

The result of calling `repr` on a value is what Python displays in an interactive session

The result of calling `str` on a value is what Python prints using the `print` function

```
>>> today = datetime.date(2019, 10, 13)
```

```
>>> repr(today) # or today.__repr__()
```

```
'datetime.date(2019, 10, 13)'
```

```
>>> str(today) # or today.__str__()
```

```
'2019-10-13'
```

The result of evaluating an f-string literal contains the str string of the value of each sub-expression.

```
f'pi starts with {pi}...'
```

```
'pi starts with 3.141592653589793...'
```

```
>>> print(f'pi starts with {pi}...')
```

```
pi starts with 3.141592653589793...
```

Lists:

```
>>> digits = [1, 8, 2, 8]
>>> len(digits)
4
>>> digits[3] digits |---> list
4
| 0 | 1 | 2 | 3
| 1 | 8 | 2 | 8
```

```
>>> [2, 7] + digits * 2
[2, 7, 1, 8, 2, 8, 1, 8, 2, 8]
```

```
>>> pairs = [[10, 20], [30, 40]]
>>> pairs[1] pairs |---> list
[30, 40]
| 0 | 1 | 0 | 1
| 10 | 20
```

Executing a for statement:

```
for <name> in <expression>:
```

```
    <suite>
```

1. Evaluate the header <expression>, which must yield an iterable value (a list, tuple, iterator, etc.)

2. For each element in that sequence, in order:

A. Bind <name> to that element in the current frame

B. Execute the <suite>

Unpacking in a for statement:

A sequence of fixed-length sequences

```
>>> pairs=[[1, 2], [2, 2], [3, 2], [4, 4]]
>>> same_count = 0
```

A name for each element in a fixed-length sequence

```
>>> for x, y in pairs:
...     if x == y:
...         same_count = same_count + 1
>>> same_count
2
```

..., -3, -2, -1, 0, 1, 2, 3, 4, ...
range(-2, 2)

Length: ending value – starting value

Element selection: starting value + index

```
>>> list(range(-2, 2)) List constructor
[-2, -1, 0, 1]
```

```
>>> list(range(4)) Range with a 0 starting value
[0, 1, 2, 3]
```

Membership: Slicing:

```
>>> digits = [1, 8, 2, 8] >>> digits[0:2]
```

```
>>> 2 in digits [1, 8]
```

```
True >>> digits[1:]
```

```
>>> 1828 not in digits [8, 2, 8]
```

```
True Slicing creates a new object
```

Identity:

`<exp0> is <exp1>`

evaluates to `True` if both `<exp0>` and `<exp1>` evaluate to the same object

Equality:

`<exp0> == <exp1>`

evaluates to `True` if both `<exp0>` and `<exp1>` evaluate to equal values

Identical objects are always equal values

```
iter(iterator): >>> s = [3, 4, 5] >>> d = {'one': 1, 'two': 2}
Return an iterator >>> t = iter(s) >>> k = iter(d)
over the elements >>> next(t) >>> next(k) >>> v = iter(d.values())
of an iterable value 3 >>> next(t) >>> next(k) 1
next(iterator): >>> next(t) >>> next(k) 2
Return the next 4 'two'
element of an iterator
```

A generator function is a function that yields values instead of returning.

```
>>> def plus_minus(x): >>> t = plus_minus(3) def a_then_b(a, b):
...     yield x >>> next(t) ...     yield a
...     yield -x >>> next(t) >>> list(a_then_b([3, 4], [5, 6]))
... -3 [3, 4, 5, 6]
```

List comprehensions:

[<map exp> for <name> in <iter exp> if <filter exp>]

Short version: [<map exp> for <name> in <iter exp>]

A combined expression that evaluates to a list using this evaluation procedure:

1. Add a new frame with the current frame as its parent
2. Create an empty `result list` that is the value of the expression
3. For each element in the iterable value of `<iter exp>`:
 - A. Bind `<name>` to that element in the new frame from step 1
 - B. If `<filter exp>` evaluates to a true value, then add the value of `<map exp>` to the result list

Dictionaries:

```
words = {
    "más": "more",
    "otro": "other",
    "agua": "water"
}
```

```
>>> len(words)
3
>>> "agua" in words
True
>>> words["otro"]
'otro'
>>> words["pavo"]
KeyError
>>> words.get("pavo", "☺")
'☺'
```

Dictionary comprehensions:

{key: value for <name> in <iter exp>}

```
>>> {x: x*x for x in range(3,6)}
{3: 9, 4: 16, 5: 25}
```

Functions that aggregate iterable arguments

- `sum(iterable[, start])` → value sum of all values
- `max(iterable[, key=func])` → value largest value
- `min(iterable[, key=func])` → value smallest value
- `min(a, b, c, ..., key=func)` → value
- `all(iterable)` → bool whether all are true
- `any(iterable)` → bool whether any is true

Many built-in Python sequence operations return iterators that compute results lazily

```
map(func, iterable):
    Iterate over func(x) for x in iterable
filter(func, iterable):
    Iterate over x in iterable if func(x)
zip(first_iter, second_iter):
    Iterate over co-indexed (x, y) pairs
reversed(sequence):
    Iterate over x in a sequence in reverse order
```

To view the contents of an iterator, place the resulting elements into a container

```
list(iterator):
    Create a list containing all x in iterable
tuple(iterator):
    Create a tuple containing all x in iterable
sorted(iterator):
    Create a sorted list containing x in iterable
```

```
def cascade(n):
    >>> cascade(123) n: 0, 1, 2, 3, 4, 5, 6, 7, 8,
    if n < 10: 123 virfib(n): 0, 1, 1, 2, 3, 5, 8, 13, 21,
        print(n) 12
    else:
        print(n) 123
        cascade(n//10)
        print(n) def virfib(n):
            if n == 0:
                return 0
            elif n == 1:
                return 1
            else:
                return virfib(n-2) + virfib(n-1)
```

Exponential growth. E.g., recursive fib

$\Theta(b^n)$ $O(b^n)$

Incrementing n multiplies time by a constant

Quadratic growth. E.g., overlap

$\Theta(n^2)$ $O(n^2)$

Incrementing n increases time by n times a constant

Linear growth. E.g., slow exp

$\Theta(n)$ $O(n)$

Incrementing n increases time by a constant

Logarithmic growth. E.g., exp_fast

$\Theta(\log n)$ $O(\log n)$

Doubling n only increments time by a constant

Constant growth. Increasing n doesn't affect time

$\Theta(1)$ $O(1)$

Global frame

```
make_withdraw_list withdraw
f1: make_withdraw_list withdraw
withdraw doesn't reassigned any name within the parent
balance 100
b 75
Return value
```

```
f2: withdraw withdraw
amount 25
b 75
Return value
```

List mutation:

```
>>> a = [10] >>> a = [10]
>>> b = a >>> b = [10]
>>> a == b >>> a == b
True True
True
>>> a.append(20) >>> b.append(20)
>>> a == b [10, 20]
True
>>> a [10, 20]
>>> b [10, 20]
False
```

You can copy a list by calling the list constructor or slicing the list from the beginning to the end.

```
>>> a = [10, 20, 30]
>>> list(a)
[10, 20, 30]
>>> a[:] [10, 20, 30]
```

Tuples:

```
>>> empty = ()
>>> len(empty)
0
>>> conditions = ('rain', 'shine')
>>> conditions[0]
'rain'
>>> conditions[0] = 'fog'
Error
```

```
>>> all([False, True]) >>> any([False, True])
False True
>>> all([])
True
>>> sum([1, 2])
2
>>> sum([1, 2], 3)
2
>>> sum([])
2
>>> max([1, 2])
2
>>> max([1, 2], 3)
2
>>> max([1, -2], key=abs)
0
>>> sum([[1], [2]], [])
[1, 2]
```

List methods:

```
>>> suits = ['coin', 'string', 'myriad']
>>> suits.pop() Remove and return the last element
'myriad'
>>> suits.remove('string') Removes first matching value
>>> suits.append('cup') Add all values
>>> suits.extend(['sword', 'club']) Replace a slice with values
>>> suits[2] = 'spade' Add an element at an index
>>> suits
['coin', 'cup', 'spade', 'club']
>>> suits[0:2] = ['diamond'] Replace a slice with values
>>> suits
['diamond', 'spade', 'club']
>>> suits.insert(0, 'heart') Add an element at an index
>>> suits
['heart', 'diamond', 'spade', 'club']
```

False values:

```
>>> bool(0) False
>>> bool(1) True
>>> bool(None) False
>>> bool("") False
>>> bool('') True
>>> bool('0') False
>>> bool([]) False
>>> bool([[]]) True
>>> bool({}) False
>>> bool({{}}) True
>>> bool(lambda x: 0) True
```

```
func make_withdraw_list(balance) [parent=Global]
make_withdraw_list withdraw
f1: make_withdraw_list withdraw
withdraw doesn't reassigned any name within the parent
balance 100
b 75
Return value
func withdraw(amount) [parent=f1]
withdraw
amount 25
b 75
Return value
def make_withdraw_list(balance):
    b = [balance]
    def withdraw(amount):
        if amount > b[0]:
            return 'Insufficient funds'
        b[0] = b[0] - amount
        return withdraw
    return withdraw
withdraw = make_withdraw_list(100)
withdraw(25)
```

- Recursive description:**
- A tree has a root label and a list of branches
 - Each branch is a tree
 - A tree with zero branches is called a leaf
- Relative description:**
- Each location is a node
 - Each node has a label
 - One node can be the parent/child of another

```
def tree(label, branches=[]):
    for branch in branches:
        assert is_tree(branch)
    return [label] + list(branches)

def label(tree):
    return tree[0]

def branches(tree):
    return tree[1:]

def is_tree(tree):
    if type(tree) != list or len(tree) < 1:
        return False
    for branch in branches(tree):
        if not is_tree(branch):
            return False
    return True

def is_leaf(tree):
    return not branches(tree)

def leaves(t):
    """The leaf values in t."""
    if is_leaf(t):
        return [label(t)]
    else:
        return sum([leaves(b) for b in branches(t)], [])

class Tree:
    def __init__(self, label, branches=[]):
        self.label = label
        for branch in branches:
            assert is_instance(branch, Tree)
        self.branches = list(branches)

    def is_leaf(self):
        return not self.branches
```

```
>>> b = Tree(2, [Tree(3)])
>>> t = Tree(1, [b, Tree(4)])
>>> t
Tree(1, [Tree(2, [Tree(3)]), Tree(4)])
>>> print(t)
1
  2
    3
    4
```

```
class Link:
    """Some zero length sequence"""
    empty = ()  

    def __init__(self, first, rest=empty):
        self.first = first
        self.rest = rest

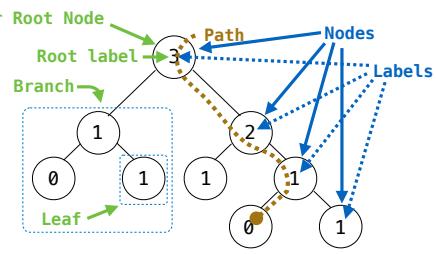
    def __repr__(self):
        if self.rest:
            rest = ', ' + repr(self.rest)
        else:
            rest = ''
        return 'Link(' + repr(self.first) + rest + ')'

    def __str__(self):
        string = '('
        while self.rest is not Link.empty:
            string += str(self.first) + ' '
            self = self.rest
        return string + str(self.first) + ')'
```

Anatomy of a recursive function:

- The **def statement header** is like any function
- Conditional statements check for **base cases**
- Base cases are evaluated **without recursive calls**
- Recursive cases are evaluated **with recursive calls**

- Recursive decomposition:** finding simpler instances of a problem.
- E.g., count_partitions(6, 4)
 - Explore two possibilities:
 - Use at least one 4
 - Don't use any 4
 - Solve two simpler problems:
 - count_partitions(2, 4)
 - count_partitions(6, 3)
 - Tree recursion often involves exploring different choices.



Python object system:
Idea: All bank accounts have a **balance** and an account **holder**; the **Account** class should add those attributes to each of its instances

```
>>> a = Account('Jim')
>>> a.holder
'Jim'
>>> a.balance
0
```

When a class is called:
1. A new instance of that class is created:
2. The `__init__` method of the class is called with the new object as its first argument (named `self`), along with any additional arguments provided in the call expression.

```
class Account:
    def __init__(self, account_holder):
        self.balance = 0
        self.holder = account_holder
    def deposit(self, amount):
        self.balance = self.balance + amount
        return self.balance
    def withdraw(self, amount):
        if amount > self.balance:
            return 'Insufficient funds'
        self.balance = self.balance - amount
        return self.balance
```

`__init__` is called a constructor
self should always be bound to an instance of the Account class or a subclass of Account
Function call: all arguments within parentheses
Method invocation: One object before the dot and other arguments within parentheses
Dot expression
Call expression

The `<expression>` can be any valid Python expression.
The `<name>` must be a simple name.
Evaluates to the value of the attribute looked up by `<name>` in the object that is the value of the `<expression>`.

To evaluate a dot expression:

1. Evaluate the `<expression>` to the left of the dot, which yields the object of the dot expression
2. `<name>` is matched against the instance attributes of that object; if an attribute with that name exists, its value is returned
3. If not, `<name>` is looked up in the class, which yields a class attribute value
4. That value is returned unless it is a function, in which case a bound method is returned instead

Assignment statements with a dot expression on their left-hand side affect attributes for the object of that dot expression

- If the object is an instance, then assignment sets an instance attribute
- If the object is a class, then assignment sets a class attribute

Account class attributes	interest: 0.02 0.04 0.05 (withdraw, deposit, __init__)
Instance attributes of jim_account	balance: 0 holder: 'Jim' interest: 0.08
Instance attributes of tom_account	balance: 0 holder: 'Tom'

```
>>> jim_account = Account('Jim')
>>> tom_account = Account('Tom')
>>> tom_account.interest
0.02
>>> jim_account.interest
0.02
>>> Account.interest = 0.04
>>> tom_account.interest
0.04
>>> jim_account.interest
0.04
```

```
class CheckingAccount(Account):
    """A bank account that charges for withdrawals."""
    withdraw_fee = 1
    interest = 0.01
    def withdraw(self, amount):
        return Account.withdraw(self, amount + self.withdraw_fee)
        ↑
        or
        return super().withdraw(amount + self.withdraw_fee)
```

To look up a name in a class:

1. If it names an attribute in the class, return the attribute value.
2. Otherwise, look up the name in the base class, if there is one.

```
>>> ch = CheckingAccount('Tom') # Calls Account.__init__
>>> ch.interest # Found in CheckingAccount
0.01
>>> ch.deposit(20) # Found in Account
20
>>> ch.withdraw(5) # Found in CheckingAccount
14
```