

Stonk Bench: Unified Benchmark for Synthetic Data Generation for Financial Time Series

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Figure 1: Toronto Stock Exchange, Toronto, 1981

Abstract

The ever emerging field of Synthetic Data Generation (SDG) has gain traction within many financial domains, including Financial Time Series (FTS) data. However, there has been discourse and lack in universal agreement in what determines a better SDGFTS (Synthetic Data Generation for Financial Time Series), which maybe hindering progress in the field. In this paper, we propose and contribute a comprehensive benchmark for SDGFTS, covering various aspects such as data quality, privacy, and utility. We evaluate several state-of-the-art SDG methods using our benchmark and provide insights into their strengths and weaknesses. Our first-of-its-kind benchmark aims to facilitate the development of more effective SDG methods for FTS data, incorporating both classical statistical measures and utility benefits, and test over (insert number) to decisively determine what is the best SDGFTS model right now and for the future.

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1 Introduction

Synthetic Data Generation (SDG) has emerged as a crucial tool in financial technology, particularly for Financial Time Series (FTS) data [11]. The ability to generate high-quality synthetic financial data addresses several critical challenges in the field, including data privacy concerns, limited data availability, and the need for diverse training datasets in machine learning applications [14].

Despite the growing importance of SDGFTS (Synthetic Data Generation for Financial Time Series), there is a notable lack of standardization in evaluating the quality and effectiveness of these generative models [14]. Current evaluation methods vary widely across studies, making it difficult to compare different approaches objectively and determine their relative strengths and weaknesses.

Our research addresses this gap by introducing a comprehensive benchmark framework that encompasses:

- Statistical fidelity measures for comparing synthetic and real FTS
- Privacy preservation metrics to ensure sensitive financial information remains protected
- Utility metrics that assess the practical value of synthetic data in downstream tasks

- Performance evaluation across multiple SDGFTS models and datasets

By analyzing the results from our MLflow experiments and applying our unified benchmark, we aim to provide clear guidelines for evaluating SDGFTS models and establish a standard for future research in this domain.

1.1 Limitations in the SDGFTS Literature

Among other things, we observed that there is currently no universal, generally accepted approach to evaluating synthetic time series [14]; this issue extends beyond FTS to generative frameworks like GANs as a whole [16]. Many evaluation measures are insufficiently defined and lack public implementations, making reuse and reproduction troublesome and error-prone [14]. This presents a challenge unique to the generation task compared to areas like time series forecasting or classification [14]. Hence, future research would immensely benefit from a widely accepted, reasonably sized set of qualified measures for the central evaluation criteria.

1.2 Our Contributions

To put it in simple terms, we are adopting the time series evaluation taxonomy outlined from Stenger et al. [14], develop a comprehensive and unified SDG benchmark expanded from the works of Ang et al. [3] in specifics to FTS by incorporating a utility evaluation framework inspired by Boursin et al. [4] through portfolio evaluations generated by a deep hedger. Our key contributions include:

- [C1] **Consolidated Evaluation Framework:** We systematically review and consolidate evaluation methods from leading papers (models and surveys) in SDG and financial time series [3, 4, 14], creating a comprehensive assessment toolkit based on established practices.
- [C2] **Unified Statistical and Utility Measures:** For the first time, we integrate both statistical fidelity metrics and practical utility measures in a single SDGFTS benchmark, providing a more complete evaluation of synthetic data quality.
- [C3] **Open Benchmark Platform:** We deliver an open-source benchmark framework for the research community, aiming to establish a gold standard for SDGFTS model evaluation and comparison.

2 Preliminaries

2.1 Problem Definition

Let us formally define the Synthetic Data Generation problem for Financial Time Series. Given a financial time series $\mathbf{X} = (\mathbf{x}_1, \dots, \mathbf{x}_R)^T$ with R individual series represented as an L -dimensional vector $\mathbf{x}_i = (x_{i1}, \dots, x_{iL})$, where x_{ij} denotes the j -th point of time series \mathbf{x}_i . Let $p(\mathbf{x}_1, \dots, \mathbf{x}_R)$ denote the real distribution of the given time series \mathbf{X} . The objective of SDG for FTS is to generate a synthetic time series $\hat{\mathbf{X}} = (\hat{\mathbf{x}}_1, \dots, \hat{\mathbf{x}}_n)^T$ such that its distribution $p(\hat{\mathbf{x}}_1, \dots, \hat{\mathbf{x}}_n)$ approximates $p(\mathbf{x}_1, \dots, \mathbf{x}_R)$, while preserving the key properties exhibited in the real financial time series, such as autocorrelation structure, volatility clustering, and distributional moments (mean, variance, skewness, kurtosis).

2.2 Scope of Project

2.2.1 Scope of Methods. Our benchmark encompasses a diverse range of SDGFTS methods, from traditional parametric approaches to modern deep learning architectures. We selected models based on three main criteria: (1) proven industry adoption, (2) research community acceptance, and (3) recent methodological innovations.

Our evaluation includes classical parametric models, which rely on predefined statistical distributions and assumptions about the underlying data generation process. These models have been extensively used in financial institutions for their interpretability and theoretical foundations.

We also evaluate modern non-parametric approaches, particularly deep learning-based models that learn the data distribution directly from observations without assuming a specific form. These include generative adversarial networks, variational autoencoders, and diffusion models, representing the cutting edge in synthetic data generation.

2.2.2 Scope of Datasets. We evaluate models on high-granularity financial time series indices prices from HistData.com [1]. Currently, we focus on univariate time series data generation. The S&P 500 (SPXUSD) index is chosen, using the minute-level closing price from 2021 through 2023. Future work may extend to multivariate series involving multiple assets or additional features.

2.2.3 Scope of Evaluation Taxonomical Criteria. Our evaluation framework follows the taxonomy structure proposed by Stenger et al. [14], incorporating various evaluation measures from different papers in the field.

We systematically integrate evaluation metrics from multiple sources while maintaining this structured taxonomical approach, ensuring comprehensive coverage of all critical aspects of SDGFTS evaluation and setting a standard for future research in time series SDG as a whole.

3 Overview of Synthetic FTS Methods

We categorize synthetic financial time series generation methods into two main families: classical parametric (stochastic) models, which rely on explicit assumptions about the data-generating process, and modern non-parametric (deep learning) models, which learn complex dependencies directly from data without predefined functional forms. The following subsections provide a detailed overview of the methods included in our benchmark.

3.1 Classical Stochastic (Parametric) Methods

Parametric models assume a specific functional form for the data-generating process, characterised by a finite set of parameters. These models are interpretable and analytically tractable, allowing for closed-form solutions in many cases. However, they may struggle to capture complex stylised facts or high-dimensional dependencies beyond their structural assumptions. Below we outline several widely-used parametric models in FTS.

- [A1] **Geometric Brownian Motion (GBM).** The price process follows a continuous-time stochastic process with constant

Table 1: Common notation and variables.

Symbol	Description
S_t	Asset price
$X_t = \ln S_t$	Log-price
$r_t = \ln(S_t/S_{t-1})$	Log-return
μ	Drift
σ	Volatility
W_t	Standard Brownian motion
Δt	Discrete time step

drift and volatility. Model-specific parameters are μ and σ .

$$dS_t = \mu S_t dt + \sigma S_t dW_t. \quad (1)$$

[A2] **Ornstein–Uhlenbeck (OU)**. A mean-reverting Gaussian process for log-prices or spreads. Model-specific parameters are $\theta > 0$ (reversion rate), μ (long-term mean), and σ (volatility).

$$dX_t = \theta(\mu - X_t) dt + \sigma dW_t. \quad (2)$$

[A3] **Merton Jump Diffusion (MJD)**. Extends the GBM equation (1) by incorporating normally-distributed jumps. Model-specific parameters are λ (jump intensity), μ_j and σ_j (mean and standard deviation of jump sizes).

$$\frac{dS_t}{S_t} = \mu dt + \sigma dW_t + J dN_t, \quad (3)$$

where $J \sim \mathcal{N}(\mu_j, \sigma_j^2)$, $N_t \sim \text{Poisson}(\lambda t)$.

[A4] **Double-Exponential Jump Diffusion (DEJD)**. Another jump-diffusion model with asymmetric double-exponential jump sizes modifying equation (1). Model-specific parameters are p (probability of upward jump) and η_1, η_2 (exponential parameters for upward/downward jumps).

$$\begin{aligned} \frac{dS_t}{S_t} &= \mu dt + \sigma dW_t + Y dN_t, \\ Y &= \begin{cases} \text{Exp}(\eta_1), & \text{with probability } p, \\ -\text{Exp}(\eta_2), & \text{with probability } 1 - p. \end{cases} \end{aligned} \quad (4)$$

[A5] **GARCH(1,1)**. A discrete-time conditional heteroskedastic model for returns. Model-specific parameters are $\omega > 0$, $\alpha \geq 0$, $\beta \geq 0$ (GARCH coefficients) and \mathcal{D} (innovation distribution, usually standard Normal or Student-t). Captures volatility clustering via time-varying conditional variance.

$$\begin{aligned} r_t &= \sigma_t z_t, \quad z_t \sim \mathcal{D}, \\ \sigma_t^2 &= \omega + \alpha r_{t-1}^2 + \beta \sigma_{t-1}^2. \end{aligned} \quad (5)$$

3.2 Deep Learning (Non-parametric) Methods

Non-parametric models, in this context, refer to generative (often implicit) models that do not assume a fixed parametric form for the underlying data-generating process. Instead, they learn latent structures directly from data through flexible architectures such as neural networks, enabling the modeling of highly nonlinear, high-dimensional, and multi-modal dependencies (e.g., multivariate financial time series with interactions across assets, time horizons,

and features). While these models trade off interpretability and analytical tractability, they offer substantially greater expressive power and flexibility. This expressiveness, however, comes at the cost of increased data requirements, more intensive hyperparameter tuning, and higher computational demands.

We categorize these approaches into three major families of deep generative models: Generative Adversarial Networks (GANs), Variational Autoencoders (VAEs), and Diffusion Models.

3.2.1 Variational Autoencoders (VAEs). Variational Autoencoders [7, 13] are latent-variable generative models that posit a probabilistic encoder $q_\phi(z | x)$ and decoder $p_\theta(x | z)$. One maximizes the evidence lower bound (ELBO):

$$\mathcal{L}_{\text{VAE}} = \mathbb{E}_{q_\phi(z|x)} [\log p_\theta(x | z)] - \text{KL}(q_\phi(z | x) \| p(z)).$$

Often one uses a standard Gaussian prior $p(z) = \mathcal{N}(0, I)$. The encoder-decoder structure allows sampling by first drawing $z \sim p(z)$, then generating $x \sim p_\theta(x | z)$.

In financial time-series generation, specialized versions such as the Time-Causal VAE (TC-VAE) have been proposed to enforce causality in the encoding/decoding of temporal data. For instance, Acciaio et al. (2024) propose TC-VAE, which ensures that generated paths respect temporal causality and show that the model reproduces stylized facts (e.g., heavy tails, volatility clustering) on real markets [2]. Because VAEs provide a principled latent representation, they are useful in finance to model underlying latent drivers of asset dynamics and to sample coherent trajectories.

[A6] **TimeVAE**. A time-series specific VAE variant that combines causal temporal encoders (e.g., causal convolutions or RNNs) with an autoregressive decoder to preserve path coherence. Training typically augments the ELBO with prediction or stepwise reconstruction losses to improve short- and long-range dependencies; TimeVAE is used in our benchmark as a dedicated VAE baseline for temporal data [5].

3.2.2 Generative Adversarial Networks (GANs). Generative Adversarial Networks [6] approach generation as a two-player game between a generator G and a discriminator D . The discriminator is trained to maximize the probability of correctly classifying real data and generated data, with loss

$$L_D = -\mathbb{E}_{x \sim p_{\text{data}}} [\log D(x)] - \mathbb{E}_{z \sim p(z)} [\log(1 - D(G(z)))].$$

The generator aims to fool the discriminator and is trained to minimize

$$L_G = -\mathbb{E}_{z \sim p(z)} [\log D(G(z))].$$

Many GAN variants, such as Wasserstein GAN or Least Squares GAN, modify these loss functions to promote more stable training and address issues like mode collapse.

In financial data synthesis, GANs have been widely used to generate realistic synthetic time series. For example, GAN-based financial data generation models (often using WGAN or improvements) show that one can improve the authenticity and predictive ability of generated financial statements or time series [12]. Another example is VRNNGAN, which uses a recurrent VAE as the generator and a recurrent discriminator to capture temporal dependencies in synthetic sequence generation [8]. GANs are relevant in finance because they can capture complex joint distributions and

dependencies in multivariate time-series without requiring explicit likelihood models.

- [A7] **QuantGAN**. A GAN variant tailored for financial applications that incorporates quantile-aware objectives or conditional quantile matching and temporal architectures (e.g., temporal convnets or transformers). QuantGANs aim to better capture tail behaviour and risk-sensitive statistics (e.g., VaR/CVaR) important for downstream financial tasks [17].

3.3 Miscellaneous

This section consists of models that are classified as neither parametric nor non-parametric.

- [A8] **Block Bootstrap (non-parametric)**. A resampling technique that preserves short-range dependence by sampling contiguous blocks of returns. Although not parametric, it is included here for completeness and baseline comparison.

4 Stonk Bench Architecture

4.1 Datasets and Preprocessing

The preprocessing procedure builds upon the TSGBench pipeline, which standardizes segmentation, normalization, and train/test splitting of the time series [3]. Several modifications were introduced to better accommodate financial time series and stochastic models.

4.1.1 Data type. Index price data at minute frequency at closing price are used. Let $X \in \mathbb{R}^{L \times N}$ denote a time series with $N = 1$ channel(s) and length L .

4.1.2 Transformations. Raw prices are converted to log-returns per channel via

$$r_t = \log S_t - \log S_{t-1} = \log(S_t/S_{t-1}), \quad r_t \in \mathbb{R}^N,$$

yielding a transformed series of length $L - 1$. Log returns are preferred in finance due to their variance-stabilizing properties, preserving heavy tails and volatility clustering, and removal of the first order integration (random walk) commonly exhibited in price series [15].

4.1.3 Model-specific preprocessing. The preprocessing follows the general TSGBench framework, with the following adaptations:

- Log returns are used directly instead of TSGBench's min-max normalization for the reasons outlined in §4.1.2.
- For parametric models, the transformed series is divided into contiguous training, validation, and test segments with ratios $(1 - \alpha - \beta) : \alpha : \beta$, where $\alpha = 0.1$ and $\beta = 0.1$. This ensures that parametric models fit parameters directly to contiguous historical data.
- For non-parametric models, overlapping sliding windows $\mathcal{W} \in \mathbb{R}^{R \times L \times N}$ with stride 1 are extracted. Unlike TSGBench, which employs an autocorrelation-based hard-coded window of 125 (often yielding a size of 1 for stock data due to fast autocorrelation decay [15]), the window length L is determined via the partial autocorrelation function (PACF). Specifically, PACF is computed for each channel up to $\lfloor 10 \log_{10} n \rfloor$ lags, and the lag corresponding to the maximum significant PACF peak across channels is selected, resulting in $L = 13$. This

approach captures relevant temporal dependencies within the data.

- The dataset is split into train, validation, and test sets while preserving temporal order to prevent future information from leaking into the past. Only the training set is shuffled during model training to improve convergence. In contrast, TSG-Bench shuffles time series samples before splitting, which introduces data leakage. Our approach ensures strictly forward-looking evaluation for realistic forecasting. proper evaluation, consistent with TSGBench.

4.1.4 Data loaders. For non-parametric models, mini-batches are generated from the windowed data \mathcal{W} using independent fixed seeds for training, validation, and test sets, enabling reproducible epoch-wise evaluation. Training batches are shuffled, while validation and test sets maintain sequential ordering. To ensure fair comparison, parametric models generate sequences of identical length L and matching sample count to the windowed data used by non-parametric models.

4.2 Statistical Evaluation Measures

All metrics below are applied **per channel**, i.e., each univariate time series (OHLC column) is evaluated independently. For multivariate data, results are reported as channel-wise statistics (e.g., mean or distribution across channels).

4.2.1 Feature-based Distance Measures. These metrics quantify how well synthetic data captures key marginal and second-order properties of real data.

- [M1] **Marginal Distribution Difference (MDD)**: Distance between real and synthetic marginals (e.g., 1-Wasserstein distance) per channel:

$$\text{MDD}_j = W_1(\hat{F}_{real}^j, \hat{F}_{synth}^j),$$

$$W_1(F, G) = \int_0^1 |F^{-1}(u) - G^{-1}(u)| du,$$

where \hat{F}_{real}^j and \hat{F}_{synth}^j are empirical CDFs of channel j .

- [M2] **Mean Difference (MD)**: Absolute difference of per-channel means:

$$\text{MD}_j = |\mu_{real}^j - \mu_{synth}^j|.$$

- [M3] **Standard Deviation Difference (SDD)**: Absolute difference of per-channel standard deviations:

$$\text{SDD}_j = |\sigma_{real}^j - \sigma_{synth}^j|.$$

- [M4] **Kurtosis Difference (KD)**: Absolute difference of per-channel excess kurtosis:

$$\text{KD}_j = |\kappa^{\text{ex}}(X_{real}^j) - \kappa^{\text{ex}}(X_{synth}^j)|,$$

$$\kappa^{\text{ex}}(X^j) = \frac{\mathbb{E}[(X^j - \mu^j)^4]}{(\sigma^j)^4} - 3.$$

- [M5] **AutoCorrelation Difference (ACD)**: Absolute difference in lag-1 autocorrelation per channel:

$$\rho^j(1) = \frac{\sum_{t=2}^L (x_t^j - \bar{x}^j)(x_{t-1}^j - \bar{x}^j)}{\sum_{t=1}^L (x_t^j - \bar{x}^j)^2},$$

$$\text{ACD}_j = |\rho_{real}^j(1) - \rho_{synth}^j(1)|.$$

4.2.2 Visualization Methods. Visual tools complement numeric metrics for face-validity and communication [3].

[M6] **t-SNE:** 2D embeddings of window-level features per channel for real vs. synthetic overlap and cluster structure.

[M7] **Distribution:** Channel-wise histograms of returns to visualize empirical distribution.

4.2.3 Diversity Metrics. Measures that prevent mode collapse, computed per channel. Pairwise distances only consider the same channel across samples.

[M8] **Intra-Class Euclidean Distance (ICD-ED):**

$$\text{ICD-ED}^j = \frac{2}{R(R-1)} \sum_{1 \leq a < b \leq R} \|\mathbf{x}_a^j - \mathbf{x}_b^j\|_2,$$

where $\mathbf{x}_a^j \in \mathbb{R}^L$ is the j -th channel of the a -th sample.

[M9] **Intra-Class Dynamic Time Warping (ICD-DTW):**

$$\text{ICD-DTW}^j = \frac{2}{R(R-1)} \sum_{1 \leq a < b \leq R} d_{\text{DTW}}(\mathbf{x}_a^j, \mathbf{x}_b^j).$$

4.2.4 Efficiency Assessment.

[M10] **Generation Time:** Wall-clock time to generate S samples:

$$T_{\text{gen}} = t_1 - t_0 \quad (\text{seconds for } S \text{ samples}).$$

4.2.5 Stylized Facts Verification. Canonical stylized facts, measured per channel:

[M11] **Heavy Tails:** Per-channel excess kurtosis:

$$\kappa^{\text{ex}}(X^j) = \frac{\mathbb{E}[(X^j - \mathbb{E}[X^j])^4]}{(\text{Var}[X^j])^2} - 3.$$

[M12] **Return Autocorrelation:** Lag-1 autocorrelation per channel, should be close to zero for liquid assets.

[M13] **Volatility Clustering:** Lag-1 autocorrelation of squared or absolute returns per channel:

$$\begin{aligned} \rho_{x^2}^j(1) &= \text{Corr}((x_t^j)^2, (x_{t-1}^j)^2), \\ \rho_{|x|}^j(1) &= \text{Corr}(|x_t^j|, |x_{t-1}^j|). \end{aligned}$$

4.3 Utility Evaluation Measures: Deep Hedging

Utility measures are critical for evaluating synthetic data beyond statistical metrics, as they assess the practical value of generated data in real-world financial applications [4]. Our benchmark incorporates deep hedging as a utility measure for several key reasons:

[U1] **Real-world Application Testing:** Deep hedging provides a concrete way to evaluate how synthetic data performs in actual financial tasks, particularly in derivatives pricing and risk management.

[U2] **Industry-relevant Metrics:** By comparing hedging strategies trained on synthetic versus real data, we can assess the practical utility of synthetic data through metrics that matter to financial practitioners, such as replication errors and hedging performance.

[U3] **Model Robustness Validation:** Deep hedging helps verify if synthetic data maintains the complex relationships and market dynamics necessary for developing reliable trading strategies.

4.3.1 Deep Hedger Problem Definition. We consider a continuous-time financial market defined on a probability space $(\Omega, \mathcal{F}, \mathbb{P})$, over a finite time horizon $0 < T < \infty$, equipped with a filtration $\mathcal{F} = (\mathcal{F}_t)_{0 \leq t \leq T}$ that represents the evolution of information through time. The market consists of $d + 1$ tradable assets $S = (S^0, \dots, S^d)$, where S_t^j denotes the price of asset j at time t . For simplicity, we assume a zero interest rate environment.

We study the hedging problem associated with a contingent claim delivering a payoff $g(S_T)$ at maturity T , where S_T represents the terminal value of the underlying asset vector. The hedging strategy is implemented at a discrete set of times $0 = t_0 < t_1 < \dots < t_{N-1} < t_N = T$. A *self-financing portfolio* is described by a d -dimensional \mathcal{F}_t -adapted process Δ_t , and its terminal wealth, denoted $X_T^{\Delta, p}$, is given by

$$X_T^{\Delta, p} = p + \sum_{i=1}^d \sum_{j=0}^{N-1} \Delta_{t_j}^i (F_{t_{j+1}}^i - F_{t_j}^i), \quad (6)$$

where $p \in \mathbb{R}$ represents the initial premium.

The objective is to determine the optimal premium and trading strategy $(p^{\text{opt}}, \Delta^{\text{opt}})$ that minimize the expected squared hedging error:

$$(p^{\text{opt}}, \Delta^{\text{opt}}) = \underset{p, \Delta}{\text{Argmin}} \mathbb{E} \left[(X_T^{\Delta} - g(S_T))^2 \right]. \quad (7)$$

To address this optimization problem, we employ the global approach proposed by Fécamp *et al.* (2020), chosen for its computational efficiency and scalability. In this framework, the control policy Δ is approximated by a feed-forward neural network—referred to as a *deep hedger*—which jointly learns the optimal trading strategy and corresponding premium through end-to-end training.

Table 2: Notations for Deep Hedger Architecture.

Symbol	Description
D	Time-series dataset
T	Task
S	Score
A	Deep hedger algorithm
\mathcal{A}_n	Set of n deep hedger algorithms
M	Deep hedger model
M_{TS}	(SDGFTS) model

4.3.2 Deep Hedger Architecture. Our deep hedger architecture centers around the Train-Synthetic-Test-Real (TSTR) evaluation framework [9], adapted for financial time series generation. We begin with our real FTS dataset D —partitioned to a training, validation, and test set respectively as $D_r = \{D_r^{\text{train}}, D_r^{\text{validate}}, D_r^{\text{test}}\}$ —along with a specific hedging task T and a performance score S to evaluate hedging effectiveness, to which we will go indepth in the next subsection. We consider a deep hedger algorithm A (a 5-layer perceptron) that takes as input the dataset D_r and task T ,

In the context of SDGFTS evaluation, we consider a SDGFTS model M_{TS} trained on D_r^{train} and validated with D_r^{validate} to generate synthetic FTS data D_g .

Now we can train a deep hedger algorithm A on the datasets D_r^{train} and D_g^{train} respectively, resulting in two deep hedger models M_r and M_g .

Finally, we evaluate both models on the real test set D_r^{test} to obtain the corresponding performance scores s_r and s_g .

The goal of the deep hedger portfolio evaluation is to evaluate the effectiveness of the model M_{TS} with downstream tasks (deep hedging) by comparing the scores s_r and s_g . The model M_{TS} is considered effective if the results yielded similar scores, i.e. $s_r \approx s_g$ —preferably having higher performance with results of $s_g > s_r$ —indicating that the synthetic data generated by M_{TS} is useful for training deep hedger models [14].

4.3.3 Deep Hedger Extensions. We proposed two extensions to the standard deep hedger architecture to better suit our benchmark need that drew inspiration from recent literature [14].

[E1] Augmented Testing [14] To better evaluate the performance of deep hedgers trained on synthetic data, we train our deep hedger A on a new dataset D_{aug} that combines both real training data D_r^{train} and synthetic data D_g . In other words, we train model M_g on D_{aug} where $D_{aug} := D_r^{train} \cup D_g$. Then we proceed to evaluate scores between models M_g and M_r on the real test set, where M_r is still trained on only real data D_r^{train} .

[E2] Algorithm Comparison [10] Another extension is to compare multiple deep hedger algorithms indicating to what degree each algorithm performs equally on the generated data relative to the other algorithms, compared to their performance on real data.

Given a set of n deep hedger algorithms $\mathcal{A}_n = \{A_1, \dots, A_n\}$, we train each algorithm $A_i \in \mathcal{A}_n$ on both real training data D_r^{train} and synthetic data D_g^{train} respectively, resulting in two sets of deep hedger models $\{M_r^1, M_r^2, \dots, M_r^n\}$ and $\{M_g^1, M_g^2, \dots, M_g^n\}$ and two ordered sets of performance scores $s_r := \{s_r^1, s_r^2, \dots, s_r^n\}$ and $s_g := \{s_g^1, s_g^2, \dots, s_g^n\}$ respectively.

Finally we compare the relative performance of each algorithm on real data versus synthetic data by computing the Spearman's rank correlation coefficient r_s [10] between the two score sets s_r and s_g :

$$r_s = 1 - \frac{6 \sum_{i=1}^n (\text{rank}(s_r^i) - \text{rank}(s_g^i))^2}{n(n^2 - 1)}, \quad (8)$$

where $\text{rank}(s_r^i)$ and $\text{rank}(s_g^i)$ denote the ranks of scores s_r^i and s_g^i within their respective sets.

We interpret a high positive correlation (i.e., r_s close to 1) as an indication that the synthetic data generated by $\text{mathcal{M}}_{TS}$ preserves the relative performance of different deep hedger algorithms.

5 Results and Analysis

5.1 Statistical Evaluation Results

We present a concise, comprehensive evaluation of the synthetic financial time series produced by each model. The analysis covers marginal and second-order statistics, temporal dependencies,

diversity measures, stylized-facts verification, and generation efficiency. Results are reported on the minute-level closing price and summarized in the tables and figures that follow: fidelity metrics, diversity metrics, stylized-fact comparisons, and generation-time measurements. Best-performing entries are highlighted where appropriate and comparative discussion appears in the subsequent analysis subsections.

5.2 Utility Evaluation Results

Results of the deep hedging evaluation (replication error, P&L distribution, risk-adjusted metrics) can be summarized in tables analogous to the above once computed.

5.3 Comprehensive Model Comparison

Provide radar plots or scorecards that combine normalized metrics (fidelity, diversity, stylized facts, efficiency) into composite ranks per task.

5.4 Ranking Analysis

Discuss trade-offs: fidelity vs. diversity, training time vs. quality, and sensitivity to window length and sample count.

6 Conclusion and Future Work

In our research, we recognize the existing limitations in the evaluation of synthetic time series, particularly the absence of a universally accepted framework. To address this, we adopt the evaluation taxonomy proposed by Stenger et al. and expand upon it to create a comprehensive benchmark specifically tailored for Synthetic Data Generation for Financial Time Series (SDGFTS). Our contributions include the development of a consolidated evaluation framework that systematically reviews and integrates various assessment methods from leading studies in the field. This approach not only enhances the rigor of evaluations but also facilitates the comparison of different SDGFTS models, ultimately providing a more standardized and reliable means of assessing synthetic data quality.

6.1 Summary of Findings

We believe that Stonk Bench will serve as a valuable resource for researchers and practitioners in the field of synthetic financial time series generation. We hope that our benchmark will facilitate more rigorous and standardized evaluations of SDGFTS models, ultimately advancing the state of the art in this important area of research. For the broader field of synthetic data generation, our work highlights the importance of a comprehensive and unifying evaluation frameworks that consider both statistical properties and practical utility that is proposed by Stenger *et al.*

6.2 Stonk Bench Shortcomings

While Stonk Bench represents a significant step forward in the evaluation of SDGFTS models, we acknowledge several limitations in our current work:

[S1] Incompatibility with other models: Stonk Bench has so far been evaluated mainly on classical stochastic models (e.g., GBM, OU, GARCH) and a subset of deep-learning approaches

(diffusion models, GANs, VAEs). Other model families — such as reinforcement-learning-based generators, normalizing flows, autoregressive networks, and hybrid methods — have not yet been benchmarked.

- [S2] **No hyperparameter tuning:** For consistency and comparability across models, StonkBench evaluations were performed using default model configurations, without performing hyperparameter optimization. This ensures a fair baseline but may not reflect the absolute best performance achievable by each model.
- [S3] **Metric and procedure generalizability:** As a consequence, some metrics or evaluation procedures may not directly translate to these untested families, which limits the framework's generalizability across all synthetic financial time-series generation methods.
- [S4] **Data Leakage from Public Datasets:** Current models can potentially overfit to publicly available datasets — the same datasets that Stonk Bench is using — leading to inflated performance metrics that do not generalize well to unseen data. One possible solution is to either curate proprietary datasets or implement a grace period so the model can be tested on new data that was not publicly available during its development.
- [S5] **Computational Resource Requirements:** The comprehensive nature of Stonk Bench — particularly accommodating any submitted deep hedging model and the deep hedging utility evaluation — demands significant computational resources. This may limit accessibility for researchers with constrained resources. demands significant computational resources. This may limit accessibility for researchers with constrained resources.

6.3 Future Research Directions

6.3.1 *Remaining progress.* In regard to the next portion of our project, we aim to expand Stonk Bench in several key areas.

- [F1] **Multivariate time series predictions.** Extend Stonk Bench to evaluate models on multivariate time series data, enabling a more comprehensive assessment of their performance in realistic scenarios. We wish test SDGFTS models on datasets with multiple correlated assets and datasets with Bid-Ask spreads and trading volume to evaluate their ability to capture inter-asset dependencies and market microstructure effects [15].
- [F2] **Add distribution-matching metrics.** Extend fidelity measures with additional tests such as the Kolmogorov–Smirnov (KS) statistic to better capture marginal and tail mismatches.

6.3.2 *Beyond the project.* We envision Stonk Bench evolving into a community-driven benchmark for SDGFTS evaluation. As we acknowledge the limitations outlined in §6.2, we propose the following future directions:

- [F3] **Continuous model inclusion.** Maintain Stonk Bench as a living benchmark by incorporating newly developed SDGFTS techniques (normalizing flows, autoregressive generators, advanced diffusion models, reinforcement-learning-based generators, and hybrids) [11].

[F4] **Rigorous metric selection and ablations.** As mentioned in Stenger et al., we wish to rigorously conduct ablation studies to identify the most informative and robust metrics for different model families and stylized facts; produce guidance for a compact, interpretable metric set [14].

[F5] **Public benchmark platform.** Launch a website with documentation, code, datasets, and a leaderboard for submitted SDGFTS models; provide CI-enabled evaluation pipelines for reproducible comparisons.

[F6] **Community engagement.** Foster collaboration via contribution guidelines, open issues, and reproducible example workflows so researchers can extend and validate the benchmark.

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A Preprocessing Diagnostics

A.1 Channel-wise Distributions

A.2 Autocorrelation Analyses

B Embedding Visualizations