4/14/2019 Calc Team

Question 2_{views} Daily Challenge 18.6 (Due: Saturday 11/17 at 12:00 noon Eastern)

We continue with the week of exercises rather than challenges.

(1) Exercise: more antiderivatives.

Suppose that F_1 and F_2 are two antiderivatives of f; that is, $F_1'(x) = f(x) = F_2'(x)$. How are F_1 and F_2 related? Must they be equal?

daily_challenge

the students' answer, where students collectively construct a single answer

They both $(F_1 \text{ and } F_2)$ have derivatives equal to f, but we see in the step back back that we gain an unknown constant for each, C_1 and C_2 . Intuitively it need not be true that these constants have the same value, as all constants have the derivative 0 that we observe in f. "They differ by some constant C" as cybirschool words it.

Updated 4 months ago by Logan Pachulski

 $\textbf{the instructors' answer,} \ \textit{where instructors collectively construct a single answer}$

If $F_1'(x)=f(x)=F_2'(X)$, then by linearity the derivative $\frac{d}{dx}(F_1(x)-F_2(x))=0$. But if the derivative of the quantity in parentheses vanishes, that quantity must be equal to a constant C. Thus $F_1(x)=F_2(x)+C$ and the two functions differ by a constant.

Updated 4 months ago by Christian Ferko

followup discussions for lingering questions and comments