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# Generalized Multi-Agent Reinforcement Learning in Cooperative and Competitive Environments

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## Abstract

Multi-agent scenarios frequently come up in the real world, but traditional reinforcement learning algorithms do not perform well on them due to constantly changing environments from the perspective of any one agent. We replicate multi-agent deep deterministic policy gradients (MADDPG), an algorithm tailored to multi-agent scenarios, and evaluate its performance in a 3-agent cooperative navigation OpenAI environment. Additionally, we perform many experiments to explore how changing hyperparameters affects performance and attempt to address the main weakness of MADDPG, which is that it does not scale well to larger numbers of agents.

Our results confirm that MADDPG performs significantly better than a single-agent policy gradient approach and show the importance of batch size in performance and training stability.

## 1. Introduction

There are many applications where multiple agents need to learn how to act together, such as multiplayer games (Peng et al., 2017), multi-robot control (Matignon et al., 2012a), communication scenarios (Foerster et al., 2016), and even self-play (Sukhbaatar et al., 2017).

Traditional reinforcement learning approaches focus on training a single agent and as a result they do not work well on multi-agent problems because the environment for any single agent changes over time as other agents change their policies, leading to instability during training and high variance in results (Matignon et al., 2012b). Additionally, experience replay as used with Q-learning cannot be directly applied in multi-agent scenarios, significantly hampering stable learning.

Research into multi-agent reinforcement learning has attempted to develop new approaches specifically for multi-agent scenarios. One such recently developed algorithm is multi-agent deep deterministic policy gradients algorithm (MADDPG), which obtains significantly improved results over other approaches by modifying DDPG to train agents while incorporating information from other agents (Lowe et al., 2017).

We replicate the MADDPG algorithm and apply it to an OpenAI cooperative navigation environment, where agents must learn to each navigate to a different fixed landmark without colliding. We experiment with various hyperparameters and exploration vs. exploitation methodologies to show how MADDPG’s performance is affected by them. We also generalize MADDPG to handle larger numbers of agents and explore how performance changes accordingly.

## 2. Related Work

### 2.1. Single-agent methods

Plenty of research has been carried out to find the optimal policy for each agent in a multi-agent environment. (Sandholm & Crites, 1996), (Claus & Boutilier, 1998) applied Q learning to cooperative multi-agent systems and found that it was as robust as in single-agent settings. (Buffet et al., 2007) tried to address the problem by using incremental learning and policy gradient approaches. The problem with these kinds of approaches is that single-agent RL methods assumes agent-independent environments. The interaction of single agents with other agents is a nonstationary environment and as research has shown the single agent RL methods will not work in a multi-agent scenario due to high variance in rewards.

### 2.2. Multi-agent methods

(Boutilier, 1996) discusses coordination and planning between multi-agents using multi-agent markov decision processes (MMDP) where all the agents know the order and information about all other agents. (Chalkiadakis & Boutilier, 2003) proposes the use of bayesian models for optimal exploration in MARL problems. (Panait & Luke, 2005) presents the survey of the state of the art in MARL citing

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team heterogeneous and hybrid team learning, concurrent learning and distributed RL.

(Busoniu et al., 2008), (Buşoniu et al., 2010) and others have stated the problems of MARL over the years and how it is very hard to tackle the problem of nonstationarity and variance reduction. (Lowe et al., 2017) has combined concepts from (Sutton & Barto, 1998) and (Lillicrap et al., 2015) to address the above mentioned issues for multi-agent scenario. We consider this paper as the main algorithm of choice for implementation and analysis in the next section.

### 3. Approach

#### 3.1. Environment

We use the cooperative navigation OpenAI Gym environment for our experiments (OpenAI, 2017). This is a 2-D world with  $N$  moving agents and  $N$  fixed landmarks ( $N = 3$  by default), where the agents must learn to each move to a different landmark while avoiding collisions with each other.

Every agent has its own state that is an 18-dimensional vector containing its own position and velocity, relative distance to each of the landmarks, and relative distance to the other agents. The action that every agent can take is represented as a 5-dimensional vector, with 4 dimensions representing movement up/down/left/right and the last dimension representing a no-move action. This is a continuous action space, with the values for each action dimension representing acceleration in a given direction.

At each timestep, all agents are rewarded based on the distance between landmarks and agents; the closer the agents are to separate landmarks, the higher the reward. If every agent was exactly on top of a different landmark, the reward at that timestep would be 0. Agents have a non-zero size, so it is possible for them to collide in this environment. Agents receive a reward of -1 if there are collisions at any timestep. Therefore, in order to maximize reward, the agents need to each learn to move to a different landmark while also avoiding collisions with each other.

We define an episode to be 25 timesteps long, as there is no defined terminal state in this environment.

#### 3.2. Policy Gradient

We implement a policy gradient algorithm as a baseline. Policy gradient algorithms seek to determine the optimal policy by directly adjusting the parameters  $\theta$  of a policy  $\pi_\theta$  in order to maximize the objective function  $J^*(\theta) = \mathbb{E}_{\pi_\theta}[R]$ . We also implemented a baseline and advantage for the policy gradient. Letting  $\hat{A} = R_t - b(s_t)$  be the advantage estimate at time  $t$ , we can write the gradient of

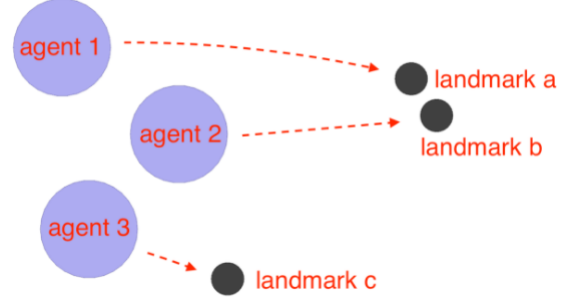


Figure 1. Cooperative navigation environment. Agents must learn to each navigate to a different landmark without colliding.

the policy as:

$$\nabla_\theta J(\theta) = \mathbb{E}_{s, \pi_\theta} [\nabla_\theta \log \pi_\theta(a|s) \hat{A}]$$

In the above equation, the expectation is taken over many sample trajectories through the environment using  $\pi_\theta$ . Policy gradient algorithms are already susceptible to high variance, and executing them in a multi-agent environments only amplifies the problem. From a single agent’s perspective not only does the world change as other agents move, but the policies other agents follow change as well. Additionally, individual agents might not always get the correct gradient signal as an agent could take a good action but if other agents took bad actions, leading to overall decrease in reward, the gradient for the agent taking the correct action could still be negative.

#### 3.3. MADDPG

##### TODO - diagram/visualization of how MADDPG works

We recreate MADDPG as our main algorithm for the cooperative navigation task (Lowe et al., 2017). MADDPG takes DDPG and tailors it to multi-agent environments, resulting in significantly better performance than single-agent methods. MADDPG trains separate policy networks for every agent, but uses a centralized action-value function that incorporates information across all agents to ensure a more stable learning process.

Consider a game with  $N$  agents, and let  $\pi = \{\pi_1, \dots, \pi_N\}$  be the associated set of agent policies that are parametrized by  $\theta_1, \dots, \theta_N$ . Additionally let  $s = \{s_1, \dots, s_N\}$  represent the set of states observed by each agent. When using MADDPG to train agents, every agent additionally maintains a critic function that outputs a Q-value given the states and actions of all agents:

$$Q_i^\pi(s, a_1, \dots, a_N)$$

Standard Q-learning techniques are used to update the critic function. Note that for the cooperative navigation environment that we run our experiments on, the Q-values will be

the same for all agents as the reward for all agents is the same. However, this Q-function formulation where every agent learns its own  $Q_i^\pi$  allows MADDPG to generalize to environments where agents have different reward functions (e.g. adversarial games).

During training, agents now have information not just about the locations of other agents, but about the actions they will take as well. Therefore, the environment is stationary for any agent as it does not depend on other agent policies:

$$P(s'_i | s_i, a_1, \dots, a_N, \pi_1, \dots, \pi_N) = P(s'_i | s_i, a_1, \dots, a_N)$$

The policy network updates for an agent are determined by maximizing the agents centralized Q-values. The gradient update is similar to the update used in the policy gradient, except that it uses the centralized Q-value instead of only looking at the returns across trajectories:

$$\nabla_{\theta_i} J(\theta_i) = \mathbb{E}_{s, \pi_i} [\nabla_{\theta_i} \log \pi_i(a_i | o_i) Q_i^\pi(x, a_1, \dots, a_N)]$$

By incorporating the actions of all agents into the action-value function during training instead of only each individual agent, MADDPG produces better and more stable results than traditional policy gradient or Q-learning approaches. During policy execution, agents only use their learned policy networks and therefore do not use any information about other agents; MADDPG is an enhancement to the training process while leaving the execution phase unchanged.

### 3.4. More scalable MADDPG

In addition to implementing MADDPG as described in the previous section, we further modify it to scale to better support large numbers of agents. The Q function described above increases linearly in input size as more agents are added to the scenario, as it has to take every agent's observation and action as an input. In order to reduce the additional computation time needed as  $N$  grows, we modify MADDPG to only look at the  $K$  nearest neighbors during training, where  $K < N - 1$ . The mathematical formulation of the algorithm remains the same, but the inputs to  $Q_i^\pi$  vary based on which agents are closest to  $i$  at each timestep.

### 3.5. OrnsteinUhlenbeck noise process

One of the exploration methods we have tried in our experiments, presented in the next section, is the Ornstein-Uhlenbeck(OU) noise process. It is the correlated additive Gaussian action space noise. The idea behind using this noise process is that if the noise generated at a given time step is correlated to previous noise, it will tend to stay in the same direction for longer durations instead of immediately cancelling itself out, which will consequently allow the agent to go towards the goal faster. So in the case of continuous actions it is better to have temporally correlated

exploration that suit the dynamics to get smoother transitions. This noise process is popularly used with DDPG and we wanted to check if MADDPG can perform better with this exploration choice.

## 4. Experiments and Results

### 4.1. Evaluation Metrics

In order to evaluate the performance of our algorithms, every 250 training steps we do evaluation by running 40 episodes using the latest learned policies and calculate various metrics over them. Our primary evaluation metric for all experiments is average reward, which in this environment corresponds to the distance between agents and the target landmarks while also accounting for collisions that occur along the way. In addition to average reward, we also look at average distance between landmarks and agents, for more intuitive interpretation of the performance. Here we provide a detailed definition of average reward and average distance used in this paper, unless specified otherwise.

**Average reward.** Average reward is calculated by summing up rewards received from all agents, all timesteps within an episode, and then averaging across multiple episodes. Average rewards shown in plots are computed during dedicated evaluation runs whose data do not go into training set. The range of average reward is zero to negative infinity.

**Average distance.** Average distance is the sum of distances between each agent and its closest landmark, across all agents and all timesteps within an episode, and then averaged across episodes.

Besides the metrics defined above, each experiment may additional context-specific evaluation metric, which will be defined for that experiment.

### 4.2. Experiments

The hyperparameters for the experiments described in this section follow the values mentioned in the Table 1 unless mentioned otherwise.

**Episode Length.** The sequence of actions an agent can take from the start state to the terminal state. This is measured in terms of steps.

**Batch size.** The sequence of agent observations, actions, rewards and next observations used to train an agent. We consider the batch size in terms of episodes. Therefore for a batch size of 50 episodes, we are actually using 50 times 25 (episode length), 1250 time steps to train an agent.

**Gamma.** It is the discount factor which models the future rewards as a fraction of the immediate rewards. It quantifies how much importance we give for future rewards.

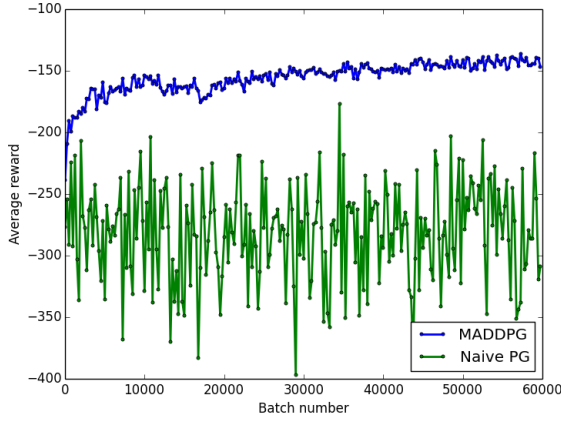


Figure 2. Average reward achieved by Naive PG (REINFORCE) algorithm and MADDPG algorithm.

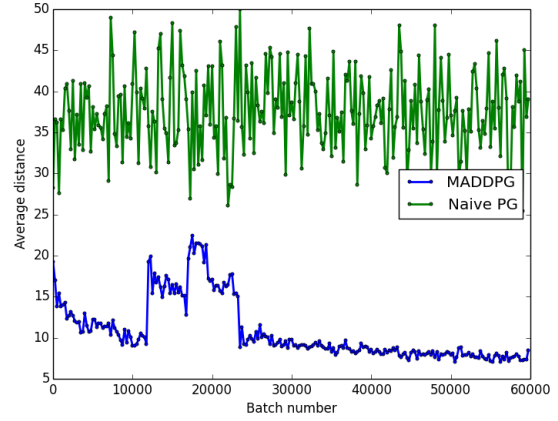


Figure 3. Average distance from landmarks with Naive PG algorithm and MADDPG algorithm.

**Learning rate.** Learning rate specifies the magnitude of step that is taken towards the solution.

Table 1. Parameters used for training MADDPG

| Metric                           | Value |
|----------------------------------|-------|
| Number of hidden layers          | 2     |
| Number of hidden units per layer | 128   |
| Episode length (steps)           | 25    |
| Batch size (episodes)            | 50    |
| Total number of episodes         | 60000 |
| Gamma, $\gamma$                  | 0.95  |
| Learning Rate, $\alpha$          | 0.01  |

**REINFORCE and MADDPG.** As the baseline we compare the performance of REINFORCE and MADDPG with the baseline hyperparameters as given in Table 1 except that the batch size is 1024 episodes (1024\*25 steps) as given in the (Lowe et al., 2017) paper. As shown in Figure 2 and Figure 3, REINFORCE has difficulties learning a good policy as the world keeps changing from each agent’s perspective. If other agents make a wrong move, it would reflect badly on this agent even though it might have picked a good action. In other words, the feedback signal is erroneous. Whereas with MADDPG, the centralized critic function takes into consideration other agents’ observations and moves, so that the network could more accurately attribute rewards and penalties.

**Exploration strategies.** We experiment with 3 different ways of action exploration. First, we try re-implementing what Open AI does, which adds noise onto unnormalized policy network output, and then takes softmax to get the final action. We also try using Ornstein-Uhlenbeck process, with  $\sigma = 0.3, \theta = 0.15$ . Lastly, we experiment sampling from

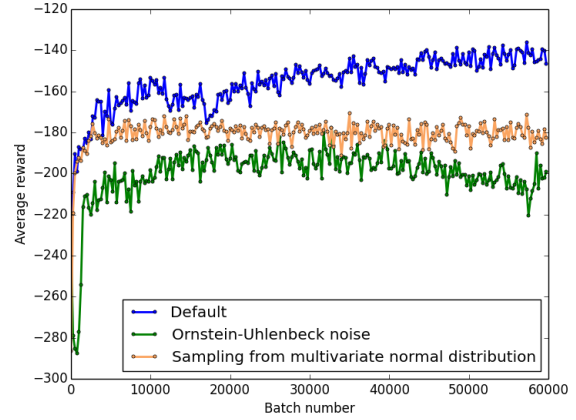


Figure 4. Average reward gained by using different exploration strategies.

multivariate normal distribution with a trainable standard deviation. Figure 4 shows the plot for average rewards with different action exploration strategies.

We found that applying noise to unnormalized policy network output outperforms other strategies. This finding corroborates the inference mentioned in (Plappert et al., 2017) and can be extended to our experiments as well. The inference is that since the reward function is well-shaped, we do not need a lot of exploration for the cooperative navigation environment we have chosen. Therefore we use that as our default exploration when conducting other experiments.

To further evaluate, we compare the Euclidean distance between the effective displacement as a result of pre-noise action versus post-noise action. The Euclidean distances are then averaged across every 100 steps (that is the training

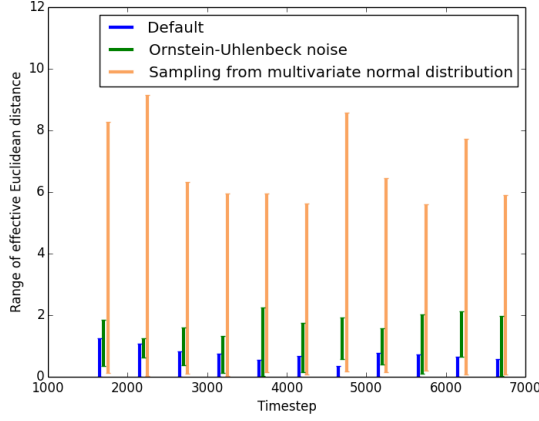


Figure 5. Range of effective euclidean distance for different exploration strategies.

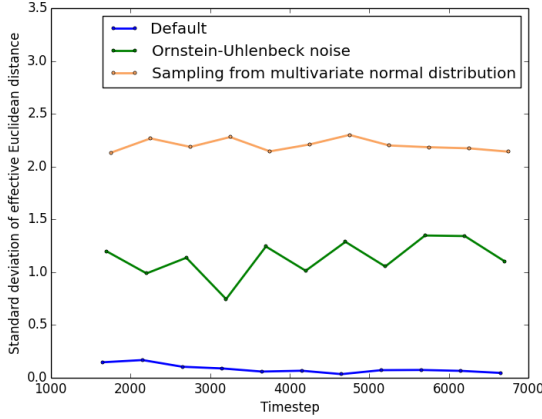


Figure 6. Standard deviation of effective euclidean distance for different exploration strategies.

frequency) across all agents. Figure 5 and 6 plot the range and standard deviation of the average Euclidean distances for the first 15000 batches.

Figures X,Y,and Z show our initial results from training with different policy network sizes. We can see that although there is a significant improvement in average reward from the start of training, the average reward is still well below 0, indicating that the agents are not able to find an optimal strategy to cooperate and cover all of the target landmarks. This result is to be expected as policy gradient will be very unstable due to the non-stationary environment from the point of view of any given agent during training. When we increased the number of layers and units per layer we saw the network reach convergence quicker, but it was still not able to improve substantially, indicating that the algorithm

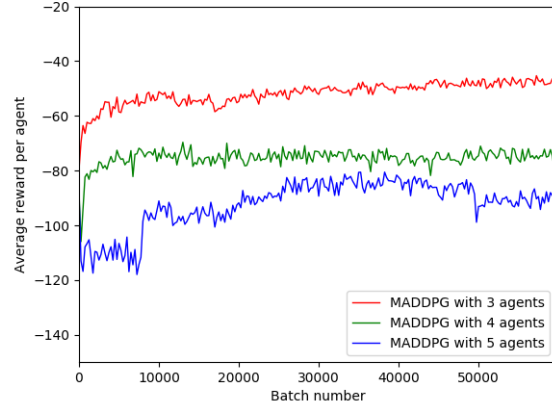


Figure 7. Average reward gained by each agent in environment with different number of agents and landmarks

itself could be a bottleneck on performance as opposed to the size of the policy networks.

**Increased number of agents and landmarks.** Figure 7 show the results from training different number of agents using MADDPG. For each result, the number of agents is equal to the number of landmarks. For smaller number of agents the average rewards increases with training whereas for even 1 or 2 more agents in the scenario, the training is not good enough. This can be attributed to the increased information from agents and increased complexity of environment due to more number of landmarks. Depending on the location of landmarks, the agents may or may not learn the policy for achieving the goal.

## 5. Conclusion

We introduced the problem of multi-agent reinforcement learning and show why traditional single-agent approaches are ineffective on these problems. We implemented a policy gradient method as a baseline and MADDPG, an algorithm designed for multi-agent scenarios, and applied them to the OpenAI cooperative navigation environment. We varied hyperparameters, changed the environment settings, applied different noise inputs and analysed the performance of MADDPG for different cases.

## 6. Future Work

We would like to try our approach on other multi-agent environments, in particular adversarial ones, to compare how MADDPG performs vs. policy gradients. It would also be interesting to explore how performance changes if agents are trained using different policies - e.g. in an adversarial game, what would happen if one set of agents



were trained with MADDPG and a competing set were trained with policy gradients.

Additionally, we would like to explore alternative forms of generalization as we feel this is key to supporting. Instead of  $Q_i^T$  looking at the  $K$  nearest neighbors to agent  $i$  for some fixed  $K$ , the Q-function could instead look at all neighbors within a particular distance to agent  $i$ . This way, the agents would have more information available to them when it is particularly important (the closer agents are to each other, the more likely it is to have a collision) while minimizing input space size when information about additional agents is less necessary.

## Contributions

Diana wrote the initial implementation of MADDPG, Shalini wrote our logging/plotting code, and Nitin wrote the initial implementation of the policy gradient baseline. All of us iterated on the code with bugfixes and enhancements and ran experiments using our implementations.

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