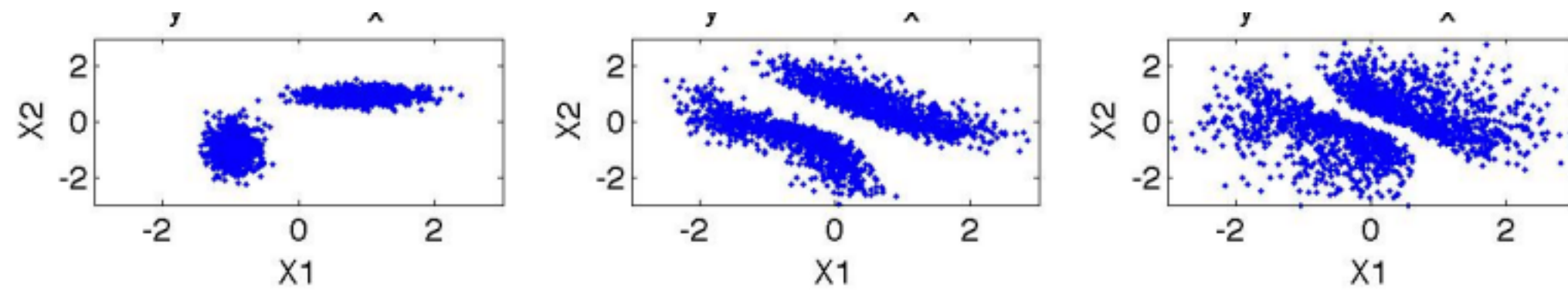


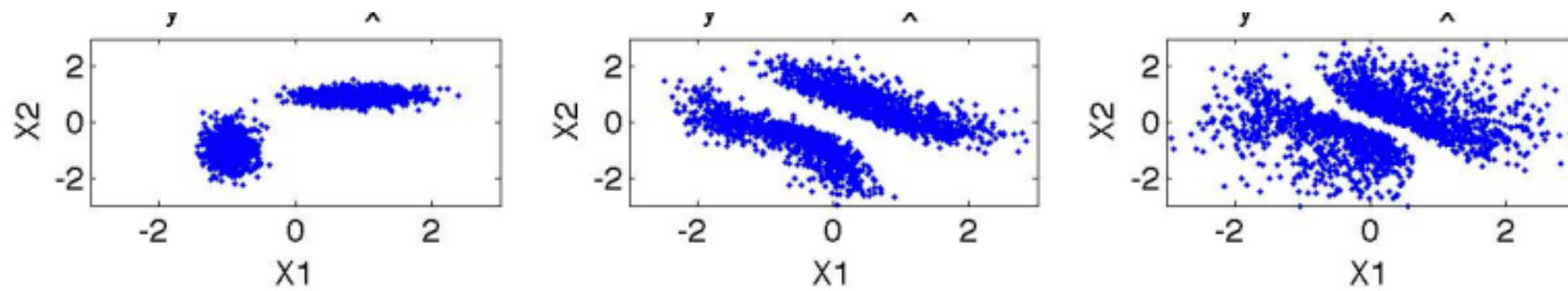
# Normalizing Flow history



**2010**

Tabak, Esteban G., and Cristina V. Turner.  
"A family of nonparametric density estimation  
algorithms."

# Normalizing Flow history



## 3.1 Regularizing the Transformations

We will train the model on data by minimizing an objective composed of several parts:

**Divergence Penalty**  $\mathcal{D}(\Psi)$ : This determines the fit of the current encoding transformation. It forces the marginal densities of the empirical distribution of the representation-space data to match a target distribution of our choice, by penalizing divergence from it.

**Invertibility Measure**  $\mathcal{I}(\Theta)$ : This ensures the invertibility of  $f_{\Theta}(\cdot)$  by penalizing poorly-conditioned transformations.

**Reconstruction Loss**  $\mathcal{R}(\Theta, \Psi)$ : This jointly penalizes the encoder  $g_{\Psi}(\cdot)$  and decoder  $f_{\Theta}(\cdot)$  to ensure that  $g_{\Psi}(y) \approx f_{\Theta}^{-1}(y)$  on the data.

Each of these participates in the overall objective given by:

$$C(\Theta, \Psi) = \mu_{\mathcal{D}}\mathcal{D}(\Theta) + \mu_{\mathcal{I}}\mathcal{I}(\Psi) + \mu_{\mathcal{R}}\mathcal{R}(\Theta, \Psi), \quad (6)$$

where  $\mu_{\mathcal{I}}, \mu_{\mathcal{D}}, \mu_{\mathcal{R}} \in \mathbb{R}$  are the weights of each term. We will examine each of these terms in more detail in the proceeding sections.

**2010**

Tabak, Esteban G., and Cristina V. Turner.  
"A family of nonparametric density estimation algorithms."

**2013**

Rippel, Oren, and Ryan Prescott Adams.

"High-dimensional probability estimation with deep density models."