

# paper de la tesis

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## Introduction

### Description and literature

#### ZW3 != QS3

XX Needs redaction: \* Zonal Waves (ZW) and Quasistationary Waves (QS) are related but conceptually distinct.

- ZW is a property of a global scalar field (geopotential in this present case) while QS are a property of *a set* of global scalar fields.
- QS for a set of fields can be defined as the ZW of the mean field. In that sense, measuring the “activity” of QS waves at a monthly scale is impossible. What *can* be measured is
  - ZW activity (and asume that is a good proxy for QS activity)
  - monthly field similarity to the QS field –this leads to non-trivial questions about *how* to measure similarity.

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## Methods

### Data source

### Fourier?

### Steadiness

Since planetary waves are charecterised by amplitude and phase, they can be treated similarly to other vector quantities like wind. Following this analogy, we measure the degree of stationarity of quasistationary waves by calculating steadiness. That is

$$k = \frac{|\overline{\mathbf{V}}|}{|\mathbf{V}|}$$
$$S = \frac{2}{\pi} \sin^{-1}(k)$$

Where  $k$  is the *constancy* and is defined as the ratio between the magnitude of the mean wave (  $|\overline{\mathbf{V}}|$  ) and the mean magnitude of waves  $|\mathbf{V}|$ . Steadiness (  $S$  ) transforms that value to linearize the  $k$  with respect to the phase range [Singer1967]. A value of 1 represents a completely stationary wave while a value of 0 represents a completely random wave.

XXX Probably needs better notation.

In practice,  $k$  can be computed more efficiently by

$$k = \frac{\sum_{i=1}^N A_i \cos(\overline{\phi} - \phi_i)}{\sum_{i=1}^N A_i}$$

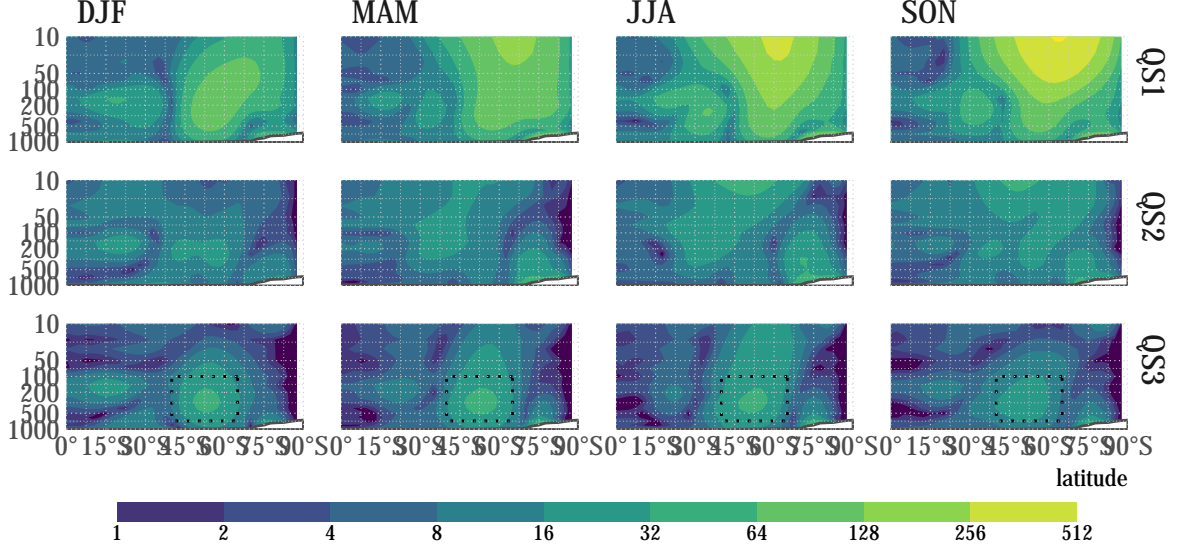


Figure 1: Fourier amplitude of the mean zonal wave 3 (contours) XXX

Where  $A_i$ ,  $\phi_i$  are the amplitude and phase of the  $i$ th wave and  $\bar{\phi}$  is the phase of the mean wave (stationary phase). That is,  $k$  is a weighted mean of the cosine of the difference between phases and the stationary phase. Further, considering that  $\cos(\bar{\phi} - \phi_i)$  is the correlation between two waves of different phase but same frequency makes the interpretation of  $k$  clearer. It can be seen that  $k$  (and by extension  $S$ ) is a measure of how similar are individual wave 3 fields to the climatological wave 3 field.

Note that in order to filter out the effect of the monthly seasonal cycle, here  $S$  is computed using  $\bar{\phi}$  for each month even though the sum is performed for each trimestre.

XXX Is this too much?

## Wave Action

XXX Needs some definition and methodology or just a citation to @Vera2004 further along?

## Results

### QS3 climatology

Figure 1 shows the amplitude of the mean wave for QS1 to 3 for each trimestre. QS1 dominates in almost all levels and latitudes during all seasons but its amplitude is strongest in the austral spring and at higher levels of the atmosphere. QS2, on the other hand... ?

The amplitude of QS3 achieves its maximum around 200hPa and 50°S during all seasons but with important changes in its vertical extent. During austral winter and autumn, wave 3 amplitude extends up to the highest model levels while it remains restricted to the troposphere and lower stratosphere during spring and summer.

The tropical upper troposphere stands out as an area of high QS amplitude for the three wavenumbers and almost during all seasons. This is probably related to the stationary response to the SAMS, specifically the Bolivian High and the xx Low (name??). This can be confirmed by a similar analysis of wave 3 amplitude but using wavelets, which shows that the area of high QS3 amplitude is located over South America (not shown). (xx not shown? I don't know if just tease an innovative result among the old methodology.)

The reconstructed QS3 field at 200hPa shows the expected maximum at 50°S and the annual cycle in its phase already observed in previous studies. It also shows an easterly inclination of the systems evident in all seasons except winter, suggesting that the QS3 might be related to southerly transport of momentum. The

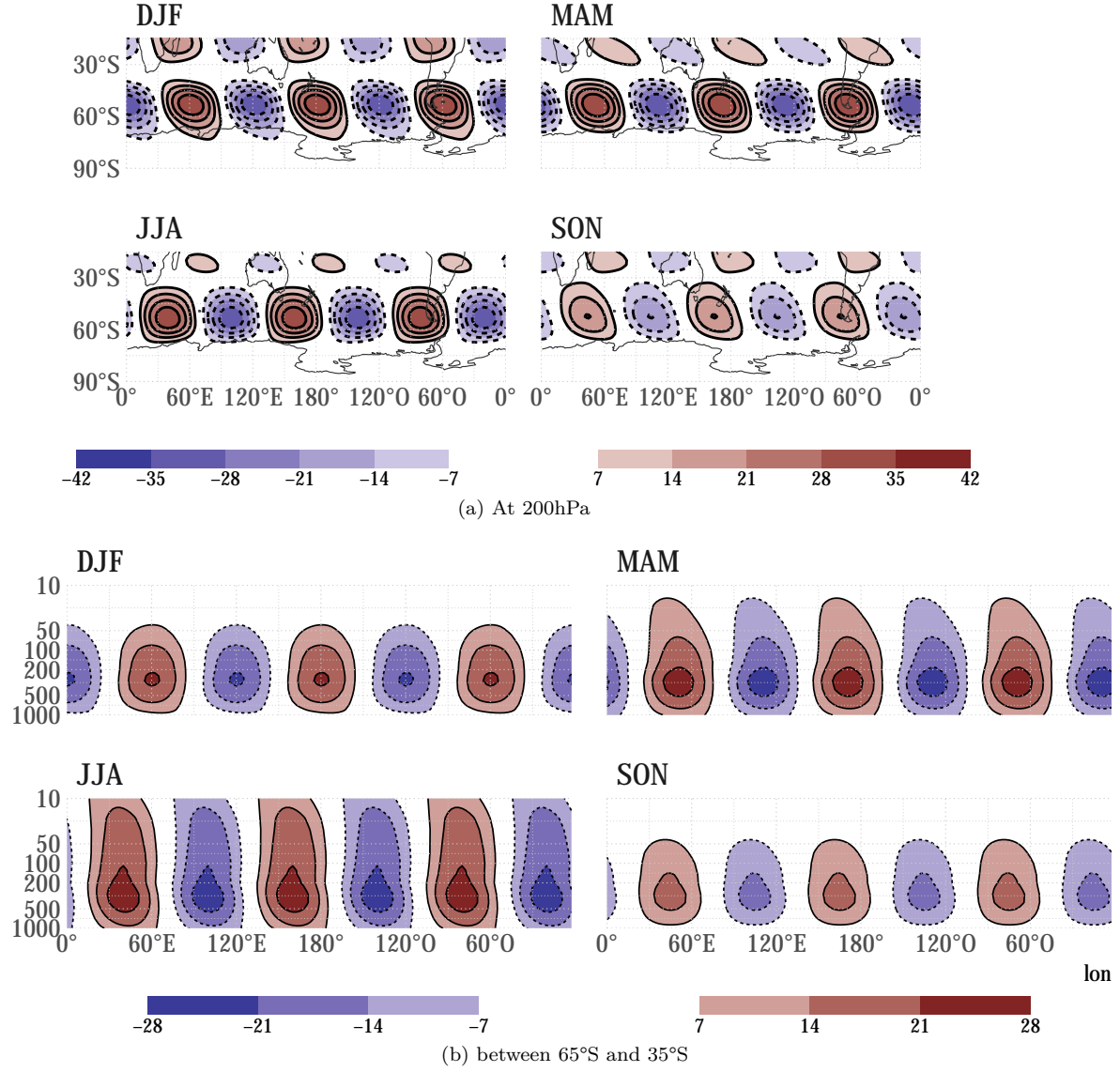


Figure 2: Wave 3 component of the geopotential field of each season

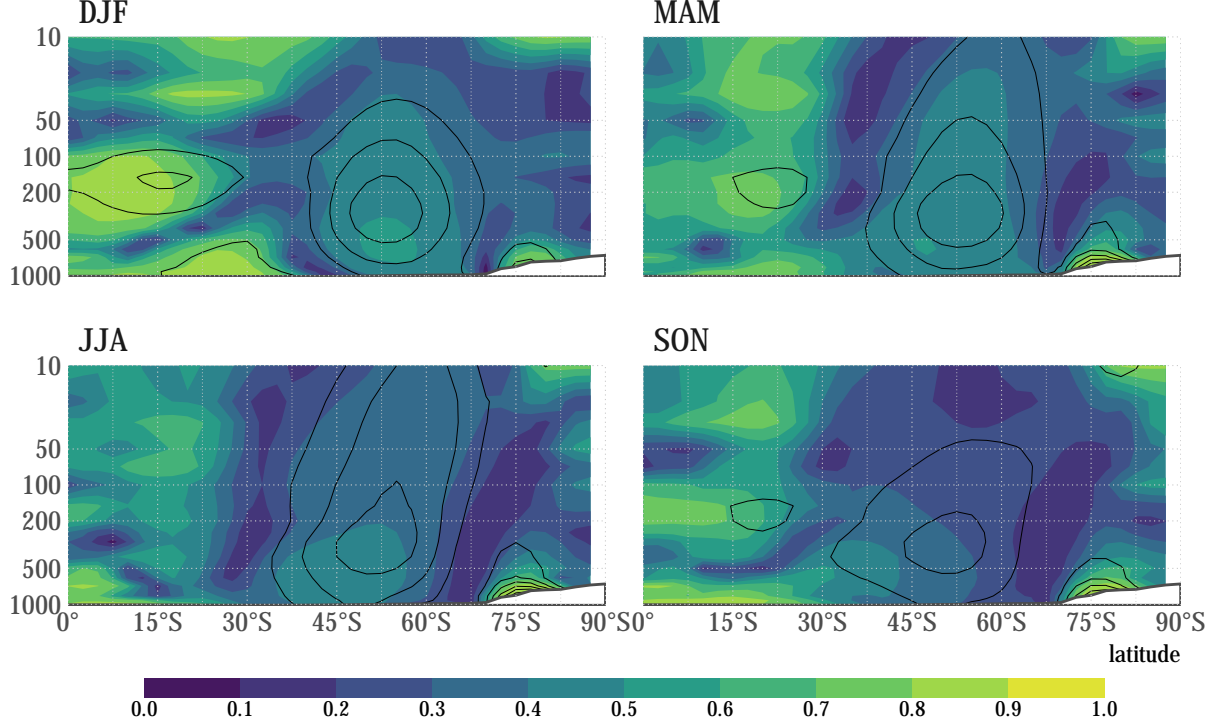


Figure 3: Stat.

vertical structure of the QS3 shows that the expected seasonal cycle in vertical extent is followed by a slight inclination of the disturbances.

Taken together, this suggests a mix of baroclinic and barotropic processes related to the QS3. The former more important during summer and the latter dominating in winter.

Figure 3 shows QS3 steadiness for each trimestre of the year. The highest steadiness can be seen in tropical upper troposphere north of 30°S, specially during the summer.

With the exception of spring, areas of high amplitude (shown in black contours in Figure 3) are colocated with areas of high steadiness –although this metric is maximized at lower levels. While the mean wave amplitude in spring is high (not shown), steadiness is low in the midlatitudes and specially in the stratosphere. This is due primarily by the behaviour during november, when steadiness is so low (reaching  $\sim 0.03$  at 60°S, 500hPa) that wave 3 arguably cannot be considered stationary in the midlatitudes.

As described before, monthly ZW activity can be used as a proxy for QS activity at a monthly scale. Following this an index for the activity of ZW3 was constructed by taking the average amplitude and phase of the wave 3 component in a box with limits between 45°S and 60°S and between 100hPa and 700hPa (shown as a dotted box in Figure 1). The seasonal cycle of the amplitude component is shown in Figure 4 along with the seasonal cycle of the amplitude of the QS3 wave in the same box.

ZW3 activity exhibits a clear annual cycle with higher amplitude during the austral winter months and lower amplitude during the summer months. This annual cycle is consistent with previous work [Loon1972; Karoly1985; Raphael2004]. There is also an annual cycle in variability with winter months showing a high degree of variability compared to summer.

There is no evidence of persistence, periodicities or xxlong time tendencies (not shown).

A comparison with the QS3 cycle (black line in Figure 4) echoes what is seen in Figure 3. Winter months have a low level of steadiness that makes the ZW and QS properties diverge. As suggested previously, the low amplitude of QS3 wave in spring is not due to a reduction in the amplitude of the planetary wave 3 but

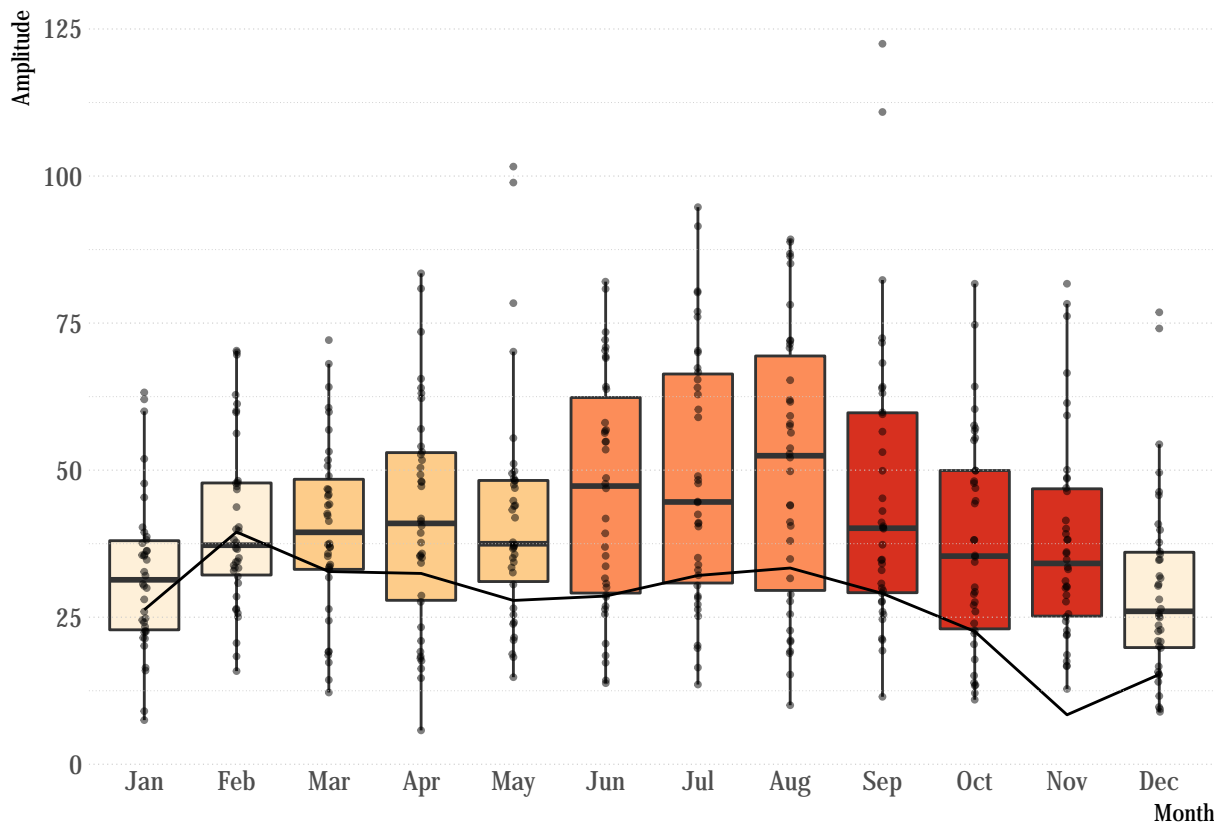


Figure 4: Seasonal cycle of QS3 index.

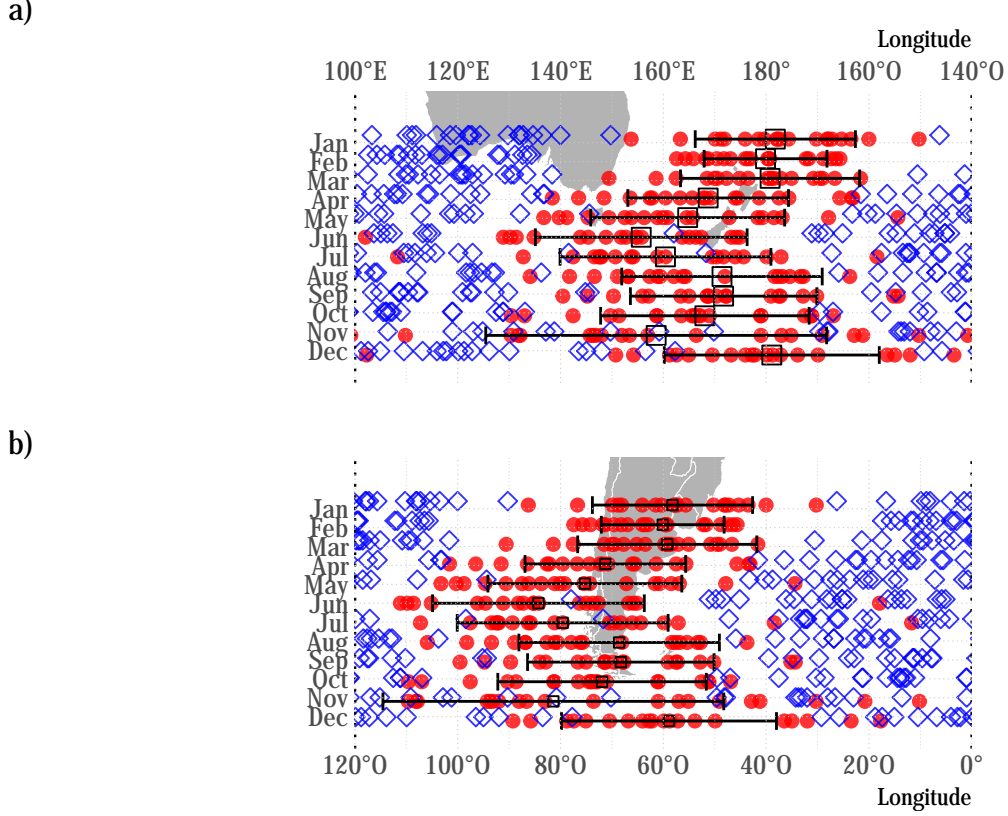


Figure 5: Phase of the mean wave for each month and  $\pm 1$  standard deviation (black dots and error bars). In red and blue, phase of the most intense 20 events for each month, representing the location of the ridge and trough respectively.

to its reduced steadiness. This divergence should guide the interpretation of results based on the index.

Figure 5 shows the mean phase of ZW3. Red circles and blue diamonds represent the position of the geopotential maximum and minimum, respectively. Mean position and  $\pm 1$  standard deviation is shown by black squares and error bars. (XX more about background and x y axis?). The importance of the phase variability in ZW3 can be appreciated in the context of the position of troughs and ridges in relationship to the continents. Ridges can be to the west or to the east of Oceania and South America even on the same month of the year. These very different forced circulations have opposite effects (i.e. advection of cold or warm air), which underscores not only the importance of taking location into account, but also the possibility that this variability could mask those impacts at a climatological level. Also of note is the non-trivial cases of troughs located in areas climatologically high pressure areas. This is specially evident in november.

Ignoring for now the issues of representation, ZW3 index can be regressed with various atmospheric variables to infer the typical structure of the circulation related to high ZW3 activity.

Figure 6 shows regressions between scaled ZW3 index and SST, and 200hPa geopotential height and wave activity flux derived from regressions between scaled ZW3 index and streamfunction at  $0.2101 \sigma$  for each month. All months show evidence of planetary wave 3 activity, but with considerable heterogeneity in its characteristics. In particular, it can be seen that some months (January, May, September and December) are characterised by a wave train emanating from the tropical western Pacific propagating to the southeast and then turning to the northeast. Other months (March, April, July and October) show a much more zonally coherent wave 3 pattern that extends along latitude circles without such a dramatic meridional propagation.

Patterns of SST variation are similarly mixed. There's a strong signal in the equatorial pacific, but it is not consistent, varying between positive (February, May and September) and negative (January, March,



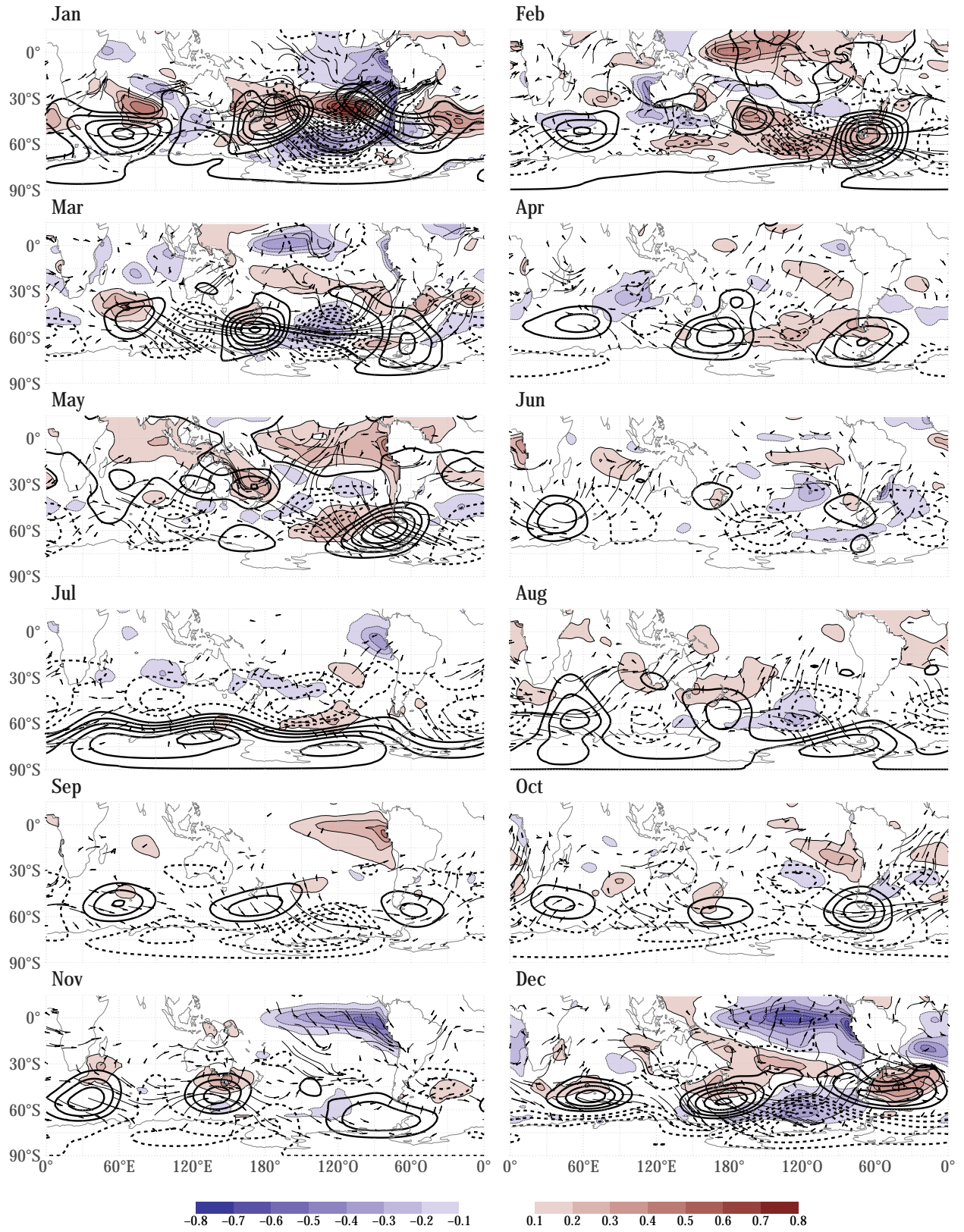


Figure 6: Regression between scaled ZW3 index and SST (shaded) and geopotential height (contours), and wave activity flux derived from regression between ZW3 index and streamfunction at 0.2101 sigma (streamlines).

November and December). This variability is masked when performing regressions or compositions for all months together (not shown) and can probably explain the small signal mentioned in @Renwick2005.

Moreover, the aforementioned problems of using ZW3 amplitude as a measure of QS3 activity puts into question the fundamental validity of the regression analysis using this variable.

## Discussion

ZW amplitude is not a good measure for characterising QS behaviour for several reasons. By ignoring the phase component, it captures waves with one common wavenumber that nevertheless are very different and are excited by different processes. This problem is exacerbated for periods or months that exhibit low levels of steadiness.