## 递归

## 2022年8月16日

```
#include <stdio.h>
   void print_syracuse_sequence_from(int n){
       printf("%d\t", n);
       if(n == 1) return;
       if(n \% 2 == 0)
          print_syracuse_sequence_from(n / 2);
       else
          print_syracuse_sequence_from(3 * n + 1);
   }
   int main(){
       int n;
11
      printf("Input a pos for a syracuse sequence:\n");
12
       scanf("%d", &n);
       print_syracuse_sequence_from(n);
      return 0;
16 }
```

1. 输入两个正整数,用递归法求最大公约数。

```
1 #include <stdio.h>
2
3 int gcd(int m, int n)
4 // 递归求m和n的最大公约数
5 {
6 if(!n) // 上一次得到余数0
7 {
8 return m;
9 }
```

```
return gcd(n, m % n); // 辗转规约

int main()

{
    int s, t;
    printf("Input two pos int for greatest common divisors:\n");
    scanf("%d%d", &s, &t);
    int m, n;
    s > t ? (m = s, n = t) : (m = t, n = s); // 保证m>=n
    int d = gcd(m, n);
    printf("The gcd is %d.\n", d);
    return 0;
}
```

## 2. 求一个输入正整数各个数位上的数字之和。

```
#include <stdio.h>
   int digit_sum(int m)
   // 递归求正整数各个数位上数字的和
      if(!m) // 上一次得到余数0
      {
         return 0;
      return digit_sum(m / 10) + m % 10;
   }
   int main()
  {
14
      printf("Input a pos int digit sum computation:\n");
16
      scanf("%d", &n);
      int s = digit_sum(n);
      printf("The digit sum of %d is %d.\n", n, s);
      return 0;
20
21 }
```

3. 输入一个字符串和一个字符,查找该字符在该字符串中第一次出现的位置并输出。如果该字符不出现,则输出不出现。

```
#include <stdio.h>
   char* search_for(char* s, char ch)
4 // 递归
   {
       if(!(*s)) return NULL;
       if(*s == ch) return s;
       return search_for(++s, ch);
   }
10
   int main()
12
   {
       char str[1024];
13
       printf("Input a string to be searched:\n");
       gets(str);
15
       printf("Input a char to be located:\n");
16
       char ch = getchar();
18
       char *p = search_for(str, ch);
19
       if(p)
          printf("1st occurence of '%c' found at %p, at index %d\n", ch, p, p - str);
22
       }
       else
       {
25
          printf("'%c' not found\n", ch);
       }
28
29
       return 0;
   }
```

4. Syracuse (也称为 "Collatz" 或 "Hailstone") 序列的生成从一个自然数开始, 重复应用以下函数, 直到达到 1:

$$syr(x) = \begin{cases} 3x+1, & \exists x$$
为奇数时;  $x \div 2, & \exists x$ 为偶数时。

例如,从 5 开始的 Syracuse 序列是 5,16,8,4,2,1。数学中有一个悬而未决的问题: 对于每个可能的起始值,该序列是否总会到达 1。编程从用户获取起始值,然后打印该起始值的 Syracuse 序列。

```
#include <stdio.h>
   void print_syracuse_sequence_from(int n)
       printf("%d\t", n);
       if(n == 1)
          return;
       if(n \% 2 == 0)
          print_syracuse_sequence_from(n / 2);
       else
14
       {
          print_syracuse_sequence_from(3 * n + 1);
   }
   int main()
   {
       int n;
       printf("Input a pos for a syracuse sequence:\n");
23
       scanf("%d", &n);
       print_syracuse_sequence_from(n);
       return 0;
26
27 }
```

5. 请求用户输入两个字符串, 然后按字典序比较两个字符串的先后。

```
#include <stdio.h>
```

```
int string_compare(char *s, char *t)
4 // 1 means t comes before
   // -1 means s comes before
   // 0 means equal
7 {
       if(!(*s) && !(*t)) return 0;
       if(!(*s)) return -1;
       if(!(*t)) return 1;
10
       if(*s > *t) return 1;
       if(*s < *t) return -1;</pre>
       return string_compare(++s, ++t);
14 }
16 int main()
17 {
       char s[1024], t[1024];
       printf("Input two strings for comparison:\n");
19
       gets(s);
20
       gets(t);
       int res = string_compare(s, t);
22
       if(res == 1)
          printf("%s comes before %s\n", t, s);
25
       else if(res == -1)
          printf("%s comes before %s\n", s, t);
29
       }
31
       else
       {
32
          printf("equal\n");
       }
       return 0;
```

6. 在数组中查找最大的元素。

```
#include <stdio.h>
```

```
#include inits.h>
4 int maximum(int *p, int n, int maxi)
5 // search a list of n element from p
   // and return the biggest one among maxi and those n elements
7 {
       if(n == 0) return maxi;
      if(maxi > *p)
10
          return maximum(++p, n - 1, maxi);
       }
       else
13
      {
          return maximum(++p, n - 1, *p);
16
17 }
19 int main()
20 {
      // int a[] = {1, 3, 7, 2, 4, 3, 2, 5};
       int a[] = {12, 43, 23, 87, 55, 24, 69, 77, 95, 34, 27};
22
       int m = maximum(a, sizeof(a) / sizeof(int), INT_MIN);
      printf("The greatest: %d\n", m);
      return 0;
25
26 }
```