

# 1 Simulation Algorithm

Following algorithm describes the discrete-event simulation loop. Each tick processes events in a fixed order to ensure deterministic execution.

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**Algorithm 1** Gossipsub Simulation Main Loop

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**Require:** Network parameters  $(n, D, D_{lazy}, c)$ , simulation length  $T$ , warmup  $T_w$   
**Ensure:** Metrics  $(\bar{\delta}, \beta_{norm}, p99)$

```
1: Initialize  $n$  peers with peer tables of size [40, 80]
2: Initialize eager mesh  $\mathcal{M}_p$  and gossip peers  $\mathcal{L}_p$  for each peer  $p$ 
3:  $t \leftarrow 0$ 
4: while  $t < T_w + T$  do
5:   REFILLOTOKENBUCKETS                                 $\triangleright$  Bandwidth accounting
6:   PRODUCEMESSAGES( $t$ )                                $\triangleright$  Poisson arrivals
7:   PROCESSDELIVERIES( $t$ )                             $\triangleright$  Scheduled network arrivals
8:   PROCESSCHURN( $t$ )                                 $\triangleright$  Bimodal leave/rejoin
9:   ENFORCEBANDWIDTH( $t$ )                             $\triangleright$  Drop excess messages
10:  if  $t \bmod 10 = 0$  then
11:    EMITGOSSIP( $t$ )                                 $\triangleright$  Heartbeat every 1 second
12:    MAINTAINMESH( $t$ )                              $\triangleright$  IHAVE announcements
13:  end if
14:   $t \leftarrow t + 1$ 
15:  if  $t = T_w$  then
16:    Reset all counters                            $\triangleright$  End of warmup
17:  end if
18: end while
19: return COMPUTEMETRICS
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**Algorithm 2** Token Bucket Refill

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```
1: procedure REFILLOTOKENBUCKETS
2:   for all peer  $p$  do
3:      $p.tokens \leftarrow \min(B/8, p.tokens + B \cdot \Delta t/8)$ 
4:   end for
5: end procedure
```

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**Algorithm 3** Message Production

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```
1: procedure PRODUCEMESSAGES( $t$ )
2:   for all online peer  $p$  do
3:      $\lambda \leftarrow v_p/384$                                  $\triangleright v_p$  validators, one attestation per epoch
4:      $p_{pub} \leftarrow 1 - e^{-\lambda \cdot \Delta t}$             $\triangleright$  Poisson probability
5:     if  $Uniform(0, 1) < p_{pub}$  then
6:        $m \leftarrow$  new message with  $origin = p, t_m = t$ 
7:        $p.seen \leftarrow p.seen \cup \{m\}$ 
8:        $p.mcache \leftarrow p.mcache \cup \{m\}$ 
9:        $p.delivered \leftarrow p.delivered \cup \{m\}$ 
10:      for all  $q \in p.\mathcal{M}$  do                       $\triangleright$  Eager forward to mesh
11:        if  $\omega_q = \text{online}$  then
12:          Schedule delivery of  $m$  from  $p$  to  $q$  at tick  $t + \text{DELAY}(p, q)$ 
13:        end if
14:      end for
15:    end if
16:  end for
17: end procedure
```

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**Algorithm 4** Process Scheduled Deliveries

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```
1: procedure PROCESSDELIVERIES( $t$ )
2:   for all  $(m, sender)$  scheduled for delivery to peer  $p$  at tick  $t$  do
3:     if  $\omega_p = \text{offline}$  then
4:       continue                                      $\triangleright$  Drop: peer offline
5:     end if
6:     if  $m \in p.seen$  then
7:       continue                                      $\triangleright$  Duplicate: already processed
8:     end if
9:      $p.seen \leftarrow p.seen \cup \{m\}$ 
10:     $p.mcache \leftarrow p.mcache \cup \{m\}$ 
11:     $p.delivered \leftarrow p.delivered \cup \{m\}$            $\triangleright$  Persistent record
12:    Record  $t_{m,p} \leftarrow t$                        $\triangleright$  For latency measurement
13:    for all  $q \in p.\mathcal{M} \setminus \{sender\}$  do       $\triangleright$  Eager forward to mesh
14:      if  $\omega_q = \text{online}$  then
15:        Schedule delivery of  $m$  from  $p$  to  $q$  at tick  $t + \text{DELAY}(p, q)$ 
16:      end if
17:    end for
18:  end for
19: end procedure
```

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**Algorithm 5** Network Delay Model

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```
1: function DELAY( $p, q$ )
2:    $r_p, r_q \leftarrow$  regions of peers  $p$  and  $q$ 
3:    $(\mu, \sigma) \leftarrow LatencyTable[r_p, r_q]$                                  $\triangleright$  See Table ???
4:    $d \leftarrow \max(0.01, \mathcal{N}(\mu, \sigma^2))$                           $\triangleright$  Sample, clip to 10ms minimum
5:   return  $\lceil d/\Delta t \rceil$                                           $\triangleright$  Convert seconds to ticks
6: end function
```

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**Algorithm 6** Bimodal Churn Model

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```
1: procedure PROCESSCHURN( $t$ )
2:   for all peer  $p$  do
3:     if  $p.type = \text{churny}$  then
4:        $\lambda_{\text{leave}} \leftarrow 0.01, \lambda_{\text{rejoin}} \leftarrow 0.05$ 
5:     else
6:        $\lambda_{\text{leave}} \leftarrow 0, \lambda_{\text{rejoin}} \leftarrow 0$                        $\triangleright$  Stable peers never leave
7:     end if
8:     if  $\omega_p = \text{online}$  and  $Uniform(0, 1) < \lambda_{\text{leave}}$  then
9:        $\omega_p \leftarrow \text{offline}$ 
10:      Clear  $p.\mathcal{M}, p.\mathcal{L}$                                           $\triangleright$  Mesh connections lost
11:     else if  $\omega_p = \text{offline}$  and  $Uniform(0, 1) < \lambda_{\text{rejoin}}$  then
12:        $\omega_p \leftarrow \text{online}$ 
13:       Clear  $p.\text{seen}, p.mcache$                                       $\triangleright$  State reset on rejoin
14:     end if
15:   end for
16: end procedure
```

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**Algorithm 7** Bandwidth Enforcement

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```
1: procedure ENFORCEBANDWIDTH( $t$ )
2:   for all message  $m$  from sender  $s$  scheduled for delivery at tick  $t + 1$  do
3:      $size \leftarrow |m|$                                                $\triangleright$  Payload or control message size
4:     if  $s.tokens < size$  then
5:       Remove  $m$  from schedule                                      $\triangleright$  Drop: insufficient bandwidth
6:     else
7:        $s.tokens \leftarrow s.tokens - size$ 
8:       if  $m$  is payload then
9:          $s.B^{\text{Payload}} \leftarrow s.B^{\text{Payload}} + size$ 
10:        else
11:           $s.B^{\text{Ctrl}} \leftarrow s.B^{\text{Ctrl}} + size$ 
12:        end if
13:      end if
14:    end for
15: end procedure
```

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**Algorithm 8** Gossip Emission (IHAVE)

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```
1: procedure EMITGOSSIP( $t$ )
2:   for all online peer  $p$  do
3:      $ids \leftarrow$  message IDs in  $p.mcache$  from last 3 heartbeats
4:     if  $ids = \emptyset$  then
5:       continue
6:     end if
7:      $k \leftarrow \min(D_{lazy}, |p.\mathcal{L}|)$ 
8:      $targets \leftarrow$  sample  $k$  peers uniformly from  $p.\mathcal{L}$ 
9:     for all  $q \in targets$  do
10:      if  $\omega_q = \text{online}$  then
11:        Schedule IHAVE( $ids$ ) from  $p$  to  $q$  at tick  $t + \text{DELAY}(p, q)$ 
12:      end if
13:    end for
14:    Advance  $p.mcache$  window                                 $\triangleright$  Expire old entries
15:  end for
16: end procedure
```

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**Algorithm 9** Process IHAVE/ IWANT

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```
1: procedure PROCESSIHAVE( $p, ids, sender$ )
2:    $missing \leftarrow ids \setminus p.seen$ 
3:   if  $missing \neq \emptyset$  then
4:     Schedule IWANT( $missing$ ) from  $p$  to  $sender$  at tick  $t + \text{DELAY}(p, sender)$ 
5:   end if
6: end procedure
7: procedure PROCESSIWANT( $p, ids, requester$ )
8:   for all  $mid \in ids$  do
9:     if  $mid \in p.mcache$  then
10:       $m \leftarrow p.mcache[mid]$ 
11:      Schedule delivery of  $m$  from  $p$  to  $requester$  at tick  $t + \text{DELAY}(p, requester)$ 
12:    end if
13:   end for
14: end procedure
```

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**Algorithm 10** Mesh Maintenance (GRAFT/ PRUNE)

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```
1: procedure MAINTAINMESH( $t$ )
2:   for all online peer  $p$  do
3:      $p.\mathcal{M} \leftarrow \{q \in p.\mathcal{M} : \omega_q = \text{online}\}$                                  $\triangleright$  Remove offline peers
4:     if  $|p.\mathcal{M}| < D - 2$  then                                               $\triangleright$  Below  $D_{lo}$ : graft
5:        $k \leftarrow D - |p.\mathcal{M}|$ 
6:        $\text{candidates} \leftarrow \{q \in p.\text{table} \setminus p.\mathcal{M} : \omega_q = \text{online}\}$ 
7:        $\text{new} \leftarrow \text{sample } \min(k, |\text{candidates}|)$  peers from  $\text{candidates}$ 
8:       for all  $q \in \text{new}$  do
9:          $p.\mathcal{M} \leftarrow p.\mathcal{M} \cup \{q\}$ 
10:        Schedule GRAFT( $p$ ) to  $q$  at tick  $t + \text{DELAY}(p, q)$ 
11:      end for
12:    else if  $|p.\mathcal{M}| > D + 2$  then                                               $\triangleright$  Above  $D_{hi}$ : prune
13:       $k \leftarrow |p.\mathcal{M}| - D$ 
14:       $\text{excess} \leftarrow \text{sample } k$  peers from  $p.\mathcal{M}$ 
15:      for all  $q \in \text{excess}$  do
16:         $p.\mathcal{M} \leftarrow p.\mathcal{M} \setminus \{q\}$ 
17:        Schedule PRUNE( $p$ ) to  $q$  at tick  $t + \text{DELAY}(p, q)$ 
18:      end for
19:    end if
20:     $\triangleright$  Update lazy mesh from remaining non-eager peers
21:     $p.\mathcal{L} \leftarrow \text{sample } D_{lazy}$  peers from  $\{q \in p.\text{table} \setminus p.\mathcal{M} : \omega_q = \text{online}\}$ 
22:  end for
23: end procedure
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**Algorithm 11** Process GRAFT/ PRUNE

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```
1: procedure PROCESSGRAFT( $p, \text{requester}$ )
2:   if  $\text{requester} \in p.\text{table}$  and  $\omega_{\text{requester}} = \text{online}$  then
3:      $p.\mathcal{M} \leftarrow p.\mathcal{M} \cup \{\text{requester}\}$ 
4:      $p.\mathcal{L} \leftarrow p.\mathcal{L} \setminus \{\text{requester}\}$ 
5:   end if
6: end procedure
7: procedure PROCESSPRUNE( $p, \text{requester}$ )
8:    $p.\mathcal{M} \leftarrow p.\mathcal{M} \setminus \{\text{requester}\}$ 
9: end procedure
```

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**Algorithm 12** Compute Final Metrics

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```
1: function COMPUTEMETRICS
2:    $R_m \leftarrow \{p \in V : m \in p.delivered\}$   $\triangleright$  Delivery set for message  $m$ : peers that received it
3:    $\bar{\delta} \leftarrow \frac{1}{|M|} \sum_{m \in M} \frac{|R_m|}{|V|}$   $\triangleright$  Delivery rate: fraction of all peers that received each message
4:    $B_{total} \leftarrow \sum_{p \in V} (p.B^{Payload} + p.B^{Ctrl})$   $\triangleright$  Total bandwidth
5:    $\beta \leftarrow B_{total} / deliveries$   $\triangleright$  Bytes per delivery
6:    $\beta_{norm} \leftarrow \beta / P$   $\triangleright$  Normalized cost
7:    $p99 \leftarrow \text{Percentile}_{99}(L)$   $\triangleright P = 1536$  bytes
8:    $L \leftarrow \{(t_{m,p} - t_m) \cdot \Delta t : m \in M, p \in R_m\}$   $\triangleright$  p99 latency over all successful deliveries
9:    $\text{return } (\bar{\delta}, \beta_{norm}, p99)$ 
10:  end function
```

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## 2 Pareto Dominance Analysis

**Definition 2.1 (Pareto Dominance)** Configuration  $A$  dominates configuration  $B$  on delivery rate and bandwidth cost if  $\delta_A \geq \delta_B$  and  $(\beta/P)_A \leq (\beta/P)_B$ , with at least one strict inequality.

We exclude latency from the dominance computation because Floodsub achieves the lowest latency (0.4s p99). Including latency would prevent any configuration from strictly dominating Floodsub, obscuring the clear delivery-cost advantage of Gossipsub. Latency is instead encoded as marker shape in Figure ?? for visual inspection.

For the dominance plot, we aggregate simulation results to worst-case metrics across churn regimes using Algorithm 13.

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**Algorithm 13** Worst-Case Aggregation Across Churn Regimes

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**Require:** Raw results  $\mathcal{R} = \{(D, D_{lazy}, c, \bar{\delta}, \beta_{norm}, p99)\}$  for all configurations  
**Ensure:** Aggregated results  $\mathcal{A}$

- 1:  $\mathcal{A} \leftarrow \emptyset$
- 2: **for** all unique  $(D, D_{lazy})$  pairs in  $\mathcal{R}$  **do**
- 3:    $\mathcal{R}_{D,D_{lazy}} \leftarrow \{r \in \mathcal{R} : r.D = D \wedge r.D_{lazy} = D_{lazy}\}$
- 4:    $\delta^* \leftarrow \min_{r \in \mathcal{R}_{D,D_{lazy}}} r.\bar{\delta}$  ▷ Worst (minimum) delivery
- 5:    $\beta_{norm}^* \leftarrow \max_{r \in \mathcal{R}_{D,D_{lazy}}} r.\beta_{norm}$  ▷ Worst (maximum) cost
- 6:    $\ell^* \leftarrow \max_{r \in \mathcal{R}_{D,D_{lazy}}} r.p99$  ▷ Worst (maximum) latency
- 7:    $\mathcal{A} \leftarrow \mathcal{A} \cup \{(D, D_{lazy}, \delta^*, \beta_{norm}^*, \ell^*)\}$
- 8: **end for**
- 9: **return**  $\mathcal{A}$

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Algorithm 14 computes the 2D Pareto frontier over delivery rate and cost. Latency ( $\ell^*$ ) is retained in the aggregated results for visualization but is not used in the dominance check.

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**Algorithm 14** Compute 2D Pareto Frontier

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**Require:** Aggregated results  $\mathcal{A} = \{(D, D_{lazy}, \delta^*, \beta_{norm}^*, \ell^*)\}$   
**Ensure:** Pareto-optimal set  $\mathcal{P} \subseteq \mathcal{A}$

- 1: **function** DOMINATES( $A, B$ ) ▷ Does  $A$  dominate  $B$  on delivery rate and cost?
- 2:   **return**  $(\delta_A^* \geq \delta_B^*) \wedge (\beta_{norm,A}^* \leq \beta_{norm,B}^*) \wedge ((\delta_A^* > \delta_B^*) \vee (\beta_{norm,A}^* < \beta_{norm,B}^*))$
- 3: **end function**
- 4:  $\mathcal{P} \leftarrow \mathcal{A}$
- 5: **for** all  $A \in \mathcal{A}$  **do**
- 6:   **for** all  $B \in \mathcal{A} \setminus \{A\}$  **do**
- 7:     **if** DOMINATES( $B, A$ ) **then**
- 8:        $\mathcal{P} \leftarrow \mathcal{P} \setminus \{A\}$
- 9:       **break**
- 10:     **end if**
- 11:   **end for**
- 12: **end for**
- 13: **return**  $\mathcal{P}$

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