```
import networkx as nx
import itertools
import matplotlib.pyplot as plt
import numpy as np
from networkx.algorithms.community import girvan_newman
```

[30 marks] Generating the graphs and visualizing them with Network-x or GEPHI.

```
def generate graph(n, k):
    G = nx.Graph()
    G.add_nodes_from(range(1, n+1))
    for i in range(1, n+1):
        for j in range(i+1, n+1):
             if i % k != j % k:
                 G.add edge(i, j)
    return G
def visualize graph(G, communities=None):
    plt.figure(figsize=(12, 8))
    pos = nx.spring layout(G, seed=42)
    if communities:
        unique communities = set(communities.values())
        color map = plt.cm.rainbow(np.linspace(0, 1,
len(unique communities)))
        color dict = {com: color map[i] for i, com in
enumerate(unique communities)}
        node colors = [color dict[communities[node]] for node in
G.nodes()1
        nx.draw(G, pos, node color=node colors, with labels=True,
node size=300, font size=8, alpha=0.7)
        nx.draw(G, pos, with labels=<mark>True</mark>, node size=<mark>300</mark>, font size=<mark>8</mark>,
alpha=0.7)
    plt.title('Graph Visualization')
    plt.tight_layout()
    plt.show()
graph sizes = [(40, 7), (20, 5), (10, 3)]
graph list = []
for n, k in graph sizes:
      print(f'' \setminus n\{''='*50\}'')
      print(f"Graph size (n, k) = (\{n\}, \{k\})")
      print(f"{'='*50}")
```

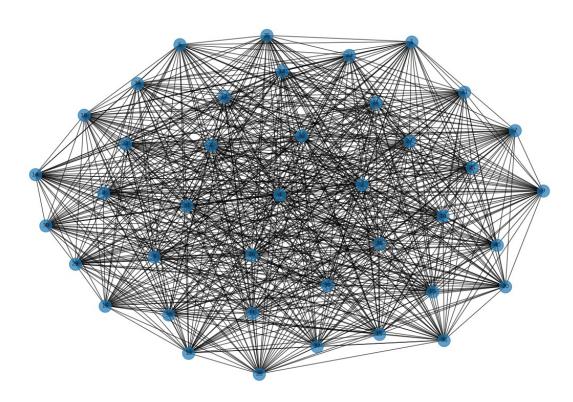
G = generate_graph(n, k)
graph_list.append(G)
visualize_graph(G)

Graph size (n, k) = (40, 7)

<ipython-input-34-cc2cc75511a1>:18: UserWarning: This figure includes
Axes that are not compatible with tight_layout, so results might be
incorrect.

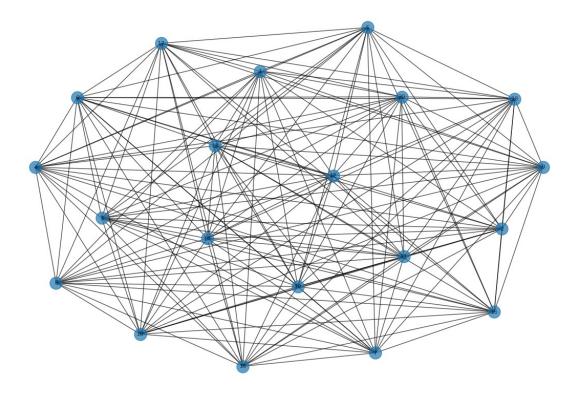
plt.tight_layout()

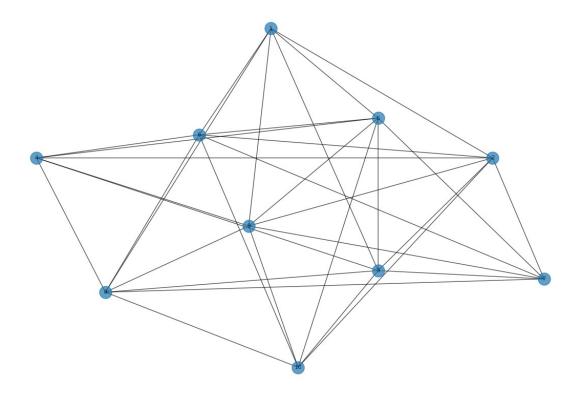
Graph Visualization



Graph size (n, k) = (20, 5)

Graph Visualization





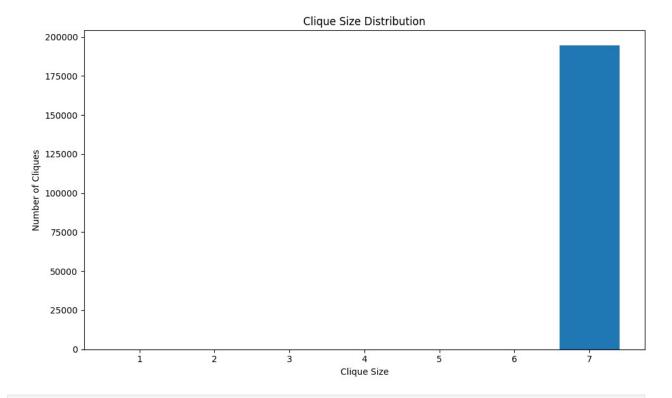
[30 marks] Count the number of cliques of each size in each graph ... Plot their histograms

```
for i, tup in enumerate(graph sizes):
    n, k = tup
    G = graph_list[i]
    cliques = list(nx.find_cliques(G))
    clique_counts = {}
    for clique in cliques:
        size = len(clique)
        clique_counts[size] = clique_counts.get(size, 0) + 1
    print("\nClique Analysis:")
    print("Total number of cliques:", len(cliques))
    print("Clique Counts:", clique_counts)
    plt.figure(figsize=(10, 6))
    if clique_counts:
        max size = max(clique_counts.keys())
        sizes = list(range(1, max_size + 1))
        counts = [clique counts.get(size, 0) for size in sizes]
    else:
```

```
sizes = []
    counts = []

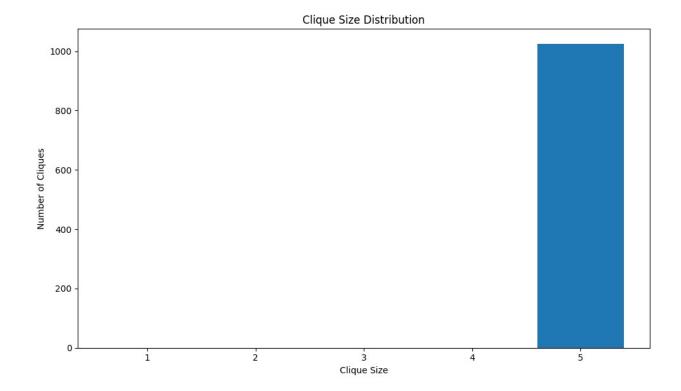
plt.bar(sizes, counts)
    plt.title('Clique Size Distribution')
    plt.xlabel('Clique Size')
    plt.ylabel('Number of Cliques')
    plt.xticks(sizes)
    plt.tight_layout()
    plt.show()

Clique Analysis:
Total number of cliques: 194400
Clique Counts: {7: 194400}
```

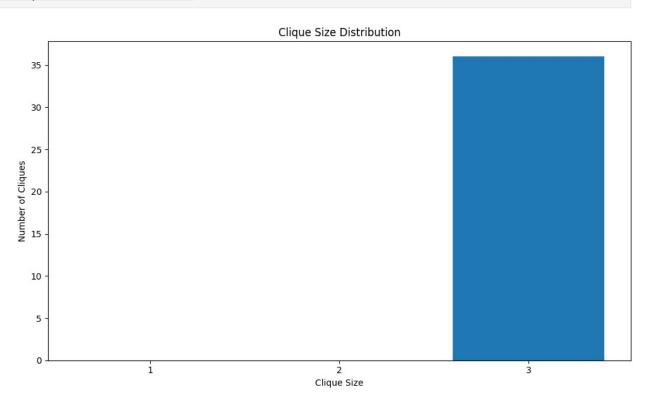


Clique Analysis: Total number of cliques: 1024

Clique Counts: {5: 1024}



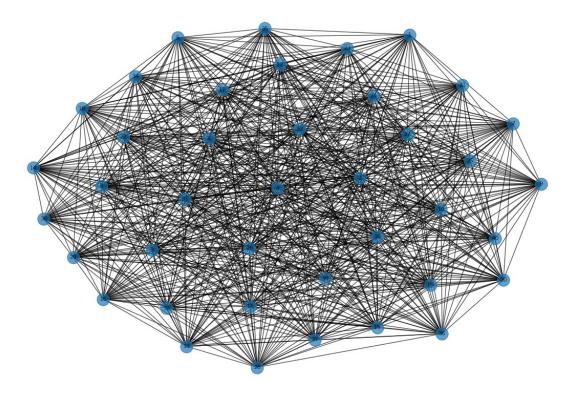
Clique Analysis: Total number of cliques: 36 Clique Counts: {3: 36}



[30 marks] Identify the main communities in the graphs generated

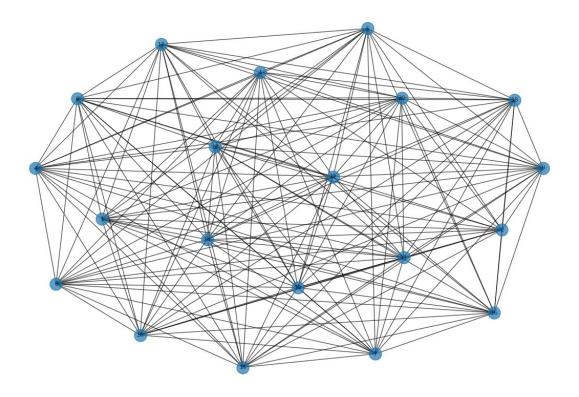
```
for i, tup in enumerate(graph sizes):
    n, k = tup
    G = graph list[i]
    comp = girvan newman(G)
    first partition = next(comp)
    communities = [list(c) for c in first partition]
    partition = {}
    for community_id, nodes in enumerate(communities):
        for node in nodes:
            partition[node] = community id
    community counts = {}
    for community id in set(partition.values()):
        community size = sum(1 for v in partition if partition[v] ==
community id)
        community counts[community id] = community size
    print("\nCommunity Analysis:")
    print("Number of Communities:", len(set(partition.values())))
    print("Community Sizes:", dict(sorted(community counts.items(),
key=lambda x: x[1], reverse=True)))
    visualize graph(G)
Community Analysis:
Number of Communities: 2
Community Sizes: {0: 39, 1: 1}
<ipython-input-34-cc2cc75511al>:18: UserWarning: This figure includes
Axes that are not compatible with tight layout, so results might be
incorrect.
  plt.tight layout()
```

Graph Visualization

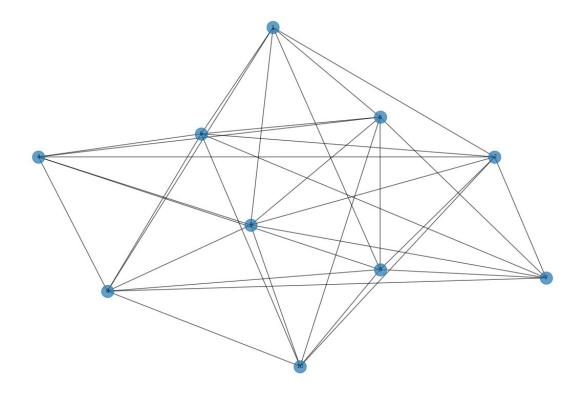


Community Analysis:
Number of Communities: 2
Community Sizes: {1: 19, 0: 1}

Graph Visualization



Community Analysis:
Number of Communities: 2
Community Sizes: {0: 9, 1: 1}



[30 marks] Based on Example 10.10,

You are given a graph say (n,k) where n represents no. of nodes numbered 1 to n & k represents an arbitrary number using which we will generate our graph. Now as per the example 10.10 In such a graph, a link exists between nodes if 2 nodes numbered i & j when divided by k doesn't leave the same remainder. Generate such a graph, calculate the number of edges present in it & compare it with the approximation offered by the fraction (k-1)/k for the following values of n & k

```
theoretical edges = n * (n-1) * (k-1) / (2 * k)
    approximation accuracy = abs(actual edges - theoretical edges) /
actual edges * 100
    return {
        'n': n,
        'k': k,
        'actual edges': actual edges,
        'theoretical edges': theoretical edges,
        'approximation accuracy': approximation accuracy
    }
results = [analyze graph(n, k) for n, k in graph sizes]
for result in results:
    print(f"\nGraph Analysis for n={result['n']}, k={result['k']}:")
    print(f"The actual number of edges: {result['actual edges']}")
    print(f"Value of theoretical approximation:
{result['theoretical edges']:.2f}")
    print(f"Value of approximation accuracy:
{result['approximation accuracy']:.2f}%")
Graph Analysis for n=40, k=7:
The actual number of edges: 685
Value of theoretical approximation: 668.57
Value of approximation accuracy: 2.40%
Graph Analysis for n=20, k=5:
The actual number of edges: 160
Value of theoretical approximation: 152.00
Value of approximation accuracy: 5.00%
Graph Analysis for n=10, k=3:
The actual number of edges: 33
Value of theoretical approximation: 30.00
Value of approximation accuracy: 9.09%
```