Training Normalizing Flows

Maximum likelihood training to find parameters θ that make our training samples likely under our parameterized model.

$$\max_{\theta} \mathbb{E}_{\mathbf{x} \sim p_{x}} p_{\theta}(\mathbf{x}) = \min_{\theta} \mathbb{E}_{\mathbf{x} \sim p_{x}} - \log p_{\theta}(\mathbf{x})$$

$$= \min_{\theta} \mathbb{E}_{\mathbf{x} \sim p_{x}} - \log \left[p_{Z}(T_{\theta}(\mathbf{x})) \left| \det \frac{\partial T_{\theta}(\mathbf{x})}{\partial \mathbf{x}} \right| \right]$$

$$= \min_{\theta} \mathbb{E}_{\mathbf{x} \sim p_{x}} \left[\frac{1}{2} ||T_{\theta}(\mathbf{x})||_{2}^{2} - \log \left| \det \frac{\partial T_{\theta}(\mathbf{x})}{\partial \mathbf{x}} \right| \right]$$

$$= \min_{\theta} \frac{1}{N} \sum_{\mathbf{x} \in X_{train}} \left[\frac{1}{2} ||T_{\theta}(\mathbf{x})||_{2}^{2} - \log \left| \det \frac{\partial T_{\theta}(\mathbf{x})}{\partial \mathbf{x}} \right| \right]$$

Training Normalizing Flows

Maximum likelihood training to find parameters θ that make our training samples likely under our parameterized model.

$$\max_{\theta} \mathbb{E}_{\mathbf{x} \sim p_{x}} p_{\theta}(\mathbf{x})$$

Change of variables makes this: ℓ_2 -norm minimization of transformed samples — volume change term.

$$\min_{\theta} \frac{1}{N} \sum_{\mathbf{x} \in X_{train}} \left[\frac{1}{2} ||T_{\theta}(\mathbf{x})||_{2}^{2} - \log \left| \det \frac{\partial T_{\theta}(\mathbf{x})}{\partial \mathbf{x}} \right| \right]$$