

KEY

Quiz Two: cs5050, 10 points

Name:

A number:

Consider the following simple solution of the Knapsack decision problem

size[i] > 0, $1 \leq i \leq n$, initial call `knapFit(n, S)`

Bool `knapFit(int i, int s)` // i is item index $\leq n$, s is the current capacity of knapsack

If (s == 0) return true;

If (i == 0 && s > 0) return false;

If (s < 0) return false;

return (knapFit(i-1, s-size[i]) || knapFit(i-1, s)) // use or don't use the item

Write the pseudo code for a dynamic programming solution that will determine if `knapFit(n, S)` is true using only space that is linear in S. The solution needed here does NOT need to report the objects used and so can be implemented as a single forward scan through the array.

```
bool knapFit(n, S)
    cache = bool array 2 x S // assume false
    cache[0,0] = true
    for i = 1 to n
        for j = 0 to S
            if (j - s[i] < 0)
                cache[i%2, j] = cache[(i-1)%2, j]
            else cache[i%2, j] =
                (cache[(i-1)%2, j] ||
                 cache[(i-1)%2, j - s[i]])
            end if
        end for
    end for
    return cache[n, S]
```