Introduction to Computer Programming for the Physical Sciences

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☐ Open a new Jupyter notebook
□ Name your notebook with your name and Homework 1
☐ Open a Markdown cell at the top and write your name and Homework 1
☐ Open a Markdown cell before each problem and write e.g. Problem 1, Problem 2(a), etc.
□ Please abide by the Policy and Guidelines on Using AI Tools
Once you finish the problems: 1) Restart the Python kernel and clear all cell outputs. 2) Rerun the notebook from start to finish so that all answers/outputs show up. 3) Save your notebook as a single .pdf file and upload it to Gradescope on Canvas by the deadline. No late homeworks will be accepted except for illness accompanied by a
doctor's note.

Homework 3

Problem 1: Working with Python Data Containers

You are tasked with developing a program to manage information on business trips made by employees to various cities where your company has offices. Unfortunately, your company did not adopt a uniform method for recording this information, so you have to first develop a program that can convert the hybrid data into a homogenous format. Specifically, the business trip data is a python list containing a combination of dictionaries and tuples, where each dictionary or tuple represents information about a specific trip. The relevant data are the employee's name, destination city, round-trip mileage, and the date of the trip. The dictionaries contain the information in key-value pairs (i.e. name, destination, mileage, date), while the tuple contains the same information ordered sequentially (i.e. tuple_data = (name, destination, mileage, date)). The employee data is given in the code cell below:

```
import numpy as np
In [ ]: trips = [
            {'name': 'Alice', 'destination': 'New York', 'mileage': 200.0, 'date': '2022
            ('Bob', 'Chicago', 300, '2022-02-01'),
            {'name': 'Charlie', 'destination': 'Los Angeles', 'mileage': 400, 'date': '2
            ('David', 'San Francisco', 500.0, '2022-04-01'),
            {'name': 'Eve', 'destination': 'Seattle', 'mileage': 620, 'date': '2022-05-0
            ('Frank', 'Boston', 705, '2022-06-01'),
            {'name': 'Grace', 'destination': 'Denver', 'mileage': 810, 'date': '2022-07-
            ('Henry', 'Austin', 911, '2022-08-01'),
            {'name': 'Ivy', 'destination': 'Atlanta', 'mileage': 1000.0, 'date': '2022-0
            ('Jack', 'Miami', 1112.0, '2022-10-01'),
            {'name': 'Kate', 'destination': 'Dallas', 'mileage': 1200.0, 'date': '2022-1
            ('Liam', 'Houston', 134, '2022-12-01'),
            {'name': 'Mia', 'destination': 'Phoenix', 'mileage': 1400.0, 'date': '2023-0
            ('Noah', 'Las Vegas', 1526.0, '2023-02-01'),
            {'name': 'Olivia', 'destination': 'San Diego', 'mileage': 1600.0, 'date': '2
            ('Peter', 'Portland', 1700, '2023-04-01'),
            ('Alice', 'Boston', 1322.0, '2023-01-01'),
            ('Bob', 'Los Angeles', 400, '2023-02-01'),
            {'name': 'Charlie', 'destination': 'Chicago', 'mileage': 500, 'date': '2023-
            ('David', 'Miami', 600.0, '2023-04-01'),
            {'name': 'Eve', 'destination': 'Dallas', 'mileage': 700.0, 'date': '2023-05-
            ('Frank', 'Houston', 800, '2023-06-01'),
            {'name': 'Grace', 'destination': 'Phoenix', 'mileage': 900.0, 'date': '2023-
            ('Henry', 'Las Vegas', 1000, '2023-08-01'),
            {'name': 'Ivy', 'destination': 'San Diego', 'mileage': 1100.0, 'date': '2023
            ('Jack', 'Portland', 1200, '2023-10-01'),
            {'name': 'Kate', 'destination': 'New York', 'mileage': 1300.0, 'date': '2023
            ('Liam', 'Austin', 1400, '2023-12-01'),
            {'name': 'Mia', 'destination': 'Denver', 'mileage': 1500.0, 'date': '2024-01
            ('Noah', 'Atlanta', 1600, '2024-02-01'),
            {'name': 'Olivia', 'destination': 'Seattle', 'mileage': 1700.0, 'date': '202
            ('Peter', 'San Francisco', 1800, '2024-04-01'),
            {'name': 'Alice', 'destination': 'Los Angeles', 'mileage': 210.0, 'date': '2
('Alice', 'Boston', 3000.0, '2023-05-01'),
            ('Bob', 'San Francisco', 310, '2022-03-01'),
            {'name': 'Charlie', 'destination': 'Seattle', 'mileage': 410, 'date': '2022-
            ('David', 'Boston', 510.0, '2022-05-01'),
            {'name': 'Eve', 'destination': 'Denver', 'mileage': 630, 'date': '2022-06-01
            ('Frank', 'Austin', 715, '2022-07-01'),
```

```
{'name': 'Grace', 'destination': 'Atlanta', 'mileage': 820, 'date': '2022-08
    ('Henry', 'Miami', 921, '2022-09-01'),
    {'name': 'Ivy', 'destination': 'Dallas', 'mileage': 1010.0, 'date': '2022-10
    ('Jack', 'Houston', 1122.0, '2022-11-01'),
    {'name': 'Kate', 'destination': 'Phoenix', 'mileage': 1210.0, 'date': '2022-
    ('Liam', 'Las Vegas', 144, '2023-01-01'),
    {'name': 'Mia', 'destination': 'San Diego', 'mileage': 1410.0, 'date': '2023
    ('Noah', 'Portland', 1536.0, '2023-03-01'),
    {'name': 'Olivia', 'destination': 'San Francisco', 'mileage': 1610.0, 'date'
    ('Peter', 'New York', 1710, '2023-05-01'),
    {'name': 'Anne', 'destination': 'Seattle', 'mileage': 220.0, 'date': '2022-0
    ('Gerald', 'Boston', 320, '2022-04-01'),
    {'name': 'Charlie', 'destination': 'Denver', 'mileage': 420, 'date': '2022-0
    ('Dirk', 'Austin', 520.0, '2022-06-01'),
    {'name': 'Eve', 'destination': 'Atlanta', 'mileage': 640, 'date': '2022-07-0
    ('Joe', 'Miami', 725, '2022-08-01'),
    {'name': 'Grace', 'destination': 'Dallas', 'mileage': 830, 'date': '2022-09-
    ('Dirk', 'Houston', 931, '2022-10-01'),
    {'name': 'Ivy', 'destination': 'Phoenix', 'mileage': 1020.0, 'date': '2022-1
    ('Henry', 'Las Vegas', 1132.0, '2022-12-01'),
    {'name': 'Kate', 'destination': 'San Diego', 'mileage': 1220.0, 'date': '202
    ('Alison', 'Portland', 154, '2023-02-01'),
    {'name': 'Mia', 'destination': 'San Francisco', 'mileage': 1420.0, 'date': '
    ('Noah', 'New York', 1546.0, '2023-04-01'),
    {'name': 'Olivia', 'destination': 'Los Angeles', 'mileage': 1620.0, 'date':
    ('Peter', 'Chicago', 1720, '2023-06-01')
]
```

a) Write a function called convert_trips to convert the trip data into a homogenouse format with behavior that follows the documentation string below:

```
def convert_trips(trips, append_new=None, filter_dict=None,
display=False):
    """
    Convert a list of trips containing dictionaries and tuples to a
list of dictionaries.

Parameters
    ------
    trips: list
        Trip database containing dictionaries and tuples, where each
dictionary or tuple
        represents information about a specific trip.

Returns
    ------
    output_list: list of dicts
        Trip database as a list of dictionaries.
```

Test your function by performing a loop over each trip in the output_list and printing the trip data (i.e. the dictionary) to the screen.

```
In [ ]: # problem 1
# a)
def convert_trips(trips, append_new=None, filter_dict=None, display=False):
"""
```

```
Convert a list of trips containing dictionaries and tuples to a list of dict
   Parameters
    _____
   trips : list
        Trip database containing dictionaries and tuples, where each dictionary
        represents information about a specific trip.
   Returns
   output_list: list of dicts
       Trip database as a list of dictionaries.
   output_list = [0 for _ in range(len(trips))]
   # set up a list with proper lentgh for future operation
   for i in range(len(trips)):
        # going through each element of trips
        if(type(trips[i]) == tuple):
            # find out if the element is a tuple type, if it is, converted it in
           output_list[i] = {'name':trips[i][0],'destination': trips[i][1], 'mi
            # if the element is not tuple, which has to be dictionary, just copy
           output_list[i] = trips[i]
    return output_list
converted_trips = convert_trips(trips)
print(converted_trips)
```

[{'name': 'Alice', 'destination': 'New York', 'mileage': 200.0, 'date': '2022-01-01'}, {'name': 'Bob', 'destination': 'Chicago', 'mileage': 300, 'date': '2022-02-01'}, {'name': 'Charlie', 'destination': 'Los Angeles', 'mileage': 400, 'date': '2022-03-01'}, {'name': 'David', 'destination': 'San Francisco', 'mileage': 500. 0, 'date': '2022-04-01'}, {'name': 'Eve', 'destination': 'Seattle', 'mileage': 62 0, 'date': '2022-05-01'}, {'name': 'Frank', 'destination': 'Boston', 'mileage': 7 05, 'date': '2022-06-01'}, {'name': 'Grace', 'destination': 'Denver', 'mileage': 810, 'date': '2022-07-01'}, {'name': 'Henry', 'destination': 'Austin', 'mileage': 911, 'date': '2022-08-01'}, {'name': 'Ivy', 'destination': 'Atlanta', 'mileage': 1000.0, 'date': '2022-09-01'}, {'name': 'Jack', 'destination': 'Miami', 'mileag e': 1112.0, 'date': '2022-10-01'}, {'name': 'Kate', 'destination': 'Dallas', 'mil eage': 1200.0, 'date': '2022-11-01'}, {'name': 'Liam', 'destination': 'Houston', 'mileage': 134, 'date': '2022-12-01'}, {'name': 'Mia', 'destination': 'Phoenix', 'mileage': 1400.0, 'date': '2023-01-01'}, {'name': 'Noah', 'destination': 'Las Ve gas', 'mileage': 1526.0, 'date': '2023-02-01'}, {'name': 'Olivia', 'destination': 'San Diego', 'mileage': 1600.0, 'date': '2023-03-01'}, {'name': 'Peter', 'destina tion': 'Portland', 'mileage': 1700, 'date': '2023-04-01'}, {'name': 'Alice', 'des tination': 'Boston', 'mileage': 1322.0, 'date': '2023-01-01'}, {'name': 'Bob', 'd estination': 'Los Angeles', 'mileage': 400, 'date': '2023-02-01'}, {'name': 'Char lie', 'destination': 'Chicago', 'mileage': 500, 'date': '2023-03-01'}, {'name': 'David', 'destination': 'Miami', 'mileage': 600.0, 'date': '2023-04-01'}, {'nam e': 'Eve', 'destination': 'Dallas', 'mileage': 700.0, 'date': '2023-05-01'}, {'na me': 'Frank', 'destination': 'Houston', 'mileage': 800, 'date': '2023-06-01'}, {'name': 'Grace', 'destination': 'Phoenix', 'mileage': 900.0, 'date': '2023-07-0 1'}, {'name': 'Henry', 'destination': 'Las Vegas', 'mileage': 1000, 'date': '2023 -08-01'}, {'name': 'Ivy', 'destination': 'San Diego', 'mileage': 1100.0, 'date': '2023-09-01'}, {'name': 'Jack', 'destination': 'Portland', 'mileage': 1200, 'dat e': '2023-10-01'}, {'name': 'Kate', 'destination': 'New York', 'mileage': 1300.0, 'date': '2023-11-01'}, {'name': 'Liam', 'destination': 'Austin', 'mileage': 1400, 'date': '2023-12-01'}, {'name': 'Mia', 'destination': 'Denver', 'mileage': 1500. 0, 'date': '2024-01-01'}, {'name': 'Noah', 'destination': 'Atlanta', 'mileage': 1 600, 'date': '2024-02-01'}, {'name': 'Olivia', 'destination': 'Seattle', 'mileag e': 1700.0, 'date': '2024-03-01'}, {'name': 'Peter', 'destination': 'San Francisc o', 'mileage': 1800, 'date': '2024-04-01'}, {'name': 'Alice', 'destination': 'Los Angeles', 'mileage': 210.0, 'date': '2022-02-01'}, {'name': 'Alice', 'destinatio n': 'Boston', 'mileage': 3000.0, 'date': '2023-05-01'}, {'name': 'Bob', 'destinat ion': 'San Francisco', 'mileage': 310, 'date': '2022-03-01'}, {'name': 'Charlie', 'destination': 'Seattle', 'mileage': 410, 'date': '2022-04-01'}, {'name': 'Davi d', 'destination': 'Boston', 'mileage': 510.0, 'date': '2022-05-01'}, {'name': 'E ve', 'destination': 'Denver', 'mileage': 630, 'date': '2022-06-01'}, {'name': 'Fr ank', 'destination': 'Austin', 'mileage': 715, 'date': '2022-07-01'}, {'name': 'G race', 'destination': 'Atlanta', 'mileage': 820, 'date': '2022-08-01'}, {'name': 'Henry', 'destination': 'Miami', 'mileage': 921, 'date': '2022-09-01'}, {'name': 'Ivy', 'destination': 'Dallas', 'mileage': 1010.0, 'date': '2022-10-01'}, {'nam e': 'Jack', 'destination': 'Houston', 'mileage': 1122.0, 'date': '2022-11-01'}, {'name': 'Kate', 'destination': 'Phoenix', 'mileage': 1210.0, 'date': '2022-12-0 1'}, {'name': 'Liam', 'destination': 'Las Vegas', 'mileage': 144, 'date': '2023-0 1-01'}, {'name': 'Mia', 'destination': 'San Diego', 'mileage': 1410.0, 'date': '2 023-02-01'}, {'name': 'Noah', 'destination': 'Portland', 'mileage': 1536.0, 'dat e': '2023-03-01'}, {'name': 'Olivia', 'destination': 'San Francisco', 'mileage': 1610.0, 'date': '2023-04-01'}, {'name': 'Peter', 'destination': 'New York', 'mile age': 1710, 'date': '2023-05-01'}, {'name': 'Anne', 'destination': 'Seattle', 'mi leage': 220.0, 'date': '2022-03-01'}, {'name': 'Gerald', 'destination': 'Boston', 'mileage': 320, 'date': '2022-04-01'}, {'name': 'Charlie', 'destination': 'Denve r', 'mileage': 420, 'date': '2022-05-01'}, {'name': 'Dirk', 'destination': 'Austi n', 'mileage': 520.0, 'date': '2022-06-01'}, {'name': 'Eve', 'destination': 'Atla nta', 'mileage': 640, 'date': '2022-07-01'}, {'name': 'Joe', 'destination': 'Miam i', 'mileage': 725, 'date': '2022-08-01'}, {'name': 'Grace', 'destination': 'Dall as', 'mileage': 830, 'date': '2022-09-01'}, {'name': 'Dirk', 'destination': 'Hous ton', 'mileage': 931, 'date': '2022-10-01'}, {'name': 'Ivy', 'destination': 'Phoe

```
nix', 'mileage': 1020.0, 'date': '2022-11-01'}, {'name': 'Henry', 'destination': 'Las Vegas', 'mileage': 1132.0, 'date': '2022-12-01'}, {'name': 'Kate', 'destination': 'San Diego', 'mileage': 1220.0, 'date': '2023-01-01'}, {'name': 'Alison', 'destination': 'Portland', 'mileage': 154, 'date': '2023-02-01'}, {'name': 'Mia', 'destination': 'San Francisco', 'mileage': 1420.0, 'date': '2023-03-01'}, {'name': 'Noah', 'destination': 'New York', 'mileage': 1546.0, 'date': '2023-04-01'}, {'name': 'Olivia', 'destination': 'Los Angeles', 'mileage': 1620.0, 'date': '2023-05-01'}, {'name': 'Peter', 'destination': 'Chicago', 'mileage': 1720, 'date': '2023-06-01'}]
```

b) Write a function called query_trips consistent with the behavior in the following documentation string.

```
def query_trips(trips, filter_dict):
   Manage business trip data.
    Parameters
    _____
    trips: list
        Trip database containing a list of dictionaries with
information about each trip.
    filter_dict : dict, optional
        If provided, return the list of trips that match the key-value
pairs in
        this dictionary. The allowed keys in the dictionary are 'name',
        'destination', and 'date'. Multiple keys can be provided.
    Returns
    _____
    output_list: list of dicts
        List of trips that match the input parameters.
    Examples
    >>> filter_dict = {'name': 'Alice', 'destination': 'Boston'}
    >>> alice_trips = manage_trips(trips, filter_dict))
    Returns the list:
    alice_trips = [{'name': 'Alice', 'destination': 'Boston',
'mileage': 1322.0, 'date': '2023-01-01'},
                   {'name': 'Alice', 'destination': 'Boston',
'mileage': 3000.0, 'date': '2023-05-01'}]
```

Note: Make sure that if multiple trip parameters (name, destination, date) are provided in filter_dict, the output is a list of trips that match ALL of those parameters.

Test your code on the following example usage cases:

```
# Test filtering trips by destination, should print trips to New York
filter_dict = {'destination': 'New York'}
filtered_trips = query_trips(trips, filter_dict)

# Test filtering trips by name, should print trips by Noah
filter_dict = {'name': 'Noah'}
```

```
filtered_trips = query_trips(trips, filter_dict)

# Test filtering trips by date, should print trips on 2023-04-01
filter_dict = {'date': '2023-04-01'}
filtered_trips = query_trips(trips, filter_dict)

# Test filtering trips by name and destination, should print trips by
Alice to New York
filter_dict = {'name': 'Alice', 'destination': 'New York'}
filtered_trips = query_trips(trips, filter_dict)
For each of these test, put the code in a separate code cell, and loop over each
trip in filtered_trips and print the trip data (i.e. the dictionary) to the screen.
```

```
In [ ]: |# b)
        def query_trips(trips, filter_dict):
            Manage business trip data.
            Parameters
            _____
            trips : list
                Trip database containing a list of dictionaries with information about e
            filter_dict : dict, optional
                If provided, return the list of trips that match the key-value pairs in
                this dictionary. The allowed keys in the dictionary are 'name',
                 'destination', and 'date'. Multiple keys can be provided.
            Returns
            output list: list of dicts
                List of trips that match the input parameters.
            Examples
            >>> filter dict = {'name': 'Alice', 'destination': 'Boston'}
            >>> alice_trips = manage_trips(trips, filter_dict))
            Returns the list:
            alice_trips = [{'name': 'Alice', 'destination': 'Boston', 'mileage': 1322.0,
                           {'name': 'Alice', 'destination': 'Boston', 'mileage': 3000.0,
            output list = []
            # set up an empty list for operation
            for i in range(len(trips)):
                # going through all the elements in trips
                output_list.append(trips[i])
                # add this element of tips to the outputlist
                for j in filter dict.keys():
                    # gonging through the elements that we have to check
                    if(trips[i][j] != filter_dict[j]):
                        # find out if the element we want is in the element of trips
                        output_list.remove(trips[i])
                        # remove the element from output list if it is not in the filter
                        # stop the cycle, since there is no need to check if other senar
            return output_list
```

```
filter_dict = {'name': 'Alice', 'destination': 'Boston'}
        alice_trips = query_trips(converted_trips,filter_dict)
        print(alice_trips)
       [{'name': 'Alice', 'destination': 'Boston', 'mileage': 1322.0, 'date': '2023-01-0
       1'}, {'name': 'Alice', 'destination': 'Boston', 'mileage': 3000.0, 'date': '2023-
       05-01'}]
In [ ]: # Test filtering trips by destination, should print trips to New York
        filter_dict = {'destination': 'New York'}
        filtered_trips = query_trips(converted_trips, filter_dict)
        print(filtered_trips)
       [{'name': 'Alice', 'destination': 'New York', 'mileage': 200.0, 'date': '2022-01-
       01'}, {'name': 'Kate', 'destination': 'New York', 'mileage': 1300.0, 'date': '202
       3-11-01'}, {'name': 'Peter', 'destination': 'New York', 'mileage': 1710, 'date':
       '2023-05-01'}, {'name': 'Noah', 'destination': 'New York', 'mileage': 1546.0, 'da
       te': '2023-04-01'}]
In [ ]: # Test filtering trips by name, should print trips by Noah
        filter_dict = {'name': 'Noah'}
        filtered_trips = query_trips(converted_trips, filter_dict)
        print(filtered trips)
       [{'name': 'Noah', 'destination': 'Las Vegas', 'mileage': 1526.0, 'date': '2023-02
       -01'}, {'name': 'Noah', 'destination': 'Atlanta', 'mileage': 1600, 'date': '2024-
       02-01'}, {'name': 'Noah', 'destination': 'Portland', 'mileage': 1536.0, 'date':
       '2023-03-01'}, {'name': 'Noah', 'destination': 'New York', 'mileage': 1546.0, 'da
       te': '2023-04-01'}]
In [ ]: # Test filtering trips by date, should print trips on 2023-04-01
        filter dict = {'date': '2023-04-01'}
        filtered_trips = query_trips(converted_trips, filter_dict)
        print(filtered_trips)
       [{'name': 'Peter', 'destination': 'Portland', 'mileage': 1700, 'date': '2023-04-0
       1'}, {'name': 'David', 'destination': 'Miami', 'mileage': 600.0, 'date': '2023-04
       -01'}, {'name': 'Olivia', 'destination': 'San Francisco', 'mileage': 1610.0, 'dat
       e': '2023-04-01'}, {'name': 'Noah', 'destination': 'New York', 'mileage': 1546.0,
       'date': '2023-04-01'}]
In [ ]: # Test filtering trips by name and destination, should print trips by Alice to N
        filter_dict = {'name': 'Alice', 'destination': 'New York'}
        filtered_trips = query_trips(converted_trips, filter_dict)
        print(filtered_trips)
       [{'name': 'Alice', 'destination': 'New York', 'mileage': 200.0, 'date': '2022-01-
       01'}]
```

Problem 2: The Fibonacci Sequence

The Fibonacci sequence begins

0, 1, 1, 2, 3, 5, 8, 13, 21, 34, 55,

and is defined by the recursion relation

$$x_{n+1} = x_n + x_{n-1}$$

with $x_0 \equiv 0$ and $x_1 \equiv 1$. Write Python code to determine the largest Fibonacci number less than 10^6 ?

```
In [ ]: # problem 2
        xn small=0 # x0
        xn=1 # x1
        # set up initial value for the fibonacci number
        xn_large = xn +xn_small # x2
        while (xn_large< 10**6):</pre>
            # if the next number in Fibonacci number is less than 1e6, keep working on i
            xn small = xn
            xn = xn_large
            # since we only need 2 numbers before the number we need to calculate in ord
            # we are also saving a lot space by doing this.
            # in the while, xn small represent x(n-1) in the formula and xn represent xn
            xn_large = xn + xn_small
            # xn large is represent x(n+1) in the formula
            # we only need to add xn and x(n-1) to get x(n+1)
        print(xn)
        # since when the loop is break xn_large is the smallest number in Fibonacci whic
        # xn should be the largest number in Fibonacci which is smaller than 1e6
```

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Problem 3: Higher Order Derivatives

We can represent the $n^{ ext{th}}$ derivative of f(x) as $f^{(n)}(x)$ where $f^0(x)\equiv f(x)$, $f^1(x)\equiv f'(x)$, $f^2(x)\equiv f''(x)$, etc.

Last week we learned how to compute numerical derivatives of a function f(x), and found that the symmetric difference formula

$$f'(x) pprox rac{f(x+h) - f(x-h)}{2h}$$

performs significantly better than the forward difference formula.

As discussed at the end of the Week3 lecture notes, recursive functions are Python functions that call themselves.

a) Code up a **recursive** Python function to compute the $n^{
m th}$ derivative of the function f(x) using the symmetric difference formula and the recursion relation

$$f^{(n)}(x)pprox rac{f^{(n-1)}(x+h)-f^{(n-1)}(x-h)}{2h}$$

Your function should be consistent with the following documentation string:

```
def deriv(f, x, n, h=1e-2):
```

Compute the nth derivative of a function f(x) using the symmetric difference formula.

```
Parameters
------
f: function
    Function to take the derivative of.

x: float
    Point at which to evaluate the derivative.

n: int
    Order of the derivative.

h: float, optional
    Step size. The default is 1e-2.

Returns
-----
f^(n)(x): float
    The nth derivative of f(x) evaluated at x.
```

- **b)** Test your function by computing the derivatives of e^x at x=1 for $n=0,1,2,3,4,\dots 10$ and compare to the analytic result. Print our your results to 16 decimal places. You can use the numpy function np.exp() to compute e^x .
- **c)** Up to what order of the derivative n can you compute before you start getting numerical errors?
- **d)** In your own words, what do you think is the source of these errors? Why do they set in at large values of n?

```
In [ ]: # problem 3
        # a)
        def deriv(f, x, n, h=1e-2):
            Compute the nth derivative of a function f(x) using the symmetric difference
            Parameters
            _____
            f : function
                Function to take the derivative of.
            x : float
                Point at which to evaluate the derivative.
            n : int
                Order of the derivative.
            h : float, optional
                Step size. The default is 1e-2.
            Returns
            _____
            f^(n)(x): float
                The nth derivative of f(x) evaluated at x.
            if(n==0):
                return f(x)
            if(n==1):
                return (f(x+h)-f(x-h))/(2*h)
            return (deriv(f,x+h,n-1,h)-deriv(f,x-h,n-1,h))/(2*h)
        # b)
```

```
for i in range(11):
    print(deriv(np.exp,1.0,i,))

2.718281828459045
2.718327133382714
2.7183724390611452
2.7184177454619984
2.7184630602139492
2.7185087514425277
2.7184643425215427
2.7144952952085077
3.660266534311063
```

b) continues:

44.23544863740858 -9540.979117872439

the derivative of e^x should alawys be e^x no matter how many times of derivative are taken. Thus, all the results should be e. However, some of them shown on screen does not.

c)

starting from order 8 the result start to be far away from e, which is the analitical result.

d)

I think the source of the error may come from the limit of flaot numbers. Since h is 1e-2, when the order gets higher, the np.exp() may result in such a small number that float is no longer accurate enough. Than things will go wrong.