

opg. 1

$$\frac{\rho[x \mapsto t_x. f \mapsto t_x \rightarrow int] \mapsto 1 : int}{\frac{\rho \mapsto f : (\alpha \rightarrow int) \rightarrow int \quad \rho \mapsto f : \alpha}{\rho[f \mapsto \forall \alpha. t_x \rightarrow int]} \quad \alpha \text{ not free in } \rho} \text{ let f x = 1 in f f end}$$

opg. 2

$$\frac{\frac{\rho \vdash x < 10 : \text{bool} \quad \rho \vdash 42 : \text{int}}{\rho \vdash x < 10 : \text{bool}} \quad \frac{\frac{\frac{p(f) = V_a 1 \dots a n \cdot \text{int}}{\rho \vdash : \text{int} \rightarrow t_r} \quad \frac{\rho \vdash : \text{int} \quad \rho \vdash 1 : \text{int}}{\rho \vdash x+1 : t_x}}{\rho \vdash f(x+1) : t_r}}{\frac{\rho[x \mapsto t_x, f \mapsto t_x \mapsto t_r] \vdash \text{if } x < 10 \text{ then } 42 \text{ else } f(x+1)}{\text{let f x = if } x < 10 \text{ then } 42 \text{ else } f(x+1) \text{ in f 20 end}} \quad \rho$$