

# cs5050

04 22 14

①

+ lower bounds

"no better than"

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Solve NP Complete problems

+ Simple generate + test (recursive knapsack)

all possible solutions

Is this the actual Sol?  
pass the test

variable assignment

n variables  $2^n$

n node  $3^n$

- ① Give something up + Solve Simpler Problem — Integer Knapsack (polynomial)  
+ Correctness — wrong answer sizes of knapsack and objects: Int.  
+ Completeness — Cannot solve all problems  
+ Optimality — near optimal, not the "best"

Solve ( )

if nothing to do  
evaluate complete possible solution

else set variable to T  
Solve()  
set variable to F  
solve

$f(n)$  is the number of  
call the alg. makes  
for problem size  $n$

$$f(n) = 2f(n-1) + 1$$

my call

P.S. A

call  $G(s)$

$$2^n$$

$$3^n$$

times for SAT

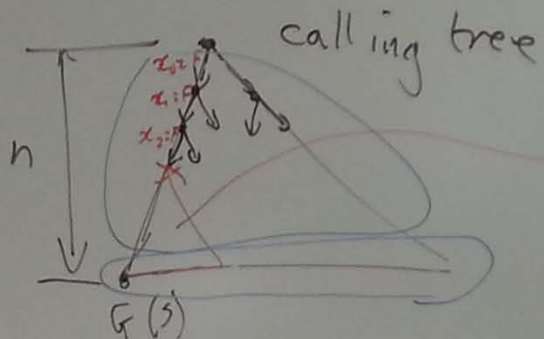
3 Color

$f(n)$  is # of calls

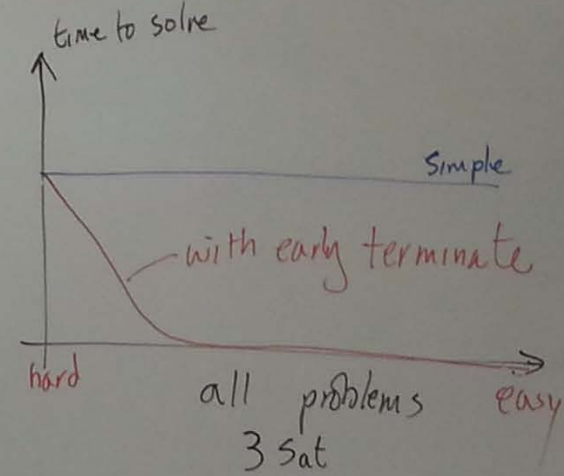
$$f(1) = 1, f(n) = 2f(n-1) + 1$$

$$f(1) = 1, f(n) = 3f(n-1) + 1$$

$$G(s) = (x_0 + x_1 + x_2) \wedge \dots \wedge \dots$$



avoid  $2^{(n-3)}$



Complete Randomness

SAT

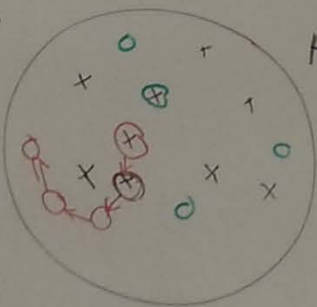
Start with random assignment of variables

IF fail try again

Monte Carlo

$2^n$   
 $n = 100$

$2^{100}$



All possible variable assignment

3SAT — Change evaluation currently T or F

clauses

$( \text{ } ) \wedge ( \text{ } ) \wedge ( \text{ } ) \wedge ( \text{ } ) \wedge ( \text{ } ) \wedge ( \text{ } )$

Count how many are false

+ make random change here

+ pick changes that decrease # of clauses false

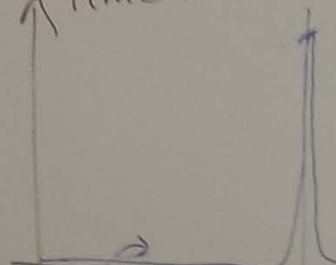
Hill Climbing  $\odot$

# Hard and Easy Problems

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3SAT

time to solve



easily true  
anything works

easily false

nothing works

$\frac{\# \text{ of clauses}}{\# \text{ of variables}}$

increase - more constrained