Trójkąty o kątach 90,45,45 oraz 90,30,60 - odpowiedzi

GRUPA A

1.
$$12\sqrt{5} + 6\sqrt{10}$$

$$2. 6 + \frac{12}{\sqrt{2}} = 6 + 6\sqrt{2}$$

3.
$$18 + 18\sqrt{3}$$

- 4. C
- 5. D

6.
$$25 + 25\sqrt{3}$$
, $25\sqrt{2}$, 50

- 7. A
- 8. N, N, N, T
- 9. $32\sqrt{3}$ cm²

10.
$$\frac{18}{\sqrt{3}} + 6 = 6\sqrt{3} + 6$$

11. C

12. Pole =
$$48 + \frac{8}{\sqrt{3}} = 48 + \frac{8}{3}\sqrt{3}$$
, obwód = $24 + \frac{12}{\sqrt{3}} + 4\sqrt{2} = 24 + 4\sqrt{2} + 4\sqrt{3}$

13.
$$9\sqrt{3} + 9$$

$$14.\ 48\sqrt{3}\ cm^2,\ 12\sqrt{3}\ cm^2,\ 24\sqrt{3}\ cm^2,\ 24\sqrt{3}\ cm^2$$

15.
$$(36 + 9\sqrt{3})$$
 cm²

16.
$$x = 8\sqrt{3}$$
, $y = 9\sqrt{6}$

- 17. 1,4 m
- 18. Około 327 m.
- *19. $75\sqrt{3}$
- *20.

*21.
$$(18 + 18\sqrt{3})$$
 cm

GRUPA B

1.
$$10\sqrt{3} + 5\sqrt{6}$$

$$2.\ 3 + \frac{6}{\sqrt{2}} = 3 + 3\sqrt{2}$$

3.
$$4,5 + 4,5\sqrt{3}$$

- 4. D
- 5. D

6.
$$30 + 30\sqrt{3}, 30\sqrt{2}, 60$$

- 7. C
- 8. T, T, N, N

9.
$$50\sqrt{3}$$
 cm²

$$10.\ \frac{30}{\sqrt{3}} + 10 = 10\sqrt{3} + 10$$

- 11. D
- 12. Pole = $\frac{69\sqrt{3}+27}{2}$, obwód = $29 + 3\sqrt{3} + 3\sqrt{6}$
- 13. $\frac{9\sqrt{3}}{4} + \frac{9}{4}$
- 14. $27\sqrt{3}$ cm², $3\sqrt{3}$ cm², $9\sqrt{3}$ cm², $9\sqrt{3}$ cm²
- 15. $12\sqrt{3}$ cm²
- 16. $x = 11\sqrt{3}, y = 15\sqrt{6}$
- 17. 1,5 m
- 18. Około 27 m.
- *19. $48\sqrt{3}$
- *20.
- *21. $(15 + 15\sqrt{3})$ cm

GRUPA C

- 1. $12\sqrt{3} + 6\sqrt{6}$
- $2.\ 10 + \frac{20}{\sqrt{2}} = 10 + 10\sqrt{2}$
- 3. $13,5 + 13,5\sqrt{3}$
- 4. A
- 5. B
- 6. $5 + 5\sqrt{3}$, 10, $5\sqrt{2}$
- 7. C
- 8. N, T, T, N
- 9. $8\sqrt{3}$ cm²
- 10. $\frac{21}{\sqrt{3}} + 7 = 7\sqrt{3} + 7$
- 11. A
- 12. Pole = $26\sqrt{3} + 6$, obwód = $30 + 2\sqrt{6} + 2\sqrt{3}$
- 13. $\sqrt{3} + 1$
- 14. $75\sqrt{3}$ cm², $48\sqrt{3}$ cm², $60\sqrt{3}$ cm², $60\sqrt{3}$ cm²
- 15. $(10 + 4\sqrt{3})$ cm²
- 16. $x = 6\sqrt{3}$, $y = 5\sqrt{6}$
- 17. 1,75 m
- 18. Około 277 m.
- *19. $108\sqrt{3}$
- *20.
- *21. $(13,5+13,5\sqrt{3})$ cm

GRUPA D

- 1. $6\sqrt{5} + 3\sqrt{10}$
- $2.\ 2 + \frac{4}{\sqrt{2}} = 2 + 2\sqrt{2}$
- $3.9 + 9\sqrt{3}$
- 4. B
- 5. C
- 6. $20\sqrt{2}$, 40, $20 + 20\sqrt{3}$
- 7. D
- 8. T, N, N, T
- 9. $12,5\sqrt{3}$ cm²
- 10. $\frac{18}{\sqrt{3}} + 6 = 6\sqrt{3} + 6$
- 11. B
- 12. Pole = $\frac{27\sqrt{3}+27}{2}$, obwód = $25 + 3\sqrt{3} + 3\sqrt{6}$
- 13. $2\sqrt{3} + 2$
- 14. $3\sqrt{3}$ cm², $12\sqrt{3}$ cm², $6\sqrt{3}$ cm², $6\sqrt{3}$ cm²
- 15. $(36 + 16\sqrt{3})$ cm²
- 16. $x = 2\sqrt{3}$, $y = 8\sqrt{6}$
- 17. 1,6 m
- 18. Około 246 m.
- *19. $3\sqrt{3}$
- *20.
- *21. $(6 + 6\sqrt{3})$ cm

GRUPA E

- 1. $10\sqrt{5} + 5\sqrt{10}$
- $2.\ 5 + \frac{10}{\sqrt{2}} = 5 + 5\sqrt{2}$
- 3. $7,5 + 7,5\sqrt{3}$
- 4. C
- 5. B
- 6. $15 + 15\sqrt{3}$, 30, $15\sqrt{2}$
- 7. B
- 8. N, T, N, N
- 9. $18\sqrt{3}$ cm²
- $10.\ \frac{21}{\sqrt{3}} + 7 = 7\sqrt{3} + 7$
- 11. B

12. Pole = $\frac{13\sqrt{3}+3}{2}$, obwód = $13 + 3\sqrt{3} + \sqrt{6}$.

13.
$$\frac{25\sqrt{3}}{4} + \frac{25}{4}$$

14. $75\sqrt{3}\,\mathrm{cm^2}$, $12\sqrt{3}\,\mathrm{cm^2}$, $30\sqrt{3}\,\mathrm{cm^2}$, $30\sqrt{3}\,\mathrm{cm^2}$

15.
$$6\sqrt{3}$$
 cm²

16.
$$x = 7\sqrt{3}$$
, $y = 10\sqrt{6}$

- 17. 1,7 m
- 18. Około 77 m.
- *19. $300\sqrt{3}$
- *20.
- *21. $(7.5 + 7.5\sqrt{3})$ cm

GRUPA F

1.
$$14\sqrt{5} + 7\sqrt{10}$$

$$2. \ 4 + \frac{8}{\sqrt{2}} = 4 + 4\sqrt{2}$$

3.
$$15 + 15\sqrt{3}$$

- 4. D
- 5. A

6.
$$12 + 12\sqrt{3}$$
, 24 , $12\sqrt{2}$

- 7. A
- 8. T, N, T, N
- 9. $18\sqrt{3}$ cm²

10.
$$\frac{30}{\sqrt{3}} + 10 = 10\sqrt{3} + 10$$

11. A

12. Pole =
$$52 + 8\sqrt{3}$$
, obwód = $34 + 4\sqrt{3} + 4\sqrt{2}$

13.
$$4\sqrt{3} + 4$$

14.
$$48\sqrt{3}\,\mathrm{cm}^2$$
, $3\sqrt{3}\,\mathrm{cm}^2$, $12\sqrt{3}\,\mathrm{cm}^2$, $12\sqrt{3}\,\mathrm{cm}^2$

15.
$$(12 + 4\sqrt{3})$$
 cm²

16.
$$x = 10\sqrt{3}$$
, $y = 12\sqrt{6}$

- 17. 1 m
- 18. Około 286 m.
- *19. $12\sqrt{3}$
- *20.
- *21. $(10,5 + 10,5\sqrt{3})$ cm

GRUPA G

1.
$$14\sqrt{3} + 7\sqrt{6}$$

2.
$$7 + \frac{14}{\sqrt{2}} = 7 + 7\sqrt{2}$$

3.
$$6 + 6\sqrt{3}$$

6.
$$16 + 16\sqrt{3}$$
, $16\sqrt{2}$, 32

9.
$$8\sqrt{3}$$
 cm²

10.
$$\frac{36}{\sqrt{3}} + 12 = 12\sqrt{3} + 12$$

12. Pole =
$$14 + 2\sqrt{3}$$
, obwód = $18 + 2\sqrt{3} + 2\sqrt{2}$

13.
$$8\sqrt{3} + 8$$

14.
$$75\sqrt{3}$$
 cm², $27\sqrt{3}$ cm², $45\sqrt{3}$ cm², $45\sqrt{3}$ cm²

15.
$$(24 + 9\sqrt{3})$$
 cm²

16.
$$x = 5\sqrt{3}$$
, $y = 3\sqrt{6}$

*19.
$$27\sqrt{3}$$

*21.
$$(12 + 12\sqrt{3})$$
 cm

GRUPA H

$$1.4\sqrt{3} + 2\sqrt{6}$$

$$2.\ 8 + \frac{16}{\sqrt{2}} = 8 + 8\sqrt{2}$$

3.
$$10,5 + 10,5\sqrt{3}$$

6.
$$10\sqrt{2}$$
, 20 , $10 + 10\sqrt{3}$

9.
$$12,5\sqrt{3}$$
 cm²

$$10.\ \frac{36}{\sqrt{3}} + 12 = 12\sqrt{3} + 12$$

12. Pole =
$$\frac{27\sqrt{3}+27}{2}$$
, obwód = $25 + 3\sqrt{3} + 3\sqrt{6}$

13.
$$4,5\sqrt{3}+4,5$$

14.
$$75\sqrt{3}$$
 cm², $3\sqrt{3}$ cm², $15\sqrt{3}$ cm², $15\sqrt{3}$ cm²

- $15.\ 20\sqrt{3}\ cm^2$
- 16. $x = 9\sqrt{3}$, $y = 11\sqrt{6}$
- 17. 0,75 m
- 18. Około 227 m.
- *19. $243\sqrt{3}$
- *20.
- *21. $(9 + 9\sqrt{3})$ cm

GRUPA I

- 1. $4\sqrt{5} + 2\sqrt{10}$
- $2. 9 + \frac{18}{\sqrt{2}} = 9 + 9\sqrt{2}$
- 3. $12 + 12\sqrt{3}$
- 4. D
- 5. D
- 6. $12 + 12\sqrt{3}$, 24, $12\sqrt{2}$
- 7. B
- 8. T, N, N, T
- 9. $50\sqrt{3}$ cm²
- 10. $\frac{24}{\sqrt{3}} + 8 = 8\sqrt{3} + 8$
- 11. A
- 12. Pole = $\frac{13\sqrt{3}+3}{2}$, obwód = $13 + 3\sqrt{3} + \sqrt{6}$.
- 13. 12,5 $\sqrt{3}$ + 12,5
- 14. $27\sqrt{3}\,\mathrm{cm}^2$, $12\sqrt{3}\,\mathrm{cm}^2$, $18\sqrt{3}\,\mathrm{cm}^2$, $18\sqrt{3}\,\mathrm{cm}^2$
- 15. $16\sqrt{3}$ cm²
- 16. $x = 3\sqrt{3}$, $y = 6\sqrt{6}$
- 17. 1,3 m
- 18. Około 419 m.
- *19. $300\sqrt{3}$
- *20.
- *21. $(19,5 + 19,5\sqrt{3})$ cm

GRUPA J

- $1.6\sqrt{3} + 3\sqrt{6}$
- $2. \ 11 + \frac{22}{\sqrt{2}} = 11 + 11\sqrt{2}$
- 3. $16,5 + 16,5\sqrt{3}$
- 4. C

- 5. B
- 6. $15 + 15\sqrt{3}$, 30, $15\sqrt{2}$
- 7. A
- 8. N, T, N, N
- 9. $32\sqrt{3}$ cm²
- $10.\ \frac{27}{\sqrt{3}} + 9 = 9\sqrt{3} + 9$
- 11. B
- 12. Pole = $52 + 8\sqrt{3}$, obwód = $34 + 4\sqrt{3} + 4\sqrt{2}$
- 13. $18\sqrt{3} + 18$
- 14. $75\sqrt{3}\,\mathrm{cm^2}$, $48\sqrt{3}\,\mathrm{cm^2}$, $60\sqrt{3}\,\mathrm{cm^2}$, $60\sqrt{3}\,\mathrm{cm^2}$
- 15. $27\sqrt{3}$ cm²
- 16. $x = 4\sqrt{3}$, $y = 4\sqrt{6}$
- 17. 2 m
- 18. Około 127 m.
- *19. $108\sqrt{3}$
- *20.
- *21. $(16.5 + 16.5\sqrt{3})$ cm