

# ECSE 420 Assignment 1

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## Question 1.6

Graph 1.4: Runtime decreases until a certain point. Afterwards, it continually increases. This makes sense, as after a certain point, the overhead generated from creating and switching threads causes diminishing returns, and eventually a decrease in performance (past the optimal thread count). This can be explained by the fact that there can only be so many actual physical threads, and past a certain point the threads being created and used are virtual, which creates more and more overhead.

Graph 1.5: The sequential multiplication run time is of  $O(n^3)$ , therefore it increases greatly as  $n$  (here: matrix size) increases. However for  $n$  rather small ( $\leq 500$ ) the overhead generated by creating and switching threads during parallel multiplication is large enough to cause sequential multiplication to run faster. However as  $n$  increases, the parallelization of the process allows the parallel multiplication's runtime to increase at a much slower rate than  $O(n^3)$ , causing it to eventually be slower than sequential multiplication's runtime.

## Question 2.2

Deadlock can be avoided in multiple ways with this example:

- 1: Forcing threads to release resources after certain time to allow other request to complete
- 2: Requiring an order of resources that ensures no deadlock (must have A to request B)
- 3: Deadlock detection and avoidance (See Bankers algorithm)

## Question 4

### 4.1

The limit would be reached if we theoretically have infinite processors working on the parallel section. This would result in the parallel section (60%) happening instantly, leaving only 40% of the processing time as the maximum possible speed up. This results in a speed up maximum of 2.5x.

### 4.2

$$S_n = 1/((1-p)+p/n). \text{ Furthermore } S'_n > 2 \cdot S_n \Rightarrow S'_n > 2/((1-p)+p/n)$$

$$S'_n = 1/((1-p/k)+p/(n \cdot k))$$

$$\Leftrightarrow 1/((1-p/k)+p/(n \cdot k)) > 2/((1-p)+p/n) \text{ Flip} \Rightarrow 1-p/k+p/(n \cdot k) < 1/2(1-p+p/n)$$

$$p=0.8$$

$$\Leftrightarrow 2-20.8/k+20.8/(n*k)<1-0.8+0.8/n$$

Multiply by k:

$$\Leftrightarrow 2k-1.6+1.6/n<k-0.8k+0.8k/n^*$$

$$\Leftrightarrow 2k-0.2k+0.8k/n<1.6-1.6/n$$

$$\Leftrightarrow k(1.8+0.8/n)<1.6-1.6/n$$

$$\Leftrightarrow k<(1.6-1.6/n)/(1.8+0.8/n)$$

### 4.3

Let  $a_1$  be the original acceleration and  $a_2$  the second. Since the program is half as fast, we know that  $a_2/a_1=2$

$$A_1=1/((1-p)+p/n)=q/(s+(1-s)/n) \quad A_2=1/((s/3)+(1-s/3)/n)$$

$$a_2/a_1=2$$

$$\Leftrightarrow 2=(1/(s/3+(1-s/3)/n))/(1/(s+(1-s)/n))$$

$$\Leftrightarrow 2*(1/(s+(1-s)/n))=(1/(s/3+(1-s/3)/n))$$

$$\Leftrightarrow 2s/3+2/n-2s/3n=s+(1-s)/n$$

$$\Leftrightarrow 2s_n + 6 - 2s = 3s_n + 3 - 3s$$

$$\Leftrightarrow 2s_n - 3s_n - 2s + 3s = -3$$

$$\Leftrightarrow -s_n + s = -3$$

$$\Leftrightarrow s(n-1)=3$$

$$\Leftrightarrow s=3/(n-1)$$