

Ex_01 – RAID Capacity

giovedì 19 marzo 2020 10:56

Consider to have 6 disks, each one with a capacity of 1TB.

What will be to total storage capacity of the system if they are in the following configurations?

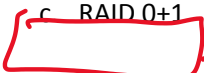
a. RAID 0



b. RAID 1



c. RAID 0+1



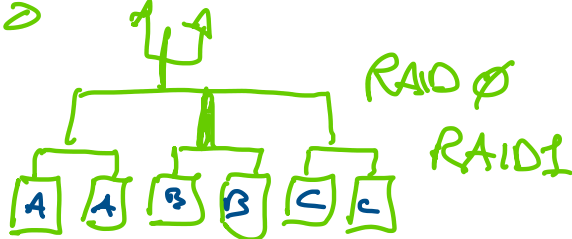
d. RAID 1+0



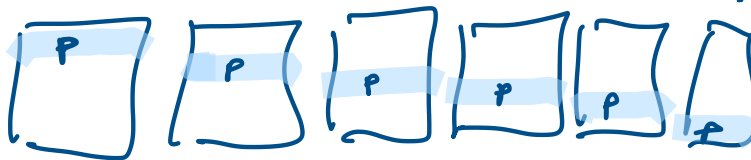
e. RAID 5



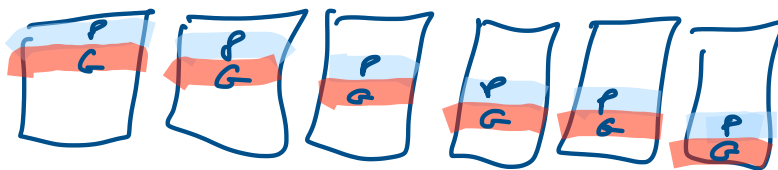
f. RAID 6



RAID 5



RAID 6

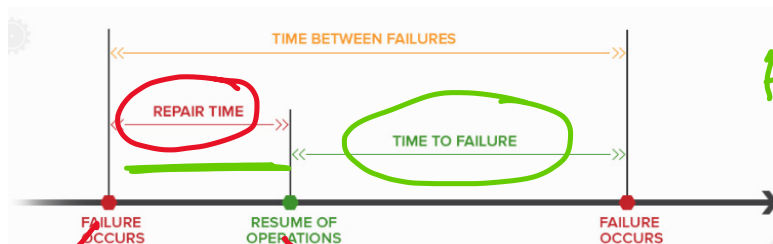


RAID Preliminaries

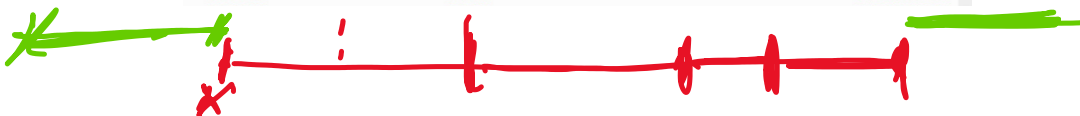
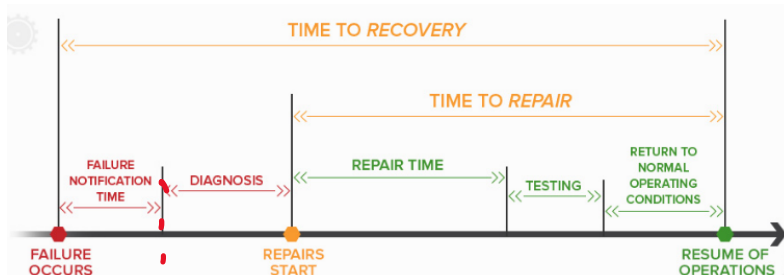
giovedì 19 marzo 2020 10:05

Definitions:

- **RAID** - Redundant Array of Independent Disks
- **MTTDL** - Mean Time To Data Loss
 - Mean time until drive failures cause data loss in the array
- **MTBF** - Mean Time Between Failures
 - is the mean time between hard disk failures.
- **MTTF** - Mean Time To Failure
 - mean time before a disk has a failure
 - $1/\text{MTTF}$ is called Failure Rate



- **MTTR** - Mean Time To Recover (or Repair)
 - Mean time to rebuild redundancy in the array.



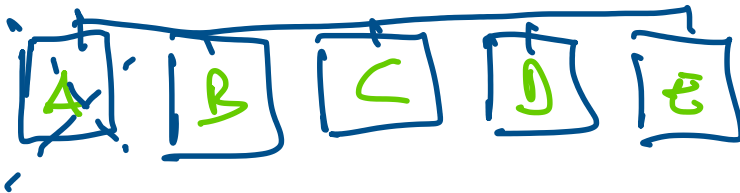
Ex_02 – RAID 0

mercoledì 4 marzo 2020 11:46

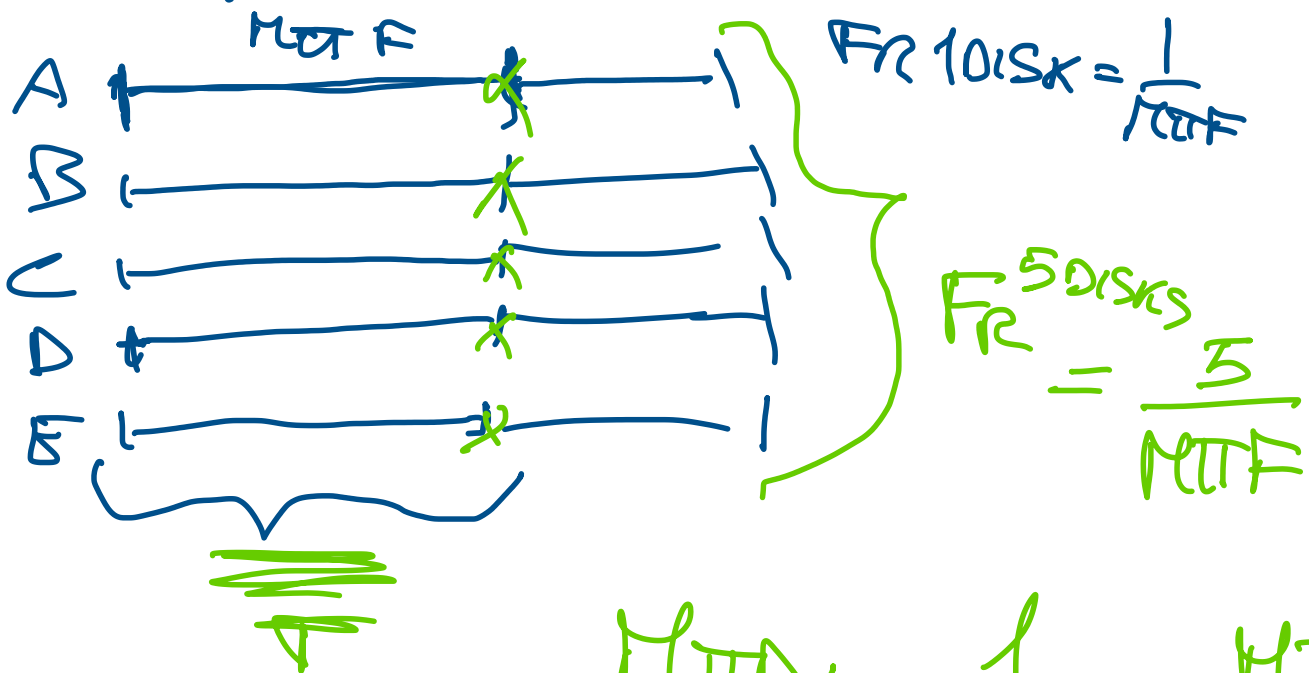
Consider the following RAID 0 setup:

- $n = 5$ disks
- $MTTR = 8$ hours
- $MTTF(\text{one disk}) = 1600$ day

The MTDDL will be:



RAID 0 \rightarrow 1 DISK



$$MTDDL = \frac{1}{FR} = \frac{MTTF}{5}$$
$$= 320 \text{ Days}$$

Quiz_1 – RAID 0

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A system administrator has decided to use a stock of disks characterized by:

MTTF = 800 days

MTTR = 20 days

The target lifetime of the system is 3 years,

The maximum number of disks that could be used in RAID 0 to have a MTTFDataLoss larger than the system lifetime is:

1. 1 disk

☒ 2. None

3. 2 disks - since RAID 0 requires at least two disks

4. $800/20 = 40$ disks

5. None of the other options

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$$MTTF > 3Y = 3 \times 365 \text{ DAYS}$$

$$MTTF = 800 \text{ DAYS}$$

$$MTTF = \frac{800}{N} > 3 \times 365$$

Ex_03 - RAID1

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Consider the following RAID 1 setup:

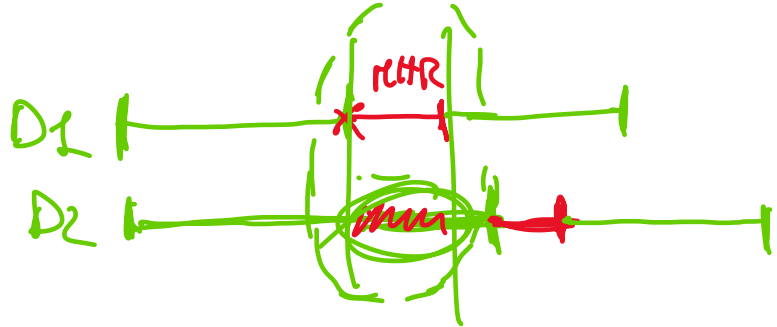
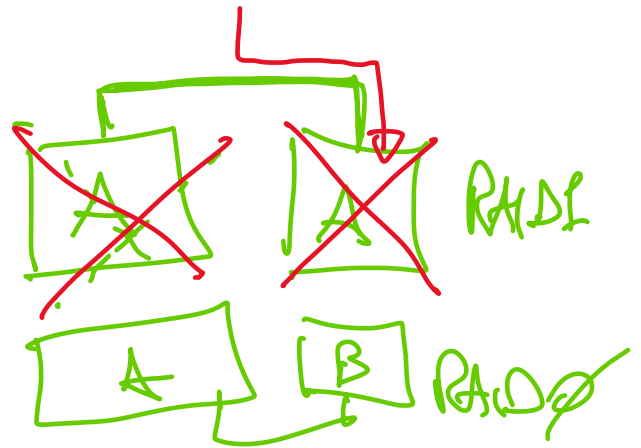
- $n = 2$ disks
- MTTR = 8 days
- MTTF(one disk) = 1800 day

The MTDDL will be:

$$FR = \left(\frac{2}{MTTF} \right) * \left(\frac{MTTR}{MTTF} \right)$$

$$= \frac{2 * MTTR}{MTTF^2}$$

$$MTDDL = \frac{MTTF^2}{2 * MTTR} = \underline{\underline{202K Days}}$$



Ex_04 - RAID 1+0

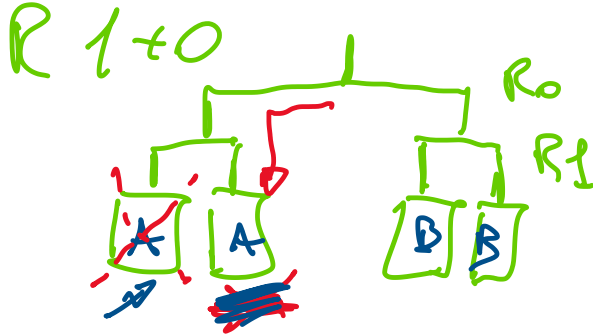
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$$2+2=N$$

Consider 2 groups (RAID 0) of 2 disks each (RAID 1), for a total of 4 disks in configuration RAID 1+0:

- MTTR = 3 days
- MTTF(one disk) = 1400 day

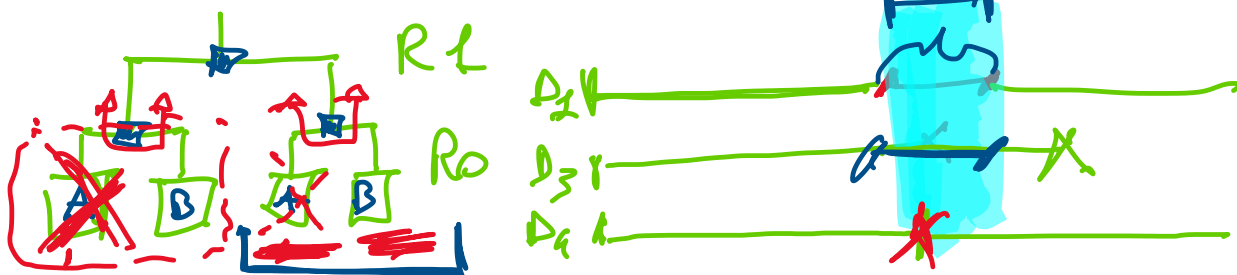
The MTDDL will be:



$$F_R = \frac{N}{MTTF} \times \left(\frac{1}{MTTF} \times MTTR \right)$$

$$= \frac{MTTF^2}{N \times MTTR} = \frac{1400^2}{3 \times 3} \approx 163K$$

THE SAME BUT ROT+1



$$F_R = \frac{N}{MTTF} \times \left(\frac{2}{MTTF} \times MTTR \right)$$

$$MTDDL_{rot1} = \frac{MTTF^2}{N \times MTTR \times 2} = MTDDL_{1+0} \times \frac{1}{2} = 81.5K$$

Ex_05 – RAID 0+1

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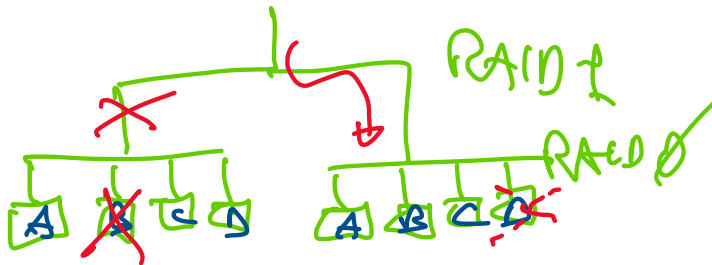
Consider 2 groups (RAID 1) of 4 disks each (RAID 0), for a total of 8 disks in configuration RAID 0+1:

- MTTR = 4 days
- MTTF(one disk) = 2200 days

The MTDL will be:

$$N = 2 \times 4 = 8 \text{ DISKS}$$

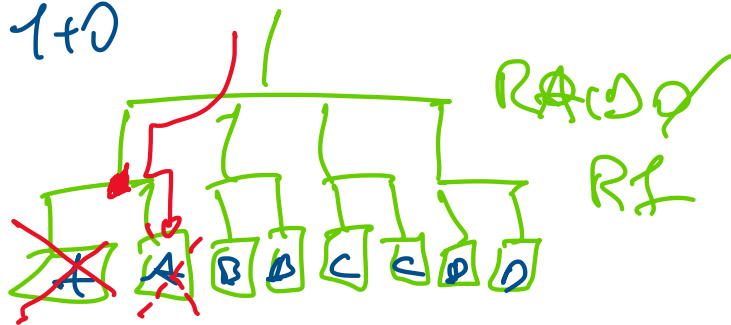
$$G = 4 \text{ DISKS}$$



$$FR = \frac{N}{MTTF} \times \left(\frac{G}{MTTF} \times MTTR \right) =$$

$$MTDL = \frac{MTTF^2}{N \times G \times MTTR} = \frac{2200^2}{8 \times 4 \times 4} \approx 37.8 \text{ K DAYS}$$

THIS SAME 1+0



$$FR = \frac{N}{MTTF} \times \left(\frac{1}{MTTF} \times MTTR \right) =$$

$$MTDL_{1+0} = \frac{MTTF^2}{N \times MTTR} = \underbrace{MTDL_{0+1}}_{\text{circled}} \times G$$

Quiz_2 - RAID 0 + 1

mercoledì 4 marzo 2020 18:31

A system administrator has decided to use a stock of disks characterized by:

MTTF = 800 days

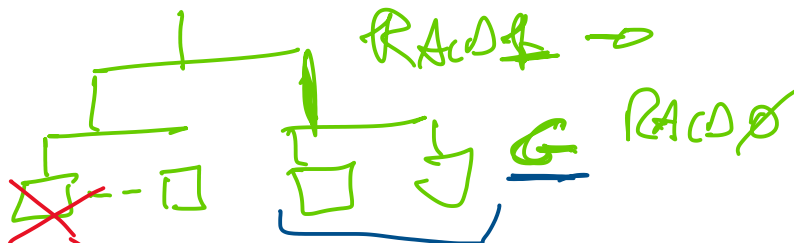
MTTR = 20 days

The target lifetime of the system is 3 years;

The maximum number of disks that could be used in RAID 01 to have a MTDDL larger than the system lifetime is:

1. No more than 58 disks
2. No more than 7 disks
3. At least 8 disks
4. No more than 6 disks
5. None of the other options

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RAID 01 →

RAID 0

$FR = \frac{N}{MTTF} * \left(\frac{G}{MTTR} * MTTR \right)$

$MTDDL = \frac{MTTF^2}{N * \frac{N}{2} * MTTR} = 1095$

$N^2 \leq \frac{MTTF^2 * 2}{MTTR * 1095} = 58$

$N < 7.6$

$N = 6$