Hw6_q3

1.

Myopathy is columns, and cows outcome is on teh y. We see that the percent of surviving cow (outcome =1) is 39% for those without myopathy and 6% for those with myopathy.

```
## 0 0.61417323 0.93684211
## 1 0.38582677 0.06315789
```

2. Fit logistic regression.

Based on the coefficient table the estimated log probability when myopathy = 0 would be -0.4649 ± 0.1823 , and when myopathy = 1 would be -2.2320 ± 0.4595 . The decrease in odds of survival from mypathy is then $\exp(-2.2320)=0.11$. Then the probability of survival when myopathy=1 is $0.11*\exp(-0.4649) = 0.07$, and when myopathy=0 is $1-\exp(-0.4649) = 0.37$. These numbers are about where the last row from Q1 are.

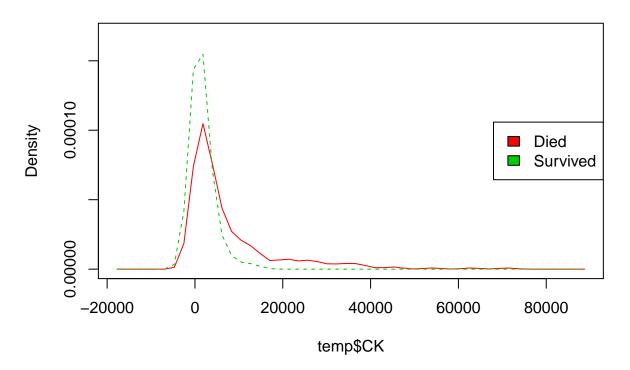
```
##
## Attaching package: 'MASS'
##
  The following object is masked from 'package:dplyr':
##
##
       select
##
  The following object is masked from 'package:alr3':
##
##
       forbes
##
## Call:
  glm(formula = Outcome ~ Myopathy, family = binomial(link = "logit"),
       data = downer)
##
##
## Deviance Residuals:
       Min
                 1Q
##
                      Median
                                   30
                                           Max
  -0.9874 -0.9874 -0.3612 -0.3612
                                        2.3504
##
## Coefficients:
##
               Estimate Std. Error z value Pr(>|z|)
## (Intercept) -0.4649
                            0.1823 -2.550
                                             0.0108 *
                            0.4595 -4.858 1.19e-06 ***
## Myopathy
                -2.2320
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
##
  (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 248.57 on 221 degrees of freedom
## Residual deviance: 214.14 on 220 degrees of freedom
     (213 observations deleted due to missingness)
## AIC: 218.14
##
## Number of Fisher Scoring iterations: 5
```

3.

We plotted the density of the CK and log(CK) below. It seems like the dead cows had higher levels of phosphokinase, and this is a bit clearer to see when we have log scale x-axis. Also the values look more normally distributed in the second graph.

```
## Package 'sm', version 2.2-5.6: type help(sm) for summary information
##
## Attaching package: 'sm'
## The following object is masked from 'package:MASS':
##
## muscle
```

Serum creatine phosphokinase



4

Here are the results, showign that the fold increase in survival for each unit increase in log(CK) is exp(-0.6117)=0.542428. This suggests perhaps myopathy is more predictive.

```
##
   glm(formula = Outcome ~ log(CK), family = binomial(link = "logit"),
##
       data = downer)
##
##
## Deviance Residuals:
##
       Min
                  1Q
                       Median
                                     3Q
                                             Max
                     -0.5608
  -2.1337
            -0.8811
                                1.0588
                                          1.9935
##
## Coefficients:
##
               Estimate Std. Error z value Pr(>|z|)
                                       6.887 5.69e-12 ***
## (Intercept)
                 4.0007
                             0.5809
```

```
## log(CK)
                -0.6117
                        0.0793 -7.714 1.22e-14 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 550.49 on 412 degrees of freedom
## Residual deviance: 475.18 on 411 degrees of freedom
     (22 observations deleted due to missingness)
## AIC: 479.18
## Number of Fisher Scoring iterations: 3
5
Here are the results of the model:
##
## Call:
## glm(formula = Outcome ~ log(CK) + Myopathy + log(CK): Myopathy,
       family = binomial(link = "logit"), data = downer)
##
## Deviance Residuals:
      Min
               10
                    Median
                                   30
                                           Max
## -1.2221 -0.9671 -0.3403
                              0.9456
                                        2.4952
## Coefficients:
##
                    Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                    0.02810
                               1.16564
                                         0.024
                                                  0.9808
                    -0.06788
## log(CK)
                                0.15872 -0.428
                                                  0.6689
## Myopathy
                     5.31297
                                3.84652
                                         1.381
                                                  0.1672
## log(CK):Myopathy -0.81290
                                0.44494 - 1.827
                                                  0.0677 .
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 246.27 on 217 degrees of freedom
## Residual deviance: 208.86 on 214 degrees of freedom
     (217 observations deleted due to missingness)
## AIC: 216.86
##
## Number of Fisher Scoring iterations: 6
Additionally we can show the deviance per term:
## Analysis of Deviance Table
##
## Model: binomial, link: logit
##
## Response: Outcome
##
## Terms added sequentially (first to last)
##
##
                    Df Deviance Resid. Df Resid. Dev Pr(>Chi)
##
```

```
## NULL
                                    217
                                           246.27
## log(CK)
                   1 21.3755
                                    216
                                           224.90 3.776e-06 ***
## Myopathy
                    1 12.6153
                                    215
                                           212.28 0.0003826 ***
## log(CK):Myopathy 1
                       3.4204
                                    214
                                           208.86 0.0643943 .
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

It seems like the effect of each of log(CK) and Myopathy is significant (p < 0.001) but their interaction is not.