

Accreting BH Timescales

NPR, Andy Lawrence, Chelsea MacLeod, Alastair Bruce

March 13, 2019

Abstract

A list of Accreting BH timescales, and how they scale with e.g. M_{BH} . (See also “General_Physical_terms” and “Xray Terminology”).

1 Accreting BH timescales

General notes: a $1 \times 10^8 M_{\odot}$ has a Schwarzschild Radius of $R_{\text{Schwarz}} = 2.954 \times 10^8 \text{ km}$.

And 1 AU is $1.496 \times 10^8 \text{ km}$.

Light travel time across this R_S is 984.77 seconds.

1.1 Light crossing

The light crossing timescale; variations in light output cannot occur on timescales less than this.

1.2 Dynamical

The shortest characteristic timescale of the disc is the dynamical timescale.

1.3 Sound

The general sound crossing timescale. Sound speed, given as:

$$c_s = \left(\frac{dP}{d\rho} \right)_0^{1/2}. \quad (1)$$

. $\gamma = 5/3$ is adiabatic, while $\gamma = 1$ is isothermal. with (from e.g. FKR2002) both c_s^{ad} and c_s^{iso} the order of the mean thermal speed of the ions of the gas,

$$c_s \approx 10(T/10^4 K)^{1/2} \text{ km s}^{-1} \quad (2)$$

Timescale	Equation	Ref
light crossing	$t_{\text{lt}} = R/c$ $\geq 2GM/c^3$ $= 0.98 \times 10^{-5} (M/M_{\odot}) \text{ secs}$ $= 980 \text{ seconds (for the } 1e8 M_{\odot} \text{ given above ;-)}$	FKR2002, Eqn (7.4)

Table 1: Light Crossing timescale; variations in light output cannot occur on timescales less than this.

Timescale	Equation	Ref
dynamical	$t_{\text{dyn}} = \sqrt{R^3/c}$ $\sim R/v_\phi$ $t_\phi \sim \Omega_K^{-1}$	FKR2002, Eqn (5.63)

Table 2: The shortest characteristic timescale of the disc is the dynamical timescale.

Timescale	Equation	Ref
Sound	$t_{\text{snd}} = R/c_s$	

Table 3: Light Crossing timescale; large variations in light output cannot occur on timescales less than this.

1.4 Thermal

From e.g. FKR2002, the *thermal timescale*:

$$t_{th} = \frac{\text{heat content per unit disc area}}{\text{dissipation rate per unit disc area}}. \quad (3)$$

i.e. a timescale for an “energy spike” to dissipate within disc.
where \mathcal{M} is Mach number, v/c_s .

1.5 Viscous

Croom et al. (2004)

Timescale	Equation	Ref
Thermal	$t_{\text{th}} = \mathcal{M}/t_{\text{visc}}$	FKR2002

Table 4: Time for an “energy spike” to dissipate within the disc.

Timescale	Equation	Ref
Viscous	$t_{\text{visc}} = R^2/\nu$	FKR2002

Table 5: where ν is *kinematic viscosity*. This is the “diffusion through disc” timescale from viscous torques.

Quasars have a whole lotta timescales

AGN Structure	physical size	angular size	t_{lt}	t_{dyn}	t_{snd}	t_{therm}
Inner disc	$5 R_S$	$0.1\mu\text{as}$	1.4hrs	4.3hrs	1.3 yrs	18.7days
Optical disc	$50 R_S$	$1\mu\text{as}$	14hrs	5.7days	23 yrs	1.6yrs
Broad Line Region	$1000 R_S$	$20\mu\text{as}$	11days	1.4yrs	800 yrs	–
Obscuring Region	$10^5 R_S$	2mas	3.1yrs	1.4kyrs	350 kyrs	–

for a $10^8 M_\odot$ black hole at 100 Mpc

- t_{lt} : light crossing timescale, $t_{lt} \sim R/c$
- t_{dyn} : dynamical timescale, $t_{dyn} \sim \sqrt{(R^3/GM)}$
- t_{snd} : sound crossing timescale, $t_{snd} = R/v_{snd}$
- t_{therm} : ‘energy spike’ to dissipate within the disc

e.g. Lawrence, 2016, *ASPC*, **505**, 107

Figure 1

Table 6: Timescales and how the scale with M , R , T etc.

Name	Scaling
Viscous	M^α

2 Time Scales

From Lawrence (2016) <http://adsabs.harvard.edu/abs/2016ASPC..505..107L> ::

All Type I AGN - those where we can see the strong blue continuum and broad emission lines - are variable.¹ This is important because variability can provide indirect information on size scales that are otherwise unmeasurable. Suppose, for illustration, we take an AGN at a distance of 100 Mpc, and we assume that it contains a black hole of mass $10^8 M_\odot$. The Table below shows the angular scale of well known AGN structures, in units of the Schwarzschild radius $R_S = 2GM/c^2$. The accretion disc, Broad Line Region (BLR) and the geometrically thick obscuring region sometimes known as the “torus” are all unresolvable by direct means, although as we will describe later, may be mappable by microlensing transits.

If the accretion disc is in a stable steady state, we might expect it to evolve gradually on the inward drift timescale set by viscosity, which is of the order 10,000 years (see e.g. ?). However, instabilities of various kinds could give us much faster changes. The *light crossing timescale* $t_{lt} = R/c$, is the shortest timescale that we could possibly see, if for example one region has variations locked to those of another region by radiation heating or reflection. This is of the order hours, days, and years for disc, BLR, and torus respectively. The *dynamical timescale*, $t_{dyn} = \sqrt{R^3/GM}$, is the shortest timescale on which we are likely to see physical changes in a region, and is of the order of days, years, and thousands of years for disc, BLR, and torus respectively. (Free-fall time is roughly the same and orbital timescale is 2π times longer.) More realistically, perturbations may transmit across a region on the sound crossing timescale $t_{snd} = R/v_{snd}$. This is somewhat model dependent but is of the order of years for the accretion disc. Note what I mean here is the global time to cross the whole region. Local hot spots could grow on the timescale it takes sound to cross the vertical height of the disc, which could be 1–3 orders of magnitude faster. Somewhat related is the “thermal” timescale t_{therm} which is roughly the time it takes for energy to dissipate within the disc, i.e. it is a kind of response timescale to a spike of energy input. This is model dependent of course, but some standard formulae are given in ? and ?. It is of the order of days for the inner disc and years for the optical disc. The analogous “response” timescale for the BLR and for the obscuring region is actually the light-crossing time - the local response time to a change in photo-ionisation or heating is very short, but what we see is smeared out by the range of light travel delays.

AGN Structure	physical size	angular size	t_{lt}	t_{dyn}	t_{snd}	t_{therm}
Inner disc	$5 R_S$	$0.1 \mu\text{as}$	1.4hrs	4.3hrs	1.3 yrs	18.7days
Optical disc	$50 R_S$	$1 \mu\text{as}$	14hrs	5.7days	23 yrs	1.6yrs
Broad Line Region	$1000 R_S$	$20 \mu\text{as}$	11days	1.4yrs	800 yrs	–
Obscuring Region	$10^5 R_S$	2mas	3.1yrs	1.4kyrs	350 kyrs	–

Are these timescales relevant to what we actually see? The UV continuum changes on timescales of weeks², with an RMS of around $\pm 30\%$, which means trough-to-peak changes of up to a factor of two are not unusual. The variations in the optical continuum, BLR, and IR seem to track these variations with roughly the light-travel time delays suggested in the Table, together with a similar amount of smearing (see recent examples in ?, ?, and Koshida (2014)). This strongly suggests that almost all the changes we see on the relevant timescales represent reprocessed emission driven by changes in the very central regions. The conventional explanation for many years has been that the driving power is from the X-ray source (e.g. ?), but in many cases this does not work in either energy budget or correlation terms (see Lawrence (2012) and references therein). A good alternative for the driving power is the (unseen) EUV peak of the very inner accretion disc.

The amplitude we see in the optical continuum on these \sim week timescales (around 3% RMS) is much smaller than that seen in the UV variations, which suggests that a very blue variable component mixes with an unchanging, or slower changing, redder component. Lawrence (2012) argues that this variable reprocessor is a system of dense inner clouds surrounding the disc, rather than the disc itself.

The variations seen in the UV, which the optical and BLR emission track, seem to follow a red-noise or random-walk like pattern, increasing in amplitude to longer timescales, flattening at a characteristic timescale of the order tens of days. This timescale depends on the mass of the black hole (Collier and Peterson 2001). This characteristic

¹For simplicity, I am only going to talk about the UVOIR spectral region, ignoring X-rays.

²Here I am assuming an Seyfert-like object appropriate to our $10^8 M_\odot$ example.

timescale seems to match the thermal timescale of the inner disc, suggesting that variability is driven by some unknown stochastic process, filtered by the physical response of the disc (??).

Note that the changes we see in broad emission lines are also of the order weeks, tracking the changes in the UV photo-ionising source. This is much shorter than the dynamical timescale of the BLR, and means we are not seeing structural changes in this region. In the popular "local optimally emitting cloud (LOC)" models we will be lighting up different pre-existing clouds at different distances as the UV goes up and down (??), which is why the amplitude of line variations (the "responsivity") varies with line species - Ly α has a large amplitude and Mg II hardly varies at all (e.g. ?). However, it is possible that on longer timescales we *will* see BLR structural changes - a point we will return to in section 5.3.

From Aneta Siemiginowska's talk::

Light crossing time at $100 r_s$:

$$t_{lc} = 1.1 M_8 R_{100r_s} \text{ days} \quad (4)$$

Orbital::

$$t_{orb} = 104 M_8 (R_{100r_s})^{3/2} \text{ days} \quad (5)$$

Thermal (note the viscosity dependence)

$$t_{th} = 4.6 (\alpha_{0.01})^{-1} M_8 (R_{100r_s})^{3/2} \text{ years} \quad (6)$$

$$\begin{aligned} r_s &= 2 GM_{bh}/c^2 \\ R_{100r_s} &= R/100r_s \\ M_8 &= M_{bh}/10^8 M_\odot. \end{aligned}$$

Note::

$$\Rightarrow t_{th} \sim (h/r)^2 t_{visc} \quad (7)$$

Timescale		Equation	Baseline	Range	Ref
Apocenter	apo	v_{radial}/g $75v_{1000} \cdot R_{1000} 2M8 \text{ d}$			Elvis17 Elvis17
Cloud crossing	cc				
Cloud crushing	ccr				
Cooling time	cool				Elvis17
Dynamical	dyn	$(R^3/GM)^{1/2}$ $P_{\text{orb}}/2\pi$ $1.4 R_{1000}^{3/2} M_8 \text{ yr}$			Elvis17 Elvis17 Elvis17
Escape	esc	v_{esc}/g $(v_{\text{esc}}/v_{\text{Kep}}) \cdot \tau_{\text{dyn}}$ $1.4\tau_{\text{dyn}} \text{ s}$			Elvis17
Light Crossing	lc	$1.1 M_8 R_{100r_S} \text{ days}$ R/c			SiemUSVI17 Lawrence16
Orbital	orb	$104 M_8 (R_{100r_S})^{3/2} \text{ days}$			SiemUSVI17
Sound crossing	sound	R/v_{snd}			
Thermal	th	$4.6 (\alpha_{0.01})^{-1} M_8 (R_{100r_S})^{3/2} \text{ years}$ $\sim (h/r)^2 t_{\text{visc}}$			SiemUSVI17 SiemUSVI17
Viscous	visc	$12.6 \text{ yr } L_E^{-3/10} M_8^{6/5} R_{30}^{5/4} \alpha_{0.1}^{-4.5} \mu_{0.1}^{3/10}$			Lawrence12
X-ray	X				

Table 7: SiemUSVI17 is Aneta Siemiginowska’s talk in the USVI Extreme AGN 2017 meeting.

Where:

α is the viscosity parameter;

$cs = (\gamma k_B T / \mu m_H^{1/2}) = 150 T_6^{1/2} \text{ km s}^{-1}$

g is the local acceleration due to gravity, GM/R^2 ;

G is the gravitational constant;

k_B is Boltzmann’s constant = $1.38 \times 10^{-16} \text{ erg K}^{-1}$;

$L/LEdd$ is the Eddington ratio;

$L_{bol, 44}$ is the ultraviolet bolometric luminosity in units of 1044 erg s^{-1} ;

\mathcal{M} is the Mach number;

M is the mass of the black hole in solar masses;

M_8 is M in units of 10^8 solar masses;

m_H is the mass of the hydrogen atom = $1.67 \times 10^{-24} \text{ g}$;

μ is the efficiency parameter;

P_{orb} is the orbital period in s;

R is the distance from the central black hole in cm;

R_{1000} is R in units of 1000 Schwarzschild radii, $rg = 2GM/c^2$;

$ri, 13$ is ri the initial radius of a condensing cloud in units of 1013 cm;

rc is the radius of the condensed cloud, = $ri \chi^{1/3}$, for a density ratio of χ ; i.e. 0.22χ for a density ratio of 100; (double check this!!!)

$T_{i,6}$ is the initial temperature of the wind in units of 106 K;

v_{1000} = initial radial WA velocity in units of 1000 km s⁻¹;

$v_{\text{esc}} = (2GM/R)^{1/2}$ is the escape velocity from radius Z/Z is gas metallicity relative to solar (section 2.1);

Λ is the cooling coefficient (erg s⁻¹ cm³) ;

$\Lambda_b(T)$ is the cooling coefficient for bremsstrahlung;

$\Lambda(T)/\Lambda_b$ is the factor increase in the cooling coefficient in a thermal plasma due to line cooling over bremsstrahlung at solar metallicity, which has values of ~ 35 for $T = 105 - 106 \text{ K}$, 100 for $T = 104.5 \text{ K}$, and peaks at ~ 500 for $T = 10^{5-5.5} \text{ K}$;

γ is the ideal gas adiabatic index = $5/3$;

μ is the mean molecular weight of the gas (~ 0.6); and

χ is the ratio of the cloud density to the ambient medium density.

References

Croom S. M., Smith R. J., Boyle B. J., Shanks T., Miller L., Outram P. J., Loaring N. S., 2004, MNRAS, 349, 1397

Koshida S. o., 2014, ApJ, 788, 159

Lawrence A., 2012, MNRAS, 423, 451