

23.6

$$(a) \text{ Integrate } \int x^2 \lambda(x) dx = \frac{m}{L} \int x^2 dx$$

$$= \frac{m}{L} \left[\frac{x^3}{3} \right]_{-\frac{L}{2}}^{\frac{L}{2}}$$

$$= \frac{m}{L} \left(\frac{L^3}{24} + \frac{L^3}{24} \right) = \frac{m}{L} \left(\frac{L^3}{12} \right)$$

$$= \frac{m}{L} \left(\frac{L^3}{24} + \frac{L^3}{24} \right) = mL^2 \cdot \frac{1}{12}$$

$$(b) \text{ Integrate } \int_0^L x^2 \lambda(x) dx = \frac{m}{L} \int_0^L x^2$$

$$\frac{m}{L} \cdot \frac{L^3}{3} = mL^2 \frac{1}{3}$$