
Meta-learning Implicit Neural Representation for Sparse Time Series Functional Data Analysis

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1 Introduction

2 Related works

2.1 Functional Data

Multivariate data versus functional data Traditional multivariate statistics take finite-dimensional vectors as the objects of study to analyze their statistical properties, such as mean vectors and covariance matrices. This approach is appropriate and easy to compute when the dimension is relatively small. However, if the dimension of the space in which the objects are analyzed is increased to infinite, for example, in L^2 space, traditional methods face certain challenges. In such functional spaces, the focus is not only on the values of vectors in a particular dimension but also on properties such as continuity and derivatives. At the same time, as the space grows to infinite dimensions, many useful tools in multivariate statistics, such as probability density functions, will lose their meaning. It is the differences in statistical properties and people's focus between infinite-dimensional and finite-dimensional spaces, that have led to widespread attention to functional data analysis (FDA) among researchers.

Time series as a representative example of functional data Time series is a typical object that needs to be addressed in an infinite-dimensional function space. This is because time series data collected in reality often exhibit continuity, and, in certain situations, people may focus on topics such as derivatives and time alignment (registration). Many previous studies have relied on multivariate statistics in the analysis of time series, such as [mention some specific examples]... From the perspective of function approximation, these multivariate-statistics-based studies can indeed reflect certain properties of time series. However, in many cases, this approach is challenging to generalize, as is the case with sparse time series data studied in this paper.

Sparse times series data analysis When the observation frequency of time series is low and irregular, sparse time series data is formed. This type of data is particularly common in the medical field, as the frequency of medical visits varies from person to person, with irregular patterns. When it comes to analyzing such "messy" data using multivariate statistics, people often find themselves at a loss. In functional data analysis, one can employ the method of local polynomial regression to initially estimate the original form of functional data. Subsequently, based on this estimation, various statistical quantities such as mean and covariance operators can be estimated (see details in the appendix). The local polynomial regression can be represented as follows:

$$\sum_{i=1}^n \left[Y_i - \sum_{j=0}^p \beta_j (X_i - x_0)^j \right]^2 K_h(X_i - x_0).$$

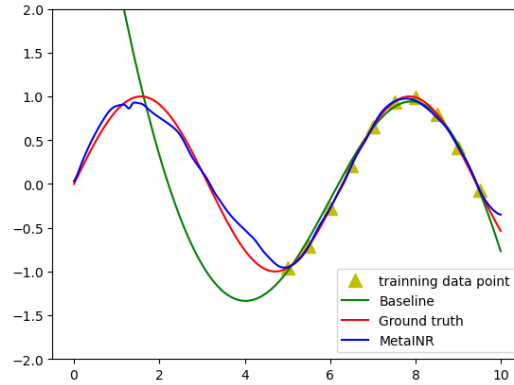


Figure 1: Learning periodicity

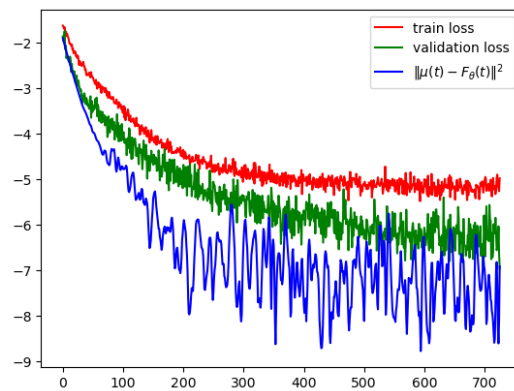


Figure 2: Learning mean

2.2 Implicit Neural Representation

SIREN for time series: advantage...

2.3 Meta-learning

different architecture: MAML / SNAIL

3 Method

advantage

4 Experiments

4.1 Synthetic data

4.1.1 what meta-learning learned in timeseries

global+differential property lead to a better PC estimation

1. periodicity
2. differential equations: No?
3. average phenomenon for meta prior model
4. based on information from whole dataset to get a estimation

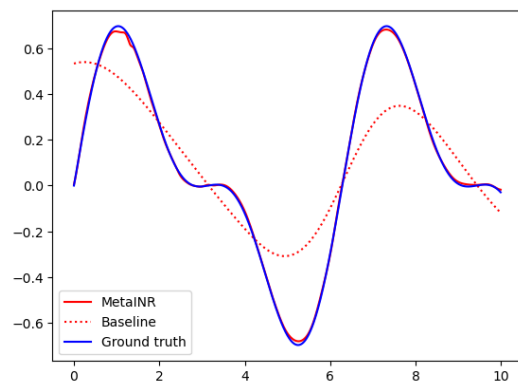


Figure 3: Mean estimation

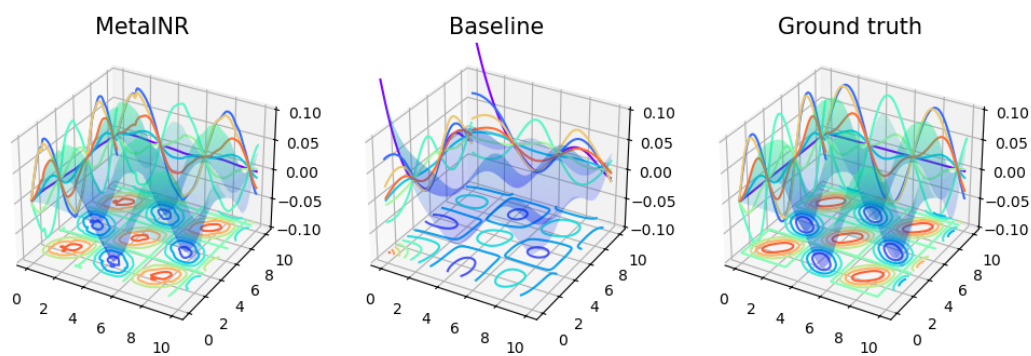


Figure 4: Covariance estimation

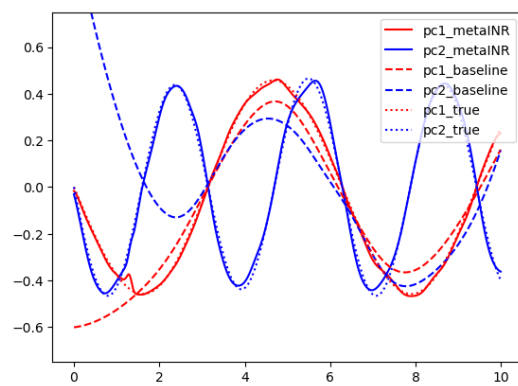


Figure 5: FPCA

4.1.2 Mean estimation

4.1.3 Covariance estimation

4.1.4 fPCA

4.2 Real-world data

5 Conclusion

6 Appendix

6.1 Traditional FDA for sparse functional data

6.2 Brief introduction to SIREN