

THE INCOMPLETENESS OF OBSERVATION

Why Quantum Mechanics and General Relativity Cannot Be
Unified From Within

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Abstract

The incompatibility between quantum mechanics and general relativity is a structural consequence of embedded observation. Any observer that is part of the universe it measures must access reality through projections that discard causally inaccessible degrees of freedom. Because this causal boundary is determined by the observer's specific kinematic state (such as generating Rindler horizons via acceleration), the resulting structural incompleteness is localized dynamically to their specific reference frame.

Using Wolpert's (2008) physics-independent impossibility theorems for inference devices, an Observational Incompleteness Theorem is introduced: the quantum-mechanical and gravitational descriptions of vacuum energy correspond to variance-type and mean-type estimations of a hidden sector, and Wolpert's mutual inference impossibility prohibits their simultaneous determination by any embedded observer.

Via the Nakajima-Zwanzig formalism and Barandes' (2023) stochastic-quantum correspondence, it is further shown that tracing out the hidden sector generically produces indivisible subsystem dynamics — mathematically equivalent to quantum mechanics — yielding non-factorable statistics that evade Bell's theorem without nonlocality.

The 10^{122} cosmological constant discrepancy is not an error but the quantitative signature of this structural incompleteness. Interpreting the 10^{122} as a variance-to-mean ratio yields roughly 10^{244} hidden-sector degrees of freedom — equal to the square of the Bekenstein-Hawking entropy of the cosmological horizon — converting the cosmological constant problem from a mystery into a measurement.

Specific experimental predictions are offered, including near-term null predictions for particles postulated to resolve the vacuum energy discrepancy and longer-term frequency-dependent scaling relations for gravitational wave echoes and a stochastic noise floor quantitatively anchored to the 10^{122} ratio.

1 THE PROBLEM

1.1 The Incompatibility

Quantum mechanics and general relativity are extraordinarily successful yet incompatible. The dominant assumption has been that this incompatibility is a deficiency — that a deeper theory will eventually unify them. The opposite is the case: **the incompatibility is a structural feature of embedded observation.**

1.2 The Cosmological Discrepancy

The sharpest manifestation of the QM-GR incompatibility is the **cosmological constant problem** [1]. It concerns the single quantity that both frameworks predict: the energy density of empty space, ρ_{vac} .

Quantum mechanics computes the vacuum energy by summing zero-point fluctuations of all quantum field modes up to the Planck scale:

$$\rho_{\text{QM}} \sim \frac{E_{\text{Pl}}^4}{(\hbar c)^3} \sim 10^{113} \text{ J/m}^3$$

General relativity measures the vacuum energy through its gravitational effect — the accelerated expansion of the universe:

$$\rho_{\text{grav}} = \frac{\Lambda c^2}{8\pi G} \sim 6 \times 10^{-10} \text{ J/m}^3$$

The ratio:

$$\frac{\rho_{\text{QM}}}{\rho_{\text{grav}}} \sim 10^{122}$$

is the largest quantitative disagreement in all of physics (conventionally rounded to 10^{120} in the literature). The standard interpretation is that some unknown mechanism cancels the QFT contribution down to the observed value, requiring fine-tuning to one part in 10^{122} . Decades of effort have failed to find such a mechanism [2, 3].

A different interpretation is proposed: **neither calculation is wrong. They disagree because they are answering fundamentally different questions about the same thing.**

2 THE ARGUMENT

2.1 Observers Are Embedded

Wolpert (2008) proved that any physical device performing observation, prediction, or recollection — an “inference device” — faces fundamental limits on what it can know about the universe it inhabits [4]. These limits hold **independent of the laws of physics**:

(a) There exists at least one function of the universe state that the device cannot correctly compute — regardless of its computational power or the determinism of the underlying physics.

(b) No two distinguishable inference devices can fully infer each other’s conclusions (the “mutual inference impossibility”).

These are physics-independent analogues of the Halting theorem, extended to physical devices embedded in physical universes [4]. The key mathematical structure is the **setup function** — a mapping from the full universe state space to the device’s state space. Wolpert’s impossibility requires only that this mapping is surjective and many-to-one: multiple universe states are indistinguishable from the device’s perspective. This condition is trivially satisfied by any observer that is part of the universe it measures.

2.2 The Hidden Sector

Let the full state space be partitioned into degrees of freedom accessible to observers (the visible sector) and degrees of freedom that are not (the hidden sector, denoted Φ). The projection discarding the hidden sector is many-to-one and therefore satisfies the requirements of a Wolpert setup function. **There exist properties of the universe that no observer confined to the visible sector can determine.**

The hidden sector consists not of exotic particles but of standard degrees of freedom rendered causally inaccessible by the structure of spacetime: (i) trans-horizon modes beyond the cosmological horizon, (ii) sub-Planckian degrees of freedom below the observer’s resolution limit, (iii) black hole interiors, and (iv) the region behind the Rindler horizon generated by an observer’s acceleration. The partition between visible and hidden is a dynamic property of the observer’s position and kinematic state, not of the hidden sector’s content.

2.3 Two Projections of the Same Thing

Vacuum energy is the energy density of the hidden sector. When physicists measure or calculate it, they are attempting to characterize Φ from within the visible sector.

Padmanabhan [19] identified the central structural point: the QFT and gravitational descriptions probe different statistical properties of the same underlying degrees of freedom. He argued that classical gravity probes vacuum *fluctuations* rather than mean energy density. Padmanabhan’s core insight is correct, but the **assignment should be inverted** — a conclusion grounded in the impossibility results of §2.4–2.5.

The inversion is motivated by each framework’s coupling structure. QFT computes a sum of positive-definite zero-point energies ($+\frac{1}{2}\hbar\omega$ per mode, no cancellation possible) — structurally analogous to a variance estimator. The Einstein equations couple to the full stress-energy tensor, which is not positive-definite and admits inter-sector cancellation (bosonic vs. fermionic, condensates) — structurally analogous to a mean estimator.

Projection 1: Fluctuation statistics (QM). The QFT vacuum energy sums zero-point energies mode by mode — each contributing $+\frac{1}{2}\hbar\omega$, proportional to the position and momentum variances of the quantum ground state. No cancellation is possible. This is structurally a variance-type quantity:

$$V = \sum_{i=1}^N \frac{1}{2}\hbar\omega_i \propto N$$

Projection 2: Mean-field pressure (gravity). The stress-energy tensor is not positive-definite: different field sectors contribute with signs $s_i = \pm 1$, and the Einstein

equations couple to the net signed aggregate. This is a mean-type quantity:

$$M = \sum_{i=1}^N s_i \frac{1}{2} \hbar \omega_i \sim \sqrt{N}$$

where the \sqrt{N} scaling follows from the central limit theorem when the signs are not fine-tuned — the same scaling underlying Padmanabhan’s geometric mean result [19].

2.4 Why They Cannot Be Unified

The two projections require **incompatible operations on the hidden sector**. The quantum projection *traces out* the hidden sector — it requires Φ to be inaccessible. The gravitational projection *couples to* the hidden sector — it requires Φ to be mechanically present. No single description available to an embedded observer can simultaneously hide and reveal Φ .

Because the two operations extract independent statistical moments of Φ (variance-type and mean-type respectively), Wolpert’s mutual inference impossibility provides a quantitative bound on their simultaneous determination.

A note on “inference device.” Both the QFT calculation and the gravitational measurement qualify as embedded inference devices in Wolpert’s sense, because both are physical processes carried out by observers inside the universe. The QFT calculation is not a Platonic computation — it is performed by a physicist whose apparatus (brain, computer, detector) is a physical subsystem with access only to the visible sector. The gravitational measurement is more obviously embedded: it reads off cosmic acceleration from photon observations. In both cases, the observer’s access to the hidden sector is mediated by a many-to-one projection, satisfying Wolpert’s setup-function requirement.

Observational Incompleteness Theorem (informal): For any embedded observer, the quantum-mechanical and gravitational descriptions of vacuum energy are structurally incompatible projections that cannot be unified into a single observer-accessible description. The cosmological constant problem is the observable signature of this structural incompleteness.

2.5 Formal Statement

Setup. The universe state is partitioned into visible and hidden sectors. Two target functions are defined: the fluctuation content of the hidden sector (a variance-type quantity, corresponding to QFT vacuum energy) and the net mechanical effect (a mean-type quantity, corresponding to gravitationally observed vacuum energy).

Inference devices and the continuous limit. Wolpert’s original framework applies rigorously to binary inference tasks. By thresholding the continuous targets (“Is the variance/mean above or below value X ?”), the continuous problem is mapped to a binary partition. Because Wolpert’s impossibility holds for *every* choice of threshold, it establishes a strict lower bound on the difficulty of the continuous problem. While a fully continuous extension (e.g., via a multi-parameter quantum Cramér-Rao bound) is required to calculate the exact functional form of the continuous trade-off (see §5.3), the binary result is sufficient to prove that perfect simultaneous inference of the continuous variables is structurally impossible.

Independent configurability. The mutual inference impossibility requires that the two targets be independently configurable. In the physical hidden sector, the mean depends on the net sign balance (determined by spin-statistics and vacuum condensate structure), while the variance depends on amplitudes (controlled by excitation level). These are set by independent physical parameters. This is a physical assumption about the hidden sector: if the ultimate UV-complete Lagrangian of the universe rigidly and exactly locks the sign structure to the excitation spectrum, independent configurability fails and this specific inference bound would not apply. However, assuming such perfect dynamical locking exists essentially begs the question of the cosmological constant problem by assuming an unknown perfect cancellation mechanism.

Robustness of the assumption. If interactions induce partial correlations between mean and variance, the Wolpert bound is conjectured to degrade gracefully — remaining nontrivial for any correlation short of perfect dynamical locking — by analogy with Robertson-Schrödinger and Cramér-Rao trade-off inequalities, where product bounds collapse only at singular (maximally correlated) points. A formal proof remains an open problem (see §5.3). Crucially, even without graceful degradation, the strict binary result already establishes that *perfect* simultaneous inference is impossible; the conjecture concerns only *how much* residual uncertainty persists at partial correlation.

The Nakajima-Zwanzig Constraint. The degradation of the Wolpert bound is not merely a conjecture; it is dynamically enforced by the trace-out operation itself. When the hidden sector is traced out, the Nakajima-Zwanzig generalized master equation dictates that the visible sector’s density matrix $\rho_v(t)$ evolves under the influence of a shared non-Markovian memory kernel, $\mathcal{K}(t, \tau)$, which encodes the hidden sector’s temporal correlations. Because both the positive-definite sum (variance/Unruh spectrum) and the sign-admitting trace (mean/gravitational curvature) must be computed from this exact same $\rho_v(t)$, any fluctuation in the hidden sector propagates through $\mathcal{K}(t, \tau)$ to simultaneously shift both projections. They are therefore permanently structurally coupled, mathematically guaranteeing that the variance and mean cannot be completely independently configured, thus locking the incompleteness discrepancy into the observable physics.

The bound. Wolpert’s stochastic extension [4, §8, Proposition 6] gives:

$$\epsilon_{\text{fluc}} \cdot \epsilon_{\text{mech}} \leq \frac{1}{4}$$

The one-quarter bound arises because independent configurability ensures the two binary partitions are cross-cutting: for any assignment of conclusions by one device, universe states exist in each equivalence class that defeat the other device’s inference. **Perfect inference of one target forces the other to be no better than chance.**

Observational Incompleteness Theorem (formal): Let the universe be partitioned into visible and hidden sectors, and let the observer’s projection from the full state to the visible sector be many-to-one. If the variance-type and mean-type targets of the hidden-sector distribution are independently configurable (a physical assumption — see §2.5), then by Wolpert’s mutual inference impossibility, no single inference device confined to the visible sector can simultaneously determine both with joint accuracy exceeding one-quarter.

2.6 The Quantum Projection as Trace-Out

The claim that the quantum projection “traces out” the hidden sector requires justification: why should the resulting reduced description be specifically *quantum-mechanical* rather than classical or arbitrary?

The answer follows from three established results:

Step 1: Trace-out produces memory. When degrees of freedom are traced out of a composite system, the Nakajima-Zwanzig formalism [22, 23] — a standard result from open quantum systems theory — shows that the remaining subsystem’s evolution acquires a **memory kernel**: a non-local-in-time integral term encoding the influence of the traced-out sector’s past states on the visible sector’s present. If the hidden sector has any finite propagation speed or internal dynamics (i.e., if perturbations persist for any nonzero time rather than vanishing instantly), the memory kernel is nonzero and the visible sector’s dynamics is non-Markovian.

Step 2: Memory produces indivisibility. A stochastic process is *divisible* if its transition probabilities factorize into independent shorter-time transitions; it is *indivisible* if they do not. A nonzero memory kernel generically produces indivisibility, because the visible sector’s state at time t depends on its history of interactions with the hidden sector, not merely on its state at an intermediate time. Fine-tuned cancellations between the system’s intrinsic dynamics and the memory kernel could in principle restore divisibility, but such cancellations would need to hold for all times and all initial states simultaneously — an extraordinarily non-generic condition when the hidden sector constitutes the vast majority of the universe’s degrees of freedom.

Step 3: Indivisibility is quantum mechanics. Barandes [24, 25] proved that any indivisible stochastic process is exactly equivalent to a unitary quantum system: it automatically reproduces interference, superposition, entanglement, and the Born rule. The equivalence is mathematical, not approximate — indivisible stochastic dynamics and quantum dynamics are the same object expressed in different formalisms.

The chain. Embedded observation \rightarrow hidden sector \rightarrow trace-out \rightarrow memory kernel (Nakajima-Zwanzig) \rightarrow indivisibility \rightarrow quantum mechanics (Barandes). The quantum-mechanical description of the visible sector is not postulated — it is *derived* from the structure of embedded observation.

Relation to Bell’s theorem. A critical consequence of this inescapable indivisibility is the natural accommodation of Bell’s theorem. Bell proved that no model whose measurement statistics *factorize* — i.e., where the joint probability $P(A, B|\lambda, a, b)$ decomposes into $P(A|\lambda, a) \cdot P(B|\lambda, b)$ — can reproduce quantum correlations. Temporal indivisibility (non-decomposability of transition matrices) is conceptually distinct from but structurally linked to spatial non-factorizability (Bell’s condition): because fine-tuning the memory kernel to zero across 10^{244} degrees of freedom is mathematically pathological, the hidden sector generically produces non-factorable statistics. Therefore, by Barandes’ correspondence, these statistics violate Bell inequalities not by exploiting a loophole but for the same structural reason quantum systems do — their correlations cannot be decomposed into independent local parts. *It must be noted that while indivisibility guarantees Bell violations, mapping the specific non-Markovian memory kernel of the cosmological hidden sector to the exact Tsirelson bound ($2\sqrt{2}$) of standard quantum mechanics remains a critical open mathematical problem (see §5.3).*

Status of results. The Nakajima-Zwanzig formalism [22, 23] and the Stinespring dilation theorem are textbook results. Barandes’ stochastic-quantum correspondence

paper is published [25]; the core mathematical theorem [24] remains a preprint. The generic indivisibility of the trace-out (Step 2) is the step with the weakest formal status — it is physically well-motivated but a rigorous measure-theoretic proof that divisibility has measure zero in the space of hidden-sector Hamiltonians remains open (see §5.3).

3 THE RATIO AS MEASUREMENT

3.1 Extracting the Hidden-Sector Dimensionality

Consider a hidden sector with N independent degrees of freedom, each contributing energy of order one in Planck units. The QFT mode-sum is positive-definite (a variance-type quantity): $V \propto N$. The gravitational coupling sees the net result after inter-sector cancellations (a mean-type quantity): $M \sim \sqrt{N}$. Their ratio is a function of N alone:

$$\frac{V}{M} \sim \frac{N}{\sqrt{N}} = \sqrt{N}$$

Setting this equal to the observed value:

$$\sqrt{N} \sim 10^{122}$$

$$N \sim 10^{244}$$

Assumption of Statistical Independence and Broken Symmetry: The derivation of $M \sim \sqrt{N}$ via the central limit theorem assumes that the N degrees of freedom contribute to the stress-energy tensor with effectively random signs. This requires that the hidden sector lacks exact, unbroken symmetries (such as exact supersymmetry) that would enforce strict, mode-by-mode cancellation (yielding $M = 0$). Provided such symmetries are dynamically broken across the vast majority of the hidden sector’s phase space, the \sqrt{N} scaling emerges not as a special condition, but as the generic macroscopic residual of high-dimensional, uncorrelated sums.

Remark on the sign structure. Individual QFT mode zero-point energies are all positive. The effective signs arise at the level of sectors: the total bosonic vacuum energy is positive, the total fermionic vacuum energy is negative. The random-sign model treats each hidden-sector degree of freedom as contributing with an effectively random sign to the net gravitational coupling. This is a modeling assumption, justified when the number of distinct sector types is large and their relative magnitudes are not fine-tuned. In the actual Standard Model, bosonic and fermionic contributions have specific, non-random relationships; the assumption is that across the full hidden sector — which extends far beyond the Standard Model’s field content — these relationships average to an effectively random distribution.

3.2 The Holographic Coincidence

The Bekenstein-Hawking entropy of the cosmological horizon is independently $S_{\text{dS}} \sim 10^{122}$ [12, 18]. The hidden-sector dimensionality is therefore:

$$N \sim S_{\text{dS}}^2 \sim (10^{122})^2 = 10^{244}$$

matching the value derived from the cosmological constant ratio.

This is supported by Sorkin’s causal-set prediction [17], which derives $\Lambda \sim N^{-1/2}$ from Poisson fluctuations in spacetime atoms — the same functional form as the variance-to-mean scaling — before the 1998 discovery of cosmic acceleration. The value $N \sim 10^{244}$ is an input to Sorkin’s model; the genuine prediction is the scaling relation, which independently confirms the statistical structure posited here.

3.3 Robustness

The \sqrt{N} scaling is robust: replacing random signs with random complex phases preserves it, and weak pairwise correlations modify the estimate only when the correlation coefficient reaches order $1/N$ — a fine-tuned regime. The result exceeds the number of Planck volumes in the observable universe ($\sim 10^{185}$) by $\sim 10^{59}$, ruling out “one degree of freedom per Planck volume” and implying a holographic or extra-dimensional structure.

3.4 Indirect Access to the Hidden Sector

The Observational Incompleteness Theorem does not imply that the hidden sector yields zero information. The Wolpert bound constrains *simultaneous complete determination* of both projections; substantial indirect knowledge remains accessible — and the results of §3.1–3.3 already depend on it.

Statistical properties are accessible even when the microstate is not. The situation is analogous to statistical mechanics: the position and momentum of every molecule in a gas are inaccessible, but temperature, pressure, entropy, and heat capacity are measurable and constitute genuine information about the microscopic degrees of freedom. The hidden sector’s effective dimensionality ($N \sim 10^{244}$), its sign structure (producing \sqrt{N} rather than exact cancellation), and its boundary entropy ($S_{\text{as}} \sim 10^{122}$) are all already-measured statistical properties of this kind.

Boundary properties are directly measurable. The Bekenstein-Hawking entropy characterizes the *interface* between visible and hidden sectors. Hawking radiation, black hole quasinormal mode spectra, and the CMB power spectrum (as a snapshot of the last scattering surface) all carry information imprinted by the hidden sector at the causal boundary. The holographic principle implies the boundary encodes the bulk — but in a form that Wolpert’s theorem guarantees no embedded observer can fully decode.

Consistency constraints are informative. If both projections describe the same underlying reality, quantities appearing in both QM and GR must satisfy cross-projection constraints. Anomaly cancellation conditions, unitarity bounds, and the convergence behavior of running couplings at high energies are all examples: they constrain the hidden sector’s structure by requiring mutual consistency between the two projections where they overlap.

The memory kernel is measurable. The Nakajima-Zwanzig memory kernel (§2.6) encodes how the hidden sector’s past states influence the visible sector’s present. Non-Markovian signatures in quantum systems — anomalous decoherence rates, quantum revival phenomena, non-exponential decay — are indirect readouts of the hidden sector’s internal dynamics and propagation structure.

Three tiers of knowledge about the hidden sector can therefore be distinguished: (i) *already measured* — dimensionality, boundary entropy, sign structure; (ii) *measurable with future instruments* — relaxation timescale (from gravitational wave echoes, §4.2), high-frequency variance spectrum (from the stochastic noise floor, §4.3), correlation struc-

ture (from precision non-Markovian signatures); (iii) *permanently inaccessible* — the full microstate, simultaneous variance-and-mean determination, any quantity requiring direct causal access to trans-horizon or sub-Planckian degrees of freedom.

4 EXPERIMENTAL PREDICTIONS

If the Observational Incompleteness Theorem is correct, General Relativity is an effective mean-field theory — a statistical summary that is reliable when the underlying degrees of freedom are averaged over slowly and smoothly, but breaks down at scales or in regimes where this averaging fails.

4.1 Null Prediction (near-term). If the discrepancy is structural rather than particle-mediated, particles invoked to cancel the QFT vacuum energy should not exist at the required scales. Current LHC bounds have excluded many simplified supersymmetric scenarios; the prediction is that no discovery in the remaining parameter space will resolve the vacuum energy discrepancy.

4.2 Gravitational Wave Echoes (future detectors). The event horizon is the limit of the mechanical projection. Future observations of binary black hole mergers should detect **post-merger echoes** [15] whose amplitude scales with the ratio of probe frequency to the hidden sector’s relaxation frequency. This frequency-dependent slope distinguishes mean-field breakdown from static surface models, which predict frequency-independent reflectivity.

4.3 Stochastic Gravitational Noise Floor (future detectors). Since gravity is the mean of a high-variance distribution, it should exhibit statistical fluctuations at high frequencies: a **stochastic gravitational wave background** in the MHz–GHz band [16], with an inverse-frequency-squared spectrum. The amplitude is anchored to the 10^{122} ratio and is falsifiable.

4.4 Dynamic Unruh-Gravity Scaling (theoretical). If the vacuum energy discrepancy is a function of the inference boundary, it must scale dynamically for an accelerating observer. Acceleration generates a Rindler horizon, establishing a localized hidden sector whose degrees of freedom, N_a , depend strictly on the horizon’s area. The framework predicts that the Unruh thermal spectrum (the local variance, V_a) and the high-frequency stochastic gravitational noise floor (the local mean, M_a) must exhibit a locked, correlated running according to:

$$\frac{V_{\text{Unruh}}(a)}{M_{\text{GravNoise}}(a)} \sim \sqrt{N_a(a)}$$

A cross-correlation between the Unruh thermal fluctuation spectrum and localized high-frequency spacetime deformations would reveal a shared non-Markovian statistical signature, falsifying the independence of QFT and GR vacuum descriptions.

Remark on detectability. The echo and noise-floor predictions yield amplitudes far below current sensitivity. Near-term empirical content resides in the null prediction (§4.1) and the correlated running of couplings suggested by the Asymptotic Safety programme (originating in [14]).

5 DISCUSSION

5.1 Relation to Prior Work

The argument connects: Wolpert’s inference impossibility [4] as the mathematical foundation, Sorkin’s causal-set prediction [17] as independent confirmation of $\Lambda \sim N^{-1/2}$, and the Barandes stochastic-quantum correspondence [24, 25] via the Nakajima-Zwanzig trace-out (§2.6) as the mechanism by which the quantum projection produces specifically quantum-mechanical statistics. The result is compatible with but distinct from Bohr’s complementarity [8] (which operates within QM, not between QM and GR), ’t Hooft’s deterministic quantum mechanics [9], and emergent gravity programmes [10, 11] (we do not derive gravity, but identify why the gravitational and quantum descriptions cannot agree).

The closest precedent is Padmanabhan [19], whose variance-mean distinction is adopted and inverted in §2.3. His later Cosmic Information programme [20] argued that demanding finite cosmic information requires a positive cosmological constant — compatible with the interpretation offered here. The key advance is the Wolpert grounding (§2.4–2.5), which converts the variance-mean distinction from a suggestive observation into a provable impossibility result.

5.2 Key Objections

“The QFT vacuum energy calculation is just wrong.” The theorem does not depend on the specific value. It depends on the structural claim that the fluctuation and mechanical measures are computed by different operations and need not agree. Even if a UV-complete theory reduces the mismatch from 10^{122} to 10^{40} , the conceptual problem remains.

“Doesn’t this just redescribe the cosmological constant problem?” The 10^{122} converts from an unexplained free parameter into a derived quantity: the 10^{122} yields $\sim 10^{244}$ hidden-sector degrees of freedom, corroborated by the de Sitter entropy and Sorkin’s scaling. It also generates falsifiable predictions (§4) that the standard formulation does not.

“A hidden sector mediating correlations between entangled particles is a local hidden variable theory, and Bell’s theorem rules those out.” As shown in §2.6, the hidden sector is not a local hidden variable theory in Bell’s sense [21]. Bell’s theorem requires that hidden variables produce *factorable* statistics — joint probabilities that decompose into products of independent local terms. The trace-out of the hidden sector produces *indivisible* statistics via the Nakajima-Zwanzig memory kernel. Temporal indivisibility and spatial non-factorizability are conceptually distinct but structurally linked: the former generically entails the latter when the hidden sector is sufficiently large. By Barandes’ correspondence [24, 25], these non-factorable statistics violate Bell inequalities for the same structural reason quantum systems do. The full argument is developed in §2.6.

“This conflates epistemology (what we can measure) with ontology (what exists).” The Observational Incompleteness Theorem strictly bounds inference accuracy, not physical ontology. The theorem does not preclude the existence of a single, objective, observer-independent vacuum state. Rather, it proves that no embedded observer can simultaneously extract both its fluctuation (quantum) and mean-field (gravitational) properties, because the operational procedures required to measure them are structurally

mutually exclusive. The 10^{122} discrepancy is therefore an epistemological artifact of embeddedness, even if the underlying ontology is perfectly unified.

“The QM-GR incompatibility has concrete mathematical manifestations that no interpretive framework can dissolve.” This is the strongest objection. Non-renormalizability of perturbative quantum gravity, the frozen-time problem, and the information paradox are structural features of the mathematical theories. The theorem’s scope is limited to the cosmological constant problem. What it claims is that even if those problems were solved, the variance-mean discrepancy would persist.

5.3 Open Problems

(1) A fully continuous formulation via the multi-parameter quantum Cramér-Rao bound; (2) a formal proof that the Wolpert bound degrades continuously under partial correlations; (3) whether the $N \sim S_{\text{dS}}^2$ relationship can be derived rather than observed; (4) whether special relativity can be derived from the hidden sector’s propagation structure; (5) whether the Einstein field equations can be derived as the mean-field equation governing the mechanical projection; (6) a rigorous measure-theoretic proof that divisibility has measure zero in the space of hidden-sector Hamiltonians (the generic indivisibility conjecture of §2.6).

6 CONCLUSION

First, embedded observers face irreducible inference limits (Wolpert), quantum mechanics and general relativity represent two structurally incompatible projections of the same hidden sector (the Observational Incompleteness Theorem), and the 10^{122} cosmological constant discrepancy is the quantitative signature of this incompleteness.

Second, the 10^{122} converts from a problem into a measurement: $\sim 10^{244}$ hidden-sector degrees of freedom — the square of the de Sitter entropy — with $\Lambda \sim N^{-1/2}$ independently confirmed by Sorkin.

If correct, the incompatibility between quantum mechanics and gravity is not a bug to be fixed. It is the physical analogue of Gödel incompleteness — the universe telling observers, in the starkest numerical terms available, that they are inside the system they are trying to describe.

DECLARATION OF AI-ASSISTED TECHNOLOGIES

During the preparation of this work, the author used **Claude Opus 4.6 (Anthropic)** and **Gemini 3 Pro (Google)** to assist in drafting, refining argumentation, and verifying bibliographic details. The author reviewed and edited the content and takes full responsibility for the publication.

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