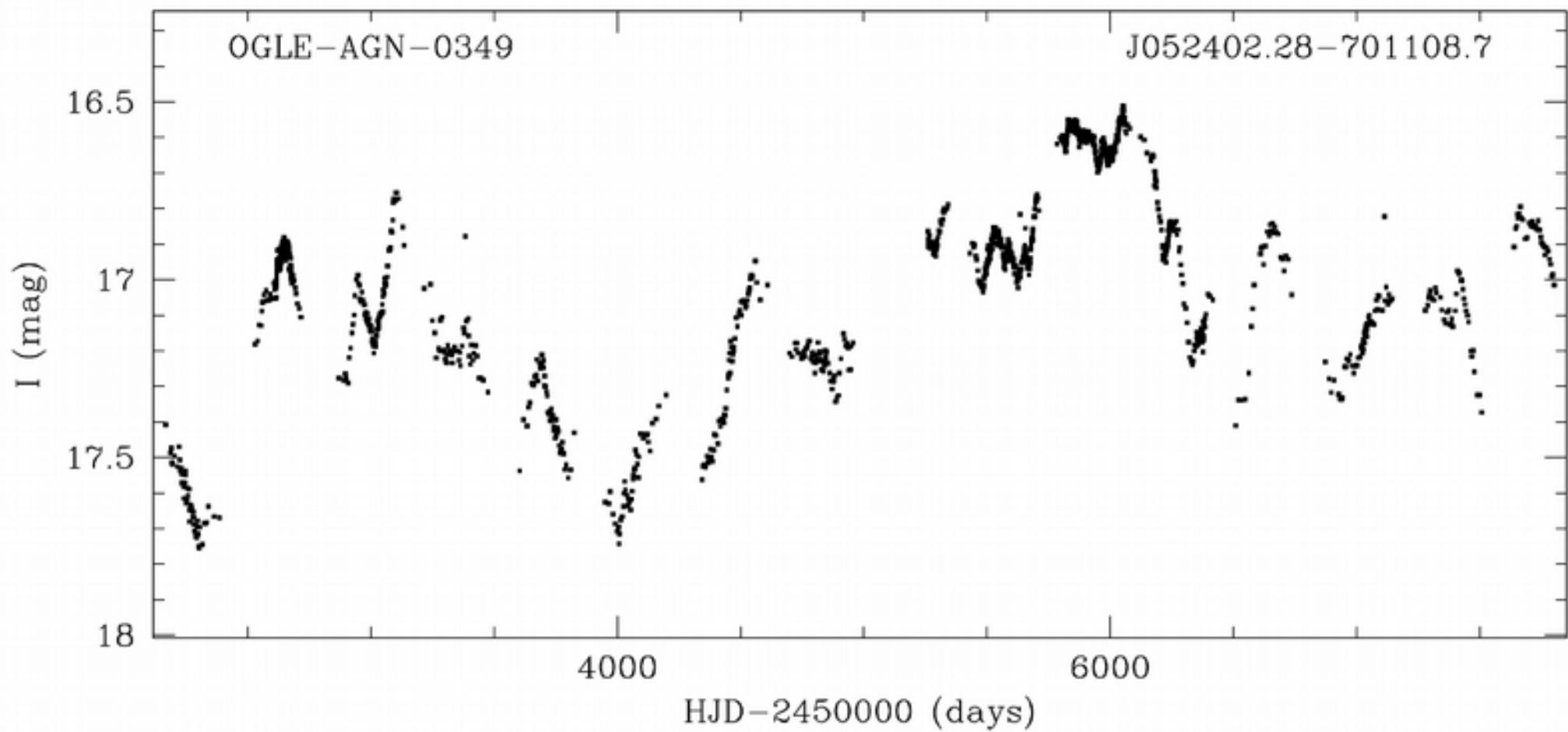


# Optical Variability of AGN

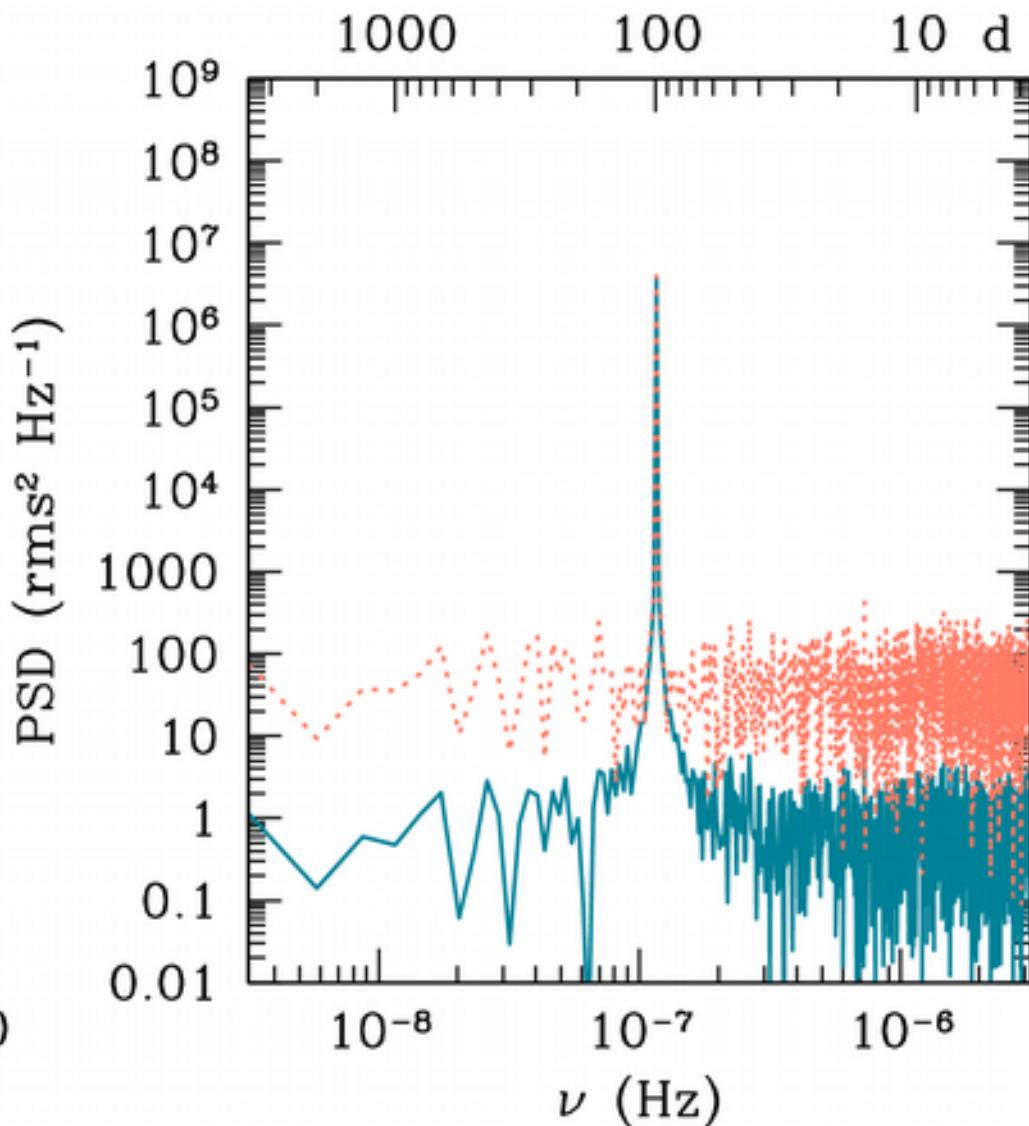
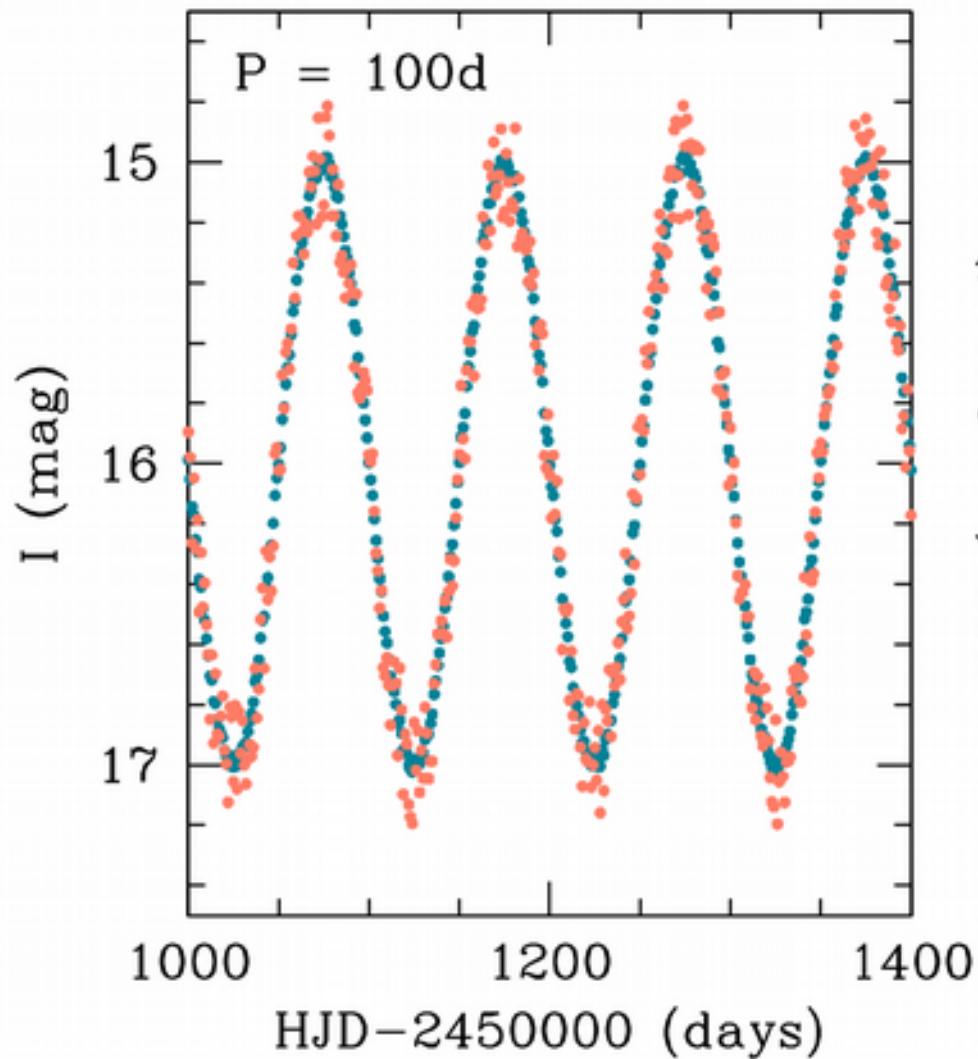
Szymon Kozłowski

Unveiling the Physics Behind Extreme AGN Variability  
10-14 July 2017

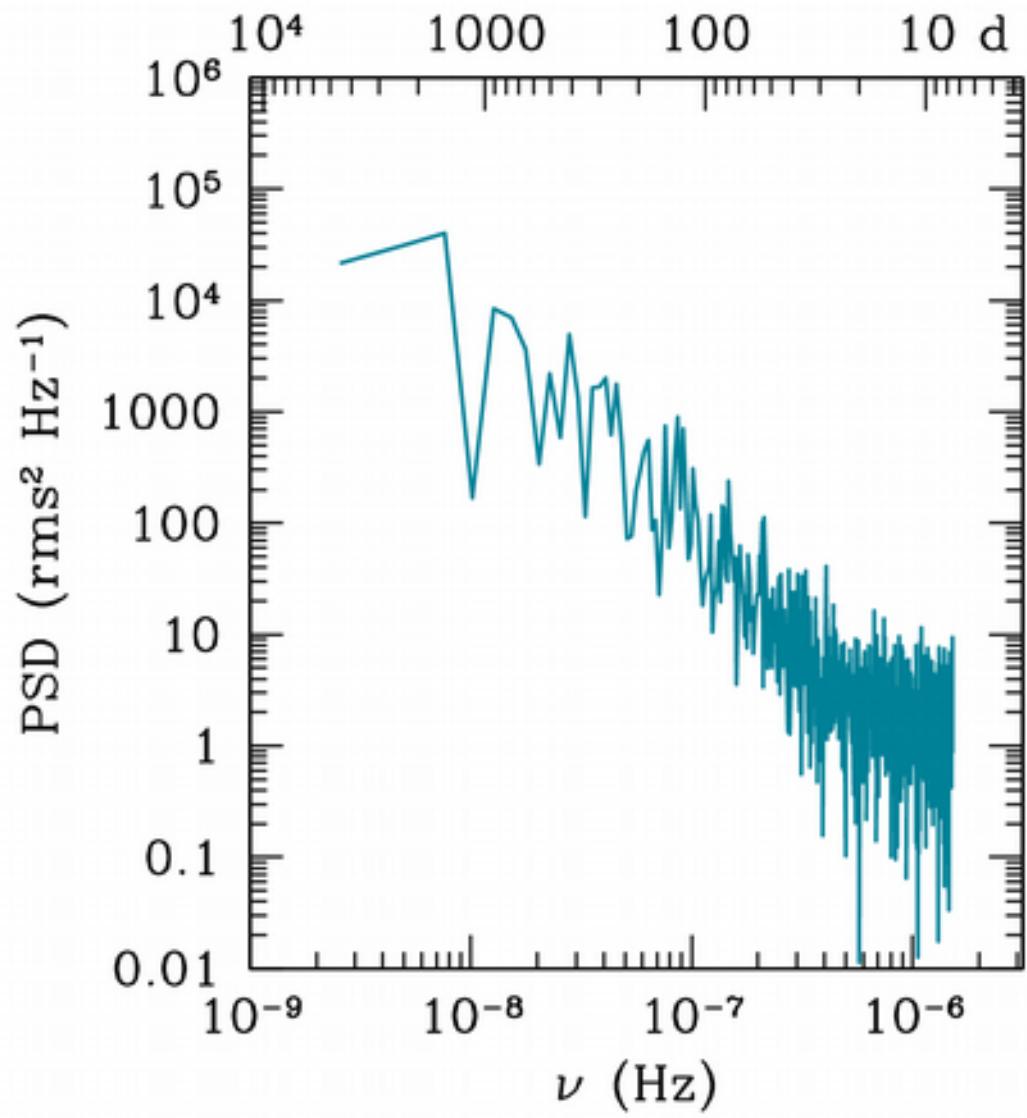
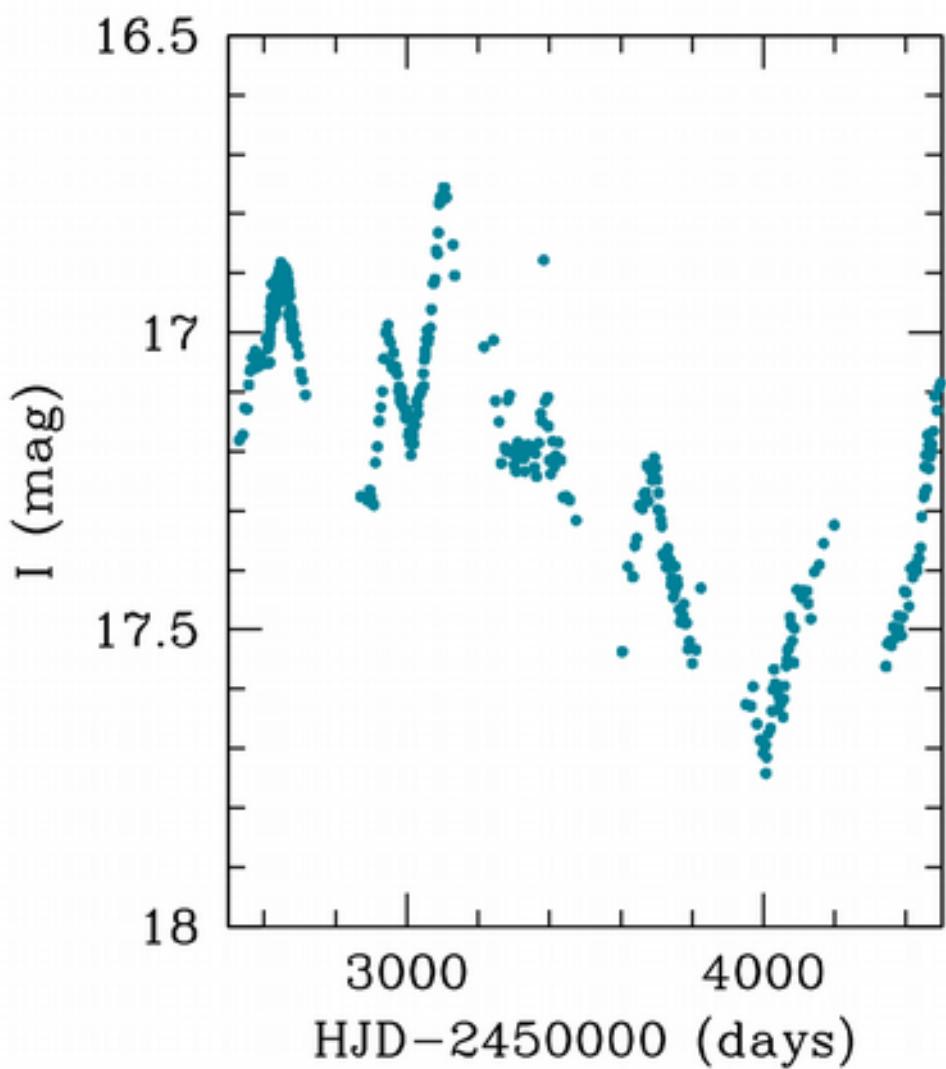
# Quasar Variability



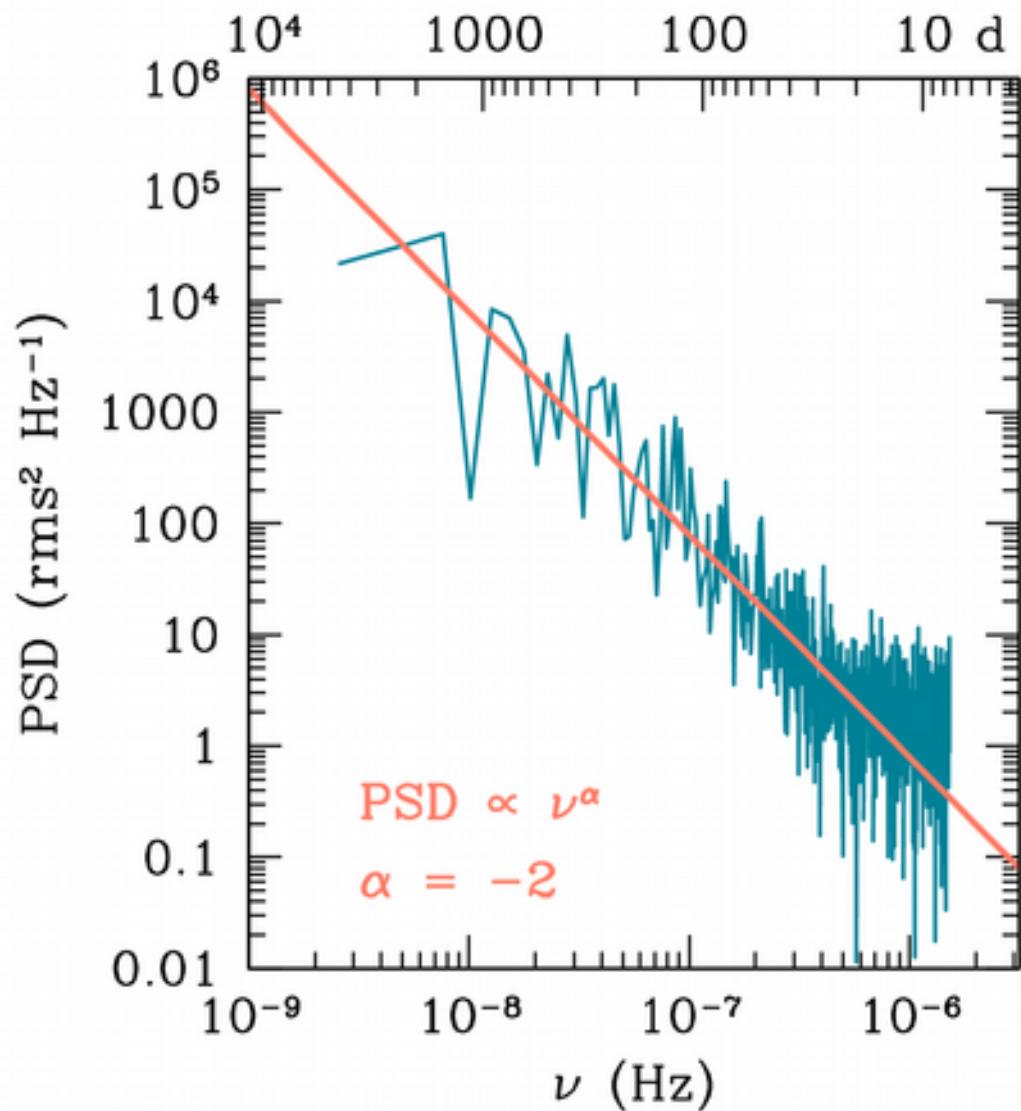
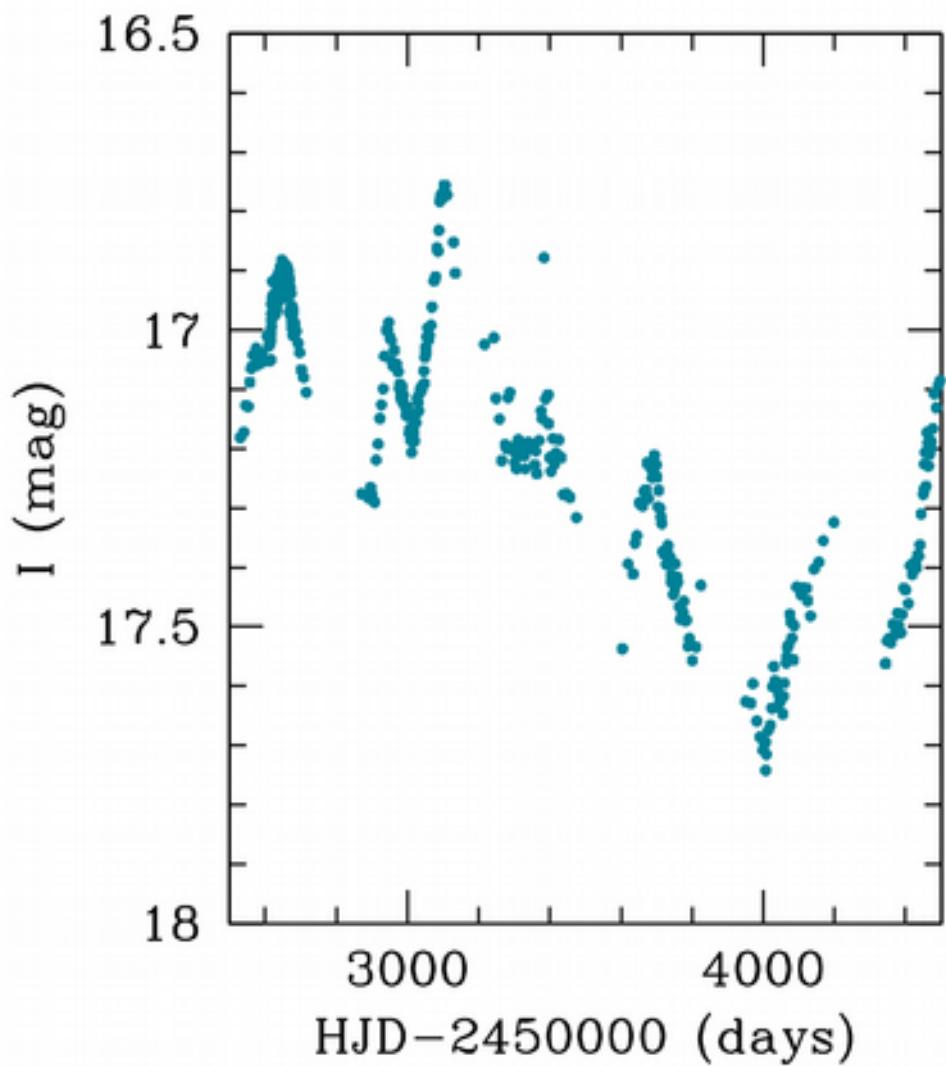
# PERIODIC OBJECT



# NON-PERIODIC OBJECT



# NON-PERIODIC OBJECT



# **Power Spectral Density (PSD)**

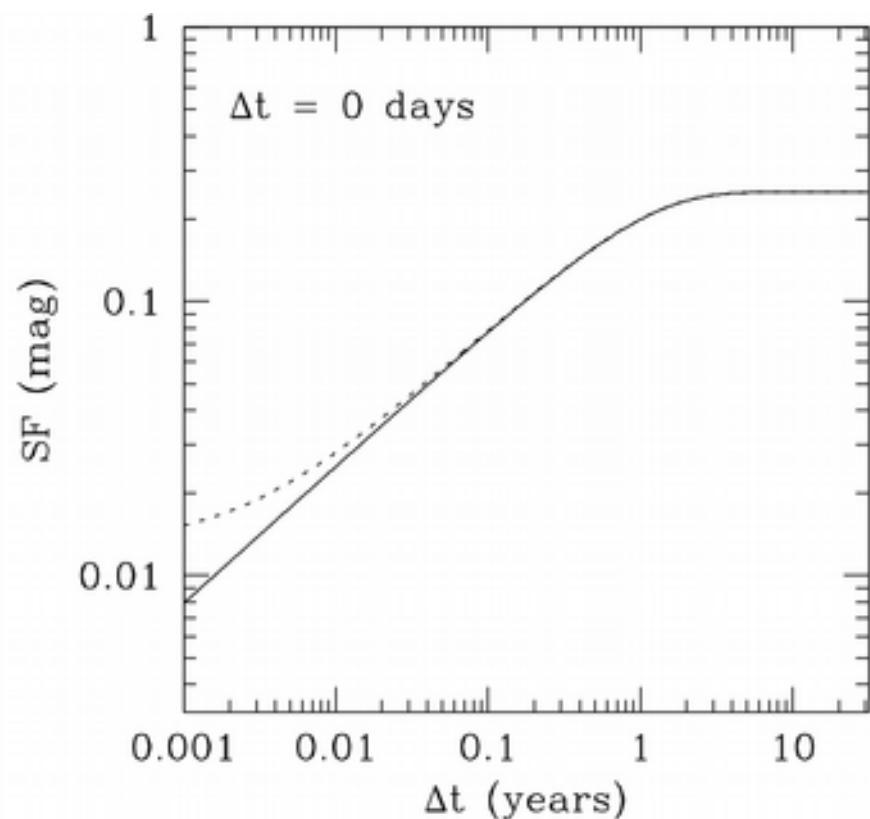
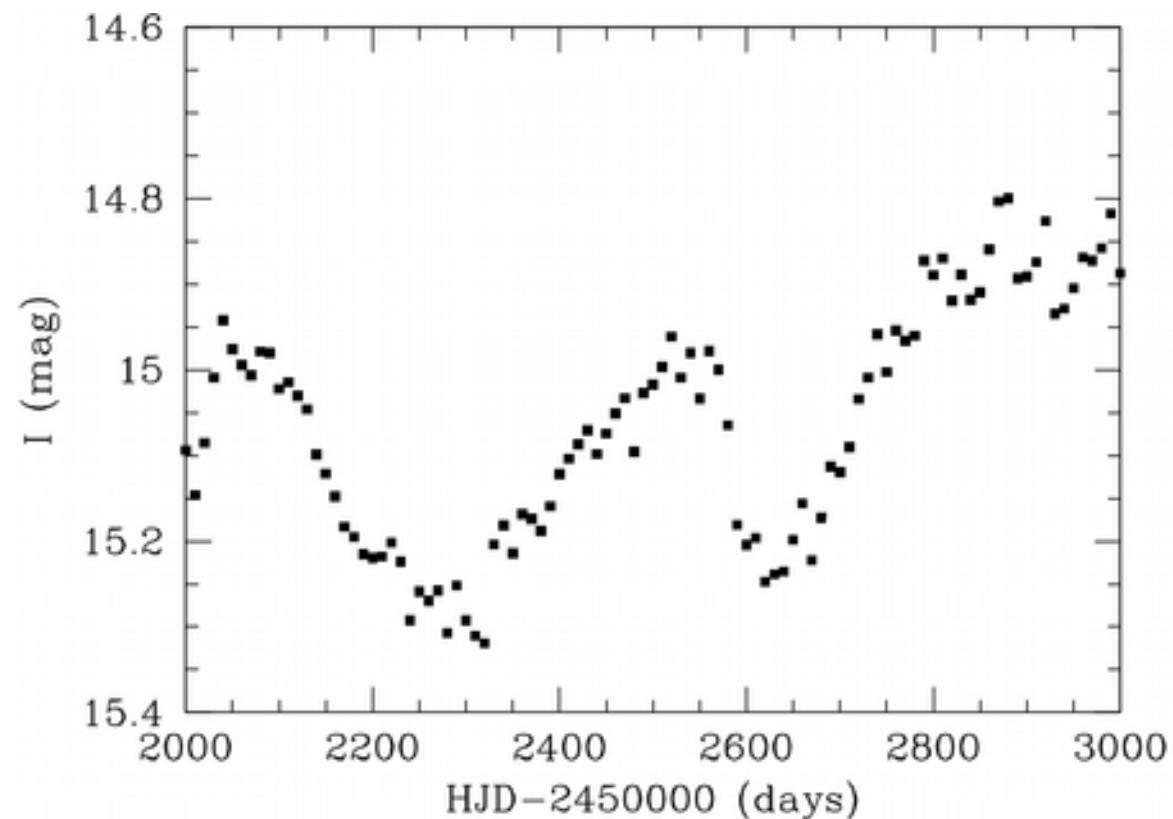
and

# **Auto-Correlation Function (ACF)**

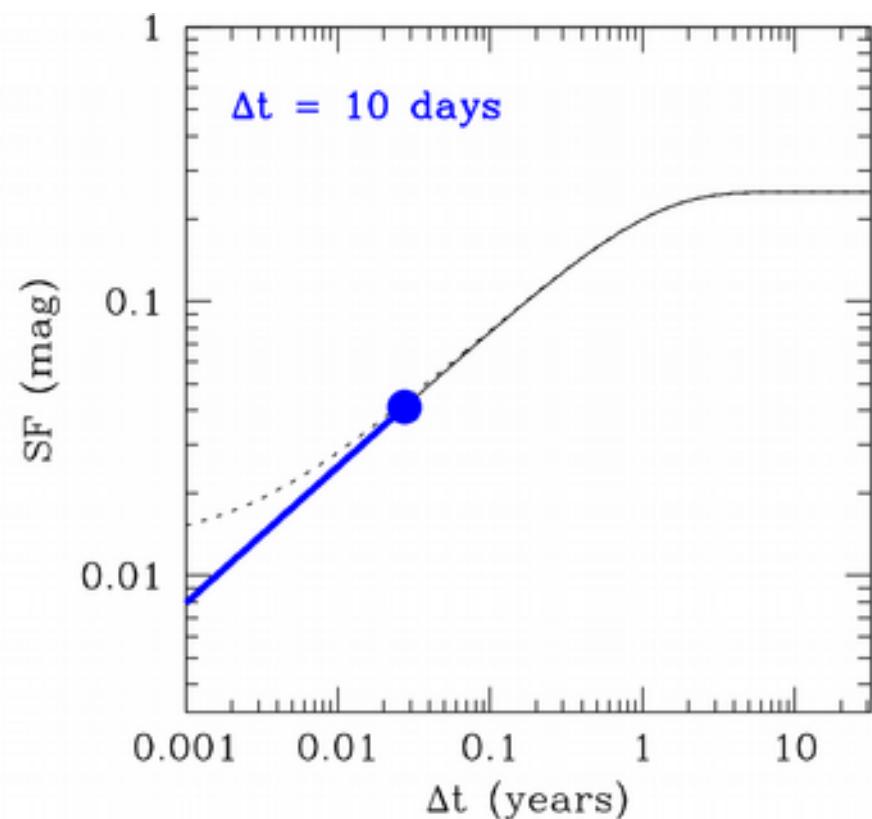
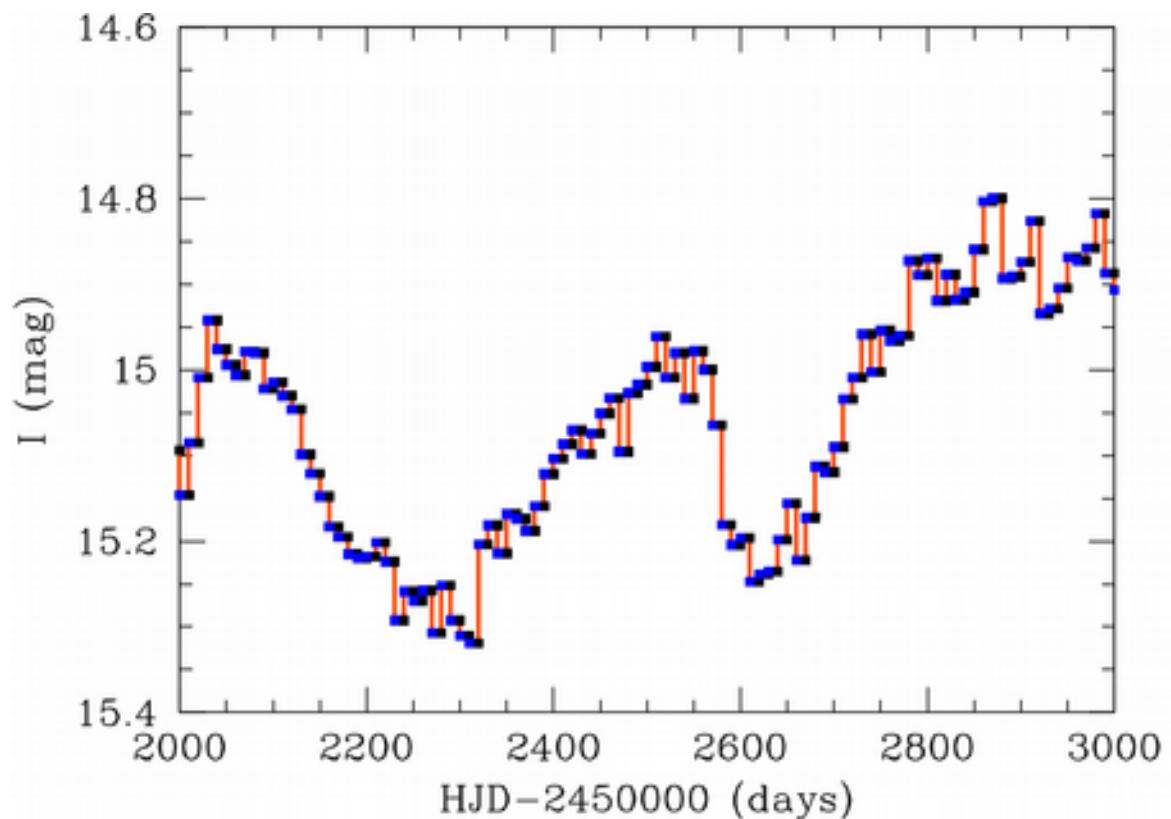
$$\text{PSD}(\nu) = \int_{-\infty}^{\infty} \text{ACF}(t) e^{-2\pi i \nu t} dt$$

$$\text{ACF}(t) = \int_{-\infty}^{\infty} \text{PSD}(\nu) e^{2\pi i \nu t} d\nu$$

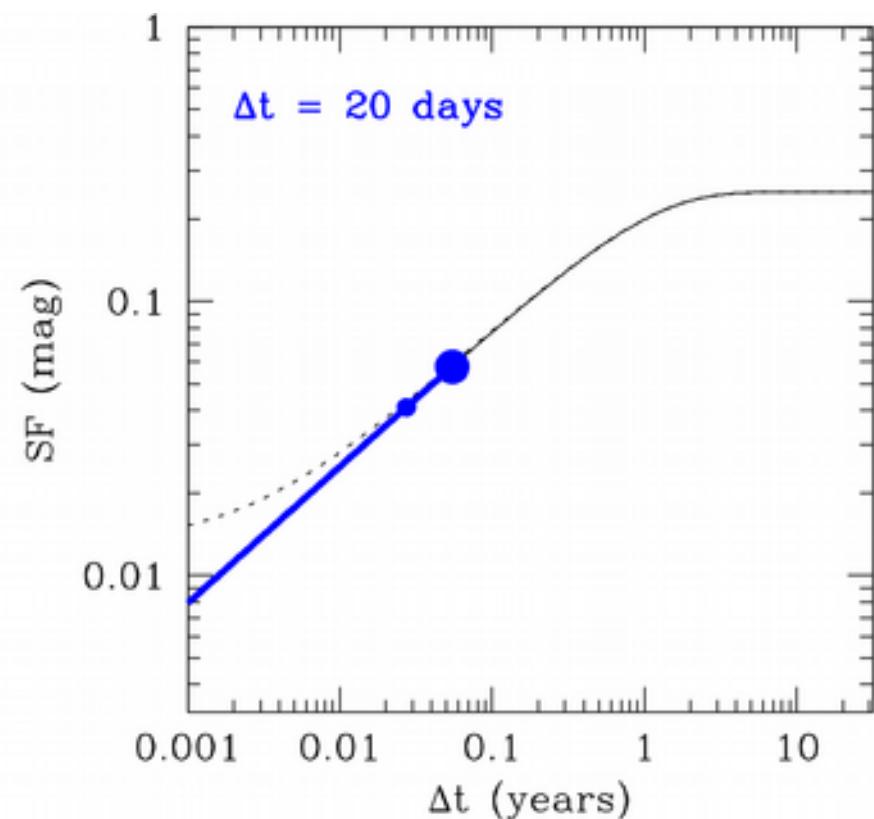
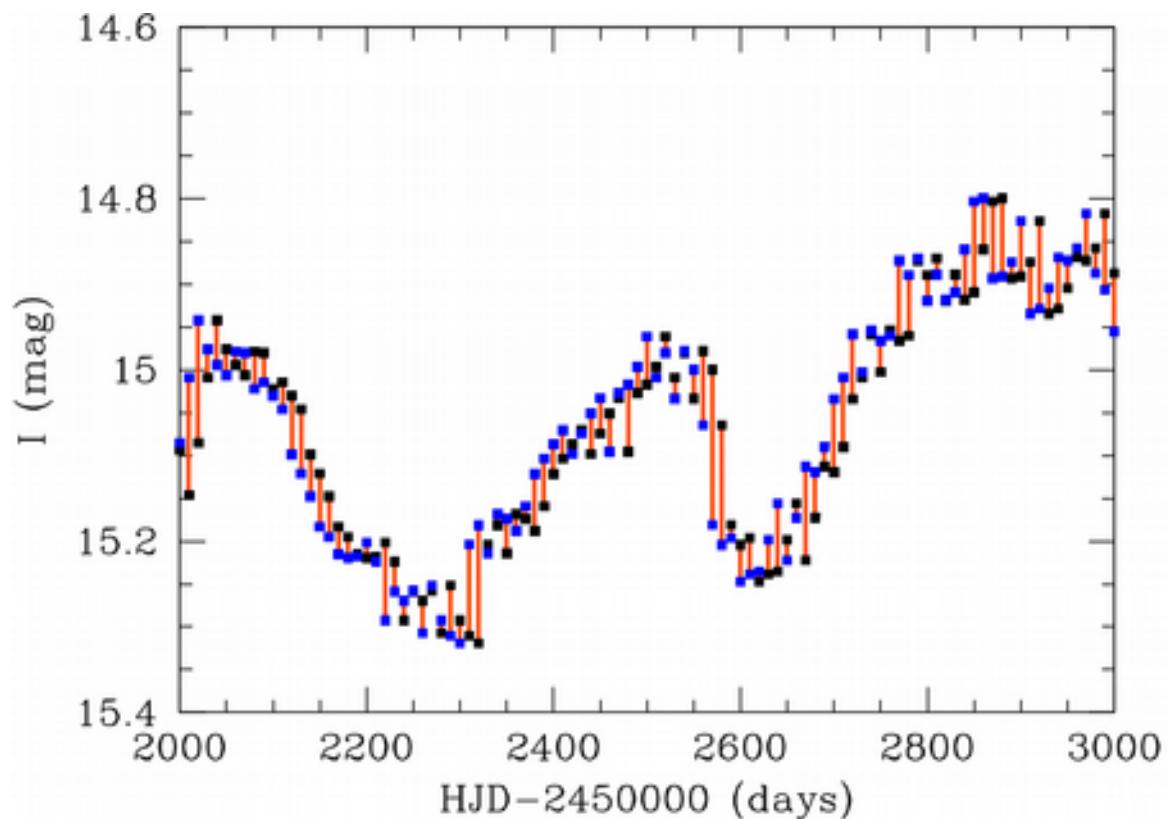
# Structure Function



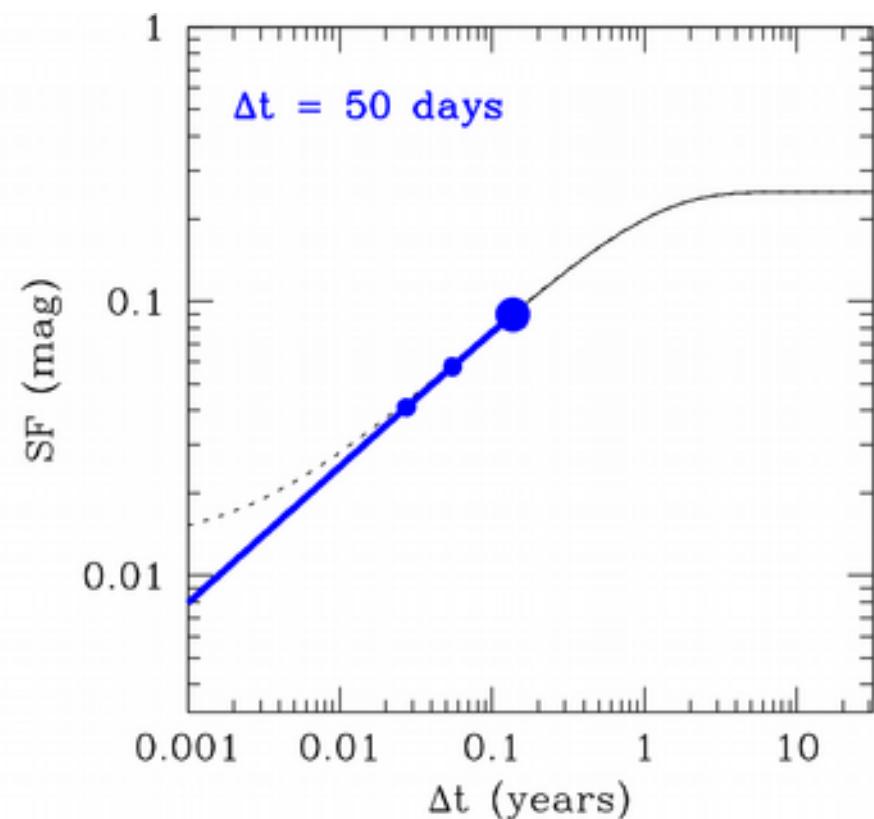
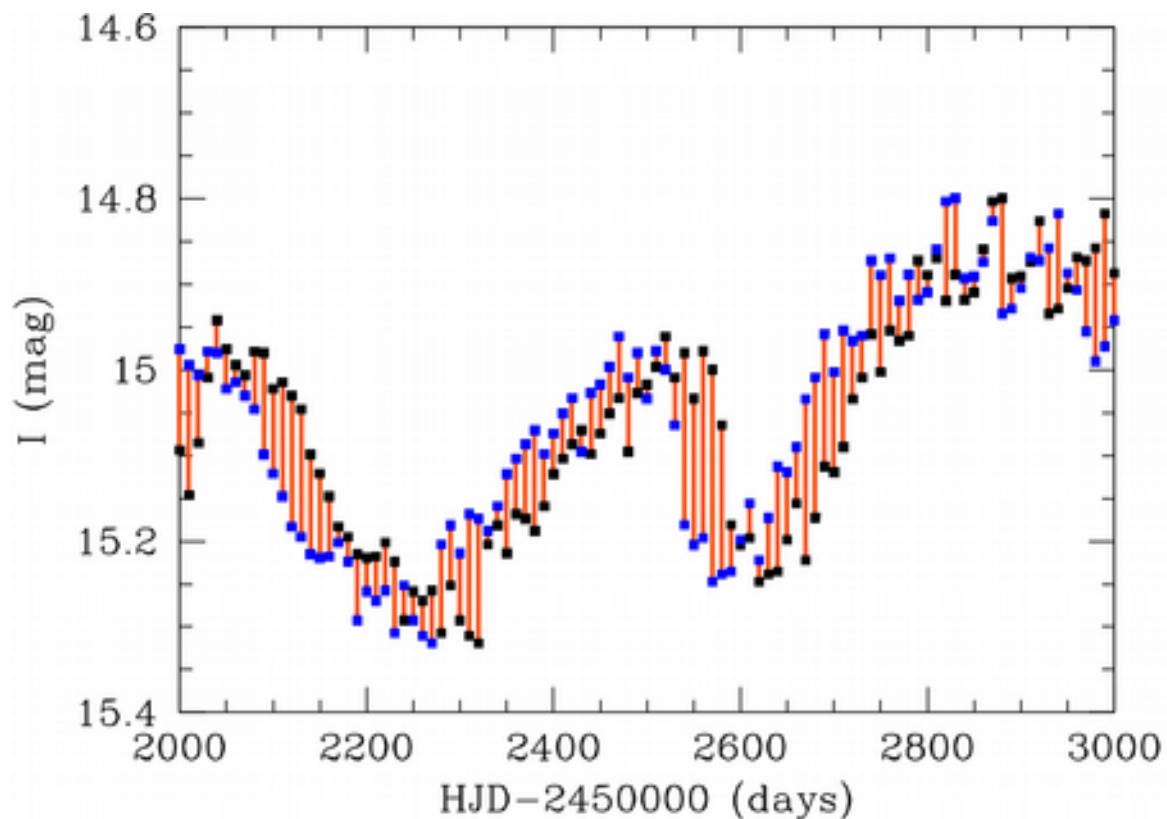
# Structure Function



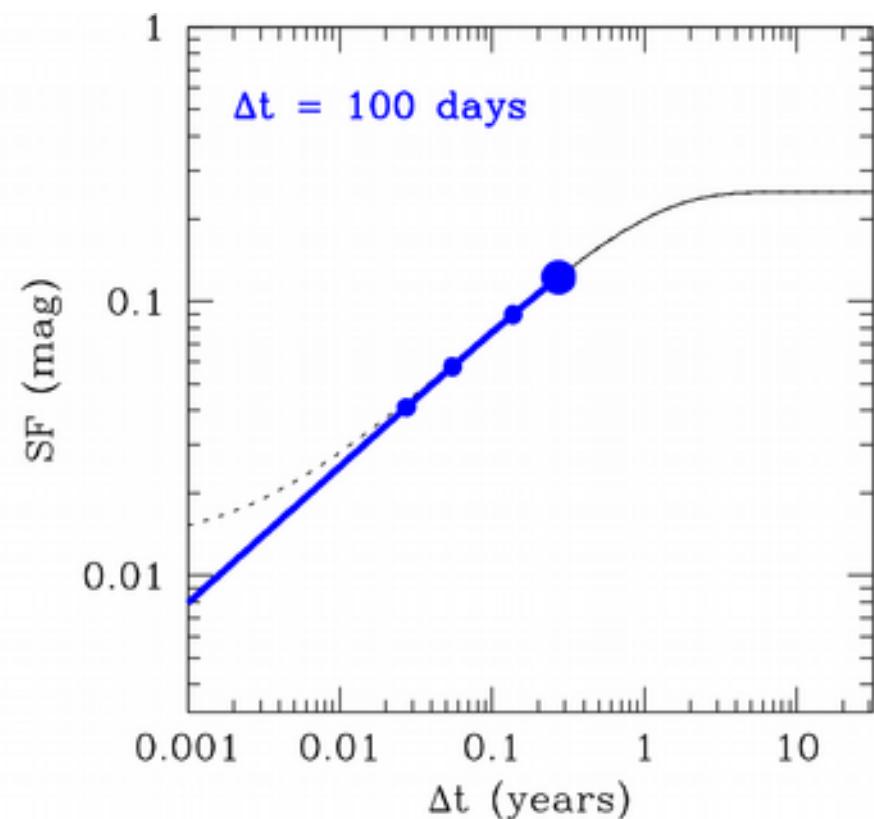
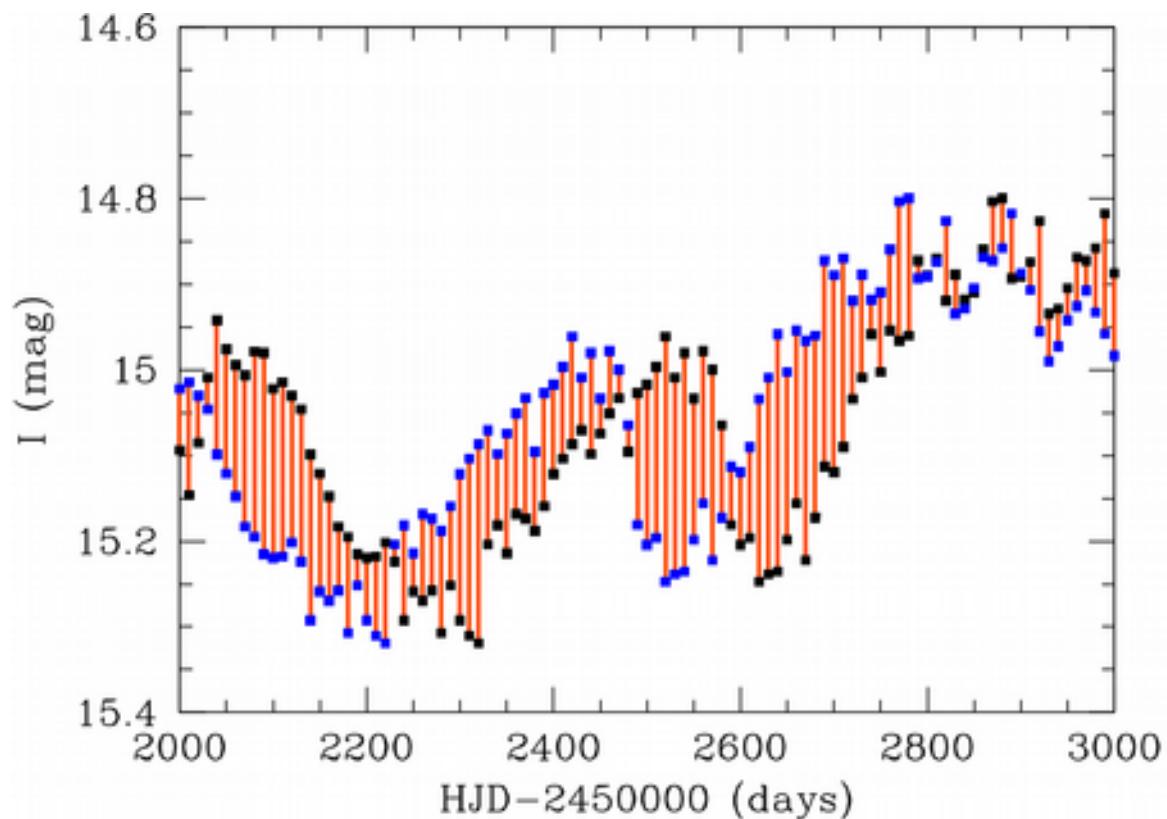
# Structure Function



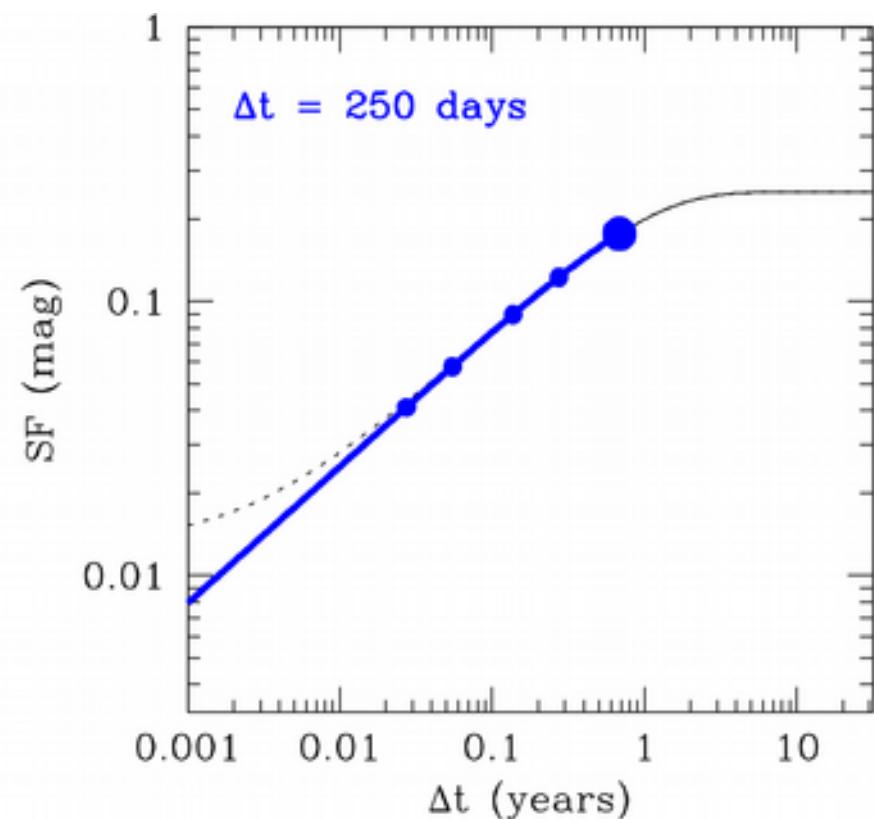
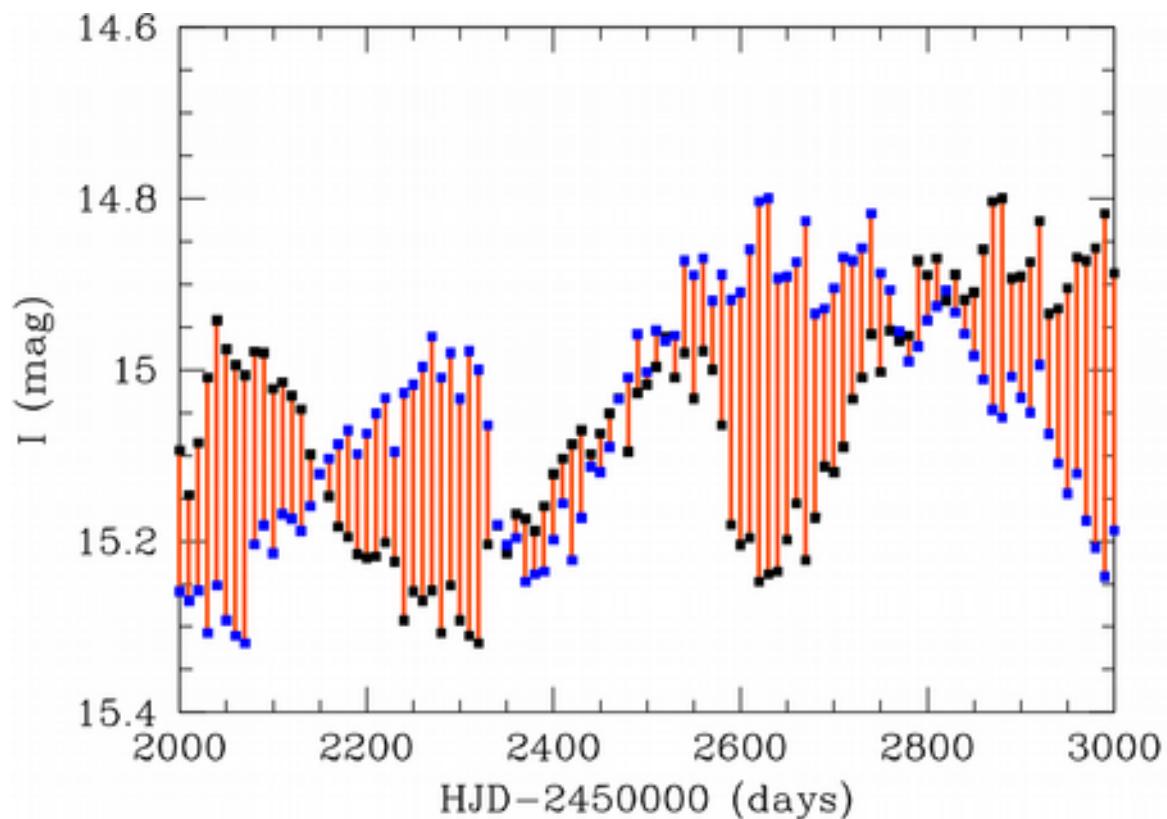
# Structure Function



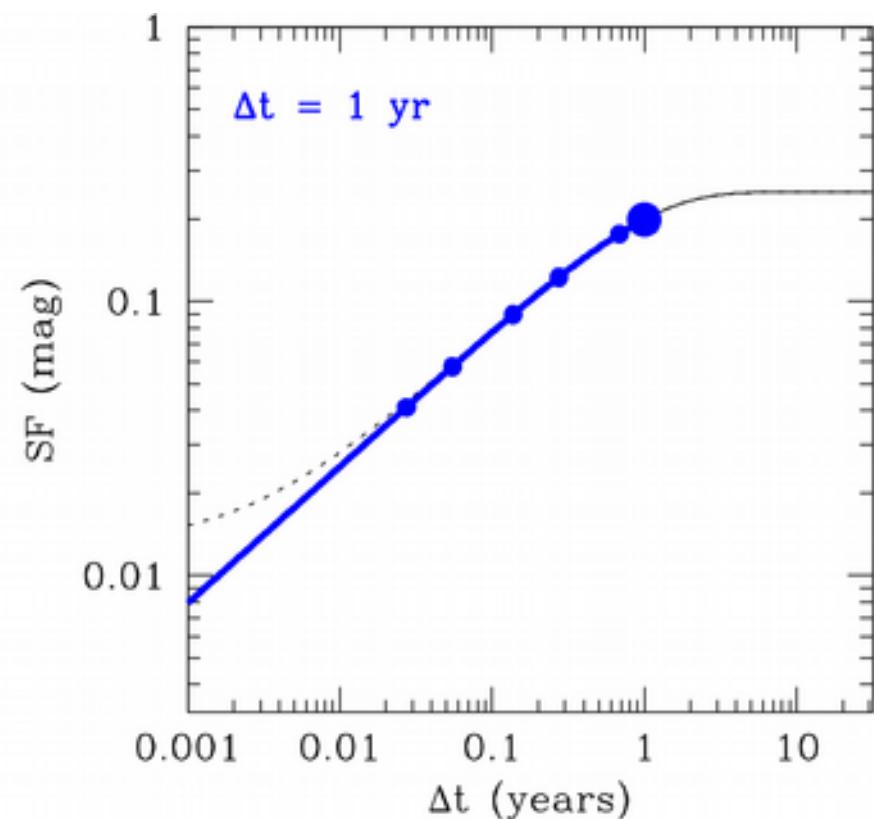
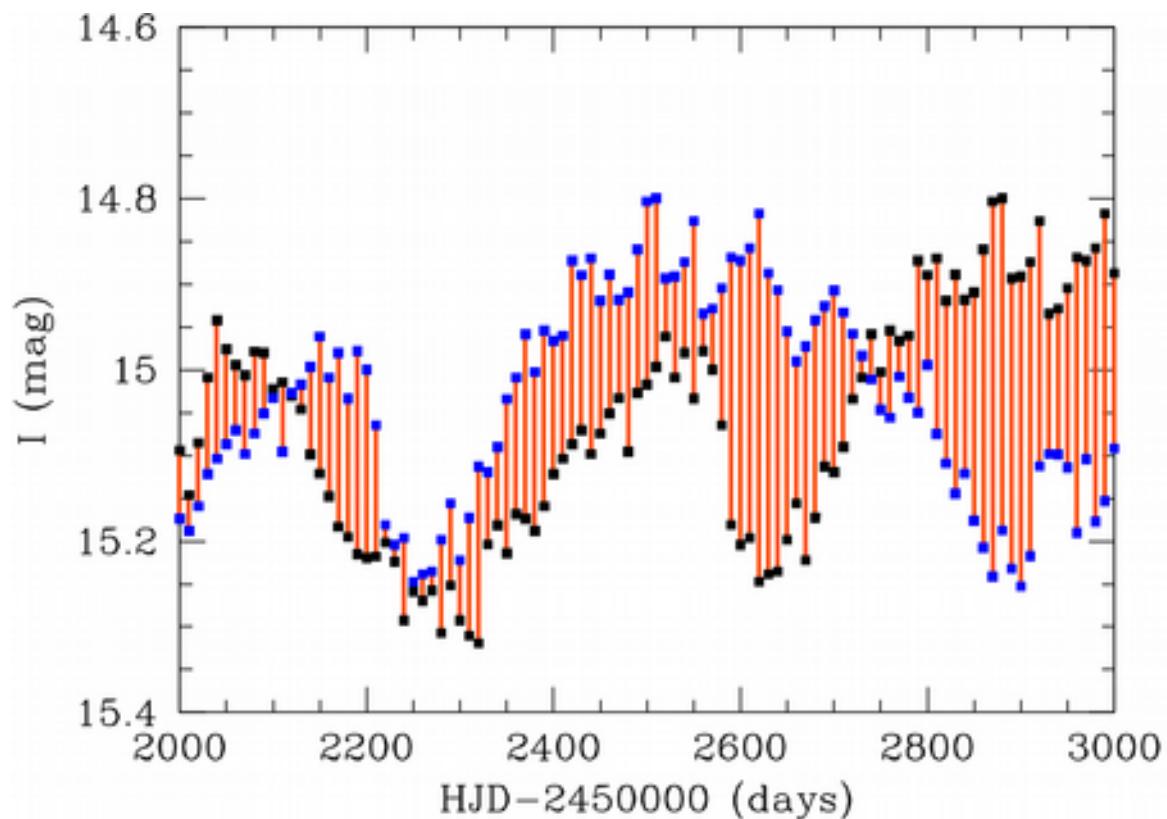
# Structure Function



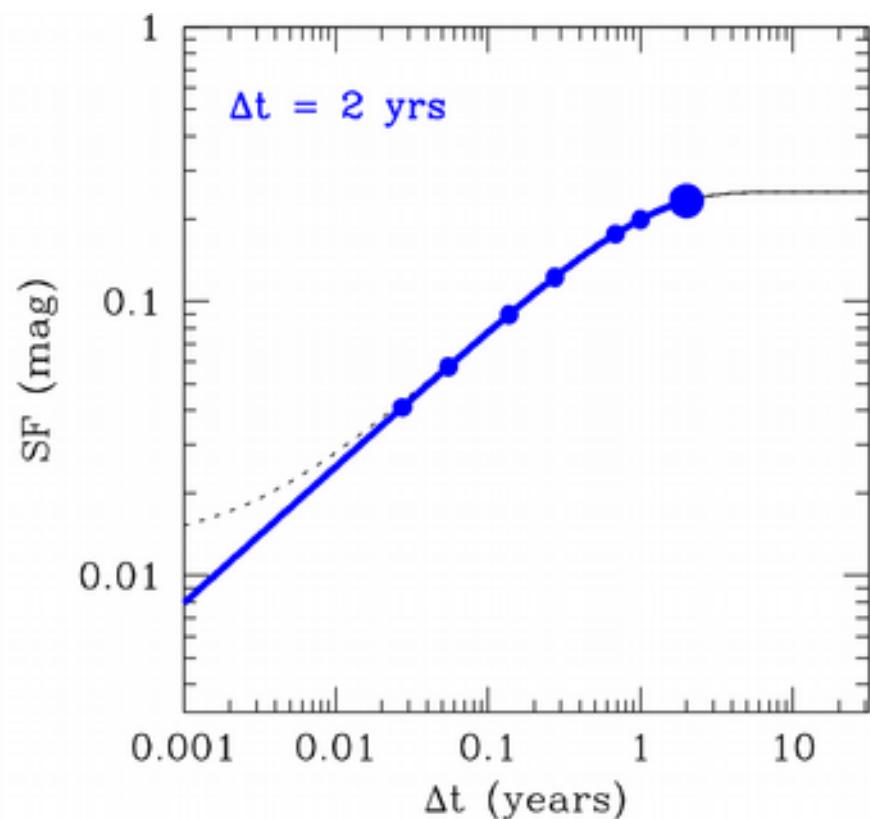
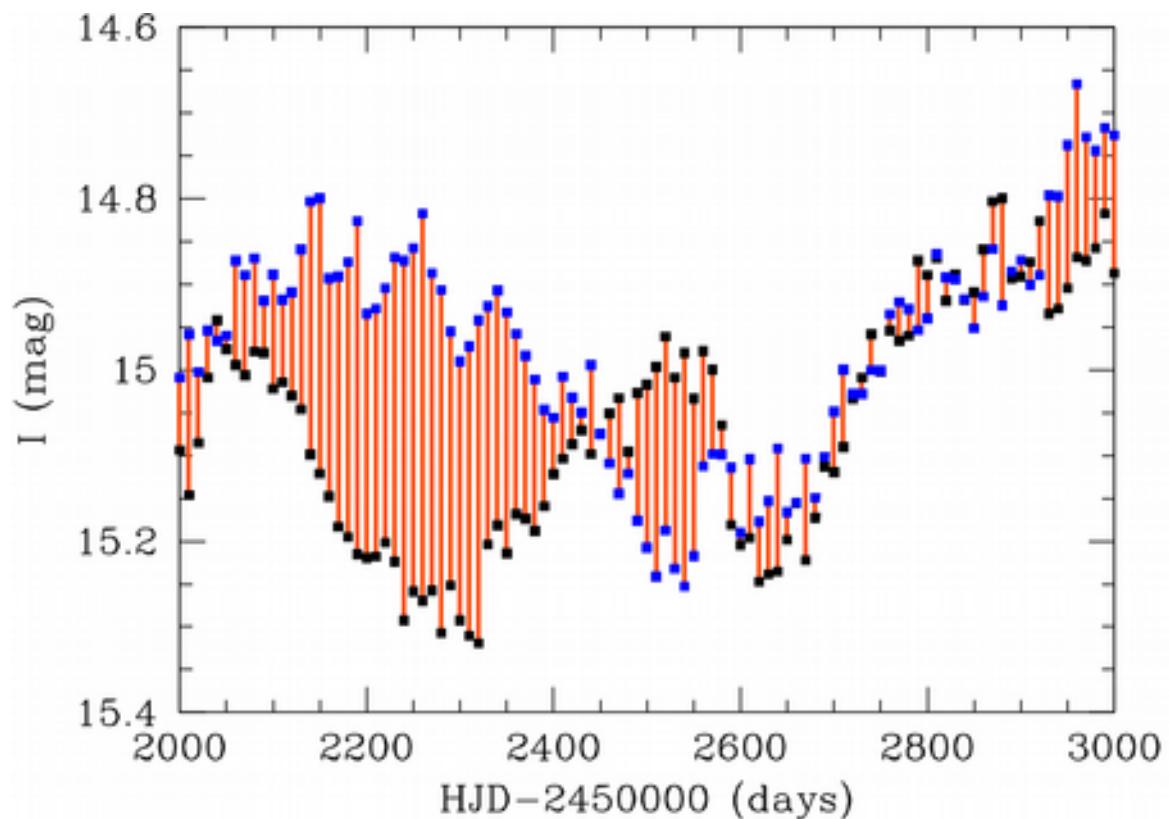
# Structure Function



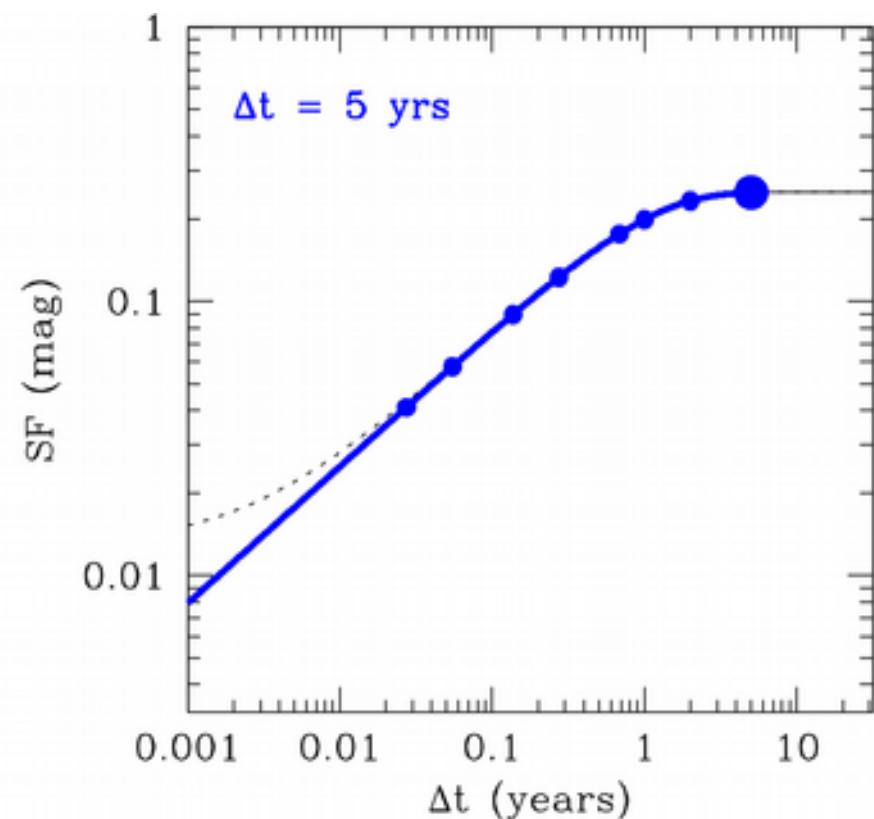
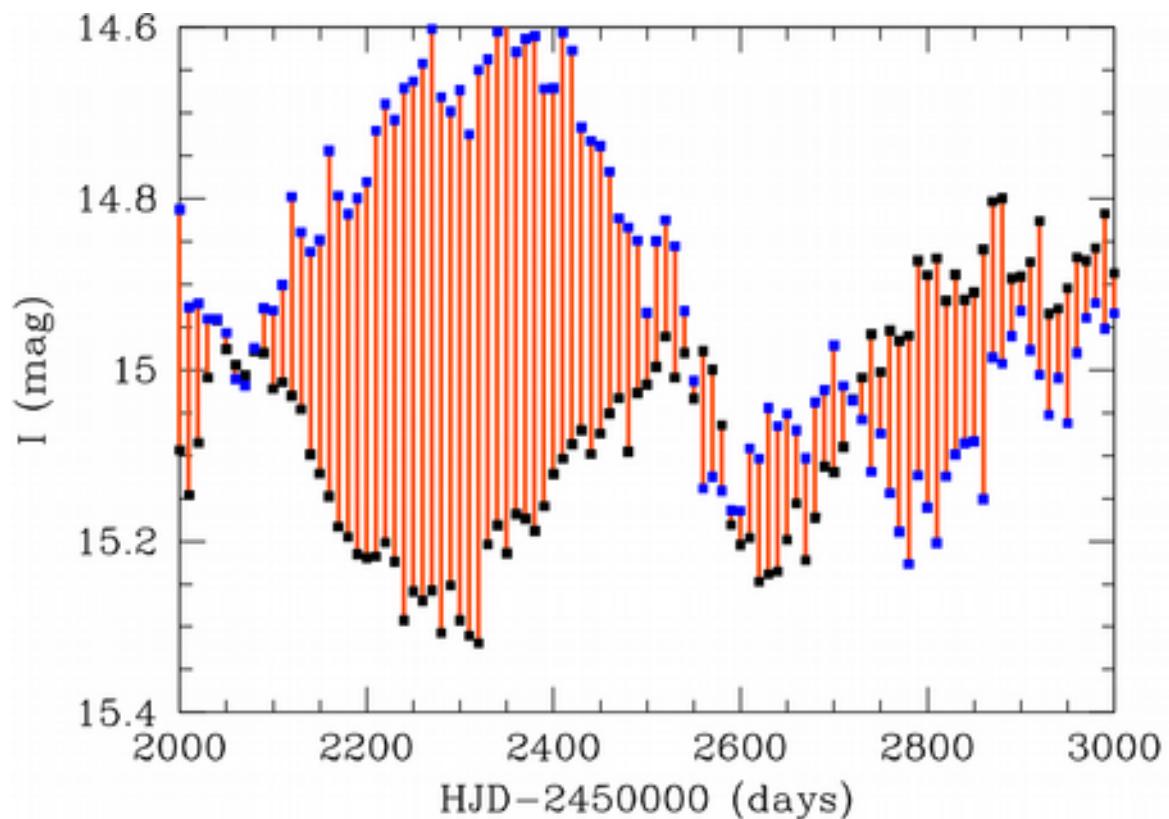
# Structure Function



# Structure Function



# Structure Function



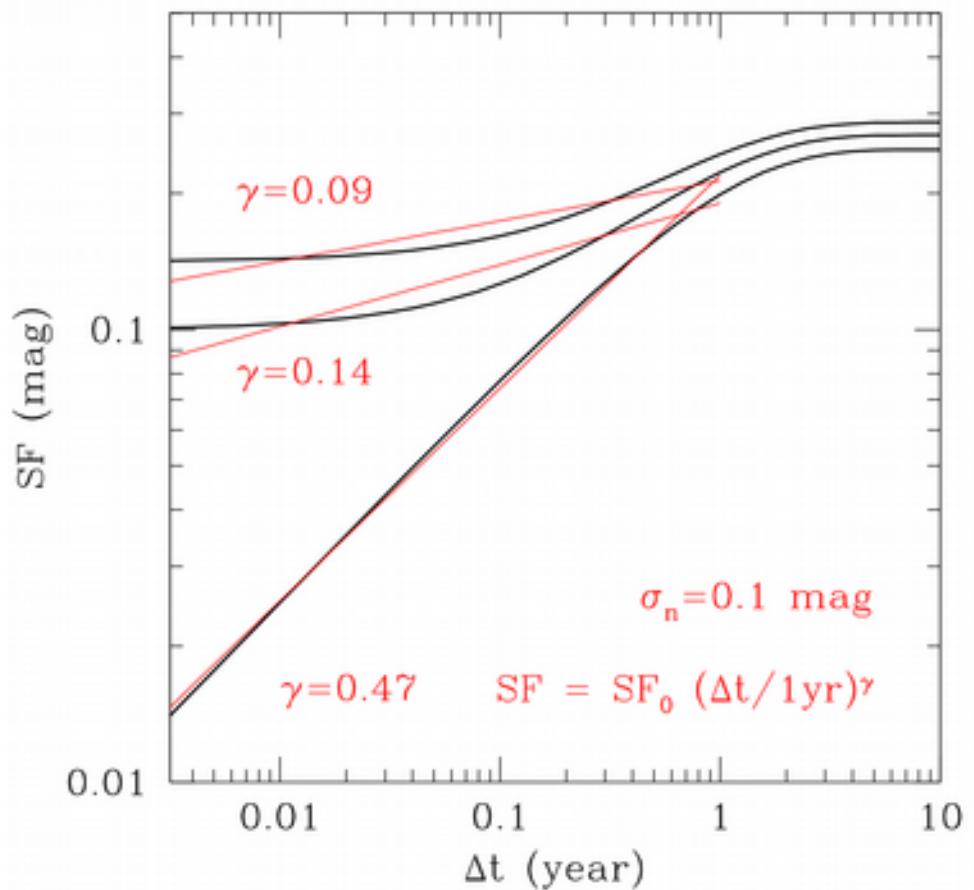
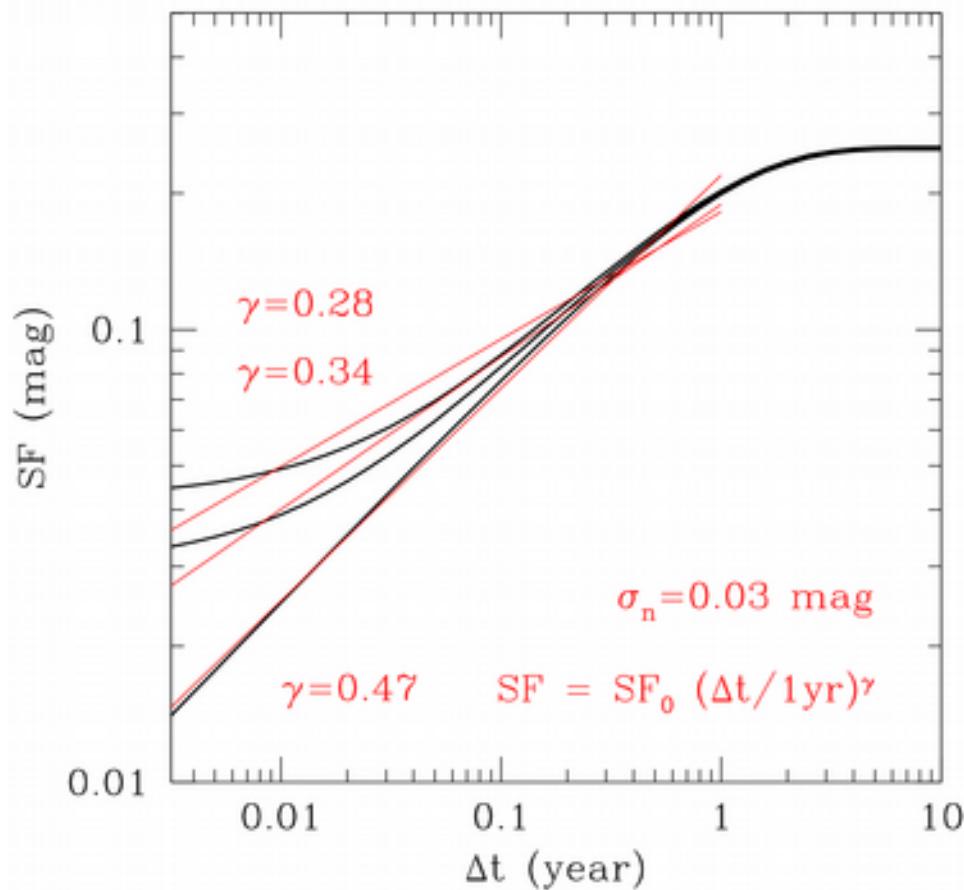
# Structure Function

$$\text{cov}(y_i, y_j) \equiv \text{var}(y_i) - V(y_i, y_j)$$

$$V(y_i, y_j) = \frac{1}{2} \langle (y_i - y_j)^2 \rangle$$

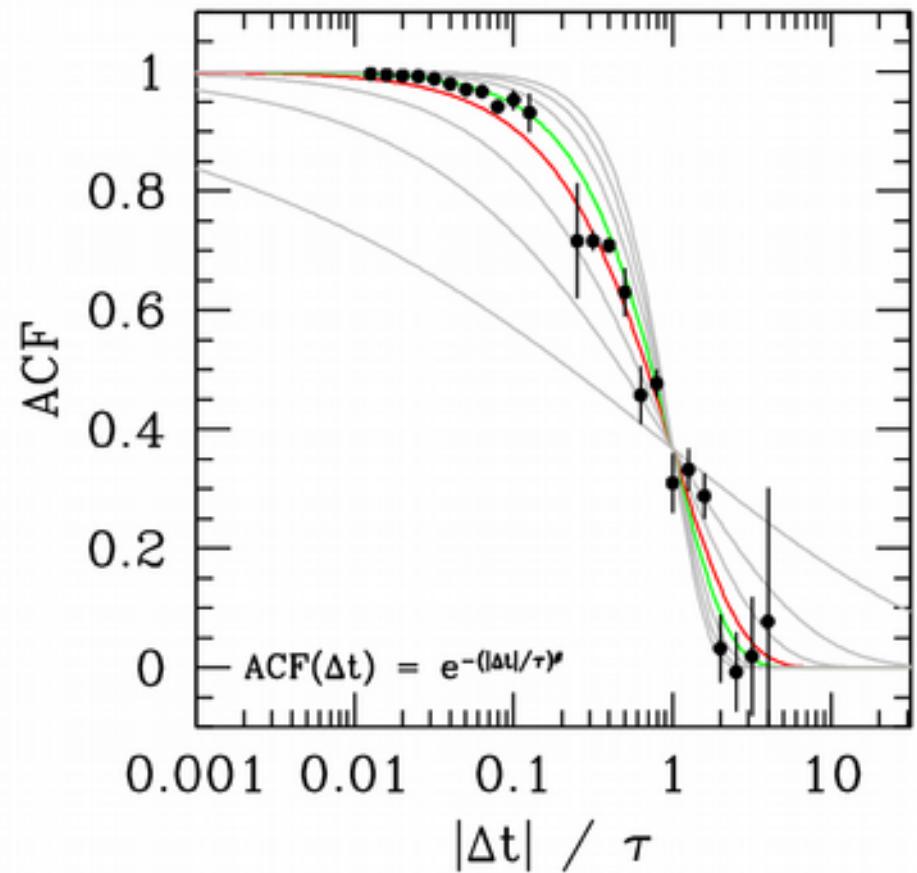
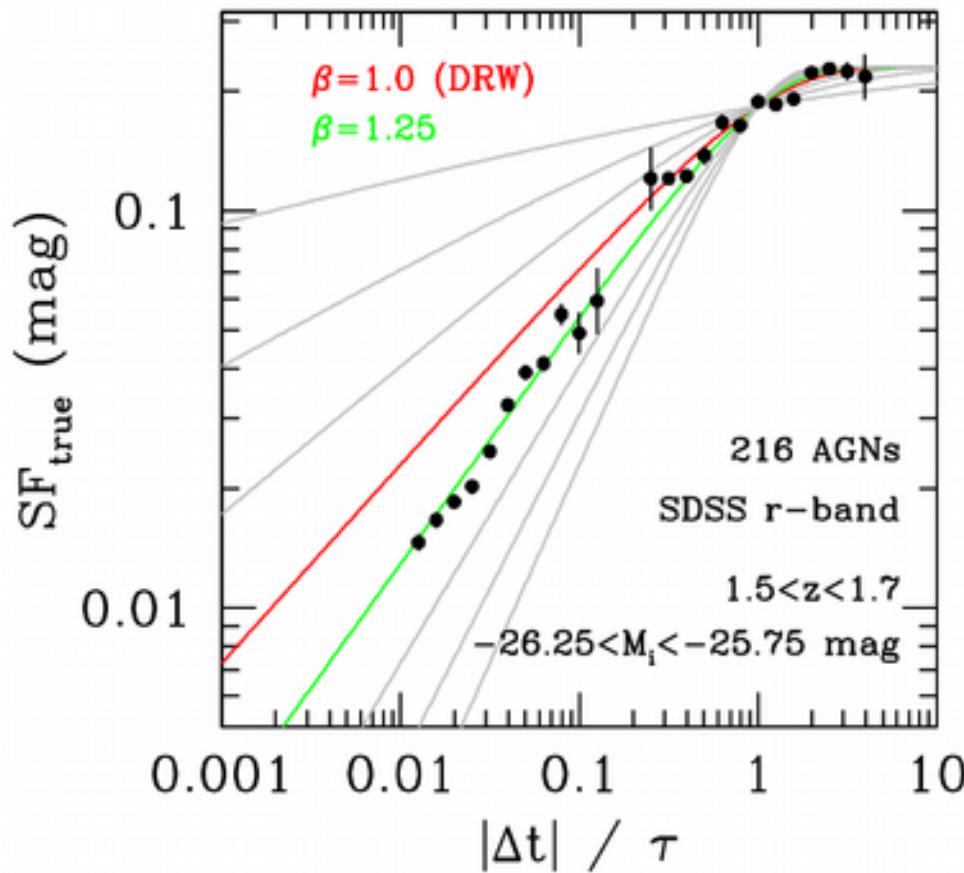
$$SF = \sqrt{2V}$$

# Structure Function



$$SF = \sqrt{SF_\infty^2 (1 - ACF) + 2\sigma_n^2}$$

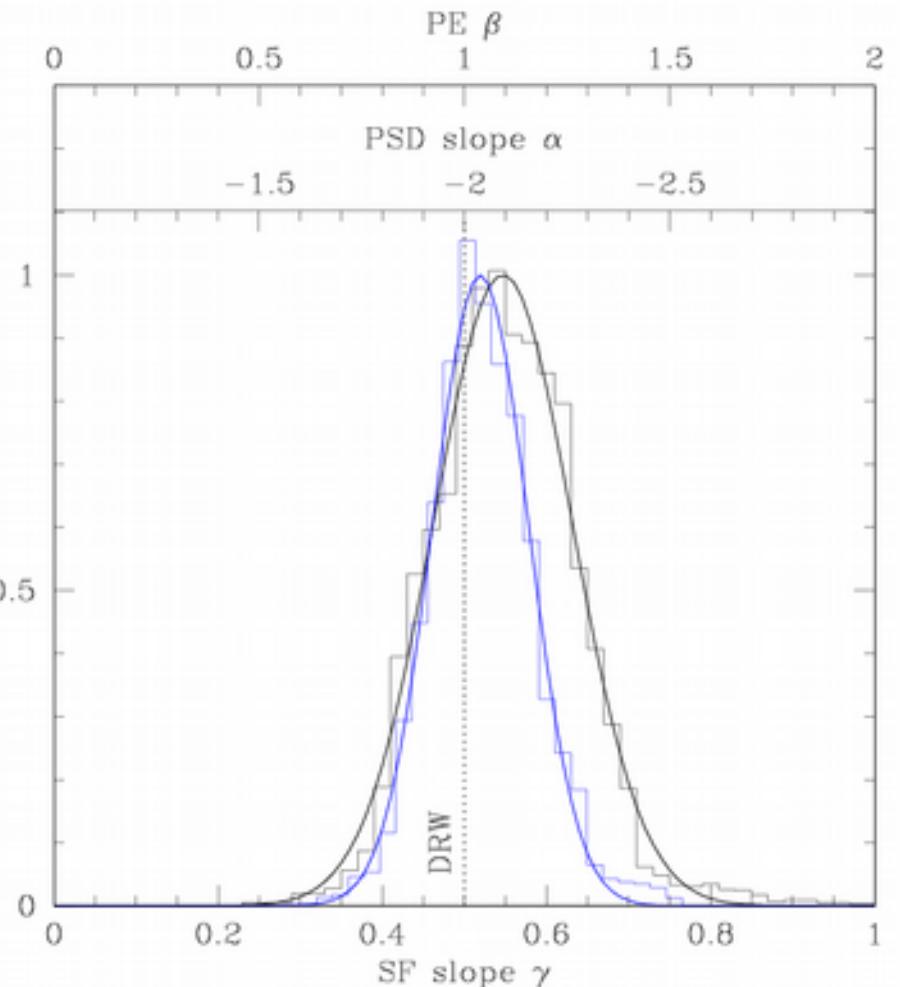
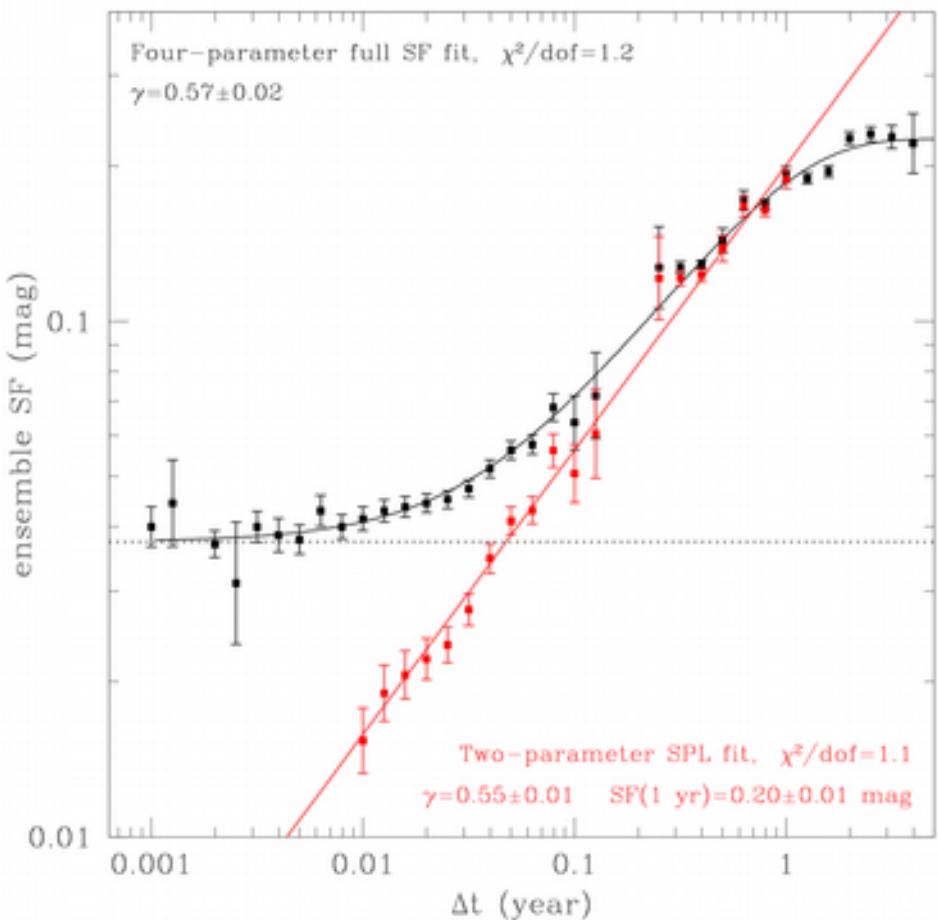
# Structure Function and ACF



$$SF = \sqrt{SF_\infty^2 (1 - ACF) + 2\sigma_n^2}$$

$$ACF = e^{-\left(\frac{|\Delta t|}{\tau}\right)^\beta}$$

# SDSS (9200 AGN, 8 yrs, 60 epochs)

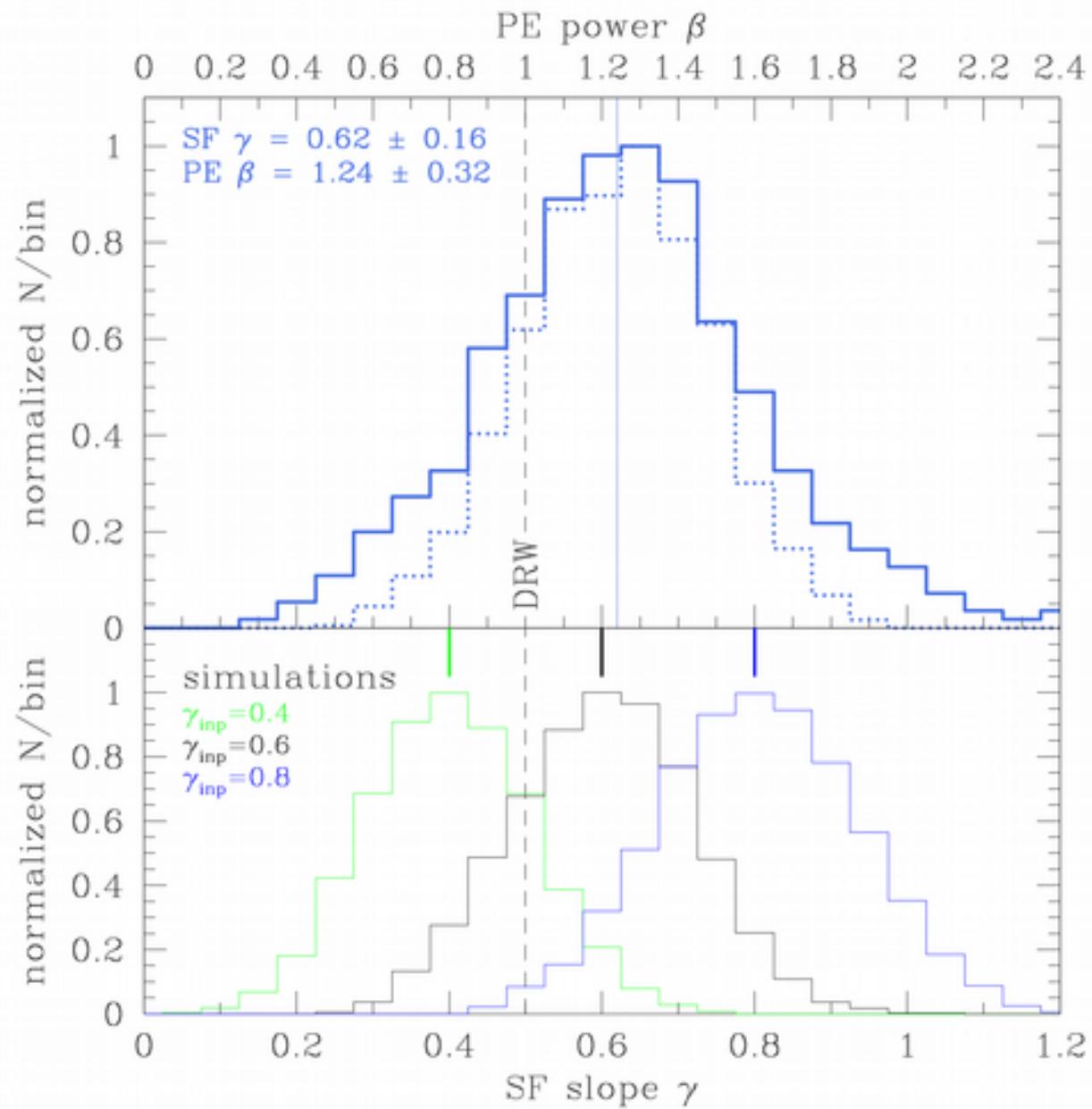


$$\text{SF} = \sqrt{\text{SF}_{\infty}^2 (1 - \text{ACF}) + 2\sigma_n^2}$$

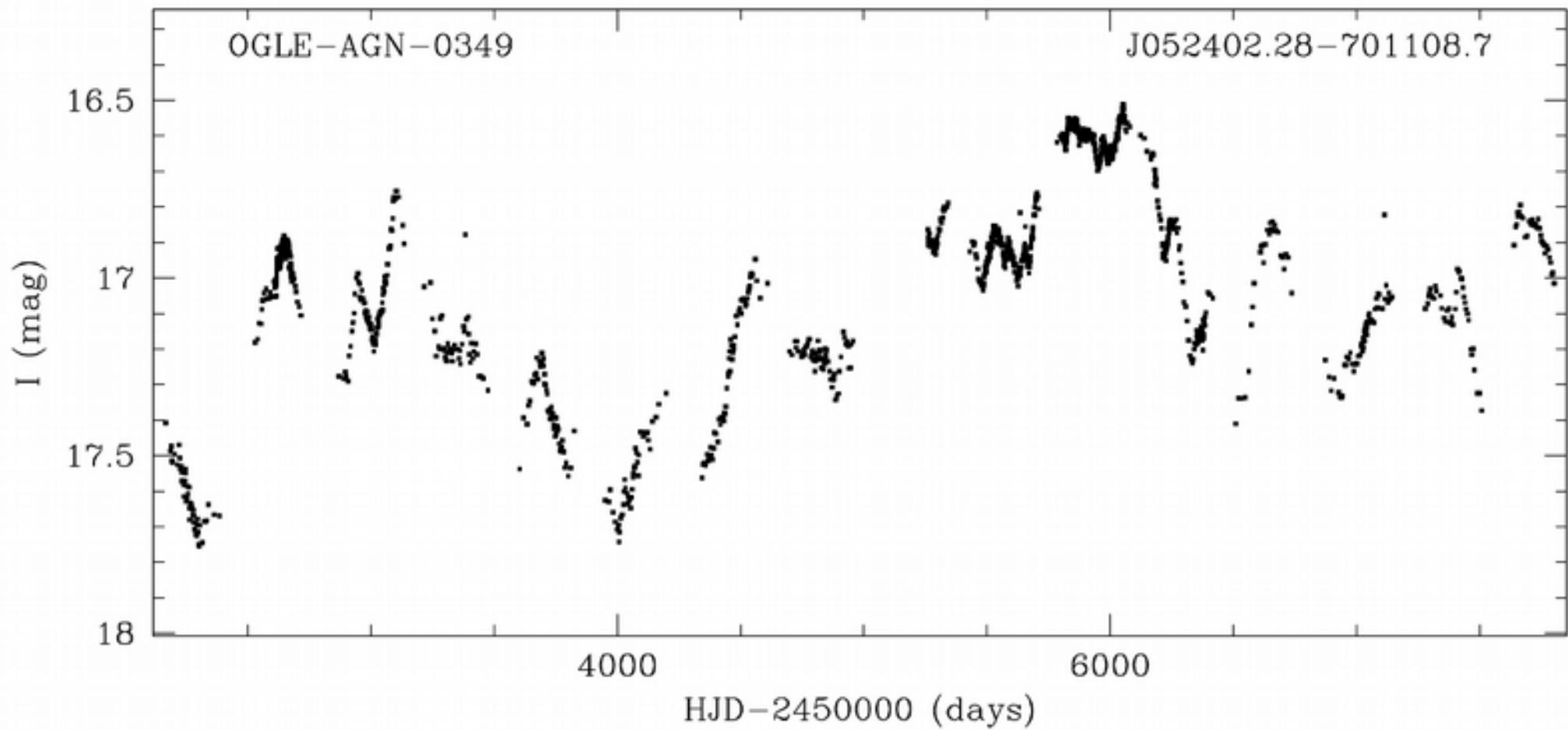
$$\text{ACF} = e^{-\left(\frac{|\Delta t|}{\tau}\right)^{\beta}}$$

$$\text{SF} = \text{SF}_0 \left(\frac{\Delta t}{1 \text{ yr}}\right)^{\gamma}$$

# Structure Function: OGLE-III + OGLE-IV

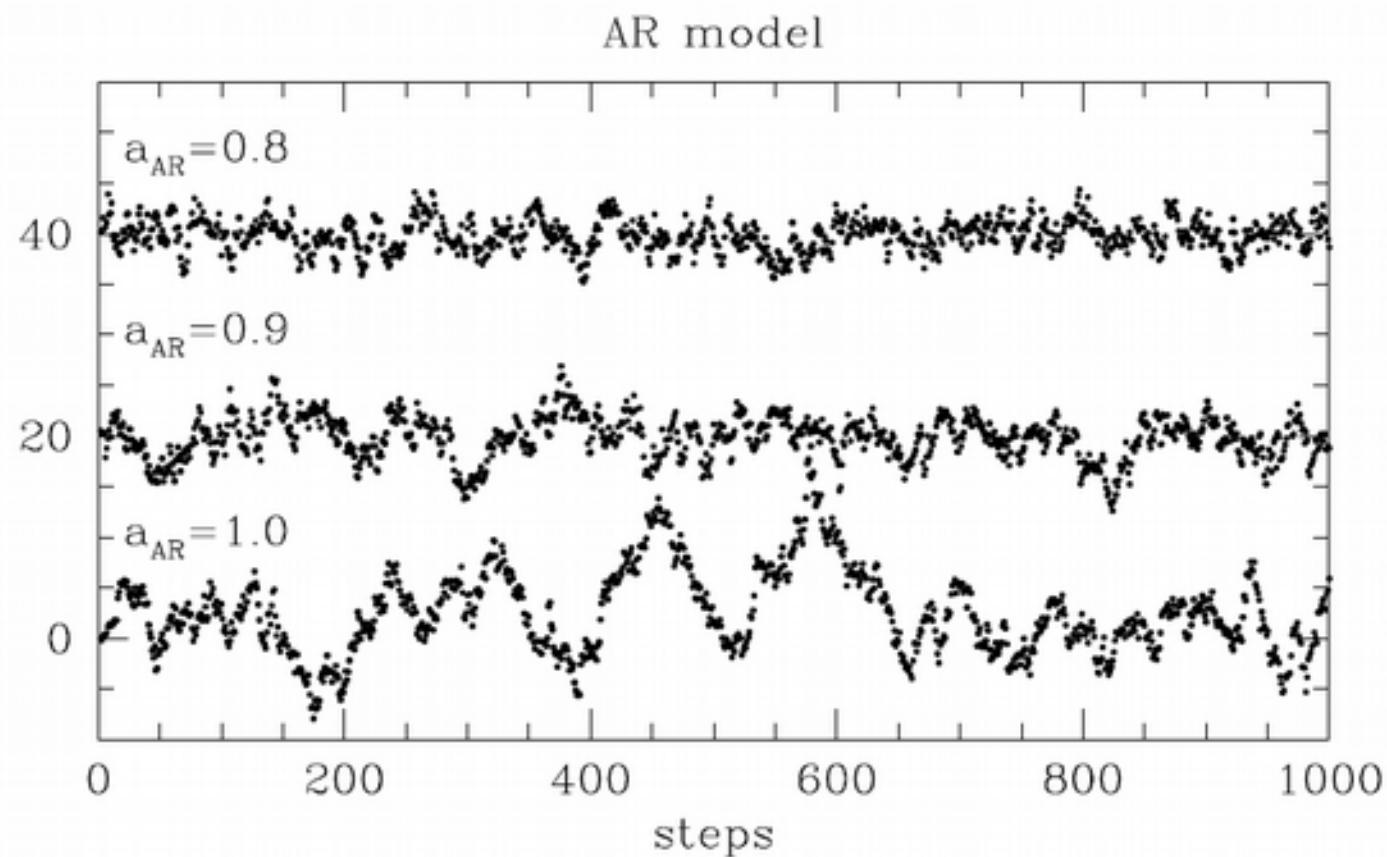


# Light Curve Modeling

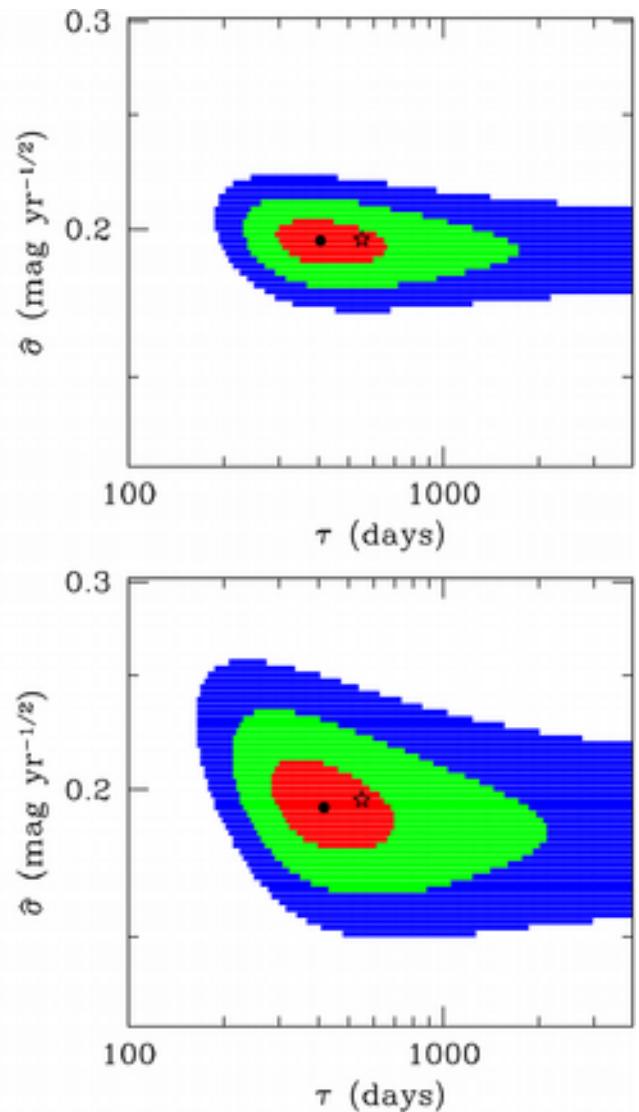
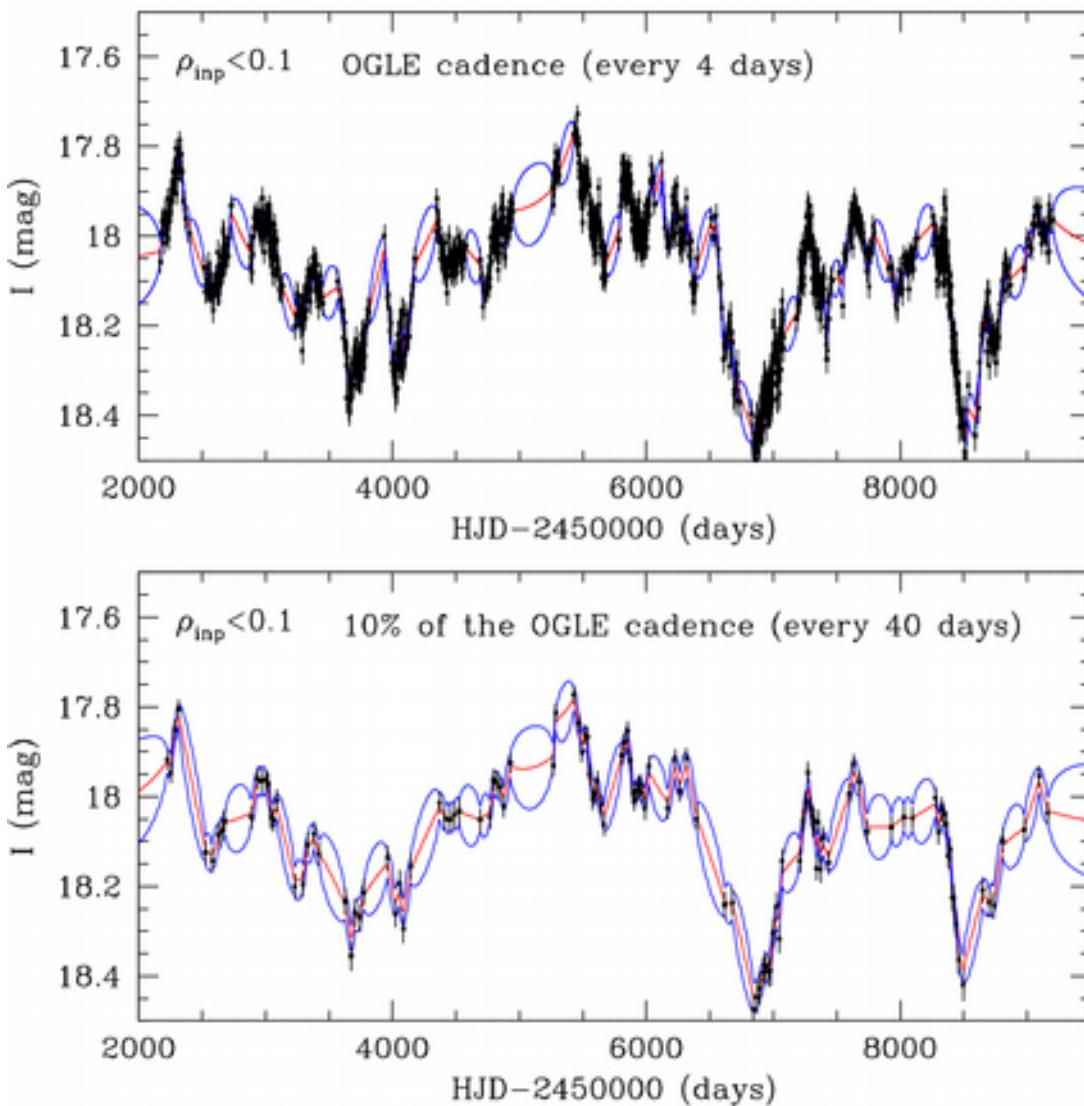


# Simple Autoregressive (AR) Model

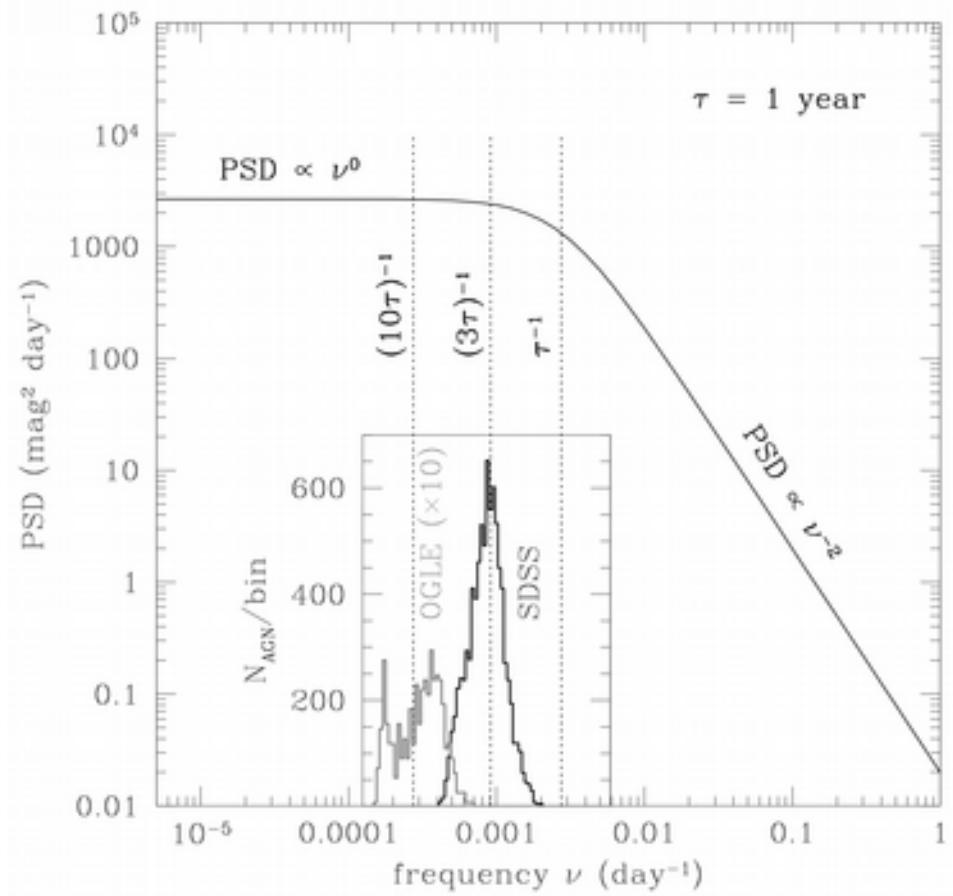
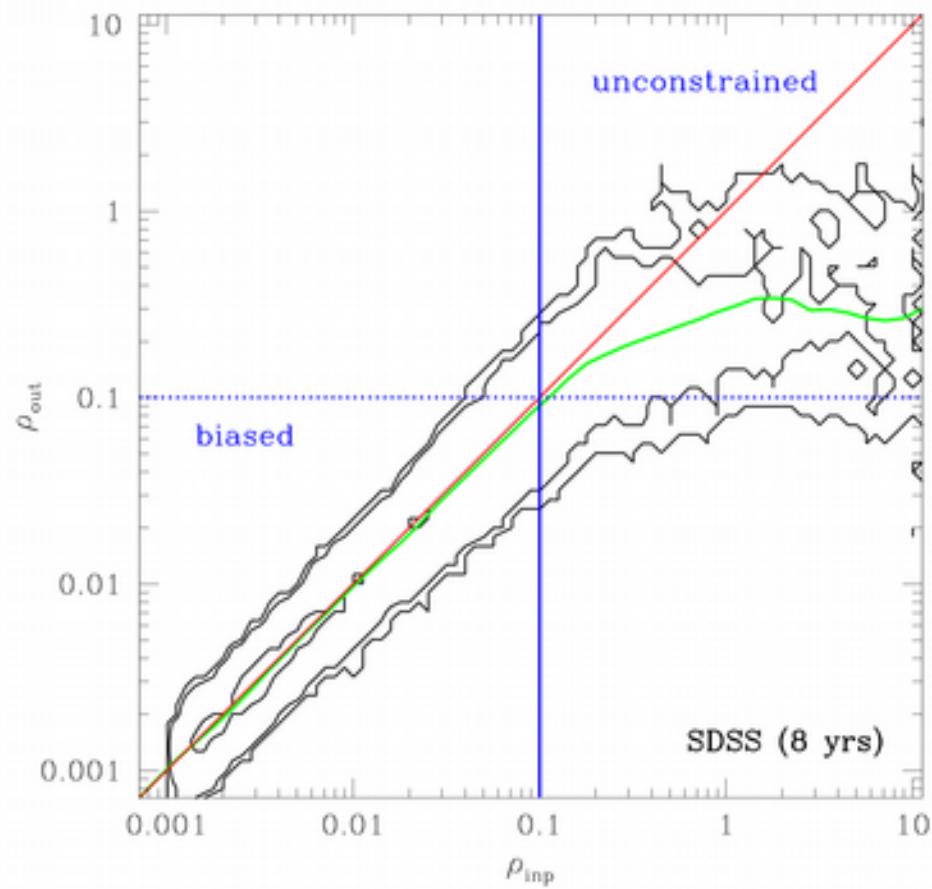
$$y_i = a_{\text{AR}} \times y_{i-1} + \epsilon_i \quad (1)$$



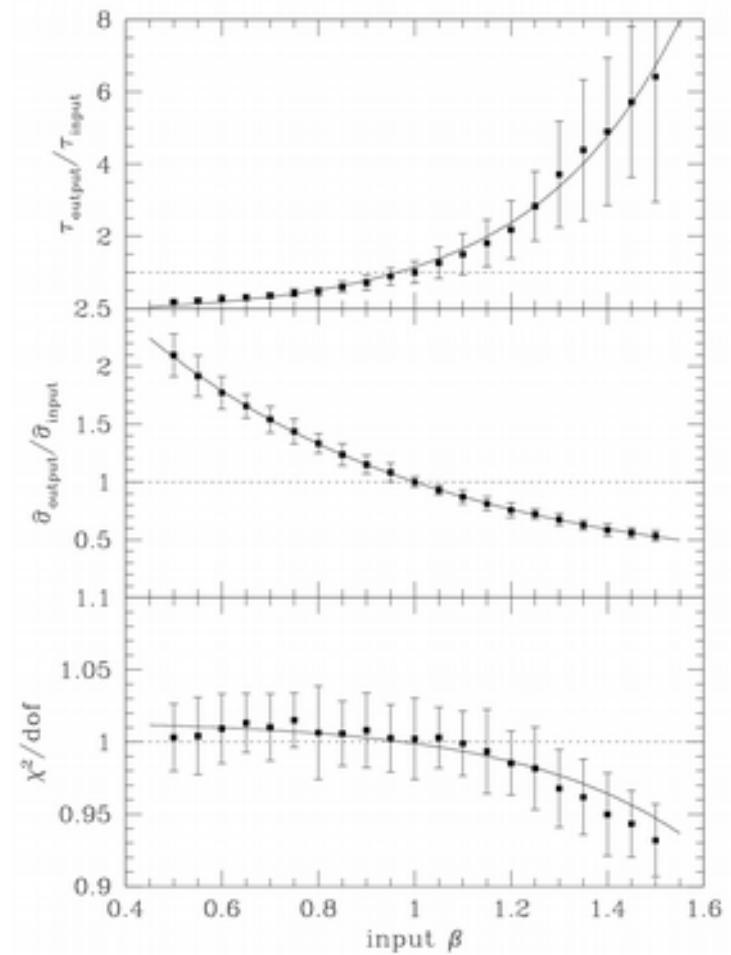
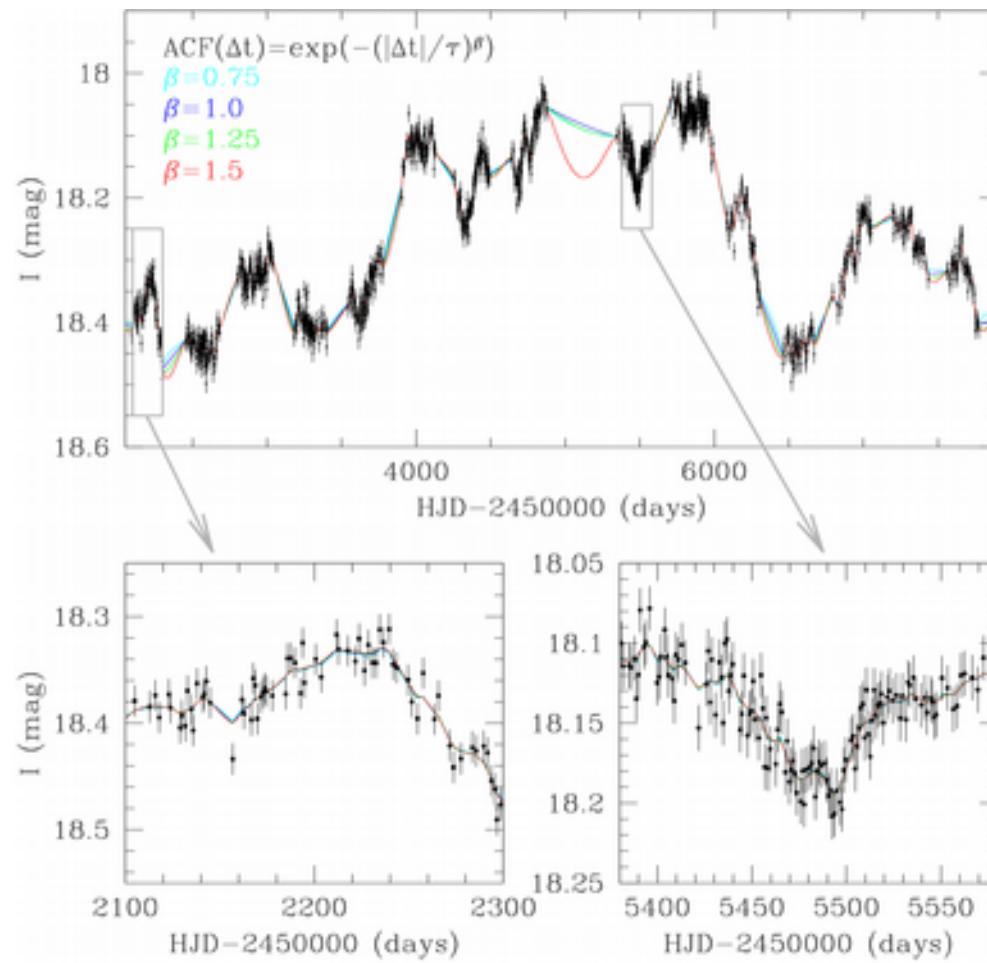
# Damped Random Walk (DRW)



# DRW Problems



# DRW Degeneracy



# Thank you!

**Revisiting Stochastic Variability of AGNs with Structure Functions**  
Kozłowski Szymon, 2016, The Astrophysical Journal, 826, 118

**A degeneracy in DRW modelling of AGN light curves**  
Kozłowski Szymon, 2016, MNRAS, 459, 2787

**Limitations on the recovery of the true AGN variability parameters  
using damped random walk modeling**  
Kozłowski Szymon, 2017, A&A, 597, 128

**A Method to Measure the Unbiased Decorrelation Timescale  
of the AGN Variable Signal from Structure Functions**  
Kozłowski Szymon, 2017, The Astrophysical Journal, 835, 250

# Structure Function

$$V(y_i, y_j) = \text{var}(y_i, y_j) - \text{cov}(y_i, y_j)$$

$$y_i = s_i + n_i$$

$$\begin{aligned} V(y_i, y_j) &= \text{var}(s_i, s_i) - \text{cov}(s_i, s_j) + \\ &+ \text{var}(n_i, n_i) - \cancel{\text{cov}(n_i, n_j)} \end{aligned}$$

$$\text{SF} = \sqrt{2V}$$

$$\text{SF} = \sqrt{2(\sigma_s^2 + \sigma_n^2 - \text{cov}(s_i, s_j))}$$

# Structure Function

$$\text{ACF} = \frac{\text{cov}(s_i, s_j)}{\text{var}(s_i, s_i)} = \frac{\text{cov}(s_i, s_j)}{\sigma_s^2}$$

$$\text{SF} = \sqrt{2\sigma_s^2 (1 - \text{ACF}) + 2\sigma_n^2}$$

$$\text{SF} = \sqrt{\text{SF}_\infty^2 (1 - \text{ACF}) + 2\sigma_n^2}$$