

# Model Identification and Data Analysis (MIDA) - Examples

AY 2019-2020



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# **Model Identification of engine-to-slip dynamics for a traction-control system using time-domain (State-Space) identification**

# The brake/traction control problem



Example of wheel lockup in braking

<https://www.youtube.com/watch?v=SHODIsUrydU>

<https://www.youtube.com/watch?v=lsb2k8yEazA>

Example of wheel overslip in traction, also affecting lateral dynamics



# Definition of longitudinal slip of the wheel (lambda)

$v$ : body speed  
 $r$ : rolling radius  
 $\omega$ : angular wheel speed

$\omega r = v_w$  «wheel speed» [m/s] at the contact point

$$\lambda = \frac{|v - \omega r|}{\max\{v, \omega r\}}$$

If brake: ↓

↓ If traction:

Free rolling

$$0 \leq \lambda \leq 1$$

Locked wheel

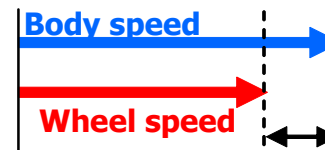
$$\lambda := \frac{v - \omega r}{v}$$

$$\lambda = \frac{(\omega r - v)}{\omega r}$$

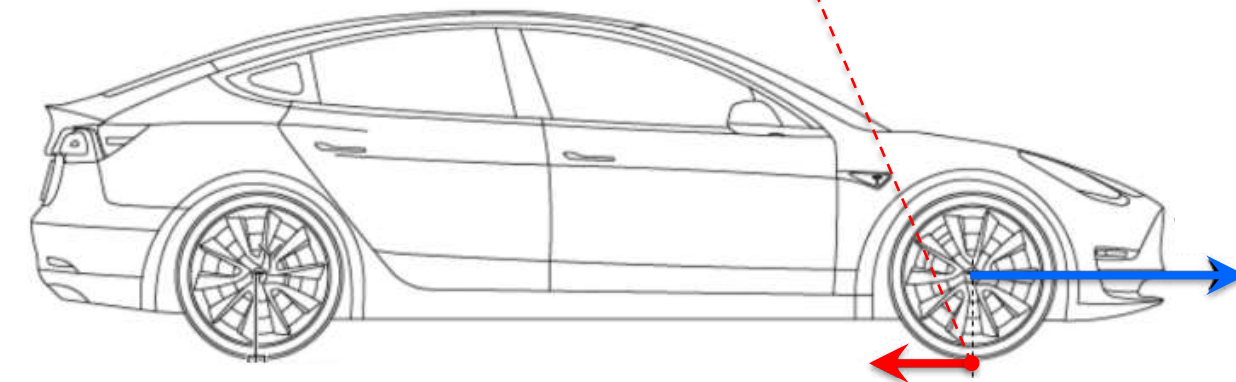
$$0 \leq \lambda \leq 1$$

«Burnout»

Free rolling

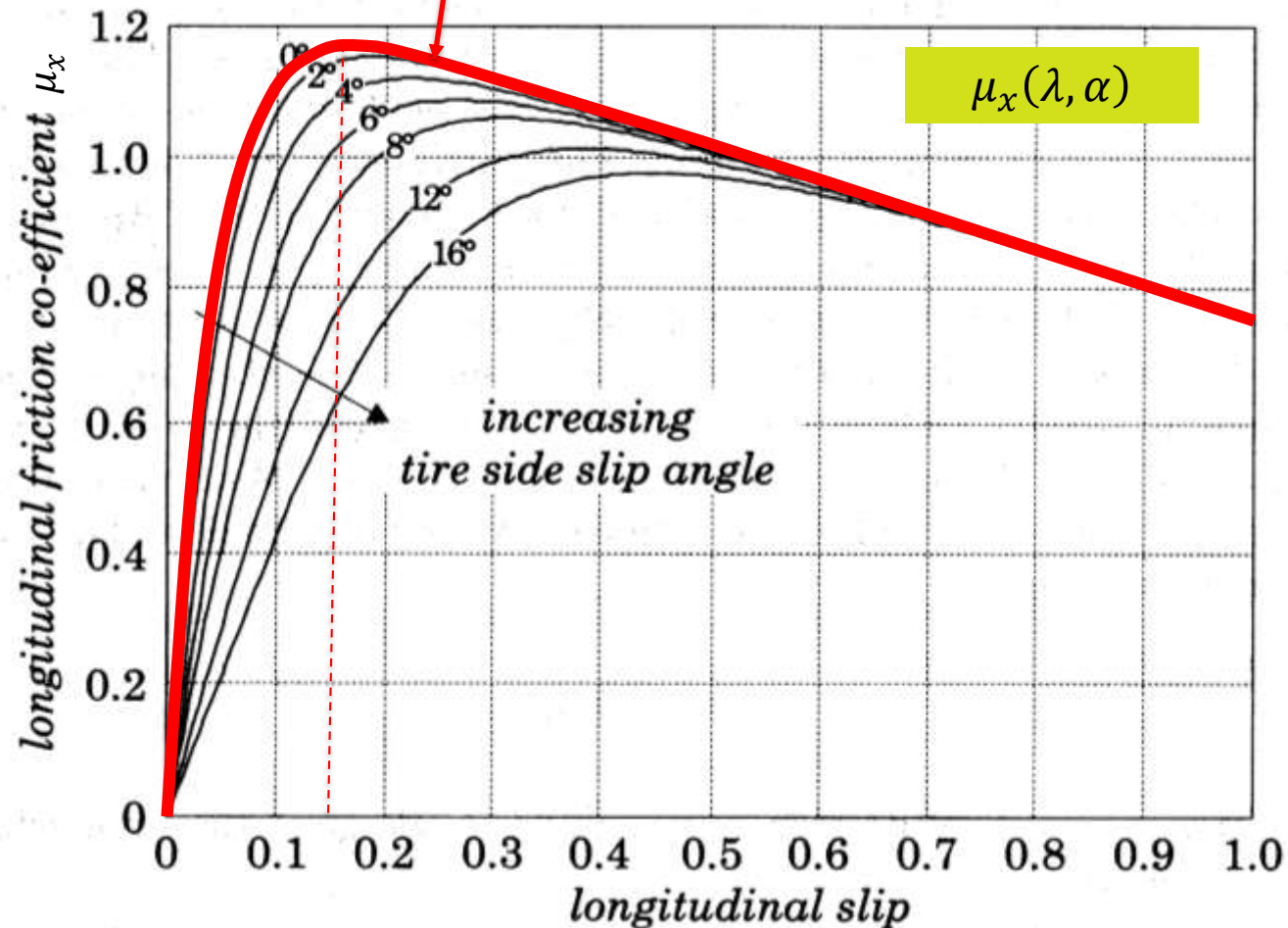


«SLIP»  $\lambda = \frac{\text{Body speed} - \text{Wheel speed}}{\text{Body speed}}$



# Contact forces: longitudinal friction coefficient

0° sideslip curve ( $\mu_x(\lambda, 0)$ ) = all-longitudinal forces



Example of dry-asphalt, with high-grip tire

If there is no slip, the longitudinal force is zero

Force increases linearly up to values of  $\lambda$  of about 0.1-0.15

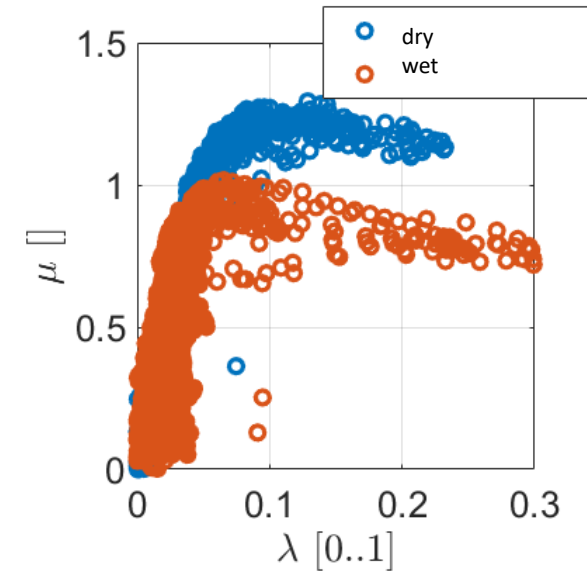
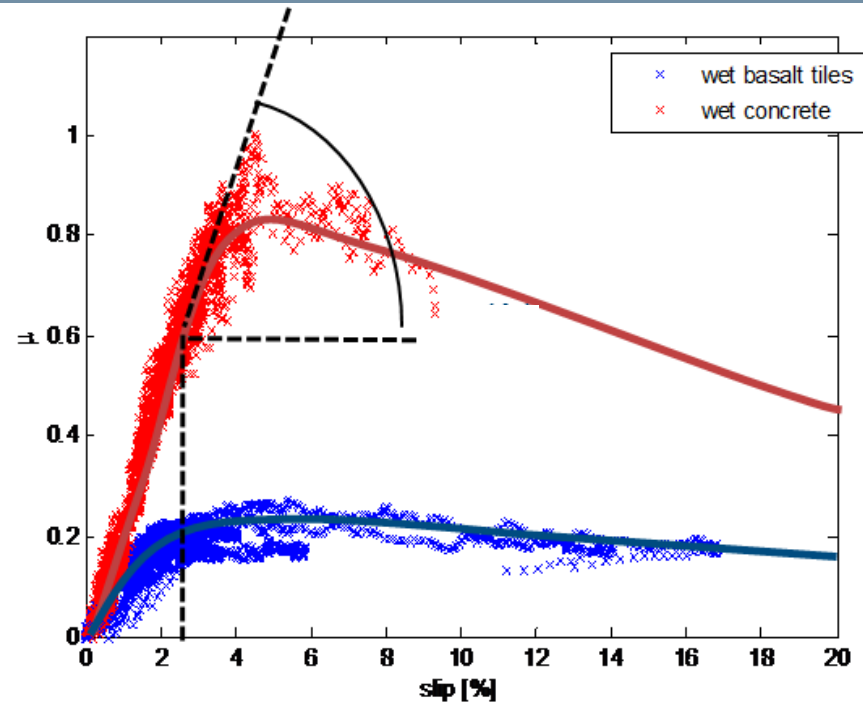
Beyond the maximum: **slope sign changes (!)**

Increasing side-slip angle:

- Reduction of longitudinal force
- The maximum point moves forward



# Example of estimation of longitudinal friction curve from experimental data



# Longitudinal-dynamics control: traction control (TC)



# Remark on motorcycles: Traction Control (TC) generations...



Generation 1  
(BMW) [2007]

Mainly (only) safety-oriented



Generation 2 (Ducati 1098)  
[2008]

Performance-oriented

Very simple roll-angle detection (yes/no)



Generation 3  
(Aprilia RSV4 and BMW S1000) [2010]

Full roll-angle estimation

Ride-by-wire

+ “Gadgets” (wheelie, launch...)



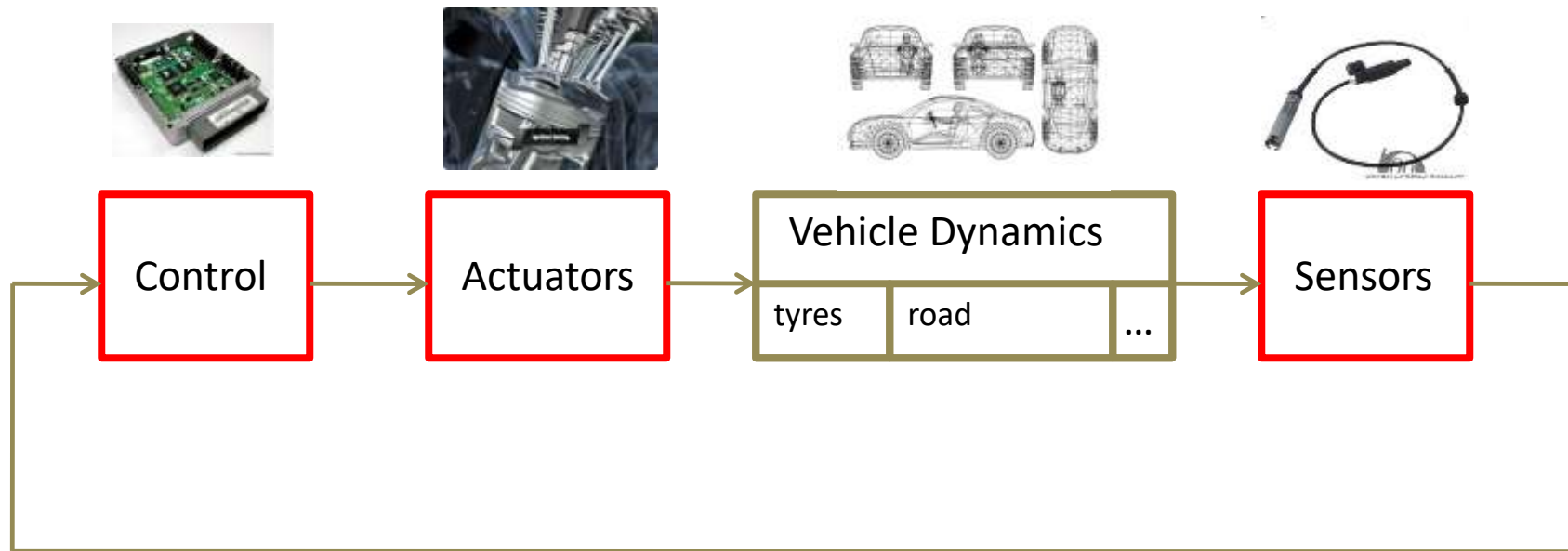
Generation 3+; Yamaha R1  
MY 2015

Includes rear wheel sideslip monitoring

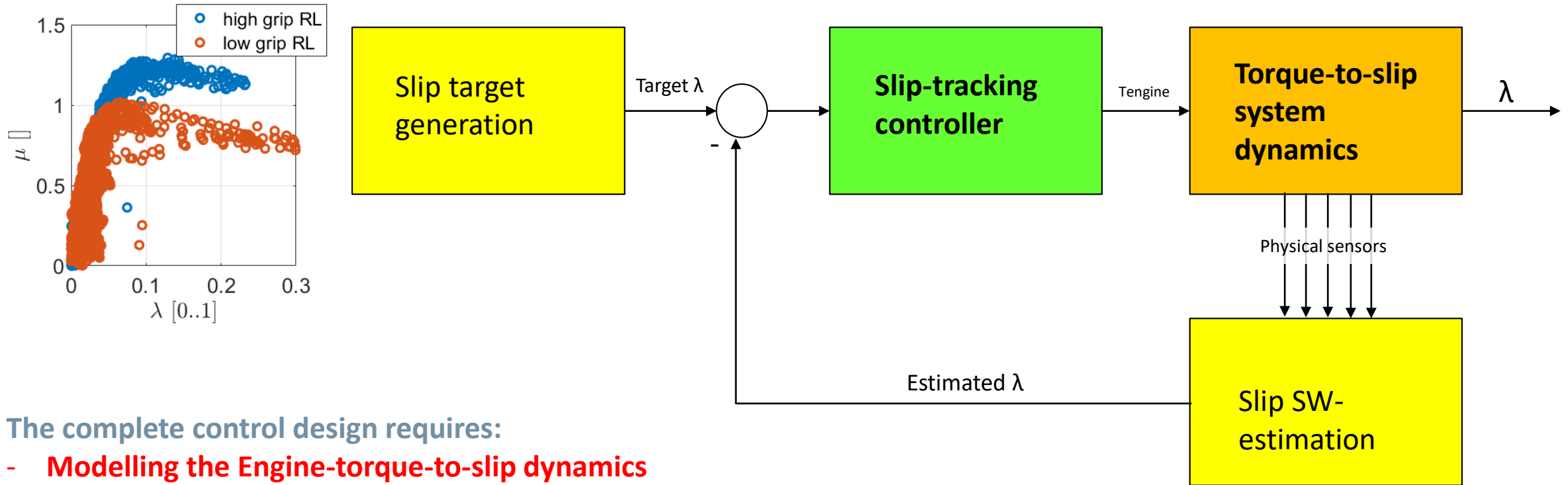


# Introduction to Traction Control (TC) system

TC is a **closed-loop electronic control system**



# Introduction to TC DESIGN: sub-problems



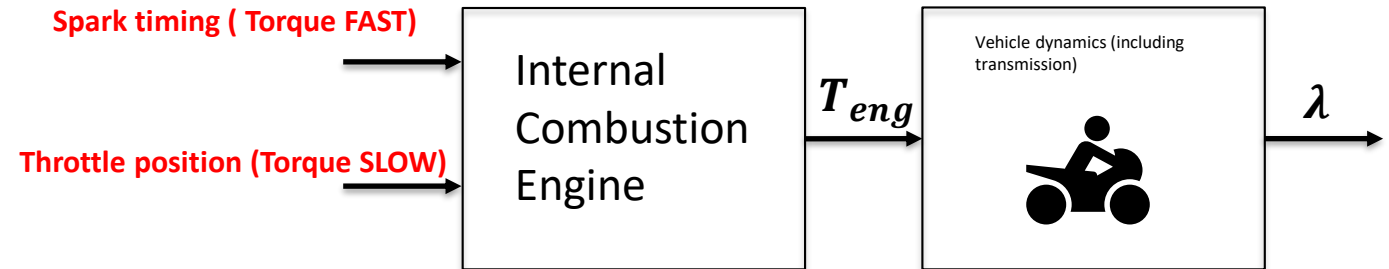
The complete control design requires:

- **Modelling the Engine-torque-to-slip dynamics**
- Design the slip-tracking control algorithm
- **Design an estimator for the slip (SW-sensing)**
- Design a slip-target generation algorithm

# Classic (most common) actuator: Torque of the Internal Combustion Engine (ICE)

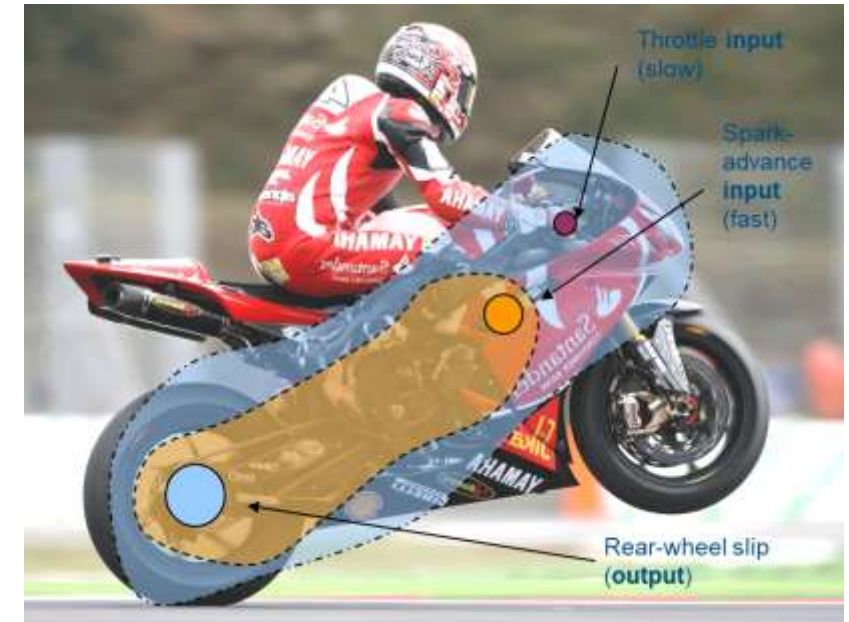


In a Spark Ignited Internal Combustion Engine, there are two variables that can be used to change the delivered torque

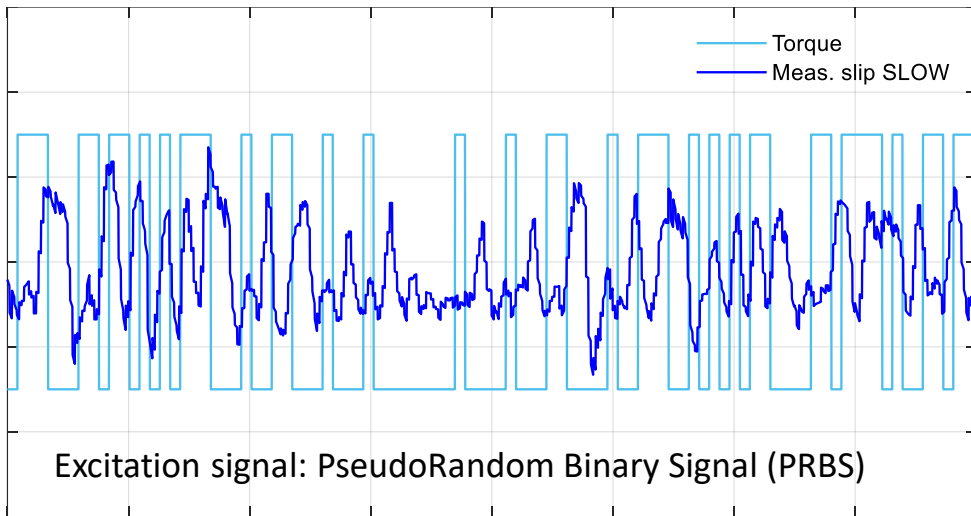


Spark-timing has a «fast» action on  $T_{eng}$

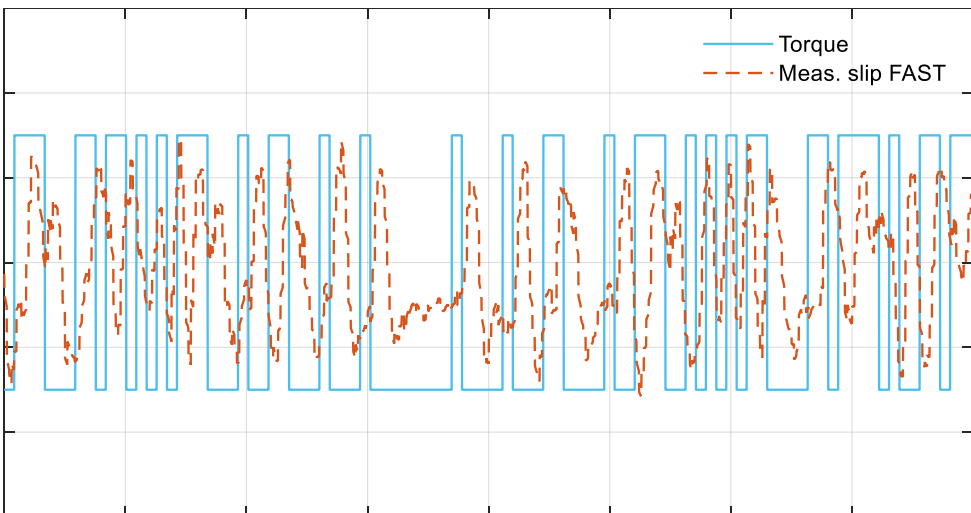
Throttle position has a «slow» action on  $T_{eng}$



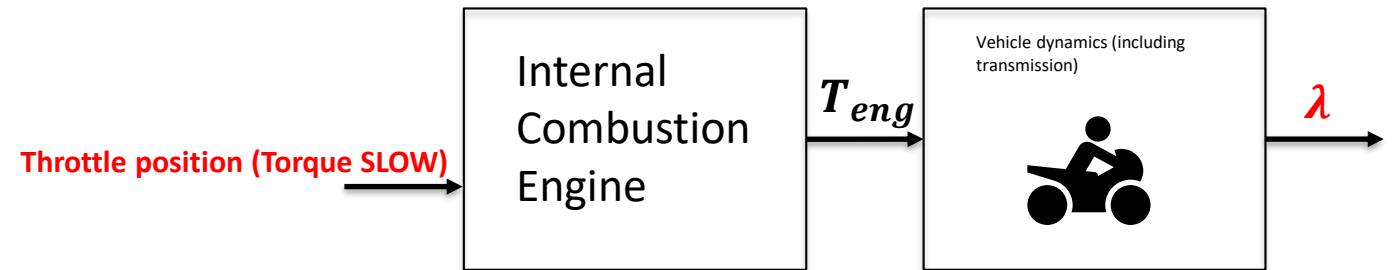
# Experimental I/O relationship from the two inputs



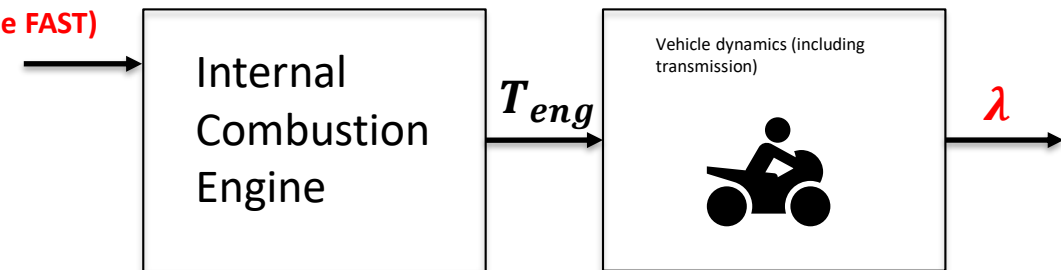
Time



Time

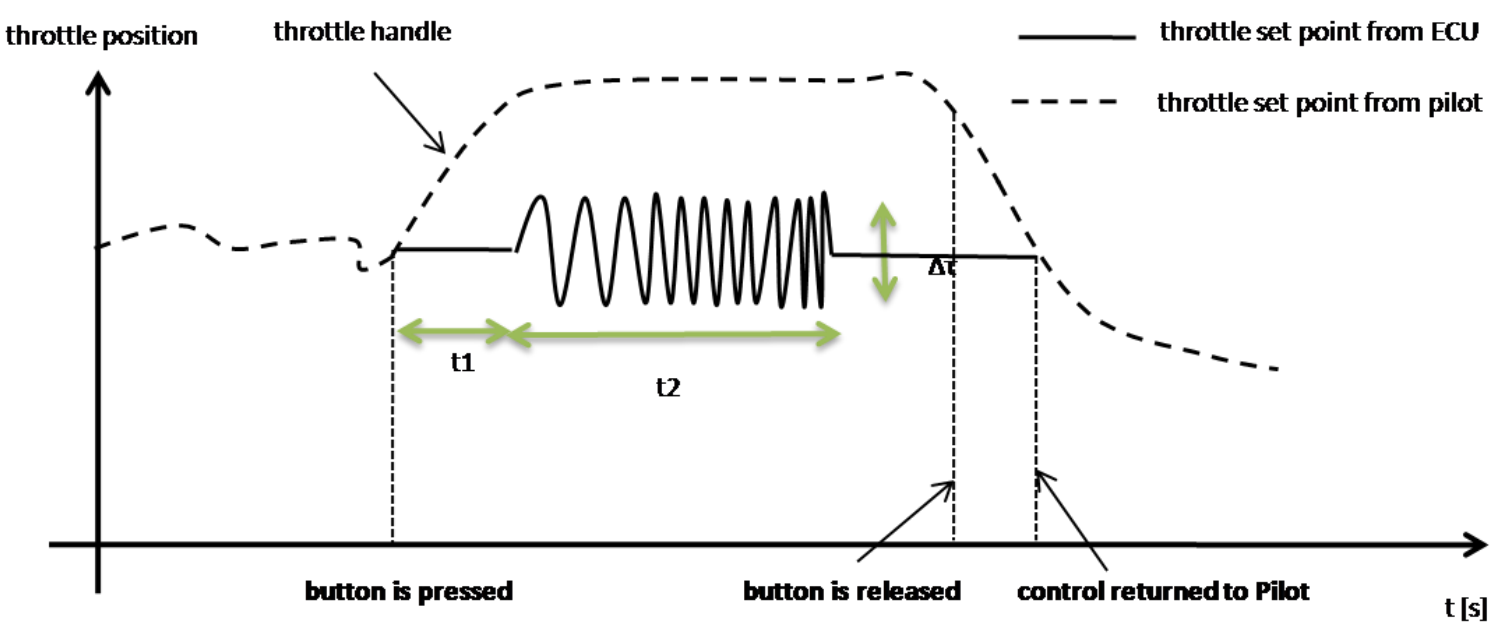


Spark timing (Torque FAST)





# Remark on experiment design

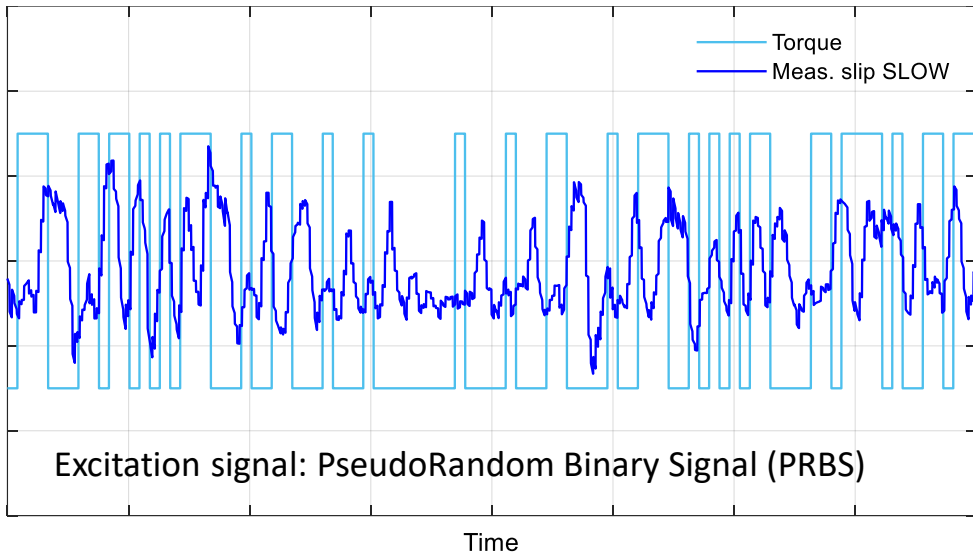


Tests on a long (3 km) straight road:

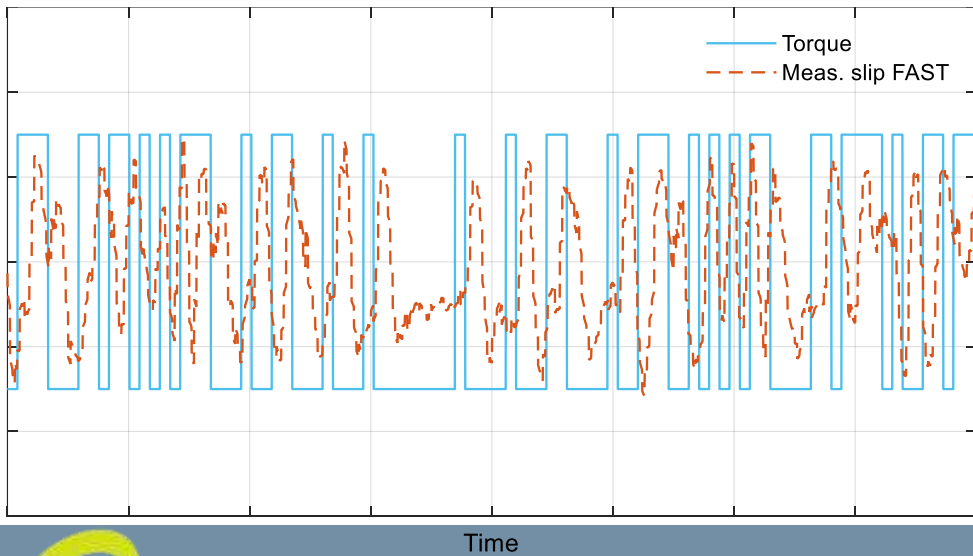
- 1) the rider is asked to Trim the motorcycle to constant speed
- 2) the test is triggered by the driver with a button: At that point the ECU completely command overrides the driver, and the excitation signal is applied around the neighborhood of the initial condition.

This experiment is non-trivial, but has the major advantage of **being repeatable and providing the real dynamic behavior of the motorbike** (And rider), on a real test-track (**Whereas test-rig Typically experiments are flawed by non-realistic conditions**).

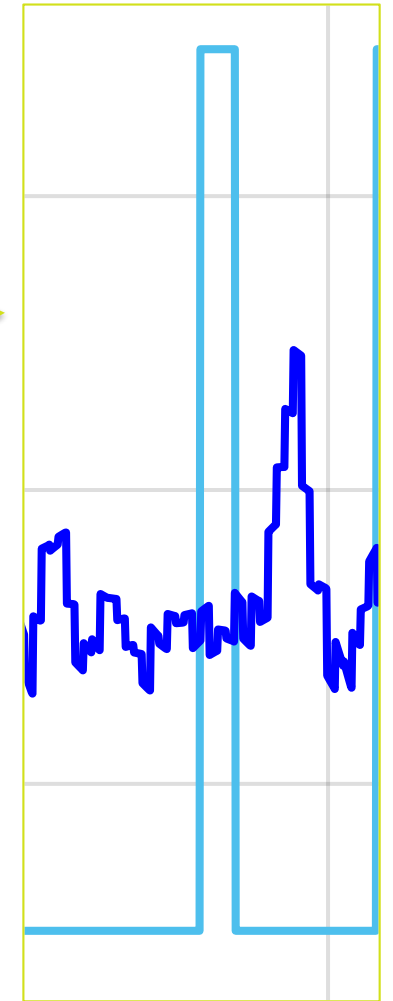
# Remark: delay



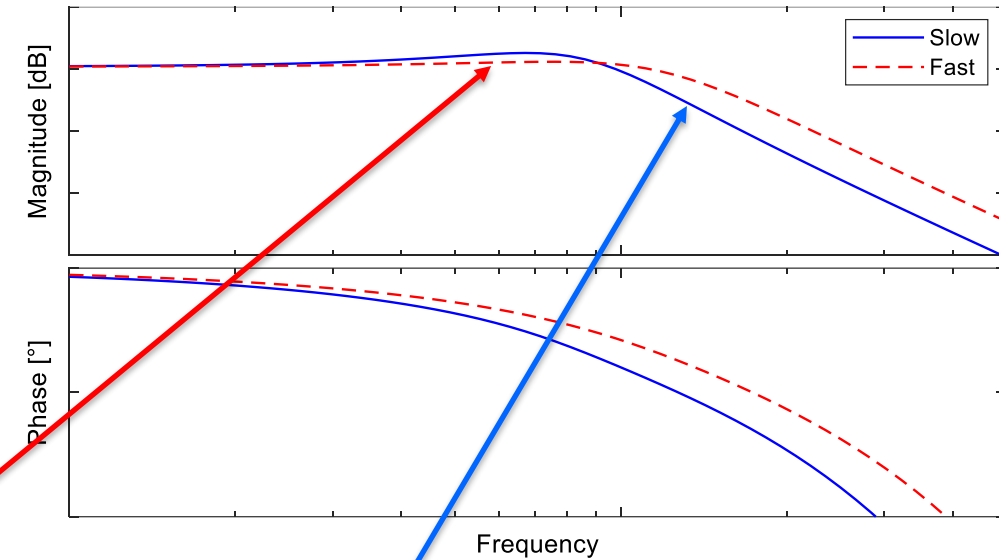
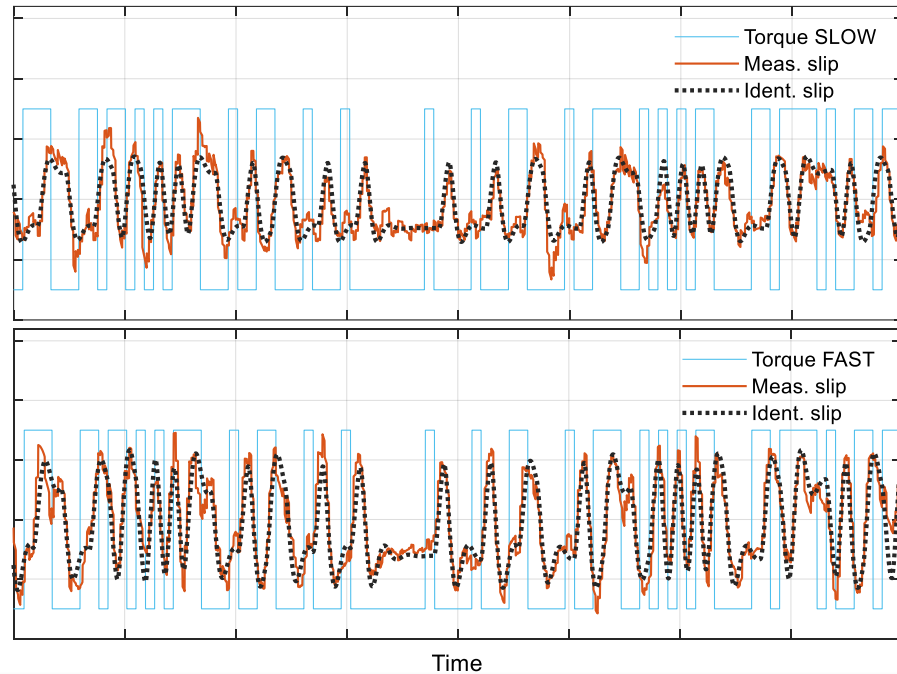
Estimated delay: 5 steps at 20ms sampling time



Estimated delay: 4 steps at 20ms sampling time



# Experimental (Black-Box) identification of I/O relationships from the two inputs



Sampling time:  $T_s=20\text{ms}$  (0.02s)

$$F_{\text{fast}}(z) = \frac{0.01412z + 0.01412}{z^2 - 0.2876z + 0.1988} (z^{-3})$$

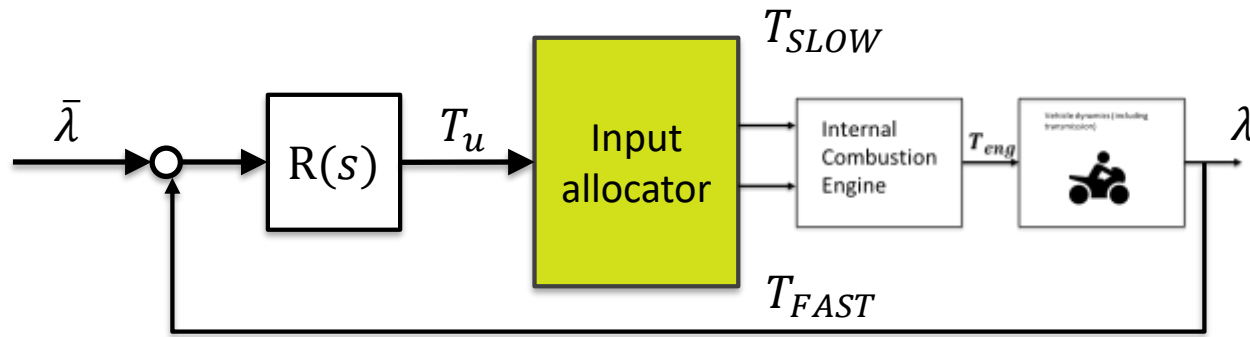
$$F_{\text{slow}}(z) = \frac{0.01116z + 0.01116}{z^2 - 0.7237z + 0.4002} (z^{-4})$$

Obtained with 4SID identification

2nd-order (only!) TF, with delays

# SISO design with input-allocator

An effective controller is a SISO controller, flanked by a proper “Input Allocator” (IA).



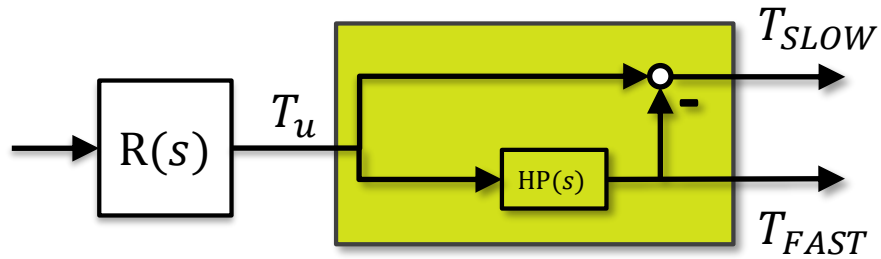
The IA must satisfy the following requirements:

1. Be “transparent” with respect to the regulator, meaning that the TOTAL engine torque should match exactly the torque requested by the regulator. This allows a SISO approach for the controller design
2. Allocate the torques according to their specific features:
  1. The high frequency torque should be delivered through the “FAST” channel
  2. The low frequency torque should be delivered through the “SLOW” channel



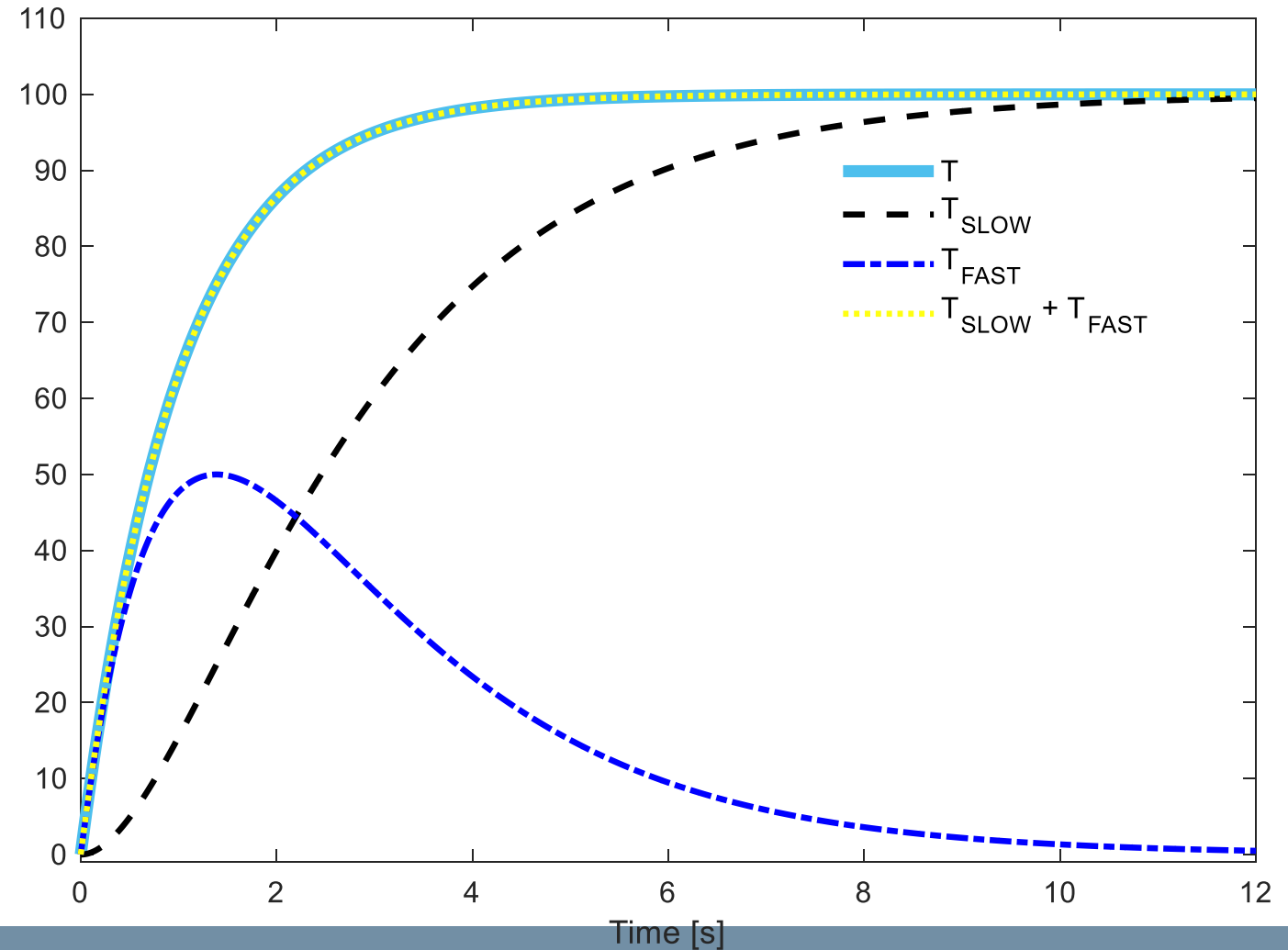
# Input-allocator (frequency-split)

The Input Allocator makes a frequency-split of the Torque requested by the slip-regulator



Example:

$$HP(s) = \frac{s}{s + 0.5}$$



## Two examples of advanced TC for high-performance motorcycles («superbike» class)



<https://www.youtube.com/watch?v=8a9LWIGkjbA>

Introducing Ducati Traction Control EVO