Drug Design with diffusion models

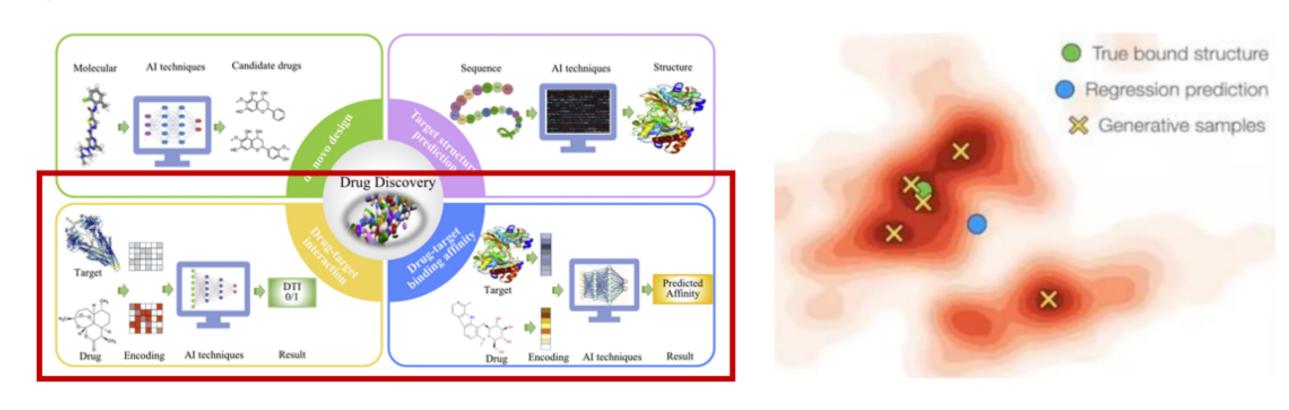
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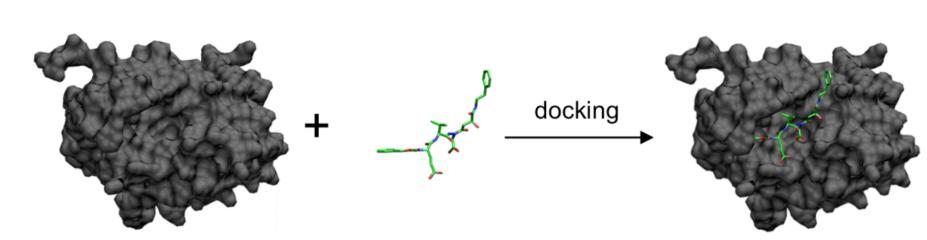


Abstract

- Artificial intelligence, through **generative models**, has emerged as a crucial tool in the realm of **drug discovery**.
- Diffusion models, which utilize **stochastic diffusion equations**, have proven successful in generating new data points to expand the molecular landscape for drug discovery.



- The **DiffDock software** represents a significant innovation in **molecular docking**, a computational technique vital for predicting the binding interactions between small molecules (ligands) and target proteins and the ligand's pose including its position and orientation.
- Molecular docking is essential for determining the potential affinity and stability of the interaction between a ligand and its protein, facilitating the identification of compounds that can effectively bind to **protein sites linked to diseases**. It is crucial for the drug discovery process.



Focus on diffusion models with score-based models

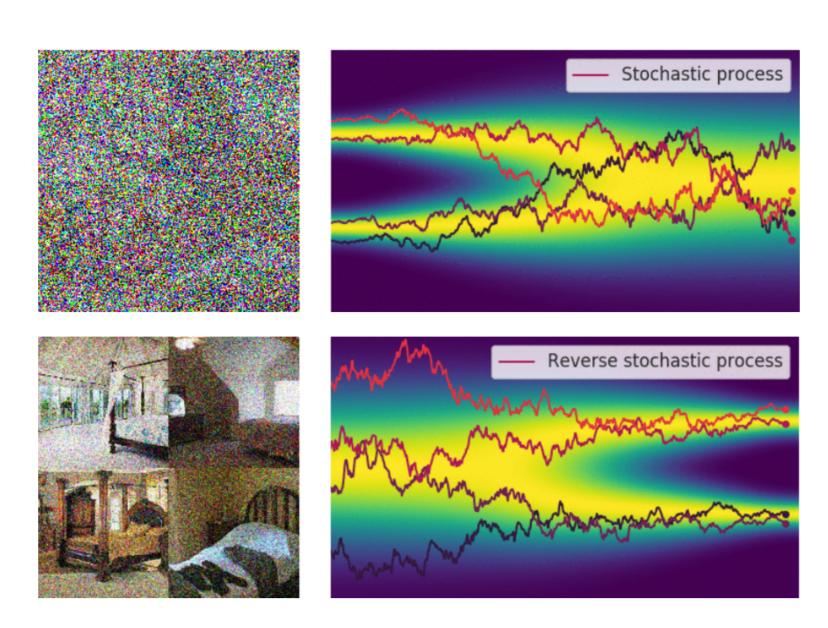
- Diffusion models work by gradually transforming an initial data distribution (noise) into a target data distribution, through an iterative process. This process is guided by models that learn to reverse these diffusions, allowing the generation of samples from noise by following the inverse steps of diffusion.
- Score models learn score functions (gradients of logarithmic probability densities) over many data distributions perturbed by noise through Stochastic Differential Equation (SDE), and then generate samples via the reverse SDE.
- SDEs and their reverse counterparts (reverse SDEs) commonly take the following forms:

$$d\mathbf{X}_t = f(\mathbf{X}_t, t) \, dt + g(t) \, \mathbf{B}_t$$

$$d\mathbf{X}_t = \left[f(\mathbf{X}_t, t) - g^2(t) \nabla_x \log p(\mathbf{X}_t) \right] \, dt + g(t) \, \mathbf{B}_t$$
 Forward SDE (data \rightarrow noise)
$$\mathbf{x}(0) \qquad \mathbf{dx} = \mathbf{f}(\mathbf{x}, t) \, dt + g(t) \, d\mathbf{w} \qquad \mathbf{x}(T)$$

$$\mathbf{x}(0) \qquad \mathbf{dx} = \left[\mathbf{f}(\mathbf{x}, t) - g^2(t) \nabla_\mathbf{x} \log p_t(\mathbf{x}) \right] \, dt + g(t) \, d\bar{\mathbf{w}} \qquad \mathbf{x}(T)$$
 Reverse SDE (noise \rightarrow data)

Process of Diffusion and Reverse Diffusion in Score-based Generative Models



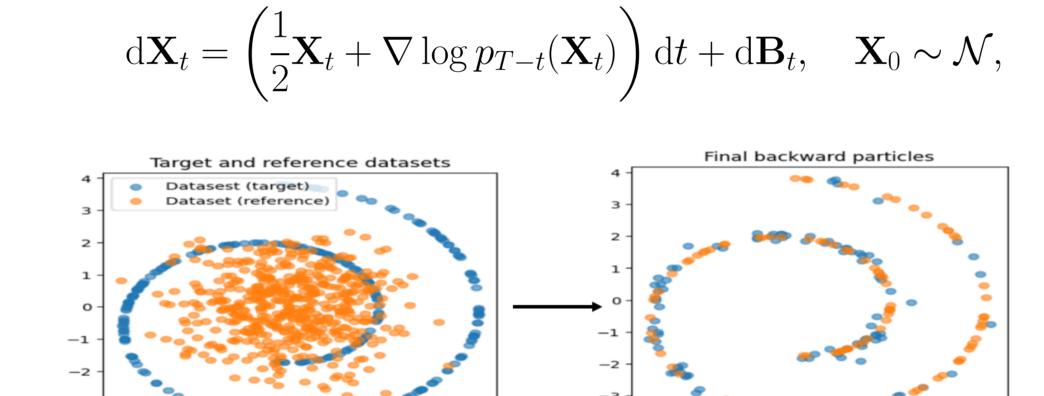
Stochastic Trajectory of Diffusion Models : from Random Noise to Structured Representation with Score Functions

We restrict ourselves to a simple two-dimensional setting and want to generate a spiral distribution from a gaussian distribution

• Forward Noising Process with the following SDE:

$$d\mathbf{X}_t = -\frac{1}{2}\mathbf{X}_t dt + d\mathbf{B}_t, \quad \mathbf{X}_0 \sim \pi,$$

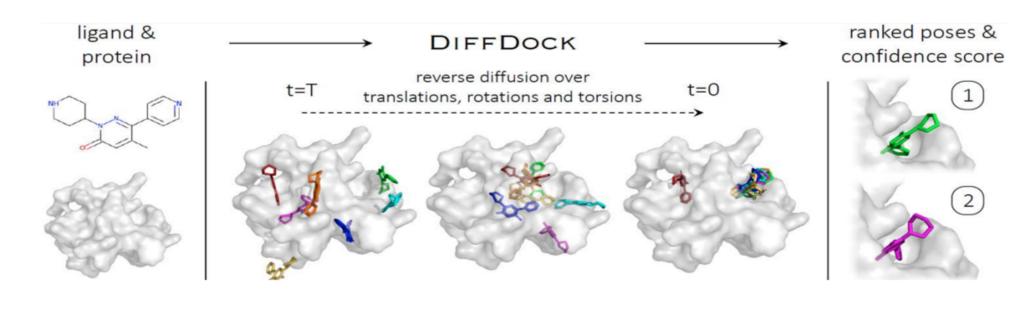
Backward Denoising Process using the reverse SDE :



Reverse Diffusion Process

Diffdock and results

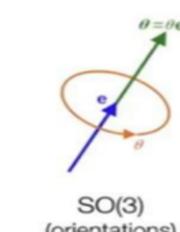
• DiffDock uses diffusion models, to simulate the binding process between ligands and proteins. By temporally reversing stochastic diffusion equations, DiffDock generates **predictions about the optimal position and orientation** of ligand molecules relative to the target protein.

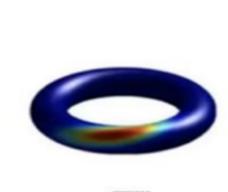


We use the following SDE to generate independently position, orientation and torsion of the ligand on the protein :

$$d\mathbf{X}_t = \sqrt{\frac{d\sigma^2(t)}{dt}}d\mathbf{B}_t$$
 where $\sigma^2 = \sigma_{\mathsf{tr}}^2, \sigma_{\mathsf{rot}}^2$, or σ_{tor}^2 for $T(3), SO(3)$, and $SO(2)^m$

Position $\in \mathbb{R}^3$ Orientation $\in SO(3)$ Torsions $\in \mathbb{T}^m$



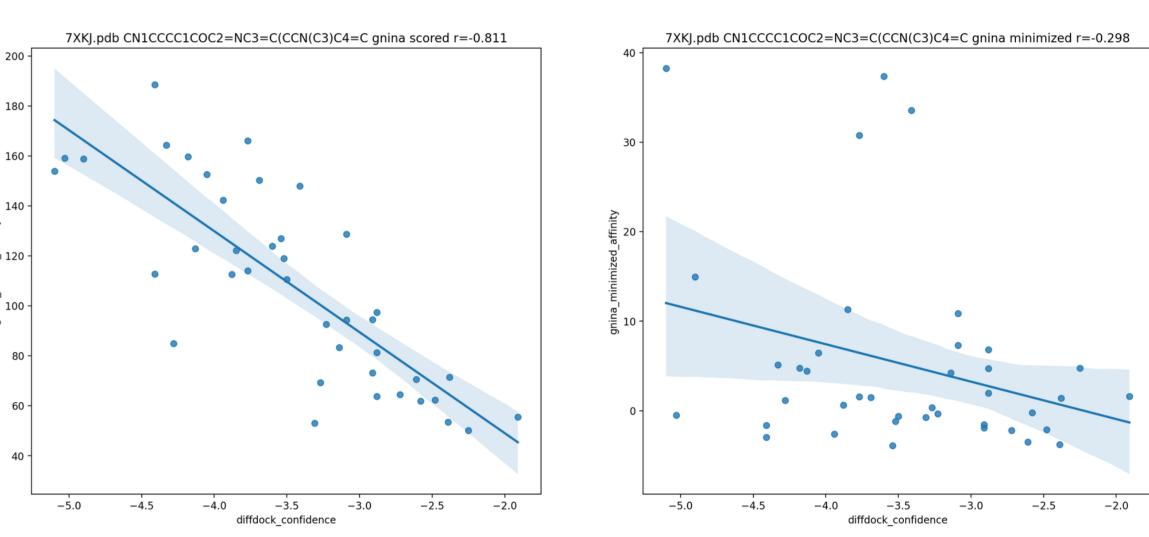


For our DiffDock test, we will focus on KRAS and Adagrasib molecules

- KRAS is a gene encoding the K-Ras protein, crucial in regulating cell growth and differentiation. Mutations in KRAS are prevalent in cancer.
- Adagrasib is an small molecule inhibitor targeting the mutated form of K-Ras. Despite challenges due to the absence of a clear binding pocket, Adagrasib has shown promising anti-tumor activity in clinical studies.

Diffdock confidence score

• DiffDock is a two-step process: we train the diffusion model and a **confidence score** model based on the root mean square distance (RMSD) between the structures.

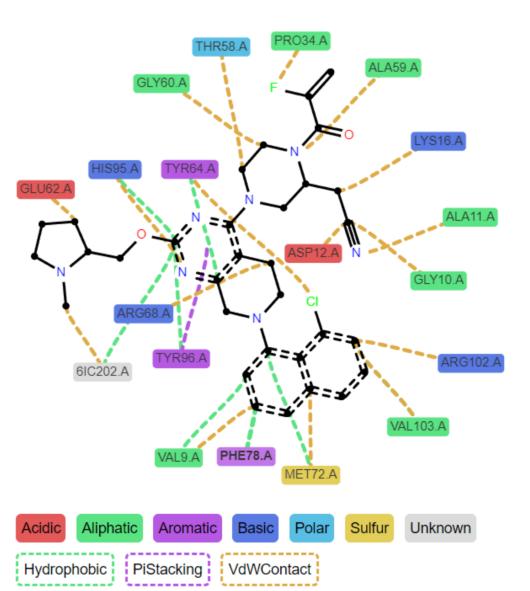


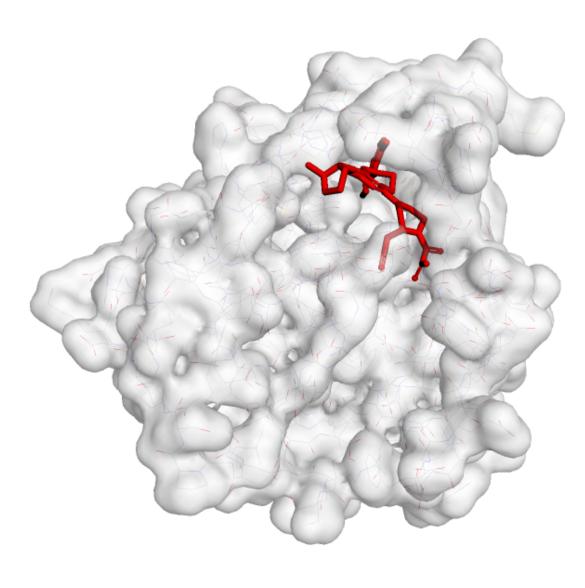
Comparison of DiffDock Confidence with Gnina Predicted Affinity

- We compare our confidence scores with others tools like GNINA affinity scores.
- Then we optimize the ligand's pose by locally minimizing the potential energy of the protein-ligand binding using the GNINA software.
- GNINA employs evolutionary algorithms to explore various ligand conformations and generate a population of ligand poses, evaluate them based on criteria such as energy and interactions. Then, it optimizes the ligand-receptor system energy using numerical optimization methods like gradient descent to find the most stable and favorable pose.

Our DiffDock results

- The different types of chemical interactions could be visualized.
- Such information is crucial for predicting the ligand's **affinity** and **specificity**, as well as for guiding the design of chemical modifications aimed at **enhancing interaction with the target protein**.





Best confidence score result achieved with DiffDock using KRAS and Mirati

References

- [1] G. Corso. Diffdock: Diffusion steps, twists, and turns for molecular docking. https://github.com/gcorso/DiffDock.
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