Training Normalizing Flows

SLIM

Maximum likelihood training to find parameters θ that make our training samples likely under our parameterized model.

$$\max_{\theta} \mathbb{E}_{\mathbf{x}\sim p_x} p_\theta(\mathbf{x}) = \min_{\theta} \ \mathbb{E}_{\mathbf{x}\sim p_x} - \log p_\theta(\mathbf{x})$$

$$= \min_{\theta} \ \mathbb{E}_{\mathbf{x}\sim p_x} - \log \left[p_Z(T_\theta(\mathbf{x})) \left| \det \frac{\partial T_\theta(\mathbf{x})}{\partial \mathbf{x}} \right| \right]$$

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$$= \min_{\theta} \ \mathbb{E}_{\mathbf{x}\sim p_x} [\frac{1}{2} || T_\theta(\mathbf{x}) ||_2^2 - \log \left| \det \frac{\partial T_\theta(\mathbf{x})}{\partial \mathbf{x}} \right|]$$