

① Since  $x_n \rightarrow 5$  for  $\varepsilon > 0 \exists K_1(\varepsilon) > 0 \ni |x_n - 5| < \varepsilon$  if  $n > K_1(\varepsilon)$ .  
 Then let  $\varepsilon > 0$  then  $\exists K_2(\varepsilon) > 0 \ni |x_n^2 - 25| < \varepsilon$  if  $n > K_2(\varepsilon)$ .  
 $|x_n^2 - 25| \leq |x_n^2 + 25|$  since  $x_n^2$  is always positive. Then  
 $|x_n^2 + 25| = |(x_n^2 - 5)^2| = (x_n - 5)^2 < \varepsilon$   $x_n - 5 < \sqrt{\varepsilon}$  and  
 since  $x_n - 5 < \varepsilon$  let  $K_2(\varepsilon) = K_1(\varepsilon)$

②  $x_n \rightarrow \frac{1}{4}$   $x_n \neq 0 \forall n \in \mathbb{N}$  prove  $\frac{1}{x_n} \rightarrow 4$   
 Since  $x_n \rightarrow \frac{1}{4}$   $\forall \varepsilon > 0 \exists K_1(\varepsilon) > 0 \ni |x_n - \frac{1}{4}| < \varepsilon$  if  $n > K_1(\varepsilon)$   
 Then we must show that  $\forall \varepsilon > 0 \exists K_2(\varepsilon) > 0 \ni |\frac{1}{x_n} - 4| < \varepsilon$   
 if  $n > K_2(\varepsilon)$ . Let  $l$