# Bitmatrix: A Constant Product Market Maker Based on Recursive Covenants

Bitmatrix is a constant product market maker built on Liquid Network, which utilizes the power of bitcoin opcodes to enable automated liquidity provision across L-BTC and other Liquid assets.

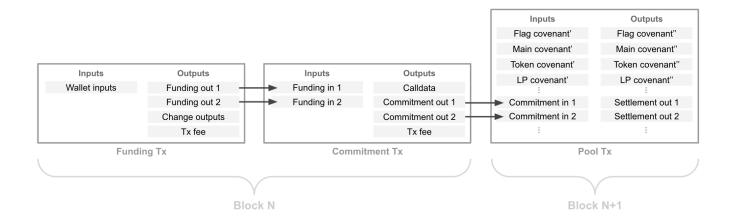
#### 1. Introduction

Bitmatrix is a covenant-based AMM protocol where users can create their pool, add liquidity to an existing pool, or swap two assets. A Bitmatrix pool is made of covenants that interoperate and enforce constraints, resulting in a fully-functional AMM based on the UTXO model. Bitmatrix users can interact with pools across multiple front-ends, such as the web-based Bitmatrix interface, a mobile device, or an Elements node. Whether swapping two assets or adding or removing liquidity, numerous users can asynchronously transact regardless of the type of interaction.

A Bitmatrix interaction involves three subsequent transactions;

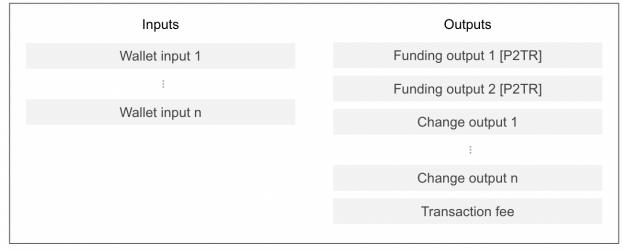
- 1. Funding transaction
- 2. Commitment transaction
- 3. Pool transaction

The *funding* and *commitment transactions* are created and broadcasted altogether, forming an unconfirmed parent-child chain. Outputs from *commitment transactions* are constrained to one block relative locktime, making them spendable in *pool transactions* once they are confirmed. This measure is taken to avoid attack vectors related to transaction pinning. Given one-minute blocks in Liquid, a Bitmatrix interaction can take one to two minutes to finalize, depending on when the interaction is attempted.



# 2. Funding Transaction

A Funding Transaction is signed and broadcasted by the user's wallet upon attempting to swap two assets or add/remove liquidity over a Bitmatrix pool. A Funding Transaction can come with various wallet inputs and change outputs but must construct two exact funding outputs to spend in the subsequent commitment transaction.



Funding Tx

# 2.1 Commitment Transaction Output Template

A template of Commitment Transaction outputs is mapped out before constructing a Funding Transaction. It's a 309-byte construction made of 11 items concatenated end to end. A single SHA256 of the entire bytedata is named "Commitment Transaction Output Template Hash".

Items	Bytes
Calldata [OP_RETURN] scriptPubKey	81
Calldata [OP_RETURN] amount	8
Calldata [OP_RETURN] asset ID	32
Commitment output 1 [P2TR] scriptPubKey	34
Commitment output 1 [P2TR] amount	8
Commitment output 1 [P2TR] asset ID	32
Commitment output 2 [P2TR] scriptPubKey	34
Commitment output 2 [P2TR] amount	8
Commitment output 2 [P2TR] asset ID	32
Transaction fee amount	8
Transaction fee asset ID	32

# 2.2 Funding Outputs

Funding output 1 and Funding output 2 are P2TR constructions whose tapscript constrain both outputs to a pre-defined *commitment transaction output template hash*:

//Inspect 1st output

<0> INSPECTOUTPUTSCRIPTPUBKEY <0> INSPECTOUTPUTVALUE <0> INSPECTOUTPUTASSET

//Inspect 2nd output

<1> INSPECTOUTPUTSCRIPTPUBKEY <1> INSPECTOUTPUTVALUE <1> INSPECTOUTPUTASSET

//Inspect 3rd output

<2> INSPECTOUTPUTSCRIPTPUBKEY <2> INSPECTOUTPUTVALUE <2> INSPECTOUTPUTASSET

//Inspect fee output

<3> INSPECTOUTPUTVALUE <3> INSPECTOUTPUTASSET

//Compute Commitment Transaction Output Template Hash

CAT CAT CAT SHA256

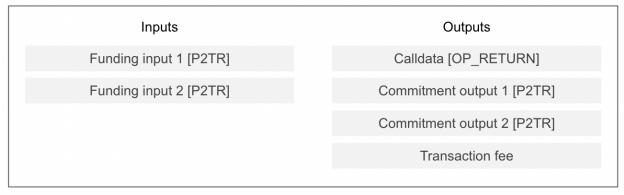
//Compare computed hash to stored hash

<Commitment Transaction Output Template Hash> EQUAL

The script TapLeaf should be tweaked with users' recovery key in case a *commitment transaction template* is somehow non-constructible. scriptPubKeys of *funding output 1* and *funding output 2* are accordingly created to contain the final tweaked result. The funding transaction is signed and broadcasted afterward.

### 3. Commitment Transaction

A commitment transaction commits to reserving a slot in a pool transaction. It's made of a standardized construction of 2 inputs and 4 outputs. The two funding outputs from the *funding transaction* are spent in the *commitment transaction* while no additional inputs are permitted. A *commitment transaction* is made of two commitment outputs, namely *commitment output 1* and *commitment output 2*. Plus an OP RETURN and a fee output.



Commitment Tx

Commitment output 1 carries L-BTC supply at all times, in contrast to commitment output 2 whose asset type depends on the type of interaction:

Case	Commitment Output 1 Asset	Commitment Output 2 Asset
Swap L-BTC for Token	L-BTC (fees + supply)	L-BTC (dust)
Swap Token for L-BTC	L-BTC (fees)	Token (supply)
Add Liquidity	L-BTC (fees + supply)	Token (supply)
Remove Liquidity	L-BTC (fees)	LP (supply)

### 3.2 Calldata

The first output of every *commitment transaction* is an OP\_RETURN followed by a 78-byte PUSHDATA called Calldata. Aggregator nodes parse this data to interpret how to spend commitment outputs in a *pool transaction*. The 78-byte push is a concatenation of 5 items:

Calldata Items	Bytes
Target Flag Asset ID	32
Method Call	1
Recipient Public Key	33
Slippage Tolerance	8
Ordering Fees	4

# 3.2.1 Target Flag Asset ID

The first item in Calldata is a 32-byte Target Flag Asset ID indicating the destination *pool transaction* where commitment outputs are made only spendable. As each Bitmatrix trading pair runs on different *pool transactions*, and each *pool transaction* is identifiable via a unique flag asset, commitment outputs are constrained to the target pool's flag asset ID.

#### 3.2.2 Method Call

The second item in Calldata is a single-byte Method Call indicating the type of interaction the user is aiming for with the Bitmatrix pool. Associated bytecodes are as follows:

Method Types	Bytecode
Swap L-BTC for Token	0x01
Swap Token for L-BTC	0x02
Add Liquidity	0x03
Remove Liquidity	0x04

# 3.2.3 Recipient Public Key

The third item in Calldata is a 33-byte compressed public key used to represent;

### 1. Settlement Output Witness Program

Recipient Public Key is encoded in a P2WSH construction where Settlement Outputs in *pool transaction* live in:

<0x01000000> CHECKSEQUENCEVERIFY <Recipient Public Key> CHECKSIG

The script enforces one block relative locktime to avoid reverse transaction pinning attacks that will later be explained in the paper. A v0 P2WSH witness program is preferred since a much less efficient script-path must be followed if this otherwise was a v1 P2TR witness program.

### 2. Recovery key

Recipient Public Key is encoded in a timeout path where Commitment Outputs in *commitment transactions live*.

# 3.2.4 Slippage Tolerance

The fourth item in Calldata is an 8-byte Slippage Tolerance indicating the minimum amount of swap amount users can receive where anything below gets programmatically canceled. Slippage tolerance must be a valid script number and is set to 0x00000000000000 if the method call is a non-swap type (0x03 or 0x04).

# 3.2.5 Ordering Fees

The sixth item in Calldata is a 4-byte ordering fees field indicating the amount of sats users are offering to reserve a slot in *pool transaction*. Commitment outputs in *pool transactions* are ordered according to a fee market which is determined by *ordering fees*. Ordering fees is a signed 32-bit integer and must be greater than 1.

# 3.3 Commitment Outputs

Commitment output 1 and output 2 are P2TR constructions whose Tapscript constrain both outputs to a Target Flag Asset ID in a success case and a Recipient Public Key in a timeout case. The following TapScript is given to commitment outputs:

//Success path:
IF
<0x01000000> CHECKSEQUENCEVERIFY
<0> INSPECTINPUTASSET < Target Flag Asset ID> EQUAL

//Timeout path:
ELSE
<0> INSPECTINPUTASSET < Target Flag Asset ID> EQUAL NOT VERIFY
<0x3c000000> CHECKSEQUENCEVERIFY
<Recipient Public Key> CHECKSIG
ENDIF

The script compiles to bytecode (variables surrounded with square brackets):

0x630401000000b200c820 [TargetFlagAssetID] 876700c820 [TargetFlagAssetID] 879169043c000000b221 [RecipientPublicKey] ac 68

The script TapLeaf is tweaked with a point with an unknown discrete logarithm to eliminate a key-path spend:

0x021dae61a4a8f841952be3a511502d4f56e889ffa0685aa0098773ea2d4309f624

A P2TR witness program is created from the final tweaked key result and is given to both Commitment output 1 and Commitment output 2 scriptPubkeys.

# 3.1 Tapscript Mask

In order to inspect user-provided P2TR commitment inputs further in *pool transaction*, tapscript bytedata for each input is provided in witness. Inside the main covenant script, each tapscript bytedata from the witness is tweaked with a pre-determined internal key with an unknown discrete logarithm to match the tweaked keys in previous scriptPubkeys.

The witness script applies a bitwise AND between the encoded *tapscript Mask* and each tapscript bytedata and compares the result to tapscript bytedata themselves.

# **4 Pool Transaction**

Pool Transaction is the main transaction where each interaction occurs in a global state. User commitment outputs are spent in this transaction as they commit to reserving a slot. These outputs are of the type anyone-can-spend and can collectively spend.



A Pool Transaction includes 4 covenant spends on the input side and 4 new covenant constructions on the output side, each from index #0 to index #4. A transaction fee and service fee output are placed at the bottom, with varying slots in between.

Each slot is made of two commitment inputs and two settlement outputs. Slots are ordered according to a fee market but are ordered lexicographically when they offer the same fee.

# 4.1 Flag Holder Covenant

Flag holder covenant is a special type of covenant carrying a unique asset called Flag Asset with one unit supply and 0 precision. A flag asset is issued before pool creation and given to the Flag holder covenant at the point of pool creation. All three other covenants, Main covenant, Token holder covenant, and LP holder covenant, are constrained to Flag Asset ID and therefore made only spendable in the presence of Flag holder covenant. Flag holder covenant is spent at the input index #0 and re-constructed at the output index #0. The covenant TapScript is as follows:

//Make sure it's spent at the input index #0

PUSHCURRENTINPUTINDEX <0> EQUALVERIFY

//Make sure its re-constructed at the output index #0

PUSHCURRENTINPUTINDEX INSPECTINPUTASSET <0> INSPECTOUTPUTASSET EQUALVERIFY

//Make sure Token holder covenant, LP holder covenant, and Main covenant are included

- <0> INSPECTINPUTOUTPOINT <0x000000000 EQUALVERIFY DUP DUP</p>
- <1> INSPECTINPUTOUTPOINT <0x01000000> EQUALVERIFY EQUALVERIFY
- <2> INSPECTINPUTOUTPOINT <0x02000000> EQUALVERIFY EQUALVERIFY
- <3> INSPECTINPUTOUTPOINT <0x03000000> EQUALVERIFY

#### 4.2 Token Holder Covenant

Token holder covenant carries Token liquidity as a pair to L-BTC liquidity held by main covenant. It's always spent at the input index #1 and re-constructed at the output index #1. Its TapScript constrain funds to target asset ID:

//Make sure it's spent at the input index #1

PUSHCURRENTINPUTINDEX <1> EQUALVERIFY

//Make sure its constrained to a target asset ID

<0> INSPECTINPUTASSET <0x01> EQUALVERIFY <Target Asset ID> EQUALVERIFY

### 4.3 LP Holder Covenant

LP holder covenant carries a pool of pre-minted LP tokens. When liquidity is added, LP tokens are given to liquidity providers proportional to added liquidity. When liquidity is removed, LP tokens are redeemed back to the pool proportional to removed liquidity. LP holder covenant is always spent at input index #2 and re-constructed at output #2. It's TapScript constraining funds to flag asset ID:

//Make sure it's spent at the input index #2

PUSHCURRENTINPUTINDEX <2> EQUALVERIFY

//Make sure its constrained to a target asset ID

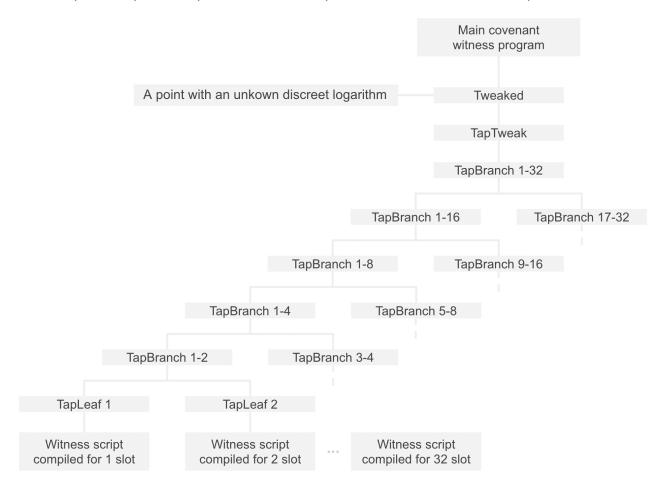
<0> INSPECTINPUTASSET <0x01> EQUALVERIFY <Target Asset ID> EQUALVERIFY

Flag holder covenant, Token holder covenant, and LP holder covenant TapScripts are all tweaked with a point with an unknown discrete logarithm to eliminate a key-path spend:

0x021dae61a4a8f841952be3a511502d4f56e889ffa0685aa0098773ea2d4309f624

#### 4.4 Main Covenant

The main covenant inside a pool transaction is a custom P2TR witness program that commits to a 32-leaf MAST construction. Each leaf index reflects the number of concurrent user calls in that leaf spend. As the number of leaves is bounded by 32 and given 1-minute blocks in Liquid, a Bitmatrix pool can process up to 32 interactions per minute or 0.53 interactions per second.



When constructing MAST, script bytedata for a single slot is compiled 32 times, each time re-adding itself endwise the times of leaf index. When spending the main covenant, a 193-byte control block is mapped out for a leaf that accommodates the number of concurrent interactions that exist in that period. Lower index leaves can be replaced with higher index leaves when the number of concurrent user calls is less than 32. When the number of concurrent user calls hits 32 or greater, an internal fee market occurs, and therefore original versions of a 32nd leaf spend can be replaced with newer versions of a 32nd leaf spend.

# 4.4.1 Concurrency

By leveraging Tapscript (BIP 342), Relative lock-time (BIP 68), and Replace-by-fee (BIP 125), multiple users can asynchronously interact with a Bitmatrix pool in a fully on-chain logic.

# 4.4.1.1 Replacement Logic

A built-in replacement logic enforced by the Bitcoin script when leveraged with BIP-125 allows concurrent users to compete over a fee market to reserve a slot in a 32-seat pool transaction.

The four base covenants in a pool transaction and all user-provided inputs signal replaceability. This is so that anyone can submit newer versions of a pool transaction within a minute as long as paying a greater absolute fee plus their bandwidth according to BIP-125. Since commitment inputs are of-type anyone-can-spend, any Elements node can monitor the network and order user calls according to a fee market based on how much fee each offers.

#### Based on parameters;

- I. *b* is the base fee amount that must be paid by every user set to 1200 sats.
- II. *o* is the ordering fee a user can offer varying from 1 to 2147482647 sats.
- III. m is the maximum number of slots available in a Pool Transaction set to 32 seats.
- IV. c is the present number of reserved slots (user calls) in a Pool Transaction bounded by m
- V. g is the vByte-length gap between two subsequent leaves in witness and base txn, set to 560 vBytes = 230 base bytes + 193 script body vBytes + 136 stack element vBytes.
- VI. s is the number of vBytes single-leaf pool spend consumes, set to 1377 vBytes.
- VII. r is the default Elements minimum relay fee set to 10 vByte/sat (0.1 sat/vByte).

Fees paid by the *transaction fee output* is calculated as  $fp = \frac{\sum\limits_{n=o1}^{oc} n+b}{3} + \frac{\left(\sum\limits_{n=o1}^{oc} n+b\right)*2*c}{3*m}$ . The formula is based on allowing newer versions of pool transactions to be replaced with original versions. Given the total fees offered by all users  $ft = \sum\limits_{n=o1}^{oc} n+b$ , the remaining fees are paid extra to service fee output fr = ft - fp.

The fourth rule of BIP-125 requires that the replacement transaction must pay for its bandwidth at or above the rate set by the node's minimum relay fee setting.

A replacement Pool Transaction at index *c* bounded by *m*;

• Pays for bandwidth 
$$\Delta b = \frac{\sum\limits_{n=o1}^{oc} n+b}{3} - \frac{\sum\limits_{n=o(c-1)}^{o(c-1)} n+b}{3} + \frac{\left(\sum\limits_{n=o1}^{oc} n+b\right)*2*c}{3*m} - \frac{\left(\sum\limits_{n=o(c-1)}^{o(c-1)} n+b\right)*2*c}{3*m}$$

• Must pay for bandwidth  $bp = \frac{s + (c-1)*g}{r}$ 

Given hardcoded values m = 32, r = 10, and b = 1000the statement  $\Delta b > bp$  is true at all times when c < m is true. An internal fee market competition occurs when c = m becomes true.

# 4.4.2 Spend Structure

A single main covenant spend takes a 193-byte control block at the bottom, a varying-size witness script, and a varying number of slot inputs that satisfy the witness script, each taking 3 stack elements. Therefore the main covenant spend has a witness element count of 2 + 3n for a value of n that is an integer between 1 and 32.



### 4.4.2.2 Slot Witness Elements

Each slot in the main covenant spend takes 3 stack elements, summing at 135.75-vBytes:

Hardcoded values	Bytes
Commitment Transaction Base Bytedata	418
Commitment Input Tapscript Bytedata	124
Commitment Input Tweaked Key Prefix	1



# 4.4.2.2.1 Commitment Transaction Base Bytedata

Non-witness bytedata of a standardized 419-base-byte *commitment transaction* is provided in witness. The witness script inspects transaction bytedata to read *calldata* within the serialization.

# 4.4.2.2.2 Commitment Input Script Bytedata

The tapscript bytedata of a commitment input is provided in witness. The witness script inspects the tapscript bytedata to avoid potential pinning attacks.

# 4.4.2.2.3 Commitment Input Tweaked Key Prefix

A TWEAKVERIFY operation is used to verify the authenticity of inspected tapscript. In order to input the tweaked key into TWEAKVERIFY, the commitment input scriptPubkey is inspected, and the 32-byte witness program is parsed. However, tweaked keys' one-byte prefix is unknown over

introspection and is therefore provided in witness. The 32-byte witness program is concatenated with Commitment Input Tweaked Key Prefix to construct the full 33-byte tweaked key.

# 4.4.2.3 Witness Script

The main covenant witness script is a varying-size expressive tapscript that validates the correct execution of each slot. Witness script is divided into three parts for better conceptualizing:

- 1. Witness Script Header
- 2. Witness Script Body
- 3. Witness Script Footer

# 4.4.2.3.1 Witness Script Header

The script header starts with six values hardcoded at the beginning of the witness script. The values are used in certain operations taking place in the script body.

Hardcoded values	Bytes
L-BTC Asset ID	32
Token Asset ID	32
Commitment Input TapScript Mask	124
A point with an unknown discrete logarithm	32
The string "TapLeaf"	7
The string "TapTweak"	8

----- BEGIN SCRIP HEADER -----

//L-BTC Asset ID

<0x6d521c38ec1ea15734ae22b7c46064412829c0d0579f0a713d1c04ede979026f>

//Token Asset ID

<0x[TOKEN\_ASSET\_ID]>

//Commitment Input TapScript Mask

//A point with an unkown discreet logarithm

<0x1dae61a4a8f841952be3a511502d4f56e889ffa0685aa0098773ea2d4309f624>

//The string "TapLeaf" in bytes

<0x5461704c656166>

//The string "TapTweak" in bytes

<0x546170547765616b>

//Inspect number of inputs

#### INSPECTNUMINPUT

//Constrain number of inputs

<Number of inputs in respective leaf spend> EQUALVERIFY

//Inspect number of outputs

#### INSPECTNUMOUTPUT

//Constrain number of outputs

<Number of outputs in respective leaf spend> EQUALVERIFY

//Constrain main covenant to a target asset ID

<0> INSPECTINPUTASSET <0x01> EQUALVERIFY <Target Asset ID> EQUALVERIFY

//Inspect pool L-BTC supply

<3> INSPECTINPUTVALUE

//Verify the prefix(1)

<0x01> EQUALVERIFY

//Send pool L-BTC supply to altstack

**TOALTSTACK** 

//Inspect pool Token supply

<1> INSPECTINPUTVALUE

//Verify the prefix(1)

<0x01> EQUALVERIFY

//Send pool Token supply to altstack

**TOALTSTACK** 

//Inspect pool LP supply and verify the prefix(1)

<2> INSPECTINPUTVALUE <0x01> EQUALVERIFY

//Send pool LP supply to altstack

TOALTSTACK

//Send int 0 (total tx fees) to altstack

<0> TOALTSTACK

//Send max 32-bit signed int to altstack (to compare 1.st index ordering fee)

<2147483647> TOALTSTACK

----- END SCRIP HEADER -----

# 4.4.2.3.2 Witness Script Body

The witness script header is followed by a varying-size witness script body making the most critical part of the overall covenant design. The witness script body hosts script enforcements for each slot. It can accommodate a minimum of 1 and a maximum of 32 slots which are serialized end-to-end and executed in order. Each slot block consists of 4 parts:

- 1. Commitment Input TapScript Inspection
- 2. Commitment Transaction Calldata Inspection
- 3. Method Call Preparations
- 4. Method Call Cases

**EQUALVERIFY** 

# 4.4.2.3.2.1 Commitment Input Inspection

The witness-provided commitment input tapscript bytedata is inspected to match a pre-defined script pattern (Tapscript mask). A TWEAKVERIFY operation is used to verify that commitment input tapscript bytedata really commits to scriptPubKeys of commitment inputs:

BEGIN SCRIP BODY
BEGIN SLOT 1
//Calculate TapLeaf given script bytedata <1> PICK SHA256 DUP CAT <0xc0> CAT <7> PICK SIZE SWAP CAT CAT SHA256
//Calculate TapTweak given hardcoded internal key and TapLeaf <1> PICK SHA256 DUP CAT <4> PICK <2> ROLL CAT CAT SHA256
<3> PICK SWAP <8> ROLL
//Make sure commitment inputs share the same scriptPubkey, and inspect their tweaked key <3+N> INSPECTINPUTSCRIPTPUBKEY DUP <4+N> INSPECTINPUTSCRIPTPUBKEY EQUALVERIFY
//Verify witness version 1 <1> VERIFY
//TweakVerify given hardcoded internal key, TapLeaf, and inspected tweaked key TWEAKVERIFY
//A bitwise AND between TapScript Mask and each tapscript bytedata from the witness are computed, and the result is compared to each tapscript bytedata.  <6> ROLL DUP <5> PICK AND EQUALVERIFY
//Fetch commitment input 1 outpoints and verify their output index <n> INSPECTINPUTOUTPOINT &lt;0x01000000&gt; EQUALVERIFY DUP</n>
//Fetch commitment input 2 outpoints and verify their output index <n+1> INSPECTINPUTOUTPOINT &lt;0x02000000&gt; EQUALVERIFY</n+1>
//Verify commitment input 1, and commitment input 2 are from the same previous transaction ID

# 4.4.2.3.2.2 Commitment Transaction Inspection

The witness-provided commitment transaction base bytedata is hashed to match the inspected commitment input outpoints. Then the whole transaction bytedata is parsed to extract individual calldata elements within the transaction serialization:

----- CONTINUE SLOT 1 -----

/////Fetch commitment transaction base bytedata, and make 4 copies

<7> ROLL DUP 2DUP

/////Hash base tx bytedata and compare to commitment input prvtxid

HASH256 <4> ROLL EQUALVERIFY

/////Enforce size 418-bytes

SIZE <418> EQUALVERIFY

//Parse 2nd sequence field and EQUALVERIFY ffffffff

<84> <4> SUBSTR <0xfffffff> EQUALVERIFY

//Parse number of inputs and make sure its 4

<88> <1> SUBSTR <0x04> EQUALVERIFY

//Parse the first output (OP RETURN)

<133> <81> SUBSTR

//Make sure its an op return and parse pushdata

DUP <0> <1> SUBSTR <0x6a> EQUALVERIFY <3> <78> SUBSTR

//Parse target flag asset ID and verify

DUP <0> <32> SUBSTR

//Inspect flag holder covenant asset ID and verify the prefix(1)

<0> INSPECTINPUTASSET

//Verify the prefix(1)

<0x01> EQUALVERIFY

//Constrain user call to Target Asset ID

**EQUALVERIFY** 

//Parse calldata to extact method call

DUP <32> <1> SUBSTR

//Parse calldata to extact recipient public key

SWAP DUP <33> <33> SUBSTR

//Parse calldata to extact slippage tolerance

SWAP DUP <66> <8> SUBSTR

//Parse calldata to extact ordering fees

SWAP <74> <4> SUBSTR

# 4.4.2.3.2.3 Method Call Preparation

A set of preparations made to get the stack ready for final method call cases:

----- CONTINUE SLOT 1 -----

//Get lower index ordering fees from the stack

#### FROMALTSTACK

//Get total ordering fees from the stack

#### FROMALTSTACK

//Make a copy of current-index ordering fees

#### <2> PICK

//Update total ordering fees

#### ADD

//Send updated total ordering fees to altstack

#### TOALTSTACK

//Send lower index ordering fees to altstack

#### TOALTSTACK

//Make a copy of current ordering fees

#### DUP

//Make sure current ordering fees is greater than 1 sat

### <1> GREATERTHANOREQUAL VERIFY

//Inspect commitment input 1 asset and verify the prefix(1)

### <3+N> INSPECTINPUTASSET <0x01> EQUALVERIFY

//Make a copy of the L-BTC asset ID (copying from the script header)

#### <10> PICK

//Verify commitment input 1 assetID(32) is L-BTC

#### **EQUALVERIFY**

//Make a copy of current-index ordering fees and get lower index ordering fees from altstack

#### DUP FROMALTSTACK

//Make a copy of current-index ordering fees lower-index ordering fees

#### 2DUP

//Compare current-index ordering fees to lower-index ordering fees

#### LESSTHAN

//If current-index ordering fees is smaller than the lower-index ordering fees

#### IF

//Ordering is based on a valid fee market. Drop copies of current-index and lower-index ordering fees

#### 2DROP

//If current-index ordering fees is not smaller than the lower-index ordering fees

#### ELSE

//Both ordering fees must be equal; otherwise, fail. Lexicographical ordering will be enforced.

#### **EQUALVERIFY**

//Inspect current-index slot commitment input 1 outpoint

#### <3+N> INSPECTINPUTOUTPOINT

//Remove vout(4) and outpoint flag(1) to keep txid(32)

#### 2DROP

//Splice the first 8 bytes of current-index commitment input txid(32)

#### <8> LEFT

//Inspect lower-index slot commitment input 1 outpoint

#### <1+N> INSPECTINPUTOUTPOINT

//Remove vout(4) and outpoint\_flag(1) to keep txid(32)

#### 2DROP

//Splice the first 8 bytes of lower-index commitment input txid(32)

#### <8> LEFT

//Enforce lexicographical ordering by comparing the two previous txid(32)

#### LESSTHAN64 VERIFY

//Drop copies of current-index and lower-index ordering fees

#### 2DROP

#### **ENDIF**

//Make a copy of current ordering fees

#### DUP

//Send the copy of current ordering fees to altstack for higher-index slot comparisons

#### **TOALTSTACK**

//Add base fee 1200 sats to current ordering fees, making up total tx fees

#### <1200> ADD

//Convert total tx fees to LE64

#### SCIPTNUMTOLE64

//Inspect commitment input 1 L-BTC value and verify the prefix(1)

#### <3+N> INSPECTINPUTVALUE <0x01> EQUALVERIFY

#### **SWAP**

//Subtract total L-BTC provided from tx fees, making up available user L-BTC amount remaining

#### SUB64

//Make sure available user L-BTC remaining is greater than 500 sats

#### DUP <500> SCIPTNUMTOLE64 GREATERTHAN64 VERIFY

//Get current-index ordering fees from altstack

#### FROMALTSTACK

//Get up-to-latest-index total accumulated fees from altstack

#### FROMALTSTACK

//Get current-index ordering fees from altstack

#### FROMALTSTACK

//Update total accumulated fees by adding the current-index base fee

#### <1200> ADD

//Get LP token pool supply from altstack

#### FROMALTSTACK

//Get Token pool supply from altstack

#### FROMALTSTACK

//Get L-BTC pool supply from altstack

#### FROMALTSTACK

//Calculate P2WSH witness program given receipent public key

#### <0x0401000000b221> <8> ROLL <Recipient Public Key> <0xac> CAT CAT SHA256

//Inspect commitment output1 scriptPubkey

#### <3+N> INSPECTOUTPUTSCRIPTPUBKEY

//Constrain commitment output1 witness version to v0:

#### <0> EQUALVERIFY

//Constrain commitment output1 witness program to calculated witness program

#### **EQUALVERIFY**

//Fetch method call extracted from calldata

#### <7> ROLL

//If the method call is either 1, 2, or 3:

#### DUP <3> LESSTHANOREQUAL

IF

//Inspect settlement output 2 asset

#### <4+N> INSPECTOUTPUTASSET

//Verify the prefix(1)

#### <0x01> EQUALVERIFY

//Verify the assetID(32) is L-BTC

#### <14> PICK EQUALVERIFY

//Inspect settlement output 2 value

#### <4+N> INSPECTOUTPUTVALUE

//Verify the prefix(1)

#### <0x01> EQUALVERIFY

//Verify the value(8) is 0

#### <0> SCIPTNUMTOLE64 EQUALVERIFY

//Verify scriptPubKey is an empty OP\_RETURN

### INSPECTOUTPUTSCRIPTPUBKEY <-1> EQUALVERIFY <0x6a0100> SHA256 EQUALVERIFY

**ENDIF** 

# 4.4.2.3.2.4 Method Call Cases

One of four code blocks is executed based on the method call parsed from the calldata:

CONTINUE SLOT 1	
//If the method call is 1: DUP <1> EQUAL IF DROP	
BEGIN CASE 1 : Swap L-BTC for Toke	en
END CACE 4 · Cover I DTC for Talcov	_
ENDIF	]
//If the method call is 2:	
DUP <2> EQUAL IF DROPBEGIN CASE 2 : Swap Token for L-BT	
END CASE 2 : Swap Token for L-BTC ENDIF	)
//If the method call is 3:	
DUP <3> EQUAL IF DROP BEGIN CASE 3 : Add Liquidity -	
·	
END CASE 3 : Add Liquidity	
ENDIF //If the method call is 4:	
DUP <4> EQUAL IF DROP	
BEGIN CASE 4 : Remove Liquidity .	/
END CASE 4 : Remove Liquidity -	
ENDIF	
END SLOT 1	
BEGIN SLOT N	
END SLOT N	
END SCRIPT BODY	

# 4.4.2.3.2.4.1 Swap L-BTC for Token

A swap-in L-BTC amount, a base fee of 1200, an ordering fee varying from 1-2147483647, and a dust 546 sats are supplied in the commitment transaction. The pool transaction constrains settlement output 1 to the Token swap-out amount based on the CPMM formula in a success case and to the initial L-BTC swap-in amount in a slippage failure case.

Inputs	Asset	Amount
Commitment Input 1	L-BTC	Swap-in Amount + Base Fee (1200) + Ordering Fee (1-2147483647)
Commitment Input 2	L-BTC	Dust (546)
Outputs (Success)	Asset	Amount
Settlement Output 1	Token	Swap-out Amount
Settlement Output 2	L-BTC	0 [OP_RETURN]
Outputs (Out of Slippage)	Asset	Amount
Settlement Output 1	L-BTC	Swap-in Amount
Settlement Output 2	L-BTC	0 [OP_RETURN]

#### Based on parameters;

- I. slis a state of L-BTC pool supply held by the main covenant
- II. stis a state of Token pool supply held by the Token holder covenant
- III. si is the swap-in L-BTC amount that the user commits
- IV. *lf* is the liquidity provider fee charged from the swap-in amount
- V. so is the swap-out Token amount that the user receives
- VI. s is the Token slippage limit
  - 1. A %0.2 LP fee is calculated  $lf = \frac{si}{500}$
  - 2. New tradable swap-in amount si' = si lf
  - 3. L-BTC pool supply for constant sl' = sl si
  - 4. L-BTC pool supply for constant (downgraded 16x)  $sl'' = \frac{sl'}{16}$
  - 5. Token pool supply downgraded (downgraded 2097152)  $st' = \frac{st}{2097152}$
  - 6. Tradable L-BTC swap-in amount downgraded (downgraded 16x)  $si'' = \frac{si'}{16}$
  - 7. The new state of Token pool supply  $st'' = \frac{st''*st'}{st''}$
  - 8. Final Token pool supply (magnified 2097152x) st''' = st'' \* 2097152
  - 9. Token user received so = st st'''
  - 10. Final L-BTC pool supply sl''' = st + si
  - 11. Success if s > so'

---- BEGIN CASE 1 : Swap L-BTC for Token - - -//Inspect commitment input 2 asset <4+N> INSPECTINPUTASSET //Verify the prefix(1) <0x01> EQUALVERIFY //verify the assetID(32) is L-BTC <13> PICK EQUALVERIFY //Inspect commitment input 2 value <4+N> INSPECTINPUTVALUE //Verify the prefix(1) <0x01> EQUALVERIFY //Verify the value(8) is dust <546> SCIPTNUMTOLE64 <0x2202000000000000 EQUALVERIFY //Fetch commitment input 1 tradable L-BTC supply <5> ROLL //Make two copies send one to altstack DUP DUP TOALTSTACK //Calculate LP fee %0.2 <500> SCIPTNUMTOLE64 DIV64 //Verify no overflow and remove remainder **VERIFY NIP** //Subtract LP fees from the L-BTC amount and verify no overflow SUB64 VERIFY //Make a copy of the total L-BTC pool supply <1> PICK //Add existing pool supply with new pool supply to calculate new token pool supply and verify no overflow ADD64 VERIFY //Make a copy of the total L-BTC pool supply and downgrade precision (Minimum unit to 16 sats) <1> PICK <16> SCIPTNUMTOLE64 DIV64 //Verify no overflow **VERIFY** //Make a copy of the total Token pool supply and downgrade precision (Minimum unit to 2097152) <3> PICK <2097152> SCIPTNUMTOLE64 DIV64 //Verify no overflow **VERIFY** //Multiply the two downgraded pool supply to calculate the constant value and verify no overflow

**MUL64 VERIFY** 

//Make a copy of L-BTC pool supply for constant and downgrade precision (Minimum unit to 16 sats)

#### <1> PICK <16> SCIPTNUMTOLE64 DIV64

//Verify no overflow

**VERIFY** 

//Divide constant with L-BTC pool supply to calculate the new Token pool supply and verify no overflow

#### **DIV64 VERIFY**

//Magnify the new Token pool supply and verify no overflow

#### <2097152> SCIPTNUMTOLE64 MUL64

//Verify no overflow

**VERIFY** 

**SWAP** 

//Make a copy of the previous Token pool supply

<3> PICK

//Make a copy of the new Token pool supply

<2> PICK

//Subtract the previous Token pool supply with the new token pool supply, making Tokens user received

#### SUB64

//Verify no overflow

**VERIFY** 

//Remove L-BTC pool supply for constant

NIP

//Make a copy of L-BTC initial pool supply

<2> PICK

//Get tradable L-BTC supply from altstack, make one copy, and sand the copy to altstack

#### FROMALTSTACK DUP TOALTSTACK

 $/\!/ Add \ initial \ L-BTC \ pool \ supply \ with \ tradable \ user \ L-BTC \ supply \ to \ calculate \ the \ final \ L-BTC \ pool \ supply$ 

ADD64

//Verify no overflow

**VERIFY** 

**SWAP** 

//Fetch slippage limit parsed from calldata

<8> ROLL

//Make a copy of the amount received

PICK

//Check slippage overflow

GREATERTHANOREQUAL64 2DROP <1> <1> EQUAL

//If the slippage is not overflowed: IF //Inspect settlement output 1 asset <3+N> INSPECTOUTPUTASSET //Verify the prefix(1) <0x01> EQUALVERIFY //Get Token asset ID <13> PICK //Verify that settlement output 1 holds the Token assetID(32) **EQUALVERIFY** //Inspect settlement output 1 amount and verify the prefix(1) <3+N> INSPECTOUTPUTVALUE <0x01> EQUALVERIFY //Verify that settlement output 1 holds the same value(8) **EQUALVERIFY** //Fetch old token pool supplies and drop <3> ROLL <3> ROLL 2DROP //If the slippage is overflow **ELSE** //Inspect settlement output 1 asset <3+N> INSPECTOUTPUTASSET //Verify the prefix(1) <0x01> EQUALVERIFY //Make a copy of Token asset ID and verify that settlement output 1 holds the L-BTC assetID(32) <14> PICK EQUALVERIFY //Drop overflown token received amount and the two new failed pool supply DROP 2DROP //Get tradable user L-BTC amount from altstack FROMALTSTACK //Inspect settlement output 1 amoun <3+N> INSPECTOUTPUTVALUE //Verify the prefix(1) <0x01> EQUALVERIFY //Verify that settlement output 1 holds the same value(8) **EQUALVERIFY ENDIF** //Send top 5 stack elements to altstack for further higher index slot interpretations TOALTSTACK TOALTSTACK TOALTSTACK TOALTSTACK 

# 4.4.2.3.2.4.2 Swap Token for L-BTC

A swap-in Token amount, a base fee 1200, an ordering fee varying from 1-2147483647, and a dust 546 sats are supplied in the commitment transaction. The pool transaction constrains settlement output 1 to the L-BTC swap-out amount based on the CPMM formula in a success case and to the initial Token swap-in amount in a slippage failure case.

Inputs	Asset	Amount
Commitment Input 1	L-BTC	Base Fee (1200) + Ordering Fee (1-2147483647) + Dust (546)
Commitment Input 2	Token	Swap In Amount
Outputs (Success)	Asset	Amount
Settlement Output 1	L-BTC	Swap Out Amount
Settlement Output 2	L-BTC	0 [OP_RETURN]
Outputs (Out of Slippage)	Asset	Amount
Settlement Output 1	Token	Swap In Amount
Settlement Output 2	L-BTC	0 [OP_RETURN]

#### Based on parameters;

- I. slis a state of L-BTC pool supply held by the main covenant
- II. stis a state of Token pool supply held by the Token holder covenant
- III. si is the swap-in Token amount that the user commits
- IV. *lf* is the liquidity provider fee charged from the swap-in amount
- V. so is the swap-out L-BTC amount that the user receives
- VI. s is the L-BTC slippage limit
  - 1. A %0.2 LP fee is calculated  $lf = \frac{si}{500}$
  - 2. New tradable swap-in amount si' = si lf
  - 3. Token pool supply for constant st' = st si
  - 4. Token pool supply for constant (downgraded 2097152x)  $st'' = \frac{st'}{2097152}$
  - 5. L-BTC pool supply downgraded (downgraded 16x)  $sl' = \frac{sl}{16}$
  - 6. Tradable Token swap-in amount downgraded (downgraded 2097152x)  $si'' = \frac{si'}{2097152}$
  - 7. The new state of L-BTC pool supply  $sl'' = \frac{st'''*sl'}{si''}$
  - 8. Final L-BTC pool supply (magnified 16x) sl''' = sl'' \* 16
  - 9. L-BTC user received so = sl sl'''
  - 10. Final Token pool supply st''' = st + si
  - 11. Success if s > so

----- BEGIN CASE 2 : Swap Token for L-BTC ------

//Fetch commitment input 1 tradable L-BTC supply

#### <5> ROLL

//Push a dust value 546 onto stack and verify that commitment input 1 holds dust L-BTC

#### <546> SCIPTNUMTOLE64 EQUALVERIFY

//Inspect commitment input 2 asset and verify the prefix(1)

#### <4+N> INSPECTINPUTASSET <0x01> EQUALVERIFY

//Get Token asset ID and verify that commitment input 2 holds the Token assetID(32)

#### <11> PICK EQUALVERIFY

//Inspect commitment input 2 amount and verify the prefix(1)

#### <4+N> INSPECTINPUTVALUE <0x01> EQUALVERIFY

//Make two copies of Token swap-in amount and send one to altstack

#### DUP DUP TOALTSTACK

//Calculate LP fee %0.2

#### <500> SCIPTNUMTOLE64 DIV64

//Verify no overflow

#### **VERIFY**

//Remove remainder

#### NIP

//Subtract LP fees from the Token amount and verify no overflow

#### SUB64 VERIFY

//Make a copy of the total Token pool supply

#### <2> PICK

//Add existing pool supply with new pool supply to calculate new L-BTC pool supply

#### ADD64 2DROP

//Verify no overflow

#### **VERIFY**

//Make a copy of the total L-BTC pool supply and downgrade precision (Minimum unit to 16 sats)

#### <1> PICK <16> SCIPTNUMTOLE64 DIV64

//Verify no overflow

#### **VERIFY**

//Make a copy of total Token pool supply downgrade precision. (Minimum unit to 2097152)

#### <3> PICK <2097152> SCIPTNUMTOLE64 DIV64

//Verify no overflow

#### **VERIFY**

//Multiply the two downgraded pool supply to calculate the constant value

#### MUL64

//Verify no overflow

#### **VERIFY**

//Make a copy of Token pool supply for constant and downgrade precision (Minimum unit to 2097152)

#### <1> PICK <2097152> SCIPTNUMTOLE64 DIV64

//Verify no overflow

**VERIFY** 

//Divide constant with Token pool supply to calculate the new L-BTC pool supply

DIV64

//Verify no overflow

**VERIFY** 

//Magnify the new L-BTC pool supply

<16> SCIPTNUMTOLE64 MUL64

//Verify no overflow

**VERIFY** 

**SWAP** 

//Make a copy of the previous pool L-BTC supply

<2> PICK

//Make a copy of the new pool L-BTC supply

<2> PICK

//Subtract the pool supply states to calculate the L-BTC user received

SUB64

//Verify no overflow

**VERIFY** 

//Remove Token pool supply for constant

NIP

//Make a copy of Token initial pool supply

<3> PICK

//Get tradable Token supply from altstack, make one copy, and send the copy to altstack

#### FROMALTSTACK DUP TOALTSTACK

//Add initial Token pool supply with tradable user Token supply to calculate the final Token pool supply

ADD64

//Verify no overflow

**VERIFY** 

**SWAP** 

//Fetch slippage limit parsed from calldata

<8> ROLL

//Make a copy of the amount received

<1> PICK

//Check slippage overflow

GREATERTHANOREQUAL64 2DROP <1> <1> EQUAL

//If the slippage is not overflow IF //Inspect settlement output 1 asset and verify the prefix(1) <3+N> INSPECTOUTPUTASSET <0x01> EQUALVERIFY //Make a copy of Token asset ID and <14> PICK //Verify that settlement output 1 holds the L-BTC assetID(32) **EQUALVERIFY** //Inspect settlement output 1 amount <3+N> INSPECTOUTPUTVALUE //Verify the prefix(1) <0x01> EQUALVERIFY //Verify that settlement output 1 holds the same value(8) **EQUALVERIFY** //Fetch old token pool supplies and drop <3> ROLL <3> ROLL 2DROP SWAP //If the slippage is overflow ELSE //Inspect settlement output 1 asset <3+N> INSPECTOUTPUTASSET //Verify the prefix(1) <0x01> EQUALVERIFY //Get Token asset ID and verify that settlement output 1 holds the L-BTC assetID(32) <13> PICK EQUALVERIFY //Drop overflown L-BTC received amount and the two new failed pool supply **DROP 2DROP** //Get tradable user Token amount from altstack FROMALTSTACK //Inspect settlement output 1 amount <3+N> INSPECTOUTPUTVALUE //Verify the prefix(1) <0x01> EQUALVERIFY //Verify that settlement output 1 holds the same value(8) **EQUALVERIFY ENDIF** //Send top 5 stack elements to altstack for further higher index slot interpretations TOALTSTACK TOALTSTACK TOALTSTACK TOALTSTACK ----- END CASE 2: Swap Token for L-BTC -----

# 4.4.2.3.2.4.3 Add Liquidity

An L-BTC supply, a Token supply, a base fee of 1200, an ordering fee varying from 1-2147483647, and a dust 546 sats are supplied in the commitment transaction. The pool transaction constrains settlement output 1 to give the user liquidity shares (LP tokens) proportional to liquidity provided.

Inputs	Asset	Amount
Commitment Input 1	L-BTC	Supply + Base Fee (1200) + Ordering Fee (1-2147483647) + Dust (546)
Commitment Input 2	Token	Supply
Outputs	Asset	Amount
Outputs Settlement Output 1	<b>Asset</b> LP	Amount Liquidity Share

#### Based on parameters;

- I. pl is a state of pool L-BTC supply held by the main covenant
- II. pt is a state of pool Token supply held by the Token holder covenant
- III. plpis a state of pool LP supply held by the LP holder covenant
- V. *olp* is a state of occupied LP supply
- VI. *ul* is the user-added L-BTC supply
- VII. *ut* is the user-added Token supply
- VIII. *ulp* is the LP tokens user receives
- IX. rl is the L-BTC addition ratio
- X. rt is the Token addition ratio
  - 1. Existing pool L-BTC supply magnified 1000x pl' = pl \* 1000
  - 2. Magnified pool L-BTC supply divided to added user L-BTC supply  $rl = \frac{pl'}{ul}$
  - 3. The current pool Token supply magnified 1000x pt' = pt \* 1000
  - 4. Magnified pool Token supply divided to added user Token supply  $rl = \frac{pt'}{nt}$
  - 5. Total occupied LP tokens olp = mlp plp
  - 6. LP tokens user received  $ulp = \frac{olp}{max(rl, rt)} * 1000$
  - 7. New state of occupied LP supply olp' = olp + ulp
  - 8. New state of pool LP supply plp' = plp' ulp

----- BEGIN CASE 3 : Add Liquidity -----

//Push 50000000000000000 max LP pool supply

#### <5000000000000000000>

//Make a copy of the current LP pool supply

#### <3> PICK

//Subtract max LP pool supply with current LP pool supply to get the current LP used

#### SUB64

//Make a copy of the current L-BTC pool supply

#### <1> PICK

//Push int 1000 and convert to LE64

#### <1000> SCIPTNUMTOLE64

//Magnify current L-BTC pool supply 1000 times

#### MUL64

//Verify no overflow

#### **VERIFY**

//Fetch available user L-BTC supply

#### <7> ROLL

//Push int 546 and convert to LE64

#### <546> SCIPTNUMTOLE64

//Subtract 546 from available user L-BTC supply, make one copy and send the copy to altstack

#### SUB64 DUP TOALTSTACK

//Divide magnified L-BTC supply with available user L-BTC supply to calculate the ratio

#### DIV64

//Verify no overflow

#### **VERIFY**

//Make a copy of the current Token pool supply

#### <3> PICK

//Push int 1000 and convert to LE64

#### <1000> SCIPTNUMTOLE64

//Magnify current Token pool supply 10000 times and verify no overflow

#### **VERIFY**

//Inspect commitment input 2 asset

#### <4+N> INSPECTINPUTASSET

//Verify the prefix(1)

#### <0x01> EQUALVERIFY

//Make a copy of Token asset ID

#### <14> PICK

//Verify that commitment input 2 holds the Token assetID(32)

#### **EQUALVERIFY**

//Inspect commitment input 2 amount

#### <4+N> INSPECTOUTPUTVALUE

//Verify the prefix(1)

#### <0x01> EQUALVERIFY

//Make a copy of the commitment input 2 amount and send the copy to altstack

#### DUP TOALTSTACK

//Divide magnified Token pool supply with available user Token supply to calculate the second ratio

#### DIV64

//Verify no overflow

#### **VERIFY**

//Duplicate the two ratios

#### 2DUP

//Compare the two ratios

#### **GREATERTHANOREQUAL64**

ΙF

//Drop the smaller ratio (last stack element)

#### **DROP**

**ELSE** 

//Drop the smaller ratio (second to last stack element)

NIP

### **ENDIF**

//Divide current LP with ratio to calculate LP amount user received

#### DIV64

//Verify no overflow

#### **VERIFY**

//Push int 1000 and convert to LE64

#### <1000> SCIPTNUMTOLE64

//Apply the same 1000x magnification this side to get LP tokens user received

#### MUL64

//Verify no overflow

#### **VERIFY**

//Inspect LP token asset ID

#### <2> INSPECTOUTPUTASSET

//Verify the prefix(1)

#### <0x01> EQUALVERIFY

//Inspect settlement output 1 asset ID

#### <3+N> INSPECTOUTPUTASSET

//Verify the prefix(1) <0x01> EQUALVERIFY //Constrain settlement output 1 to LP token asset ID **EQUALVERIFY** //Make a copy of LP tokens user received DUP //Inspect settlement output 1 amount <4+N> INSPECTOUTPUTVALUE //Verify the prefix(1) <0x01> EQUALVERIFY //Make sure user receives deserved LP tokens **EQUALVERIFY** //Fetch previous LP pool supply <3> ROLL **SWAP** //Update new LP pool supply and verify no overflow SUB64 VERIFY //Fetch previous Token pool supply <2> ROLL //Get Token user supply from altstack FROMALTSTACK //Update new Token pool supply ADD64 //Verify no overflow **VERIFY** //Fetch previous L-BTC pool supply <2> ROLL //Get user L-BTC supply from altstack FROMALTSTACK //Update new L-BTC pool supply ADD64 //Verify no overflow **VERIFY** //Send top 5 stack elements to altstack for further higher index slot interpretations TOALTSTACK TOALTSTACK TOALTSTACK TOALTSTACK //Drop slippage limit DROP ----- END CASE 3 : Add Liquidity ----

# 4.4.2.3.2.4.4 Remove Liquidity

A base fee of 1200, an ordering fee varying from 1-2147483647, a dust 546 sats, and LP tokens are supplied in the commitment transaction. The pool transaction redeems LP tokens and constrains settlement output 1 and 2 to give the user their proportional liquidity.

Inputs	Asset	Amount
Commitment Input 1	L-BTC	Base Fee (1200) + Ordering Fee (1-2147483647) + Dust (546)
Commitment Input 2	LP	Liquidity Share
Outputs	Asset	Amount
Outputs Settlement Output 1	Asset L-BTC	Amount Supply

#### Based on parameters;

- I. pl is a state of pool L-BTC supply held by the main covenant
- II. pt is a state of pool Token supply held by the Token holder covenant
- III. plpis a state of pool LP supply held by the LP holder covenant
- V. *olp* is a state of occupied LP supply
- VI. *ulp* is the amount of LP tokens the user redeems
- VII. rlp is the amount of LP redemption ratio
- VIII. *ul* is the L-BTC amount user receives
- IX. *ut* is the Token amount user receives
  - 1. Total occupied LP tokens olp = mlp plp
  - 2. Total occupied LP tokens is magnified 1000x olp' = olp \* 1000
  - 3. LP redemption ratio  $rlp = \frac{olp'}{ulp}$
  - 4. L-BTC amount user receives  $ul = \frac{pl}{rlp} * 1000$
  - 5. Token amount the user receives  $ut = \frac{pt}{rlp} * 1000$
  - 6. New occupied LP token supply olp'' = olp ulp
  - 7. New pool LP token supply plp' = plp + ulp
  - 8. New pool L-BTC supply pl' = pl ul
  - 9. New pool Token supply pt' = pt ut

----- BEGIN CASE 4 : Remove Liquidity ------

//Fetch commitment input 1 tradable L-BTC supply

<5> ROLL

//Push a dust value 546 onto stack

<546> SCIPTNUMTOLE64

//Verify that commitment input 1 holds dust L-BTC

**EQUALVERIFY** 

//Inspect commitment input 2 asset and verify the prefix(1)

<4+N> INSPECTINPUTASSET <0x01> EQUALVERIFY

//Get LP token asset ID and verify the prefix(1)

<2> INSPECTOUTPUTASSET <0x01> EQUALVERIFY

//Verify that commitment input 2 holds the LP assetID(32)

**EQUALVERIFY** 

//Push 50000000000000000 max LP pool supply

<5000000000000000000>

//Make a copy of the current LP pool supply

<3> PICK

//Subtract max LP pool supply with current LP pool supply to get the current LP used

SUB64

//Verify no overflow

**VERIFY** 

//Push int 1000 and convert to LE64

<1000> SCIPTNUMTOLE64

//Magnify current lp pool supply 10000 times and verify no overflow

**MUL64 VERIFY** 

//Inspect commitment input 2 amount and verify the prefix(1)

<4+N> INSPECTINPUTVALUE <0x01> EQUALVERIFY

//Make one copy and send to altstack

**DUP TOALTSTACK** 

//Calculate the LP ratio and verify no overflow

**DIV64 VERIFY** 

//Make a copy of the current L-BTC pool supply

<1> PICK

//Make a copy of LP ratio

<1> PICK

//Divide current L-BTC pool supply with LP ratio to calculate L-BTC user received and verify no overflow

**DIV64 VERIFY** 

//Push int 1000 and convert to LE64

<1000> SCIPTNUMTOLE64

//Apply the same 1000x magnification on this side and verify no overflow

#### **MUL64 VERIFY**

//Make one copy and send to altstack

#### **DUP TOALTSTACK**

//Inspect settlement output 1 asset

#### <3+N> INSPECTOUTPUTASSET

//Verify the prefix(1)

#### <0x01> EQUALVERIFY

//Get L-BTC asset ID

<14> PICK

//Verify that settlement output 1 holds the L-BTC assetID(32)

#### **EQUALVERIFY**

//Inspect settlement output 1 amount

#### <3+N> INSPECTOUTPUTVALUE

//Verify the prefix(1)

#### <0x01> EQUALVERIFY

//Make sure user gets deserved L-BTC amount

#### **EQUALVERIFY**

//Make a copy of the current L-BTC pool supply

<2> PICK

#### **SWAP**

//Divide current Token pool supply with LP ratio to calculate Token amount user received

#### DIV64

//Verify no overflow

#### **VERIFY**

//Push int 1000 and convert to LE64

#### <1000> SCIPTNUMTOLE64

//Apply the same 1000x magnification on this side and verify no overflow

#### MUL64 VERIFY

//Make one copy and send to altstack

#### DUP TOALTSTACK

//Inspect settlement output 2 asset and verify the prefix(1)

#### <4+N> INSPECTOUTPUTASSET

//Get Token asset ID

#### <12> PICK

//Verify that settlement output 1 holds the Token assetID(32)

#### **EQUALVERIFY**

//Inspect settlement output 2 amount <4+N> INSPECTOUTPUTVALUE //Verify the prefix(1) <0x01> EQUALVERIFY //Make sure user gets deserved Token amount **EQUALVERIFY** //Get Token user received FROMALTSTACK //Get L-BTC user received FROMALTSTACK //Get LP tokens user sent FROMALTSTACK //Fetch previous LP pool supply <5> ROLL //Update new LP pool supply and verify no overflow ADD64 VERIFY //Fetch previous Token pool supply <4> ROLL //Fetch Token user received <3> ROLL //Update new Token pool supply and verify no overflow SUB64 VERIFY //Fetch previous L-BTC pool supply <3> ROLL //Fetch L-BTC user received <3> ROLL //Update new L-BTC pool supply and verify no overflow SUB64 VERIFY //Inspect settlement output 1 witness program and verify v0 witnes version //<N+3> INSPECTOUTPUTSCRIPTPUBKEY <0> EQUALVERIFY //Inspect settlement output 2 witness program and verify v0 witnes version <N+4> INSPECTOUTPUTSCRIPTPUBKEY <0> EQUALVERIFY //Make settlement output 1 and settlement output 2 witness programs are equal **EQUALVERIFY** //Send top 5 stack elements to altstack for further higher index slot interpretations TOALTSTACK TOALTSTACK TOALTSTACK TOALTSTACK //Drop slippage limit DROP ----- END CASE 4: Remove Liquidity ----

# 4.4.2.3.3 Witness Script Footer

The witness script footer is a fixed-size witness script making the last part of the maing covenant witness script.

//Get latest-index leaf tx fees

FROMALTSTACK

//Get total leaf tx fees

FROMALTSTACK

//Get latest-state pool LP supply

FROMALTSTACK

//Get latest-state pool Token supply

FROMALTSTACK

//Get latest-state pool L-BTC supply

FROMALTSTACK

//Inspect L-BTC amount the main covenant holds and verify the prefix(1)

<3> INSPECTINPUTVALUE <0x01> EQUALVERIFY

//Constrain main covenant L-BTC pool amount to latest state L-BTC supply

**EQUALVERIFY** 

//Inspect Token amount the main covenant holds and verify the prefix(1)

<1> INSPECTINPUTVALUE <0x01> EQUALVERIFY

//Constraint Token covenant L-BTC pool amount to latest state Token supply

**EQUALVERIFY** 

//Inspect LP amount the LP holder covenant holds and verify the prefix(1)

<1> INSPECTINPUTVALUE <0x01> EQUALVERIFY

//Constrain LP covenant LP pool amount to latest state LP supply

**EQUALVERIFY** 

//Convert total fees paid to LE64

SCIPTNUMTOLE64

//Calculate fees paid as tx fees and verify no overflow

INSPECTNUMINPUTS <4> SUB VERIFY

//Multiply the number of inputs with total fees paid and verify no overflow

MUL64 VERIFY

//Divide the result with the max number of inputs to calculate the total tx fees paid

<64> SCIPTNUMTOLE64 DIV64

//Verify no overflow

**VERIFY** 

//Get the fee output index

INSPECTNUMOUTPUTS <8> <1> SUB

/Make a copy of fee output index DUP //Inspect fee output value and verify the prefix(1) INSPECTOUTPUTVALUE<0x01> EQUALVERIFY //Constrain tx fees **EQUALVERIFY** //Get the service fee output index INSPECTNUMOUTPUTS <8> <2> SUB //Inspect service fee output asset and verify the prefix(1) INSPECTOUTPUTASSET <0x01> EQUALVERIFY //Make a copy of the L-BTC asset ID <8> PICK //Constrain service fee output asset ID to L-BTC **EQUALVERIFY** //Inspect service fee output witness program INSPECTOUTPUTSCRIPTPUBKEY //Constrain to witness version 0 <0> EQUALVERIFY //Constrain witness program 1ef08948ed902a517d90ef6955c66c183a444afd <0x1ef08948ed902a517d90ef6955c66c183a444afd> EQUALVERIFY //Empty stack 2DROP 2DROP 2DROP <1>

# 5. Precision Downgrade

Applying arithmetic operations over two 64-bit signed asset values to calculate a constant value overflows the operation. To avoid this, inspected L-BTC and Token amounts are downgraded to fit in 32-bit form. A 32-bit signed int could store max 21.47483647 L-BTC value and 21.47483647 USDT. By downgrading L-BTC value 16 times and Token value 2097152 times, a Bitmatrix pool can accommodate up to 343.59738352 L-BTC and 45,035,996 USDT. The tradeoff counts a single L-BTC unit for 16 sats and a minimum USDT unit for 2 cents. More than one AMM pool for the same pair can be created if one pool hits the max liquidity limit (343 L-BTC).

----- END SCRIPT FOOTER -----