4/14/2019 Calc Team

question 2 views

Daily Challenge 18.2

(Due: Tuesday 11/13 at 12:00 noon Eastern)

Reminder: since we will be preparing for Splash this week, I will post much shorter exercises (rather than problems/challenges) for the week of 11/12 to 11/19. Each of these should take 5-10 minutes.

This should leave you more time to finish slides and to catch up on other challenges. I still expect you to finish any overdue DCs before working on these easier ones, and to keep up on these exercise DCs, even while traveling and at Splash.

(1) Exercise: area between curves

Find the area of the region between the graphs of $f(x)=x^2$ and $g(x)=-x^2$ and the vertical lines through (-1,0) and (1,0).

[Hint: the answer is not zero. When we say "between" two graphs, we mean the integral of the upper function minus the integral of the lower function. This always gives a non-negative result, even though the individual integrals we are subtracting each give a signed area.]

daily_challenge

Updated 5 months ago by Christian Ferko

the students' answer, where students collectively construct a single answer

The hint tells us to find the integral of the upper function minus the integral of the lower function on (-1,1); We see that the "anti-derivative" of f is $\frac{1}{3}x^3$, and similarly that of g is $-\frac{1}{2}x^3$; we see by applying the sophomores FTC that

$$\int_{-1}^{1} f = \frac{1}{3} (1)^3 - \frac{1}{3} (-1)^3 = \frac{1}{3} - \frac{-1}{3} = \frac{2}{3} \; ,$$

$$\begin{split} &\int_{-1}^1 g = -\frac{1}{3}(1)^3 - -\frac{1}{3}(-1)^3 = \frac{-1}{3} - \frac{1}{3} = \frac{-2}{3} \;, \\ &\text{so } \int_{-1}^1 f - \int_{-1}^1 g = \frac{4}{2} \text{:wow:} \end{split}$$

Updated 4 months ago by Logan Pachulski

the instructors' answer, where instructors collectively construct a single answer

The area is

$$\int_{-1}^1 \left(x^2 - (-x^2) \right) \ dx = 2 \bigg[\frac{x^3}{3} \bigg]_{-1}^1 = \frac{2}{3} \big((1^3) - (-1)^3 \big) = \frac{4}{3}.$$

Updated 4 months ago by Christian Ferko

followup discussions for lingering questions and comments