

1) Details on how you detect parallelograms:

a) Edge Detection:

1) Colour Image to Gray Scale Image:

Using the luminance formula I converted the RGB image(24 bits) to Gray Scale image(8 bits) where pixel value ranges from 0-255.

$$\text{luminance} = 0.30R + 0.59G + 0.11B$$

2) Smoothing Filter:

To remove the noise, I applied 3*3 mean filter over the entire image to remove the noise.

3) Sobel Operator:

The smoothed image is passed through the mask of Sobel operator to detect the edges.

-1	0	1	1	2	1
-2	0	2	0	0	0
-1	0	1	-1	-2	-1
Gx			Gy		

Thus using the above mask I calculated the gradient magnitude and gradient angle to detect the edges. The gradient magnitude is then normalized to give the Normalized Gradient Magnitude image.

4) Non-Maxima Suppression:

To avoid the thick edges in the image and to get the local maxima I have used the concept of quantized angle and non-maxima suppression. The gradient angles obtained from the Sobel Operator lies between -90° to $+90^\circ$ because 'math.atan()' function in python gives the values in that range.

5) Thresholding:

6) The non-maxima suppressed image is then passed through a suitable value called threshold wherein the values above a threshold limit is set to white pixel (black pixel just for display purpose) and below the limit is set to black pixel.

7) The image thus obtained is in binary form having many curved lines apart from straight lines.

b) Hough Transform

8) To detect the straight lines, the image space is converted to parametric space using the equation of $\rho = x \cdot \cos(\theta) + y \cdot \sin(\theta)$.

9) In this the concept of the accumulator array is used wherein on the x-axis is the rho and on y-axis is theta to represent the 2-D accumulator array.

10) Here the rho ranges from -maximumDistance to +maximumDistance and theta varies from -90° to $+90^\circ$ where maximumDistance = square root(width*width + height*height), where width and height is the size of image.

11) Every detected edge in the binary image is visited and the corresponding (x,y) value is substituted on the above equation to get the value of rho.

12) Subsequently, the values in the accumulator array is incremented by 1. Hence more the value denotes the possibility of more edges passing through that point.

- 13) The above technique will result in many such values and thus taking only top 150 maximum values. Also to suppress the neighbouring values in the accumulator array using the 3*3 mask.
- 14) Now using the peak values of (rho, theta), the equation of $\rho = x \cdot \cos(\theta) + y \cdot \sin(\theta)$ is used over all the pixel of grey image and whichever value of rho gets satisfied will be taken and that pixel value will be assigned as white (value = 255). This will give the relevant straight lines.
- 15) These straight lines can then be superimposed on the binary image and compared whether both the binary image and straight line have pixel value of 255, if yes keep that value else discard that part of straight line. This will finally give us the line segments.

c) Parallelogram detection:

- 16) Using the above straight lines, we can find the intersecting points using the equation
 $\rho_1 = x \cdot \cos(\theta_1) + y \cdot \sin(\theta_1)$
 $\rho_2 = x \cdot \cos(\theta_2) + y \cdot \sin(\theta_2)$
This will give the value of (x,y) which will be the coordinates where the lines intersect.
- 17) Also using the theta values from the peak values of the accumulator, if theta value is same or approximately same, they can be treated as parallel lines.
- 18) Now the above found coordinates we want coordinates which lie on these parallel lines. So again using the formula of $\rho = x \cdot \cos(\theta) + y \cdot \sin(\theta)$, I find those values of (x,y) which lie on the parallel lines.
- 19) Consider the pair of parallel lines with parameter (rho1, theta1) representing L1 and (rho2, theta1) representing L2. Let say there are 4 points [(x1,y1), (x2,y2), (x3,y3), (x4,y4)] lying on L1 and 3 points [(x5,y5), (x6,y6), (x7,y7)] lying on L2. Consider another set of parallel lines (rho3, theta2) and (rho4, theta2).
- 20) For now, consider 2 points (x1,y1), (x5,y5) to calculate the slope using the slope formula,
 $\text{slope} = (y_5 - y_1) / (x_5 - x_1)$
if this slope is equal to theta2 consider the points (x1,y1), (x5,y5) as this is forming the part of parallelogram.
If not, then consider next 2 points (x1,y1), (x6,y6) and calculate the slope using the above formula and compare that with theta2.
Repeat the step for all the combinations of the coordinates. This way all the coordinates obtained will eventually lead to the formation of parallelograms.

d) Superimpose the Parallelogram:

- 21) Based on the set of coordinates obtained and using the drawLine function of the built-in python Image library, we can draw the line segments on the original image forming a parallelogram.

2) Programming Language used and Instruction on how to compile the program:

Programming Language: Python 2.7

Instruction to compile:

- a) Go to command prompt of the desktop
- b) Copy and paste the below code in the editor of python and save the file name as *file_name.py*
- c) Go to the path where the *file_name.py* file is located
- d) Write the below commands

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Python file_name.py *path to the image file* Image_1

See the below screenshot for example



Please note: Below libraries are required for the code to be compiled

sys

math

PIL → Image, ImageDraw

numpy

3) **Source code of the program with inline comments**

#importing the libraries to be used

#PIL is the library used for the built-in functions to read, show an image

#numpy library is used for the matrix related basic operations

#math is used for gradient calculation

import sys

import math

from PIL import Image, ImageDraw

import numpy as np

#convert RGB image to Gray Level Image

#function returns the converted gray image object

def convertToGrayLevel(image_object):

 #width and height of image from the size function of PIL library

 width , height = image_object.size

 #Creating a new Image object for Gray Image. Here 'L' is the mode denoting the 8 bit pixel value

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```
grayLevelImage = Image.new("L",(width,height))
```

#To convert the image to gray, parse all the pixels of the RGB image and apply the luminance formula to get the gray level pixel value

```
for i in range(0,width):
```

```
    for j in range(0,height):
```

```
        R,G,B = image_object.getpixel((i,j))
```

```
        #getpixel fuction is used to get the value of corresponding (i,j) pixel value
```

```
        #luminance is calculated as  $R*0.30 + G*0.59 + B*0.11$ 
```

```
        luminance = 0.30 * R + 0.59 * G + 0.11 * B
```

```
        #the corresponding pixel in the image would have the graylevel value as determined by luminance
```

```
        #putpixel fuction is used to put the value in corresponding (i,j) pixel value
```

```
        grayLevelImage.putpixel((i,j),int(luminance))
```

```
#return the object of Gray Image for further processing
```

```
return grayLevelImage
```

```
#smooth the image by applying mean filter of mask 3*3
```

```
#Take the input as object of gray image obtained above
```

```
#function returns smoothed image
```

```
def smoothImage(grayLevelImage):
```

```
    for i in range(1,grayLevelImage.size[0]-1):
```

```
        for j in range(1,grayLevelImage.size[1]-1):
```

```
            #mean filter is the sum of all the 9 (3*3 mask) pixel values divide by 9
```

```
            mean_value = (grayLevelImage.getpixel((i-1,j-1))+grayLevelImage.getpixel((i-1,j))+grayLevelImage.getpixel((i-1,j+1))+grayLevelImage.getpixel((i,j-1))+grayLevelImage.getpixel((i,j))+grayLevelImage.getpixel((i,j+1))+grayLevelImage.getpixel((i+1,j-1))+grayLevelImage.getpixel((i+1,j))+grayLevelImage.getpixel((i+1,j+1)))/9
```

```
            grayLevelImage.putpixel((i,j),int(mean_value))
```

```
    return grayLevelImage
```

```
#finding the gradient magnitude and gradient angle at each pixel point by applying the sobel operator
```

```
#function returns the image after applying sobel operator, gradientAngles
```

```
def SobelOperator(smoothedImage):
```

```
    #Initialize all the values of 2-D gradientAngles array to 0
```

```
    gradientAngles = np.zeros(shape = (smoothedImage.size))
```

```
    #Creating the object for Sobel Image
```

```
    sobelMagnitudeImage = Image.new('L',(smoothedImage.size))
```

```
    #Initialize all the values of 2-D magnitude array to 0
```

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```
magnitude = np.zeros((smoothedImage.size[0], smoothedImage.size[1]), dtype = np.uint64)

min_grad = 0

max_grad = 0

#Applying the sobel mask to the smooth image

for i in range(1,smoothedImage.size[0]-1):

    for j in range(1,smoothedImage.size[1]-1):

        gradient_x = (-1)*smoothedImage.getpixel((i-1,j-1)) + (-2)*smoothedImage.getpixel((i,j-1)) + (-1)*smoothedImage.getpixel((i+1,j-1)) +
smoothedImage.getpixel((i-1,j+1)) + (2)*smoothedImage.getpixel((i,j+1)) + smoothedImage.getpixel((i+1,j+1))

        gradient_y = smoothedImage.getpixel((i-1,j-1)) + (2)*smoothedImage.getpixel((i-1,j)) + smoothedImage.getpixel((i-1,j+1)) + (-
1)*smoothedImage.getpixel((i+1,j-1)) + (-2)*smoothedImage.getpixel((i+1,j)) + (-1)*smoothedImage.getpixel((i+1,j+1))

        magnitude[i][j] = math.sqrt(gradient_x*gradient_x + gradient_y*gradient_y)

        min_grad = min(min_grad,magnitude[i][j])

        max_grad = max(max_grad,magnitude[i][j])

        if gradient_x == 0:

            gradientAngles[i,j] = 90

        else:

            gradientAngles[i,j] = math.degrees(math.atan(gradient_y/gradient_x))

#normalizing the Gradient magnitude to obtain the Normalized Gradient Magnitude

mag_norm=np.zeros((smoothedImage.size[0], smoothedImage.size[1]),dtype = np.uint64)

for i in range(1,smoothedImage.size[0]):

    for j in range(1,smoothedImage.size[1]):

        mag_norm[i][j]=((magnitude[i][j]-min_grad)/(max_grad-min_grad))*255

        sobelMagnitudeImage.putpixel((i,j),int(mag_norm[i][j]))

return sobelMagnitudeImage,gradientAngles

#Applying angle quantization method to thin the lines(non maxima suppression)

#taking the input as the gradientAngles obtained above in the sobel

#function returns the quantized angles

def quantizeAngles(gradientAngles):

    for i in range(0,gradientAngles.shape[0]):

        for j in range(0,gradientAngles.shape[1]):

            #defining the sector in which the pixel lies

            if -22.5 <= gradientAngles[i,j] < 22.5 :

                gradientAngles[i,j] = 0

            elif 22.5 <= gradientAngles[i,j] < 67.5 :

                gradientAngles[i,j] = 1
```

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```
elif 67.5 <= gradientAngles[i,j] <= 90 or -90 <= gradientAngles[i,j] <=-67.5:
```

```
    gradientAngles[i,j] = 2
```

```
elif -67.5 < gradientAngles[i,j] < -22.5 :
```

```
    gradientAngles[i,j] = 3
```

```
return gradientAngles
```

#perform non maxima suppression by using the quantized angles

#if the value of center pixel is greater than the pixel value along the gradient line than keep that value else assign that pixel to value 0

#function returns the image with thinned edges

```
def nonMaximaSuppression(sobelMagnitudelImage,quantizeAngles):
```

```
    for i in range(1,sobelMagnitudelImage.size[0]-1):
```

```
        for j in range(1,sobelMagnitudelImage.size[1]-1):
```

```
            if quantizeAngles[i,j] == 0:
```

```
                if sobelMagnitudelImage.getpixel((i,j)) < sobelMagnitudelImage.getpixel((i,j-1)) or sobelMagnitudelImage.getpixel((i,j)) < sobelMagnitudelImage.getpixel((i,j+1)):
```

```
                    sobelMagnitudelImage.putpixel((i,j),0)
```

```
            elif quantizeAngles[i,j] == 1 :
```

```
                if sobelMagnitudelImage.getpixel((i,j)) < sobelMagnitudelImage.getpixel((i-1,j+1)) or sobelMagnitudelImage.getpixel((i,j)) < sobelMagnitudelImage.getpixel((i+1,j-1)):
```

```
                    sobelMagnitudelImage.putpixel((i,j),0)
```

```
            elif quantizeAngles[i,j] == 2 :
```

```
                if sobelMagnitudelImage.getpixel((i,j)) < sobelMagnitudelImage.getpixel((i-1,j)) or sobelMagnitudelImage.getpixel((i,j)) < sobelMagnitudelImage.getpixel((i+1,j)):
```

```
                    sobelMagnitudelImage.putpixel((i,j),0)
```

```
            elif quantizeAngles[i,j] == 3 :
```

```
                if sobelMagnitudelImage.getpixel((i,j)) < sobelMagnitudelImage.getpixel((i-1,j-1)) or sobelMagnitudelImage.getpixel((i,j)) < sobelMagnitudelImage.getpixel((i+1,j+1)):
```

```
                    sobelMagnitudelImage.putpixel((i,j),0)
```

```
    return sobelMagnitudelImage
```

#Applying thresholding to convert the image to binary form

#Different threshold needs to be used for different image based on the desired output

#Threshold for, 'Test Image 1 = 115' ; 'Test Image 2 = 20'; 'Test Image 3 = 18'

#function returns the binary image

```
def binaryConversion(sobelMagnitudelImage):
```

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```
edgesAt = []
```

```
#the input is sobelized image
```

```
binaryImage = Image.new('L',(sobelMagnitudelImage.size))
```

```
for i in range(0,sobelMagnitudelImage.size[0]):
```

```
    for j in range(0,sobelMagnitudelImage.size[1]):
```

```
        #for display purpose we can change the output and assign the foreground to be black (pixel value = 0) and background to be white (pixel value = 255)
```

```
        #below the foreground is considered to be white and background is considered to be black
```

```
        if sobelMagnitudelImage.getpixel((i,j)) <= 115:
```

```
            #identifying as background below threshold
```

```
            binaryImage.putpixel((i,j),0)
```

```
        else:
```

```
            binaryImage.putpixel((i,j),255)
```

```
            #identifying as foreground above threshold
```

```
            #the foreground pixels are saved in an array to be used for further processing
```

```
            edgesAt.append([i,j])
```

```
return binaryImage, edgesAt
```

```
#rho ranges from -maximum distance to +maximumDistance with step size of 1. maximumDistance = sqrt(width*width + height*height)
```

```
#theta ranges from -90 to +90 and step size is 1
```

```
#function returns the accumulator array(parametric space) for hough transform
```

```
def formAccumulatorArray(edgesAt,binaryImage):
```

```
    maximumDistance = int(math.sqrt(binaryImage.size[0]**2 + binaryImage.size[1]**2))
```

```
    #thetas ranging from -90 to +90 and step size is 1
```

```
    thetas = [i for i in range(-90,91,1)]
```

```
    #Initializing accumulator with 0's
```

```
    accumulator = np.zeros((2*maximumDistance,len(thetas)),dtype = np.uint64)
```

```
    height = binaryImage.size[1]
```

```
    for x,y in edgesAt:
```

```
        #print("Edge points :",str(x),str(y))
```

```
        for theta in thetas:
```

```
            #converting degrees to radians
```

```
            radian = math.radians(theta)
```

```
            rho = int(x*math.cos(radian) + y*math.sin(radian))
```

```
            if -maximumDistance <= rho <= maximumDistance:
```

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```
accumulator[rho+maximumDistance,90+theta] +=1
```

```
return accumulator,maximumDistance
```

```
#sorting the accumulator in reverse order
```

```
#taking the first 150 values from the accumulator array
```

```
#returning the indexes (rho, theta) based on the accumulator value chosen
```

```
def maxIndex(accumulator,theta):
```

```
    indexes = []
```

```
    reverseSorted = np.sort(np.ndarray.flatten(accumulator))[:-1]
```

```
    indexes=[]
```

```
    for i in range(0,len(reverseSorted[0:150])):
```

```
        val = reverseSorted[i]
```

```
        index=[(x,y) for x, row in enumerate(accumulator) for y, i in enumerate(row) if i == val]
```

```
        indexes.append(index)
```

```
    return indexes
```

```
#based on the above final_indexes, eliminating if not local maxima
```

```
#using 3*3 mask to identify the neighbouring pixels and suppress
```

```
#returns the final accumulator array with the suppressed values if not maxima
```

```
def changedAccumulator(accumulator,final_indexes):
```

```
    for k in range(0,len(final_indexes)):
```

```
        indexes = final_indexes[k]
```

```
        for l in range(0,len(indexes)):
```

```
            index = indexes[l]
```

```
            i = index[0]
```

```
            j = index[1]
```

```
            for x in range(i-1,i+1):
```

```
                for y in range(j-1,j+1):
```

```
                    if accumulator[i][j] > 0 and accumulator[i][j] > accumulator[x][y]:
```

```
                        accumulator[x][y] = 0
```

```
    return accumulator
```

```
#choosing the values greater than a particular threshold value
```

```
#returns the (rho,theta) value above a particular threshold
```

```
def getPeakValues(accumulator,maximumDistance):
```


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```
peakList = []
```

```
thetas = [i for i in range(-90,91,1)]
```

```
for i in range(0,accumulator.shape[0]):
```

```
    for j in range(0,accumulator.shape[1]):
```

```
        x = accumulator[i,j]
```

```
        if x > 100:
```

```
            peakList.append([i-maximumDistance,thetas[j]])
```

```
return peakList
```

#eliminating the values which are near in rho's and thetas

#eliminating the redundant rho,theta

```
def removerepeatedLines(peakValues):
```

```
    redundantvalues = []
```

```
    for i in range(0,len(peakValues)-1):
```

```
        temp_i = peakValues[i]
```

```
        p_i = temp_i[0]
```

```
        t_i = temp_i[1]
```

```
        for j in range(i+1,len(peakValues)):
```

```
            temp_j = peakValues[j]
```

```
            p_j = temp_j[0]
```

```
            t_j = temp_j[1]
```

```
            if abs(p_i - p_j) < 15 and abs(t_i - t_j) < 4 :
```

```
                redundantvalues.append(peakValues[i])
```

```
    for i in range(0,len(redundantvalues)):
```

```
        if redundantvalues[i] in peakValues:
```

```
            peakValues.remove(redundantvalues[i])
```

```
return peakValues
```

#it detects the edges of binary image

#whichever is satisfying the (rho, theta) equation take that and plot the line segments on the original colour image

```
def drawLineSegment(peakValues,binaryImage, image_object_for_line_segment_superimpose):
```

```
    pixelsAt = []
```

```
    for k in range(0,len(peakValues)):
```

```
        for i in range(0,binaryImage.size[0]):
```

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```
for j in range(0,binaryImage.size[1]):
    temp = peakValues[k]
    p = temp[0]
    t = math.radians(temp[1])
    if p == int(i*(math.cos(t)) + (j)*(math.sin(t))):
        image_object_for_line_segment_superimpose.putpixel((i,j),(255,0,0))
        pixelsAt.append([i,j])
return image_object_for_line_segment_superimpose,pixelsAt
```

#it finds the coordinates of the intersecting points. These are not the coordinates of the parallelogram

#this function returns all the coordinates where the lines are intersecting

```
def findCoordinates(pixelsAt,peakValues):
    coordinate_points = []
    coordiantesAt=[]
    for i in range(0,len(pixelsAt)):
        pixel = pixelsAt[i]
        for k in range(0,len(peakValues)-1):
            temp_k = peakValues[k]
            p_k = temp_k[0]
            t_k = math.radians(temp_k[1])
            for l in range(k+1,len(peakValues)):
                temp_l = peakValues[l]
                p_l = temp_l[0]
                t_l = math.radians(temp_l[1])
                if p_k == int(pixel[0]*math.cos(t_k) + pixel[1]*math.sin(t_k)) and p_l == int(pixel[0]*math.cos(t_l) + pixel[1]*math.sin(t_l)):
                    coordinate_points.append(pixelsAt[i])
    for i in range(0,len(coordinate_points)):
        if coordinate_points[i] not in coordiantesAt:
            coordiantesAt.append(coordinate_points[i])
    return coordiantesAt
```

#finds the parallel lines having the same theta value

#approximation is taken with theta in some range consider that to be equal

#returns the rho,theta value in pair

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```
def findParallel(peakValues):
```

```
    parallelLines = []
```

```
    for i in range(0,len(peakValues)-1):
```

```
        temp_i = peakValues[i]
```

```
        for j in range(i+1,len(peakValues)):
```

```
            temp_j = peakValues[j]
```

```
            if abs(temp_i[1] - temp_j[1]) < 7:
```

```
                parallelLines.append([peakValues[i],peakValues[j]])
```

```
    return parallelLines
```

```
#combine the theta having similar(nearly equal) values
```

```
#this is used in the parallelogram formation
```

```
#later, used to compare the theta values
```

```
def combineParallelLines(parallelLines):
```

```
    parallelTheta = []
```

```
    for i in range(len(parallelLines)):
```

```
        parallelTheta.append([])
```

```
        for j in range(len(parallelLines[i])):
```

```
            parallelTheta[i].append(parallelLines[i][j][1])
```

```
    return parallelTheta
```

```
#the coordinates found in above defination will return all intersecting lines coordinates
```

```
#using that find only those values which lie on parallel line
```

```
def pointsCorrespondingToParallel(parallelLines, coordinates):
```

```
    parallelCoordinateSet = {}
```

```
    for subList in parallelLines:
```

```
        for lines in subList:
```

```
            temp_theta = math.radians(lines[1])
```

```
            parallelCoordinateSet[lines[1]] = []
```

```
            for points in coordinates:
```

```
                #print int(points[0]*math.cos(temp_theta) + points[1]*math.sin(temp_theta))
```

```
                if (lines[0] == int(points[0]*math.cos(temp_theta) + points[1]*math.sin(temp_theta))):
```

```
                    parallelCoordinateSet[lines[1]].append([points[0], points[1]])
```

```
    return parallelCoordinateSet
```

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```
def finalCoordinates(pointsCorrespondingToParallel, sameTheta):
```

```
    coordinates = []
```

```
    for theta in pointsCorrespondingToParallel:
```

```
        for i in range(len(pointsCorrespondingToParallel[theta])):
```

```
            first_coordinate = pointsCorrespondingToParallel[theta][i]
```

```
            x1 = first_coordinate[0]
```

```
            y1 = first_coordinate[1]
```

```
            for j in range(len(sameTheta)):
```

```
                if theta in sameTheta[j]:
```

```
                    for other_thetas in sameTheta[j]:
```

```
                        if other_thetas != theta:
```

```
                            for k in range(len(pointsCorrespondingToParallel[other_thetas])):
```

```
                                second_coordinate = pointsCorrespondingToParallel[other_thetas][k]
```

```
                                x2 = second_coordinate[0]
```

```
                                y2 = second_coordinate[1]
```

```
                                angle = int(math.degrees(math.atan2((y2-y1),(x2-x1))))
```

```
                                if angle < 0:
```

```
                                    angle = angle + 90
```

```
                                else:
```

```
                                    angle = angle - 90
```

```
                                if angle in pointsCorrespondingToParallel:
```

```
                                    coordinates.append([first_coordinate, second_coordinate])
```

```
    return coordinates
```

```
def drawParallelogram(coordinates, image_object_for_parallelogram_superimpose):
```

```
    draw = ImageDraw.Draw(image_object_for_parallelogram_superimpose)
```

```
    for segmentCoordinate in coordinates:
```

```
        draw.line((segmentCoordinate[0][0], segmentCoordinate[0][1], segmentCoordinate[1][0], segmentCoordinate[1][1]), fill = 128, width = 1)
```

```
    #image_object_for_parallelogram_superimpose.save("----PATH TO SAVE THE FILE----", "JPEG")
```

```
    image_object_for_parallelogram_superimpose.show()
```

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```
if __name__ == "__main__":

    image_object = Image.open(sys.argv[1])

    image_object_for_line_segment_superimpose = Image.open(sys.argv[1])

    image_object_for_parallelogram_superimpose = Image.open(sys.argv[1])

    grayLevelImage = convertToGrayLevel(image_object)

    smoothedImage = smoothImage(grayLevelImage)

    sobelMagnitudelImage,gradientAngles = SobelOperator(smoothedImage)

    #sobelMagnitudelImage.show()

    #sobelMagnitudelImage.save("----PATH TO SAVE THE FILE---", "JPEG")

    quantizedGradientAngles = quantizeAngles(gradientAngles)

    nonMaximasuppressedImage = nonMaximaSuppression(sobelMagnitudelImage,quantizedGradientAngles)

    binaryImage, edgesAt = binaryConversion(nonMaximasuppressedImage)

    #binaryImage.show()

    #binaryImage.save("----PATH TO SAVE THE FILE---", "JPEG")

    accumulator,maximumDistance = formAccumulatorArray(edgesAt,binaryImage)

    thetas = [i for i in range(-90,91,1)]

    final_indexes=maxIndex(accumulator,thetas)

    accumulator = changedAccumulator(accumulator,final_indexes)

    peakValues = getPeakValues(accumulator,maximumDistance)

    removeTheseValues = peakValues

    peakValues = removerepetatedLines(removeTheseValues)

    drawLineSegmentImage,pixelsAt = drawLineSegment(peakValues,binaryImage, image_object_for_line_segment_superimpose)

    #drawLineSegmentImage.show()

    coordinates = findCoordinates(pixelsAt,peakValues)

    parallelLines = findParallel(peakValues)

    sameTheta = combineParallelLines(parallelLines)

    pointsCorrespondingToParallel = pointsCorrespondingToParallel(parallelLines, coordinates)

    coordinates = finalCoordinates(pointsCorrespondingToParallel, sameTheta)

    #print coordinates

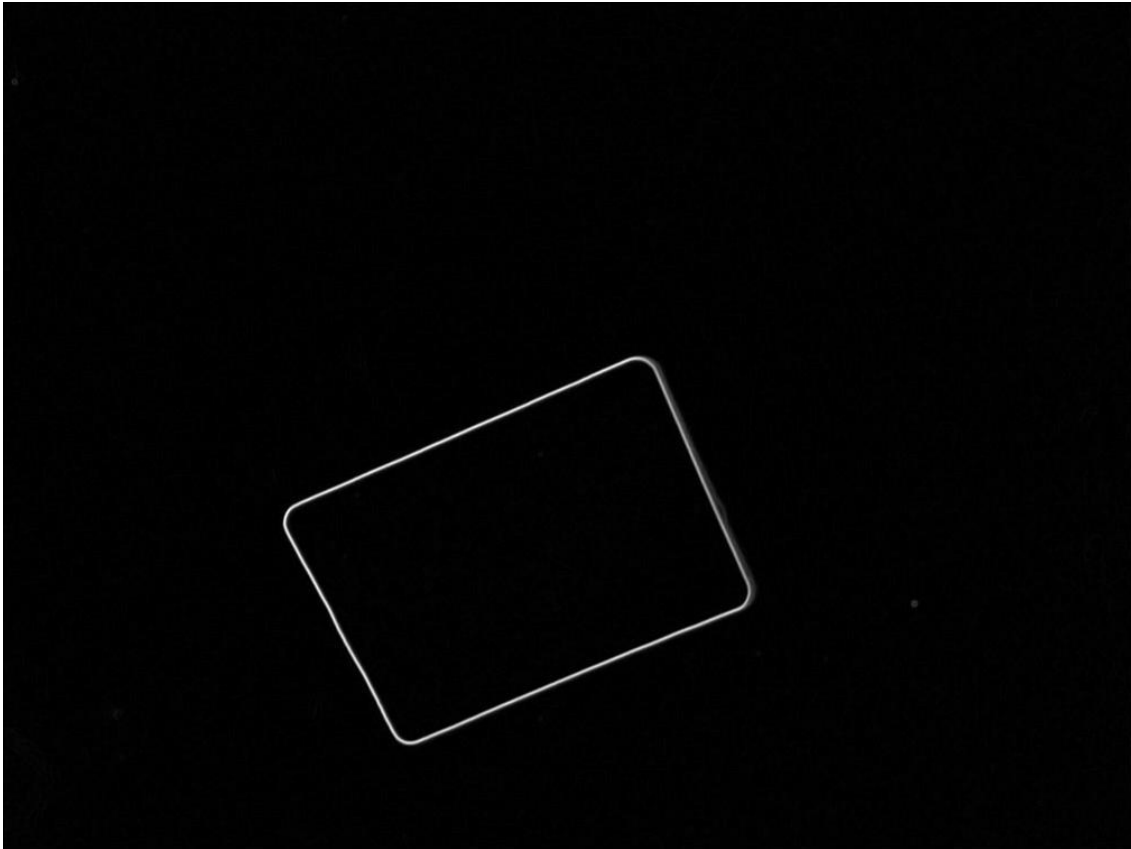
    drawParallelogram(coordinates, image_object_for_parallelogram_superimpose)
```

4) Test Images:



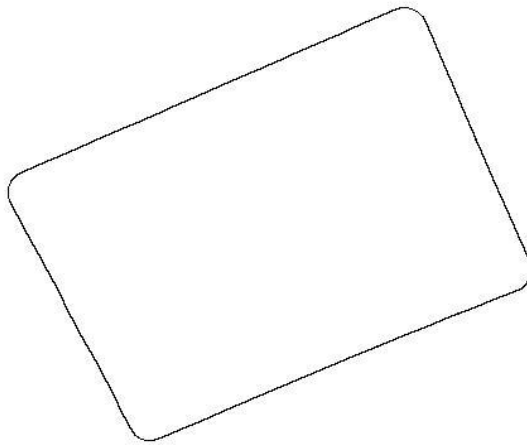
Original Image

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Normalised gradient Magnitude Image

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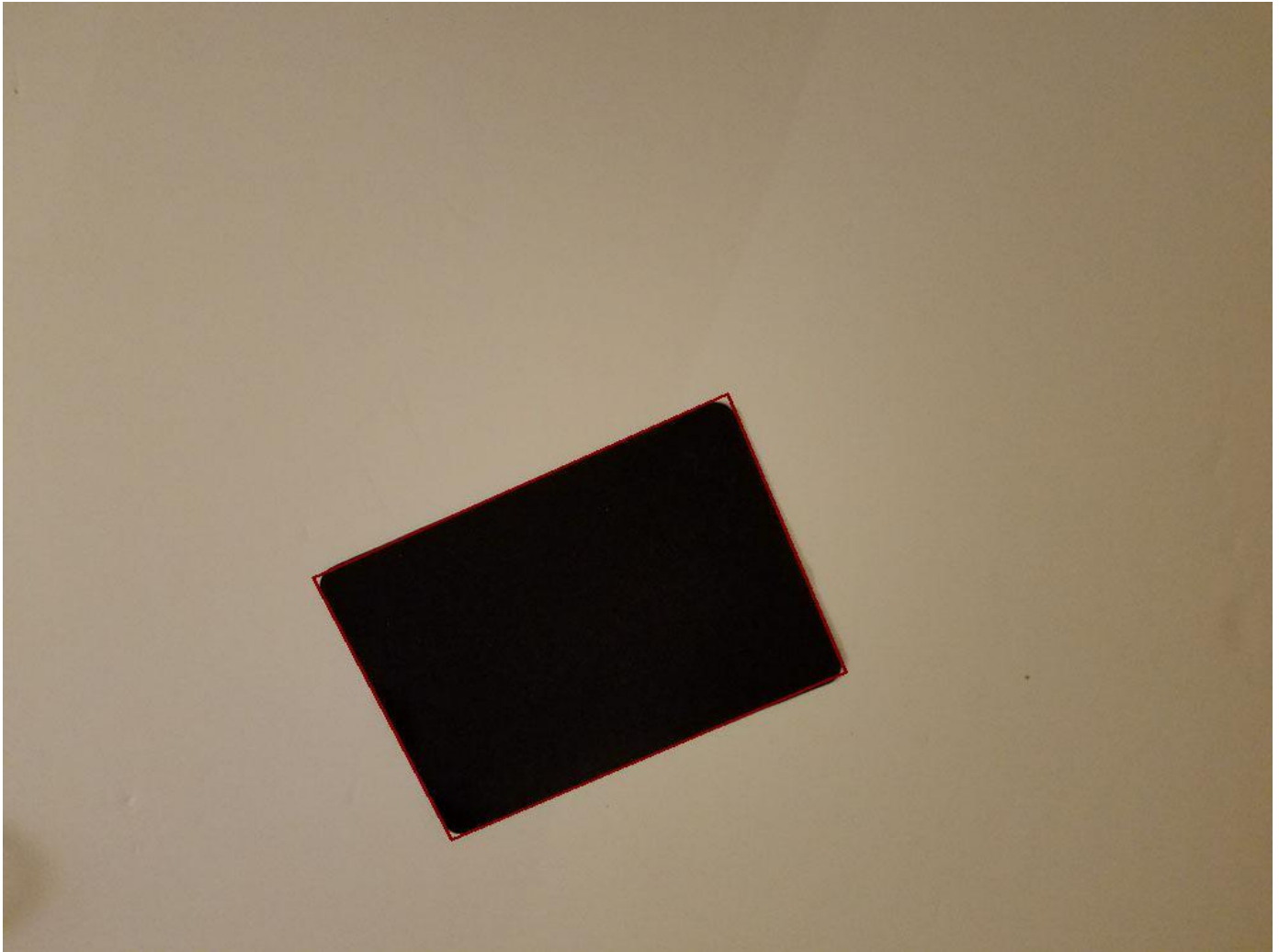


Binary Image

Threshold Value for Image1 is 115

Coordinates of Image 1

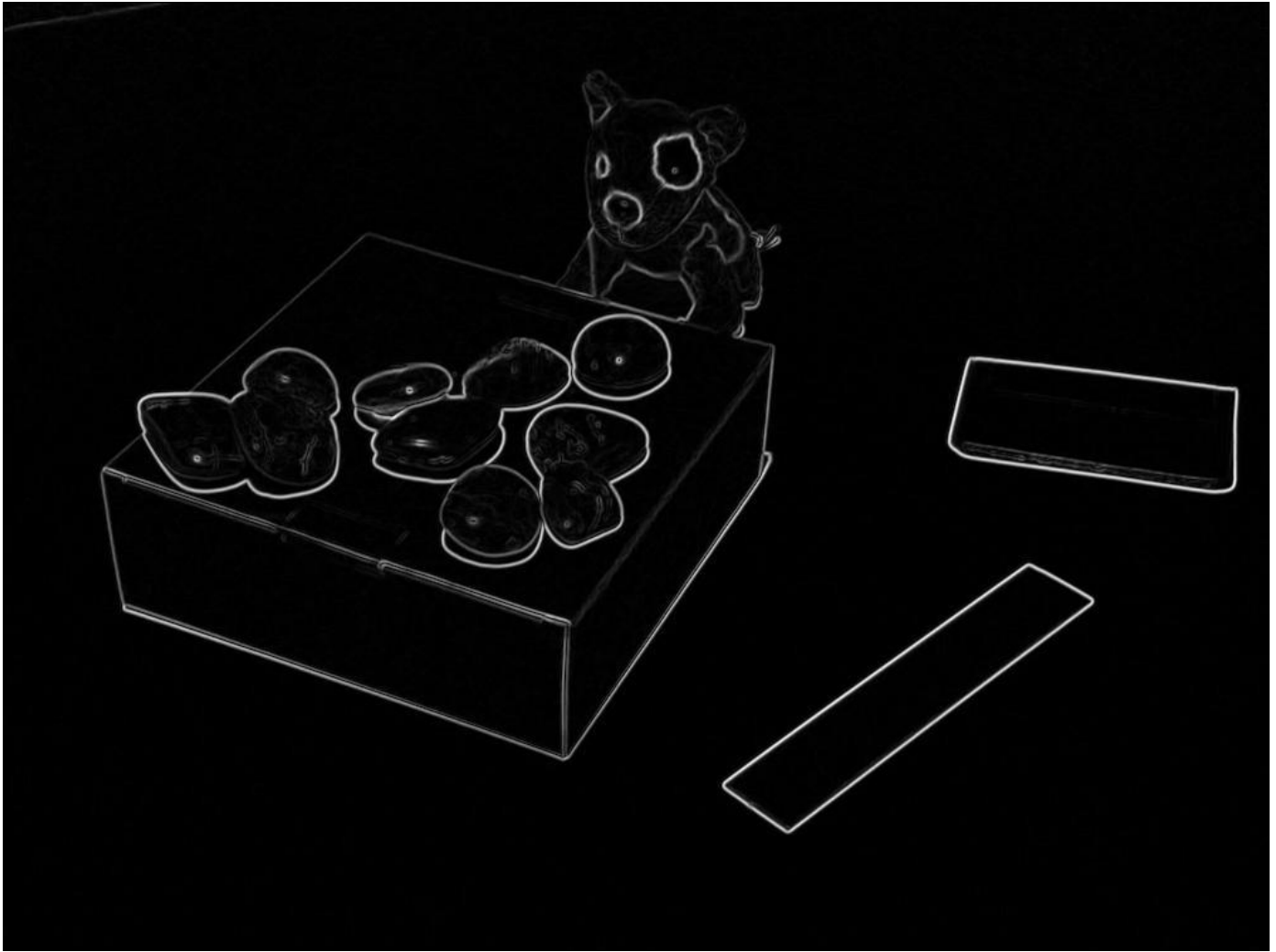
[575, 311] ; [246, 457] ; [669, 532] ; [356, 665]



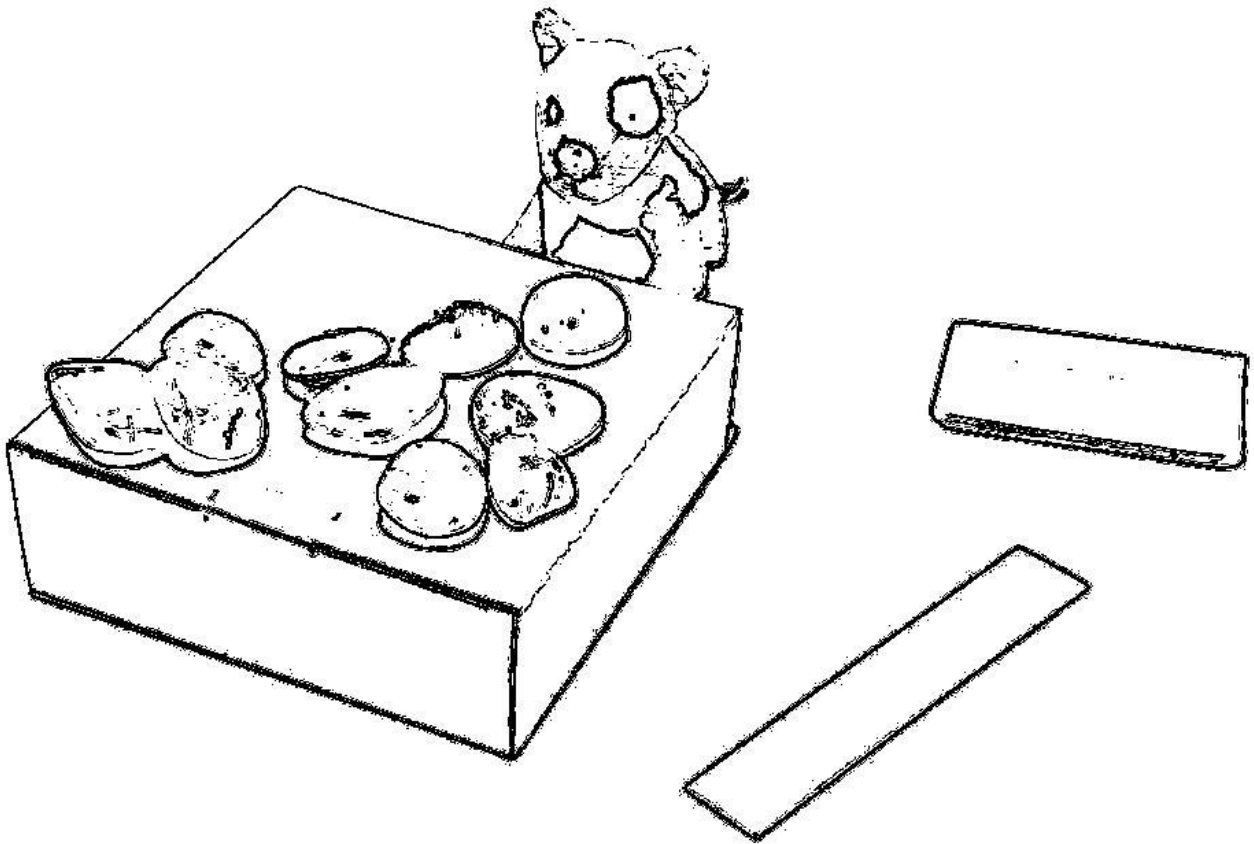
Parallelogram Superimposed Image



Original Image



Normalised gradient Magnitude Image

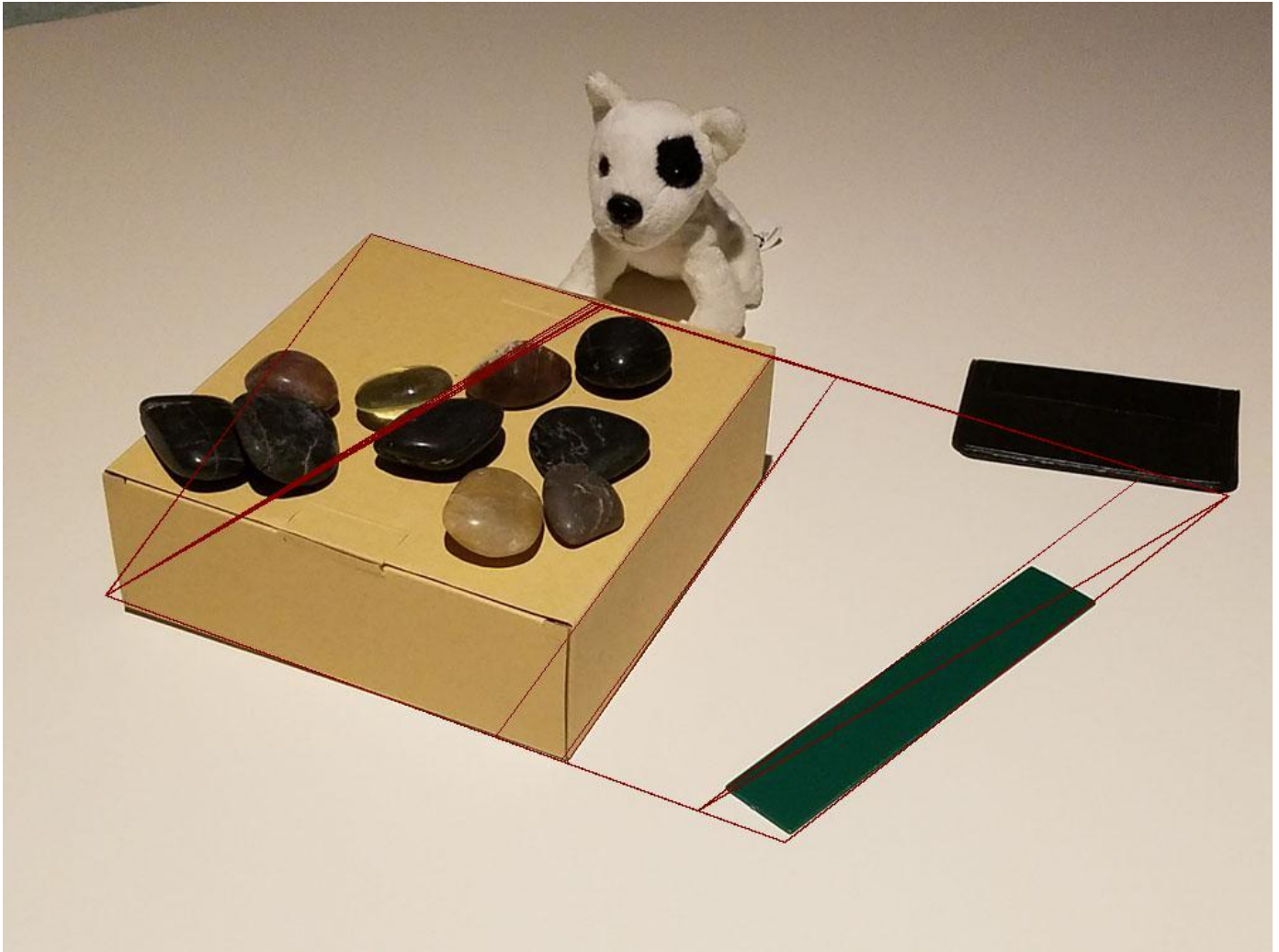


Binary Image

Threshold Value for Image2 is 20

Coordinates of Image 2

[467, 239], [474, 240], [480, 241], [292, 184], [611, 281], [391, 583], [81, 471], [447, 604], [662, 297], [551, 642],
[620, 667], [909, 373], [972, 392], [986, 314], [987, 314], [434, 730]



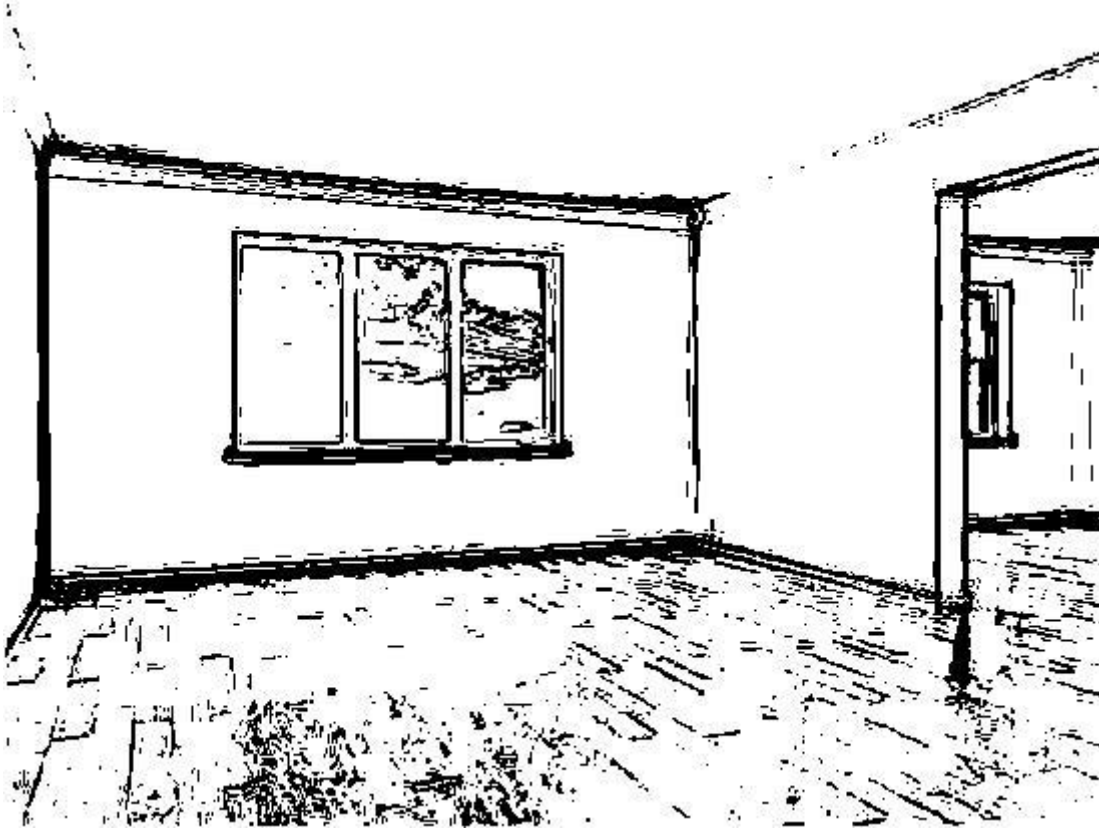
Superimposed Image



Original Image



Normalized Gradient Magnitude

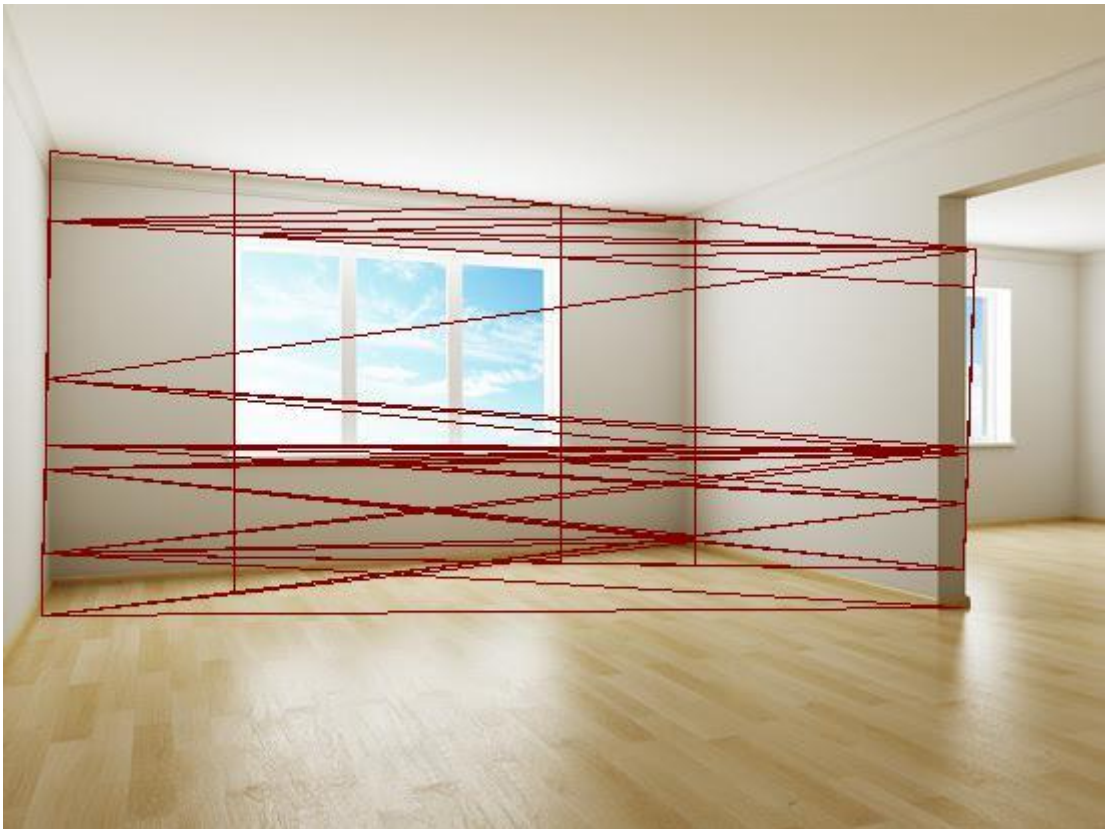
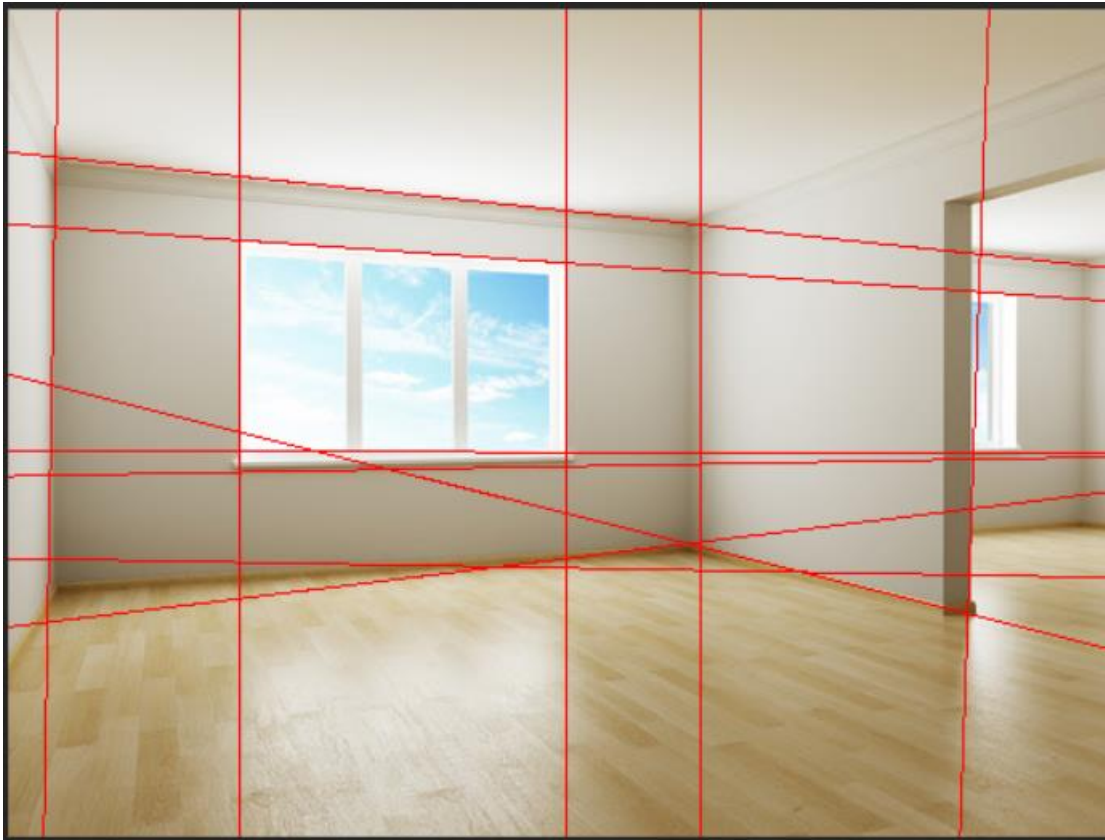


Binary Image

Threshold Value for Image3 is 18

Coordinates of Image 3

[21, 187], [21, 187], [345, 268], [345, 227], [345, 268], [345, 268], [345, 268], [478, 301], [478, 301], [20, 232], [21, 20], [23, 73], [21, 220], [23, 73], [115, 83], [278, 278], [21, 220], [23, 73], [115, 276], [115, 83], [278, 278], [345, 131], [345, 221], [345, 131], [484, 141], [481, 221], [23, 73], [20, 274], [23, 73], [21, 220], [23, 73], [115, 83], [115, 276], [115, 83], [115, 220], [115, 83], [115, 115], [278, 278], [278, 100], [278, 221], [278, 100], [278, 126], [345, 280], [345, 221], [23, 108], [345, 107], [345, 131], [479, 282], [485, 122], [481, 221], [20, 232], [115, 231], [20, 232], [345, 265], [345, 227], [187, 229], [188, 229], [189, 229], [190, 229], [278, 228], [20, 232], [337, 266], [20, 232], [338, 266], [20, 232], [339, 266], [20, 232], [19, 305], [115, 231], [115, 294], [278, 228], [278, 274], [345, 227], [345, 265], [481, 224], [480, 249]



Superimposed image