

Q1. Convert the date 5/23/2020 to hex. Write in the form: M/DD/YYYY

When converting decimal to hexadecimal, keep dividing the quotients by base 16 and reassemble the remainders as the digits of the resulting number:

Month: $5(10) = 5(16)$ Day: $23(10) = 23(10) / 16(10) = 1 \text{ R } 7 = 17(16)$

$2020 / 16 = 126 \text{ R } 4$, take 4

$126 / 16 = 7 \text{ R } 12$, take $12(10) = E(16)$

$7 / 16 = 0 \text{ R } 7$, take 7

$2020(10) = 7E4(16)$

Answer: 5/17/7E4

Q2. Which number has the most 2's when converted to octal? $508(16)$ $88A(16)$ $195(16)$ $348A(16)$ $1050(16)$

Step1. Convert each digit of the hexadecimal numbers into 4-digit binary groups

Step2. Re-group the binaries into 3-digit groups starting from the right (append leading zeros if it helps)

Step3. Convert each 3-digit binary group into an octal digit

Step4. Count the number 2's, and compare the counts

$508(16) = 0101\ 0000\ 1000$	$(2) = 010\ 100\ 001\ 000$	$(2) = 2\ 5\ 1\ 0$	(8)	One 2
$88A(16) = 1000\ 1000\ 1010$	$(2) = 100\ 010\ 001\ 010$	$(2) = 4\ 2\ 1\ 2$	(8)	Two 2's
$195(16) = 0001\ 1001\ 0101$	$(2) = 000\ 110\ 010\ 101$	$(2) = 0\ 6\ 2\ 5$	(8)	One 2
$348A(16) = 0011\ 0100\ 1000\ 1010$	$(2) = 011\ 010\ 010\ 001\ 010$	$(2) = 3\ 2\ 2\ 1\ 2$	(8)	Three 2's
$1050(16) = 0001\ 0000\ 0101\ 0000$	$(2) = 001\ 000\ 001\ 010\ 000$	$(2) = 1\ 0\ 1\ 2\ 0$	(8)	One 2

If you believe you are better with binaries, you can count how many 010's in binaries are after step#2! 😊

Answer: 348A

Q3. Find $f(90)$ given: $f(x) = 2 * f(x/3) - 1$ if x is a multiple of 3 and odd
 $= -1 * f(x/2) + 2$ if x is even
 $= x + 4$ otherwise

$$\begin{aligned} f(90) &= -1 * f(90/2) + 2 = -1 * f(45) + 2 &= -1 * 33 + 2 = -31 \\ f(45) &= 2 * f(45/3) - 1 = 2 * f(15) - 1 &= 2 * 17 - 1 = 33 \\ f(15) &= 2 * f(15/3) - 1 = 2 * f(5) - 1 &= 2 * 9 - 1 = 17 \\ f(5) &= 5 + 4 = 9 \end{aligned}$$

Answer: -31

Q4. Find $f(f(f(6)))$ given: $f(x) = 2 * f(x-3) - 1$ if $x > 10$
 $= f(x-3) + 3$ if $2 \leq x \leq 10$
 $= 3^x * x^3$ if $x < 2$

Calculate from inside-out:

1) $f(6)$; 2) $f(f(6))$; 3) $f(f(f(6)))$

$$\begin{aligned} f(6) &= f(6-2) + 3 = f(4) + 3 &= 6 + 3 = 9 \\ f(4) &= f(4-2) + 3 = f(2) + 3 &= 3 + 3 = 6 \\ f(2) &= f(2-2) + 3 = f(0) + 3 &= 0 + 3 = 3 \\ f(0) &= 3^0 * 0^3 = 0 \end{aligned}$$

$$f(6) = 9$$

$$\begin{aligned} f(f(6)) &= f(9) = f(9-2) + 3 = f(7) + 3 &= 12 + 3 = 15 \\ f(7) &= f(7-2) + 3 = f(5) + 3 &= 9 + 3 = 12 \\ f(5) &= f(5-2) + 3 = f(3) + 3 &= 6 + 3 = 9 \\ f(3) &= f(3-2) + 3 = f(1) + 3 &= 3 + 3 = 6 \\ f(1) &= 3^1 * 1^3 = 3 * 1 = 3 \end{aligned}$$

$$f(f(6)) = 15$$

$$\begin{aligned} f(f(f(6))) &= f(15) = 2 * f(15-3) - 1 = 2 * f(12) - 1 &= 2 * 29 - 1 = 57 \\ f(12) &= 2 * f(12-3) - 1 = 2 * f(9) - 1 &= 2 * 15 - 1 = 29 \end{aligned}$$

$f(9)=15$ from Step#2

Answer: 57

Q5. What is outputted when this program is executed?

	a	b	c	d	e	
a = 12 : b = 6 : c = 3 : d = 2	12	6	3	2		
if a == b * d then						12==6*2, true
e = a / b					2	
end if						
if b - d == a / c then						6-2==4, 12/3==4, true
e = e + a / c					6	2+12/3==2+4==6
end if						
e = a / c - e					-2	12/3-6==4-6=-2
if b / c == a / e then						pos != neg, false
a = 2 * d						
else						
a = 2 * e	-4	6	3	2	-2	
end if						
if (a < b) (c < d) then						a<b, true
a = a + b	2					-4+6==2
else						
c = c + d	2	6	5	2	-2	3+2==5
end if						(2<6) && (6+5>5*5),
if (a < d) && (b + c > c * c) then						11>25, false
d = a + c						
else						
c = d - b	2	6	-4	2	-2	d-b==2-6==-4
end if						6/2+(-4)*(-2)/(2+6)-(6+2)/2*2
x = b / a + c * e / (d + b) - (b + d) / a * a						=3+8/8-8/2*2=3+1-8=4-8=-4
print x						
end						

Answer: -4