

Computer Architecture

Tutorial 1 – Boolean Algebra - Answers

- 1) Write the Truth Table for the following Boolean expression: $R = A \cdot B + C'$

A	B	C	C'	$A \cdot B$	$R = A \cdot B + C'$
0	0	0	1	0	1
0	0	1	0	0	0
0	1	0	1	0	1
0	1	1	0	0	0
1	0	0	1	0	1
1	0	1	0	0	0
1	1	0	1	1	1
1	1	1	0	1	1

- 2) Simplify the following Boolean Expressions to its simplest form

a) $R = A + A' \cdot B$

$$\begin{aligned} R &= (A + A') \cdot (A + B) \\ &= 1 \cdot (A + B) \\ &= A + B \end{aligned}$$

Distributive Rule
Negation Rule
Simplification Rule

b) $R = A \cdot (A' + B)$

$$\begin{aligned} R &= (A \cdot A') + (A \cdot B) \\ &= 0 + A \cdot B \\ &= A \cdot B \end{aligned}$$

Distributive Rule
Negation Rule
Simplification Rule

c) $R = (A + C) \cdot (A \cdot D + A \cdot D') + A \cdot C + C$

$$\begin{aligned} R &= (A + C) \cdot (A \cdot (D + D')) + A \cdot C + C \\ &= (A + C) \cdot A + A \cdot C + C \\ &= A \cdot A + C \cdot A + A \cdot C + C \\ &= A + A \cdot C + C \\ 1 \cdot (A + C) + C &= A + C + C \\ A + C + C &= A + C \\ A + C & \end{aligned}$$

Distributive Rule
Negation Rule
Distributive Rule
Idempotent Rule
Distributive Rule
Simplification Rule