic greedy	Pre-visit: $log(d)$: 24	Very poor	Easy
Geolocation	Explicit movement: $25E/p$: $4V$	Okay	Easy
Geolocation	UVM or peer access: 25 : 1	Good	Easy
Vertex nomination	$E: 8V \times \min(d, p)$	Okay	Easy
Scan statistics	Duplicated graph: infinity	Perfect	Trivial

Application	Computation to communication ratio	Scalability	Implementation diff.
Scan statistics	Distrib. graph: \sim (d + a * $\log(d)$) : 12	Okay	Easy
Sparse fused lasso	~ a:8	Less than okay	Hard
Graph projection	Duplicated graph: infinity	Perfect	Easy
Graph projection	Distrib. graph : $dE/p + E'$: $6E'$	Okay	Easy
Local graph clustering	(6 + d)/p : 4	Good	Easy

Really wide table

Parts	Comp.	Comm.	Comp. to comm. ratio	Scalability	Memory usage
Feature duplication					
Children selection	BC	8BC bytes	1:8	Poor	
Child-centric comp.	BCF x (2 + L + Wf1.y + Wa1.y)	4B x (F + Wf1.y + Wa1.y) x min(C, 2p) bytes	\sim CF : min(C, 2p) x 4	Good	
Source-centric comp.	B x (CF + (Wf1.y + Wa1.y) x (C + F + Wf2.y + Wa2.y)	0 bytes	N.A.	N.A.	
Graph SAGE	B x (C + 3CF + 3LCF + (Wf1.y + Wa1.y) x (CF + C + F + Wf2.y + Wa2.y))	8BC + 4B x (F + Wf1.y + Wa1.y) x min(C, 2p) bytes	at least \sim CF : min(C, 2p) x 4	Good	

 $\begin{array}{c} Direct\ feature\\ access \end{array}$

	Comp.	Comm.	Comp. to		Memory
Parts	cost	cost	comm. ratio	Scalability	usage
Child-centric comp.	BCF x (2 + L + Wf1.y + Wa1.y)	4B x ((F + Wf1.y + Wa1.y) x min(C, 2p) + CLF) bytes	~ (2 + L + Wf1.y + Wa1.y) : 4L	poor	
Graph SAGE	B x (C + 3CF + 3LCF + (Wf1.y + Wa1.y) x (CF + C + F + Wf2.y + Wa2.y))	8BC + 4B x (F + Wf1.y + Wa1.y) x min(C, 2p) + 4BCFL bytes	~ (2 + L + Wf1.y + Wa1.y) : 4L	poor	
$Feature \ in \\ UVM$					
Child-centric comp.	BCF x (2 + L + Wf1.y + Wa1.y)	4B x (F + Wf1.y + Wa1.y) x min(C, 2p) bytes over GPU-GPU + 4BCLF bytes over	~ (2 + L + Wf1.y + Wa1.y) : 4L over GPU-CPU	very poor	
Graph SAGE	B x (C + 3CF + 3LCF + (Wf1.y + Wa1.y) x (CF + C + F + Wf2.y + Wa2.y))	GPU-CPU 8BC + 4B x (F + Wf1.y + Wa1.y) x min(C, 2p) bytes over GPU-GPU + 4BCFL bytes over GPU-CPU	~ (2 + L + Wf1.y + Wa1.y) : 4L over GPU-CPU	very poor	

Really wide table, with math

	Comp.	Comm.	Comp. to		Memory
Parts	cost	cost	comm. ratio	Scalability	usage

 $Feature \\ duplication$

	Comp.	Comm.	Comp. to		Memory
Parts	$\cos t$	cost	comm. ratio	Scalability	usage
Children selection	BC	8BC bytes	1:8	Poor	
Child-centric comp.	$BCF \cdot (2 + L + Wf1.y + Wa1.y) 4I$ $(F + Wf1.y + Wa1.y) \cdot \min(C, 2p)$ bytes		Good		
Source-centric comp.	$B \cdot (CF + (Wf1.y + Wa1.y) \cdot (C + F + Wf2.y + Wa2.y)$	0 bytes	N.A.	N.A.	
Graph SAGE	$B \cdot (C + 3CF + 3LCF +$	$8BC + 4B \cdot (F + Wf1.y + Wa1.y) \cdot \min(C, 2p)$ bytes	at least CF : $\min(C, 2p) \cdot 4$	Good	
Direct feature access	DCE	4D (/E)	(0 I W.f1		
Child-centric comp.	$BCF \cdot (2 + L + Wf1.y + Wa1.y)$	$4B \cdot ((F + Wf1.y + Wf1.y + Wa1.y) \cdot \min(C, 2p) + CLF)$ bytes	(2+L+Wf1.y+Wa1.y):4L	poor	
Graph SAGE	$B \cdot (C + 3CF + 3LCF + (Wf1.y + Wa1.y) \cdot (CF + C + F + Wf2.y + Wa2.y))$	8BC +	(2+L+Wf1.y+Wa1.y):4L	poor	

 $Feature\ in \\ UVM$

Parts	Comp.	Comm.	Comp. to comm. ratio	Scalability	Memory usage
Child-centric comp.	$\begin{array}{l}(2+L+\\Wf1.y+\end{array}$	Wf1.y +	(2+L+Wf1.y+Wa1.y): 4L over GPU-CPU	very poor	
Graph SAGE	$3CF + 3LCF + (Wf1.y+Wa1.y) \cdot (CF + C + F + Wf2.y + CF + CF + Wf2.y + CF + CF + Wf2.y + CF + C$	$8BC + 4B \cdot (F + Wf1.y +$	(2+L+Wf1.y+Wa1.y): 4L over GPU-CPU	very poor	

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Parts	Comp. cost
Feature duplication	
Children selection	BC
Child-centric comp.	$BCF \times (2 + L + Wf1.y +$
-	Wa1.y)
Source-centric comp.	$B \times (CF + (Wf1.y +$
	Wa1.y) x (C + F + Wf2.y
	+ Wa2.y)
Graph SAGE	$B \times (C + 3CF + 3LCF +$
	$(Wf1.y + Wa1.y) \times (CF +$
	C + F + Wf2.y + Wa2.y))
Direct feature access	
Child-centric comp.	$BCF \times (2 + L + Wf1.v +$
•	Wa1.y)
Graph SAGE	$B \times (C + 3CF + 3LCF +$
	$(Wf1.y + Wa1.y) \times (CF +$
	C + F + Wf2.y + Wa2.y)
Feature in UVM	
Child-centric comp.	BCF x $(2 + L + Wf1.y +$
r·	
	Wa1.y)

Parts	Comp. cost
Graph SAGE	B x (C + 3CF + 3LCF + (Wf1.y + Wa1.y) x (CF + C + F + Wf2.y + Wa2.y))

Parts	Comm. cost
Feature duplication	
Children selection	8BC bytes
Child-centric comp.	$4B \times (F + Wf1.y + Wa1.y) \times min(C, 2p)$ bytes
Source-centric comp.	0 bytes
Graph SAGE	$8BC + 4B \times (F + Wf1.y +$
	Wa1.y) $x \min(C, 2p)$ bytes
Direct feature access	
Child-centric comp.	$4B \times ((F + Wf1.y + Wa1.y) \times min(C, 2p) + CLF)$ bytes
Graph SAGE	8BC + 4B x (F + Wf1.y + Wa1.y) x min(C, 2p) + 4BCFL bytes
Feature in UVM	
Child-centric comp.	4B x (F + Wf1.y + Wa1.y) x min(C, 2p) bytes over GPU-GPU + 4BCLF bytes over GPU-CPU
Graph SAGE	8BC + 4B x (F + Wf1.y + Wa1.y) x min(C, 2p) bytes over GPU-GPU + 4BCFL bytes over GPU-CPU

Parts	Comp/comm ratio	Scalability
Feature duplication		
Children selection	1:8	Poor
Child-centric comp.	$\sim CF : min(C, 2p) \times 4$	Good
Source-centric comp.	N.A.	N.A.
Graph SAGE	at least $\sim CF : min(C, 2p) \times 4$	Good
Direct feature access		
Child-centric comp.	$\sim (2 + L + Wf1.y + Wa1.y) : 4L$	poor
Graph SAGE	$\sim (2 + L + Wf1.y + Wa1.y) : 4L$	poor
Feature in UVM		
Child-centric comp.	$\sim (2 + L + Wf1.y + Wa1.y) : 4L \text{ over GPU-CPU}$	very poor
Graph SAGE	\sim (2 + L + Wf1.y + Wa1.y) : 4L over GPU-CPU	very poor