

Constrained Function Optimization using Evolutionary Learning

Specification

The goal is to utilize a form of evolutionary learning, a genetic algorithm, to find the minima of a function given certain constraints. The function to be optimized is the 2-variable Goldstein-Price function.

Optimization Problem

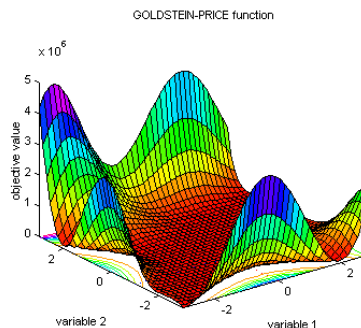
Genetic algorithms can effectively be used to find the maxima/minima of a function, by searching the function variable space to find the global optimum. The particular function to optimize in this test is the Goldstein-Price function, defined as:

$$f(x, y) = ((x + y + 1)^2 (19 - 14x + 3x^2 - 14y + 6xy + 3y^2) + 1) \left((2x - 3y)^2 (18 - 32x + 12x^2 + 48y - 36xy + 27y^2) + 30 \right)$$

The function is subject to the following constraints:

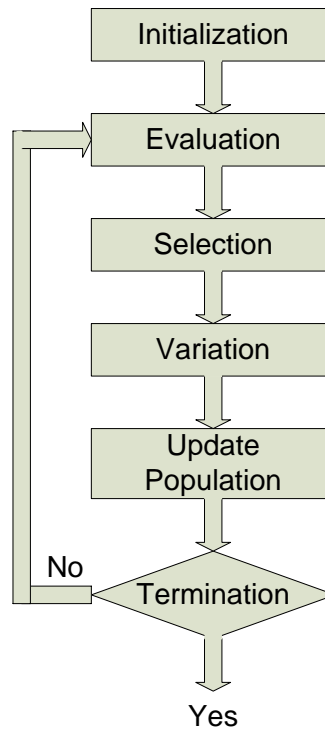
$$-2.0 \leq x \leq 2.0, \quad -2.0 \leq y \leq 2.0$$

Below is a visualization of the function in the defined range. Note the presence of several local minima, and one global minimum:



Algorithm

Idea: simulate natural selection:



The Fitness function is obvious: plug in x and y values and evaluate the Goldstein-Price equation. The key is determining how to encode the x, y real number values into a chromosome. Consider a scaling function that represents a number in the constraint range as a bit string (e.g. the range $-2.0 \dots 2.0$ becomes $0 \dots 4.0$).

Requirements:

As usual, your program can be written in any language. Submit a written analysis of your project and be prepared to present your solution to the class:

- ☐ Describe any interesting experiments, configuration details, problems, etc.
- ☐ Demonstrate the effectiveness of your program in finding the optimum.
- ☐ Include a discussion/analysis of your results.