LALE: Consistent Automated Machine Learning

Guillaume Baudart, Martin Hirzel, Kiran Kate, Parikshit Ram, and Avraham Shinnar IBM Research, USA

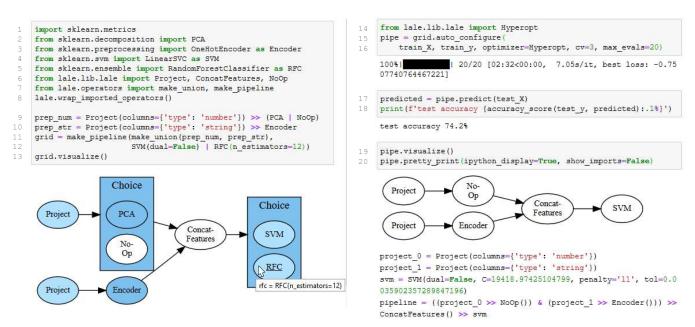


Figure 1: LALE example for consistent automated machine learning, explained in Section 3.

ABSTRACT

Automated machine learning makes it easier for data scientists to develop pipelines by searching over possible choices for hyperparameters, algorithms, and even pipeline topologies. Unfortunately, the syntax for automated machine learning tools is inconsistent with manual machine learning, with each other, and with error checks. Furthermore, few tools support advanced features such as topology search or higher-order operators. This paper introduces LALE, a library of high-level Python interfaces that simplifies and unifies automated machine learning in a consistent way.

1 INTRODUCTION

Machine learning (ML) is widely used in various data science problems. There are many ML *operators* for data preprocessing (scaling, missing imputation, categorical encoding), feature extraction (principal component analysis, non-negative matrix factorization), and modeling (boosted trees, neural networks). A machine learning *pipeline* consists of one or more operators that take the input data through a series of transformations to finally generate predictions. Given the plethora of ML operators (for example, in the widely used scikit-learn library [5]), the task of finding a good ML pipeline for the data at hand (which involves not only selecting operators but also appropriately configuring their hyperparameters) can be tedious and time consuming if done manually. This has led to a wider adoption of automated machine learning (AutoML), with the

development of novel algorithms (such as SMAC [12], hyperopt [3], and subsequent work), open source libraries (auto-sklearn [10], hyperopt-sklearn [4, 14], TPOT [15]), and even commercial tools.

Scikit-learn provides a consistent programming model for manual ML [5], and various other tools (such as XGBoost [6], Light-GBM [13], and Tensorflow's tf.keras.wrappers.scikit_learn) maintain consistency with this model whenever appropriate. AutoML tools usually feature two pieces - (i) a way to define the search space corresponding to the pipeline topology, the operator choices in that topology, and their respective possible hyperparameter configurations, and (ii) an algorithm that explores this search space to optimize for predictive performance. Many of these also try to maintain consistency with the scikit-learn model but only when the user gives up all control and lets the tool completely automate the ML pipeline configuration, eschewing item (i) above. Users often want to retain some control over the automation, for example, to comply with domain-specific requirements by specifying operators or hyperparameter ranges to search over. While fine-grained control over the automation is possible (we will discuss examples), users need to manually configure the search space. This search space specification differs for each of the different AutoML tools and differs from the manual programming model.

We believe that proper *abstractions* are necessary to provide a consistent programming model across the entire spectrum of controlled automation. To this end, we introduce LALE, an open-source Python library¹, built upon mathematically grounded abstractions of the elements of the pipeline (for example, topology, operator, hyperparameter configurations), and designed around scikit-learn [5]

Figure 2: Example for manual scikit-learn pipeline.

Figure 3: Example for scikit-learn GridSearchCV.

and JSON Schema [16]. LALE provides a programming interface for specifying pipelines and search spaces in a consistent manner while providing fine-grained control across the automation spectrum. The abstractions also allow us to provide a consistent programming interface for capabilities for which no such interface currently exists: (i) search spaces with higher-order operators (operators, such as ensembling, that have other operators as hyperparameters), and (ii) search spaces that include search for the pipeline topology via context-free grammars [7]. The contributions of this paper are:

- 1. A pipeline specification syntax that is consistent across the automation spectrum and grounded in established technologies.
- 2. Automatic search space generation from pipelines and schemas for a consistent experience across existing AutoML tools.
- 3. Higher-order operators (for ensembles, batching, etc.) with automatic AutoML search space generation for nested pipelines.
- 4. A grammar syntax for pipeline topology search that is a natural extension of the pipeline syntax.

Overall, we hope LALE will make data scientists more productive at finding pipelines that are consistent with their requirements and yield high predictive performance.

2 PROBLEM STATEMENT

Consistency is a core problem for AutoML and existing libraries fall short on this front. This section uses concrete examples from popular (Auto-)ML libraries to present four shortcomings in existing systems. We strive to do so in a factual and constructive way.

 P_1 : Provide a consistent programming model across the automation spectrum. There is a spectrum of AutoML ranging from manual machine learning (no automation) to hyperparameter tuning, operator selection, and pipeline topology search. Unfortunately, as users progress across this spectrum, the state-of-the-art libraries require them to learn and use different syntax and concepts.

Figure 4: Example for hyperopt-sklearn.

```
estim = AutoSklearnClassifier(
   include_preprocessors=['pca'],
   include_estimators=['liblinear_svc', 'random_forest'],
   time_left_for_this_task=1800, per_run_time_limit=120)
estim.fit(train_X, train_y)
```

Figure 5: Example for auto-sklearn based on SMAC.

Figure 2 shows an example from the no-automation end of the spectrum using scikit-learn [5]. The code assembles a two-step pipeline of a PCA transformer and a Linear SVC classifier and manually sets their hyperparameters, for example, n_components=4.

The example in Figure 3 automates hyperparameter tuning and operator selection using GridSearchCV from scikit-learn. Lines 1–3 resemble Figure 2. Lines 4–11 specify a search space, consisting of a list of two dictionaries. In the first dictionary, Line 7 specifies the list of values to search over for the n_components hyperparameter of the PCA operator; Line 8 specifies the classify step of the pipeline to be a LinearSVC operator; and Line 9 specifies the list of values to search over for the C hyperparameter of the LinearSVC operator. The second dictionary is similar, but specifies the RandomForestClassifier.

The syntax for a pipeline (Figure 2 Lines 1–3) differs from that for a search space (Figure 3 Lines 4–11). The mental model is that operators and hyperparameters are pre-specified and then the search space selectively overwrites them with different choices. To do so, the code uses strings to name steps and hyperparameters, with a double underscore ('__') name mangling convention to connect the two. Relying on strings for names can cause hard-to-detect mistakes [1]. In contrast, using a single syntax for both manual and automated pipelines would make them more consistent and would obviate the need for mangled strings to link between the two.

 P_2 : Provide a consistent programming model across different AutoML tools. Compared to GridSearchCV, Bayesian optimizers such as hyperopt-sklearn [14] and auto-sklearn [10] speed up search using smarter search strategies. Unfortunately, each of these AutoML tools comes with its own syntax and concepts.

Figure 4 shows an example using the hyperopt-sklearn [14] wrapper for hyperopt [3]. Line 1 specifies a discrete search space N with a logarithmic prior, a range from 2..8, and a quantization to multiples of 1. Line 2 specifies a continuous search space C with a logarithmic prior and a range from 1..1000. Line 4 sets the transform step of the pipeline to pca with hyperparameter n_components=N. Lines 5–7 set the classify step to a choice between linear_svc and random_forest.

Figure 5 shows the same example using auto-sklearn [10]. While power users can use the ConfigurationSpace used by SMAC [12] to adjust search spaces for individual hyperparameters, we elide this

¹https://github.com/ibm/lale

for brevity. Line 2 sets the preprocessor to 'pca' and Line 3 sets the classifier to a choice of 'linear_svc' or 'random_forest'.

The syntaxes for the three AutoML tools in Figures 3, 4, and 5 differ. There are three ways to refer to the same operator: PCA, pca(..), and 'pca'. There are three ways to specify an operator choice: a list of dictionaries, hp. choice, and a list of strings. The mental model varies from overwriting to nested configuration to string-based configuration. Users must learn new syntax and concepts for each tool and must rewrite code to switch tools. Moreover, as we consider more sophisticated pipelines (beyond the simple two-step one presented in the example), the search space specifications get even more convoluted and diverse between these existing specification schemes. A unified syntax would make these tools more consistent, easier to learn, and easier to switch. Furthermore, this syntax should unify not just AutoML tools but also be consistent with the manual end of the spectrum (P_1) . More specifically, given that scikit-learn sets the de-facto standard for manual ML, the syntax should be scikit-learn compatible.

*P*₃: Support topology search and higher-order operators in AutoML tools. The tools previously discussed search operators and hyperparameters but do not optimize the topology of the pipeline itself. There are some tools that do, including TPOT [15], Recipe [8], and AlphaD3M [9]. Unfortunately, their methods for specifying the search space are inconsistent with manual machine learning and established tools. TPOT does not allow the user to specify the search space for pipeline topologies (the user can specify the set of operators and can fix the pipeline topology, disabling the topology search). Recipe and AlphaD3M use context-free grammars to specify the search space for the topology, but in a manner inconsistent with each other or with other levels of automation.

Some transformers (e.g. RFE in Figure 6 Line 7) and estimators (e.g. AdaBoostClassifier) are *higher-order*: they take other operators as arguments. Using the AutoML tools discussed so far to search inside their nested operators is not straightforward. The aforementioned TPOT, Recipe, and AlphaD3M do not handle higher-order operators in their search for pipeline topology.

A unified syntax for topology search and higher-order operators that is a natural extension of the syntax for manual machine learning, algorithm selection, and hyperparameter tuning would make AutoML more expressive while keeping it consistent.

*P*₄: Check for invalid configurations early and prune them out of search spaces. Even if the search for each hyperparameter uses a valid range in isolation, their combination can violate side constraints. Worse, these errors may be detected late, wasting time.

Figure 6 shows a misconfigured pipeline: the hyperparameters for LR in Line 7 are valid in isolation but invalid in combination. Unfortunately, this is not detected when the pipeline is created on Line 7. Instead, when Line 10 tries to fit the pipeline, it first fits the first step of the pipeline (see RFE in Line 6). Only then does it try to fit the LR and detect the mistake. This wastes 10 minutes (Line 15).

In contrast, a declarative specification of the side constraints would both speed up this manual example and enable AutoML search space generators to prune cases that violate constraints, thus speeding up the automated case too. Furthermore, in some situations, invalid configurations cause more harm than just wasted

```
from sklearn.pipeline import Pipeline
    from sklearn.feature_selection import RFE
   from sklearn.ensemble import RandomForestClassifier
   from sklearn.linear_model import LogisticRegression as LR
   pipe = Pipeline([
        ('rfe', RFE(RandomForestClassifier(n estimators=10))),
        ('lr', LR(solver='sag', penalty='ll'))])
    %%time
    try:
       pipe.fit(train X, train y)
   except ValueError as e:
       message = str(e)
   print (message, file=sys.stderr)
   CPU times: user 9min 19s, sys: 30 s, total: 9min 49s
   Wall time: 10min 5s
16 Solver sag supports only 12 penalties, got 11 penalty.
```

Figure 6: Example of scikit-learn error checking.

time, leading optimizers astray (Section 6). It is possible (with varying levels of difficulty) to incorporate these side constraints with the search space specification schemes used by the tools discussed earlier, but they each have inconsistent methods for doing this. Moreover, the complexity of these specifications make them error prone. Additionally, while these side constraints help the optimizer, they do not directly help detect misconfigurations (as in Figure 6). Custom validators would need to be written for each tool.

3 PROGRAMMING ABSTRACTIONS

This section shows Lale's abstractions for consistent AutoML, addressing the problem statements $P_1 \wedge P_2 \wedge P_3 \wedge P_4$ from Section 2.

3.1 Abstractions for Declarative AutoML

An *individual operator* is a data science algorithm (aka. a primitive or a model), which may be a transformer or an estimator such as classifier or a regressor. Individual operators are modular building blocks from libraries such as scikit-learn. Figure 1 Lines 2–6 contain several examples, e.g., import LinearSVC as SVM. Mathematically, LALE views an individual operator as a function of the form

$$indivOp: \theta_{\text{hyperparams}} \to \mathcal{D}_{\text{fit}} \to \mathcal{D}_{\text{in}} \to \mathcal{D}_{\text{out}}$$

This view uses *currying*: it views an operator as a sequence of functions each with a single argument and returning the next in the sequence. An individual operator (e.g., SW) is a function from hyperparameters $\theta_{\rm hyperparams}$ (e.g., dual=False) to a function from training data $\mathcal{D}_{\rm fit}$ (e.g., train_X, train_y) to a function from input data $\mathcal{D}_{\rm in}$ (e.g., test_X) to output data $\mathcal{D}_{\rm out}$ (e.g., predicted in Figure 1 Line 17). In the beginning, all arguments are latent, and each step in the sequence captures the next argument as given. The scikitlearn terminology for the three curried sub-functions is init, fit, and predict. Viewing operators as mathematical functions avoids complications arising from in-place mutation. It lets us conceptualize *bindings as lifecycle*: each bound, or captured, argument unlocks the functionality of the next state in the lifecycle.

A *pipeline* is a directed acyclic graph (*DAG*) of operators and a pipeline is itself also an operator. Since a pipeline contains operators and is an operator, it is highly composable. Furthermore, viewing both individual operators and pipelines as special cases of *operators* makes the concepts more consistent. An example

is make_pipeline(make_union(PCA, RFC), SVM), which is equivalent to ((PCA & RFC) >> ConcatFeatures >> SVM). Here, & is the and combinator and >> is the pipe combinator. Combinators make edges more explicit and code more concise. An expression x & y composes x and y without introducing additional edges. An expression x >> y introduces edges from all sinks of subgraph x to all sources of y. Mathematically, LALE views a pipeline as a function of the form

$$pipeline: \theta_{topology} \rightarrow \theta_{hyperparams} \rightarrow \mathcal{D}_{fit} \rightarrow \mathcal{D}_{in} \rightarrow \mathcal{D}_{out}$$

This uses currying just like individual operators, plus an additional $\theta_{\mathrm{topology}}$ at the start to capture the steps and edges. A pipeline is trainable if both $\theta_{\mathrm{topology}}$ and $\theta_{\mathrm{hyperparams}}$ are given, i.e., the hyperparameters of all steps have been captured. To fit a trainable pipeline, iterate over the steps in a topological order induced by the edges. For each step s, let $\mathcal{D}_{\mathrm{fit}}^s$ be the training data for the step, which is either the pipeline's training data if s is a source or the predecessors' output data $\mathcal{D}_{\mathrm{fit}}^s = [\mathcal{D}_{\mathrm{out}}^p]_{p \in preds(s)}$ otherwise. Then, recalling that s is a curried function, calculate $s_{\mathrm{trained}} = s(\mathcal{D}_{\mathrm{fit}}^s)$ and $\mathcal{D}_{\mathrm{out}}^s = s_{\mathrm{trained}}(\mathcal{D}_{\mathrm{fit}}^s)$. The trained pipeline substitutes trained steps for trainable steps in $\theta_{\mathrm{topology}}$. To make predictions with a trained pipeline, simply interpret >> as function composition \circ .

An *operator choice* is an exclusive disjunction of operators and is itself also an operator. Operator choice specifies algorithm selection, and by being an operator, addresses problem P_1 from Section 2. An example is (SVM | RFC), where | is the *or combinator*. Mathematically, LALE views an operator choice as a function of the form

$$opChoice: \theta_{steps} \rightarrow \theta_{hyperparams} \rightarrow \mathcal{D}_{fit} \rightarrow \mathcal{D}_{in} \rightarrow \mathcal{D}_{out}$$

This again uses currying. Argument $\theta_{\rm steps}$ is the list of operators to choose from. The $\theta_{\rm hyperparams}$ of an operator choice consists of an indicator for which of its steps is being chosen, along with the hyperparameters for that chosen step. Once $\theta_{\rm hyperparams}$ is captured, the operator choice is equivalent to just the chosen step, as shown in the visualization after Figure 1 Line 20.

The *combined schema* of an operator specifies the valid values along with search guidance for its latent arguments. It addresses problem P_4 from Section 2, supporting automated search with a pruned search space and early error checking all from the same single source of truth. Consider the pipeline PCA >> (J48 | LR), where PCA and LR are the principal component analysis and logistic regression from scikit-learn and J48 is a decision tree with pruning from Weka [11]. These operators have many hyperparameters and constraints and LALE handles all of them. For didactic purposes, this section discusses only a representative subset. Figure 7 shows the JSON Schema [16] specification of that subset. The open-source LALE library includes JSON schemas for many operators, some handwritten and others auto-generated [2]. The number of components for PCA is given by N, which can be a continuous value in (0..1)or the categorical value *mle*. The prior distribution helps AutoML tools search faster. J48 has a categorical hyperparameter R to enable reduced error pruning and a continuous confidence threshold C for pruning. Mathematically, we denote allOf as ∧, anyOf as ∨, and not as \neg . Even though the valid values for C are (0..1), search should only consider values $C \in (0..0.5)$. The constraint in Lines 16–19 encodes a conditional (R = true) \Rightarrow (C = 0.25) by using the equivalent $\neg (R = true) \lor (C = 0.25)$. LR has two categorical hyperparameters S (solver) and P (penalty), with a constraint that solvers sag

```
PCA: {
     type: object,
     properties: {
       N: { anyOf: [
         { description: "Amount of variance to explain",
            type: number, minimum: 0.0, maximum: 1.0,
            distribution: uniform},
          { description: "Guess with Minka's MLE", enum: [mle]}]}}}
     { type: object,
       properties: {
         R: { description: "Use reduced error pruning", type: boolean },
          C: { description: "Pruning confidence threshold",
               type: number, minimum: 0.0, maximum: 1.0,
14
               maximumForOptimizer: 0.5, distribution: uniform }}},
     { description: "Setting confidence makes no sense for R",
          { not: { type: object, properties: {R: {enum: [true]}}}},
         { type: object, properties: {C: {enum: [0.25]}}}}}}
19
   LR: { allOf: [
     { type: object,
       properties: {
         S: { description: "Optimization problem solver",
               enum: [linear, sag, lbfgs], default: linear},
24
          P: { description: "Penalization norm",
               enum: [11, 12], default: 12}}},
     { description: "Solvers sag and lbfgs support only 12.",
         { not: { type: object, properties: {S: {enum: [sag, lbfgs]}}}},
         { type: object, properties: {P: {enum: [12]}}}]}]
```

Figure 7: JSON Schemas for hyperparameters.

and *lbfgs* only support penalty *l2*, which we already encountered in Figure 6. Going forward, we will denote a JSON Schema object with **properties** as dict{} and a JSON Schema **enum** as []. Eliding priors, this means Figure 7 becomes:

```
\begin{split} PCA: & \operatorname{dict}\{N:(0..1) \lor [mle])\} \\ \mathcal{J}48: & \operatorname{dict}\{R:[true, false], C:(0..0.5)\} \land \\ & (\operatorname{dict}\{R:[true]\} \Rightarrow \operatorname{dict}\{C:[0.25]\}) \\ LR: & \operatorname{dict}\{S:[linear, sag, lbfgs], P:[l1, l2]\} \land \\ & (\operatorname{dict}\{S:[sag, lbfgs]\} \Rightarrow \operatorname{dict}\{P:[l2]\}) \end{split}
```

To auto-configure an operator means to automatically capture $\theta_{\text{hyperparams}}$, which involves jointly selecting algorithms (for operator choices) and tuning hyperparameters (for individual operators). We saw examples for doing this with scikit-learn's Grid-SearchCV [5], hyperopt-sklearn [14], and auto-sklearn [10] in Figures 3, 4, and 5. Lale offers a single unified syntax shown in Figure 1 Lines 15–16 to address problem P_2 from Section 2. Mathematically, let op be either an individual operator or a pipeline or choice whose θ_{topology} or θ_{steps} are already captured. That means op has the form $\theta_{\text{hyperparams}} \rightarrow \mathcal{D}_{\text{fit}} \rightarrow \mathcal{D}_{\text{in}} \rightarrow \mathcal{D}_{\text{out}}$. Then $auto_configure(op, \mathcal{D}_{\text{fit}})$ returns a function of the form $\mathcal{D}_{\text{in}} \rightarrow \mathcal{D}_{\text{out}}$. Section 4 discusses how to implement $auto_configure$ using schemas.

3.2 Abstractions for Controlled AutoML

AutoML users rarely want to completely surrender all decisions to the automation. Instead, users typically want to control certain decisions based on their problem statement and expertise. This section discusses how LALE supports such *controlled* AutoML.

```
from xgboost import XGBRegressor as Forest
import lale.schemas as schemas
lale.wrap_imported_operators()
Grove = Forest.customize_schema(
n_estimators=schemas.Int(min=2, max=6),
booster=schemas.Enum(['gbtree']))
```

Figure 8: Example for custom schemas.

The *lifecycle state* of an operator is the number of curried arguments it has already captured that determines the functionality it supports. To enable controlled AutoML, LALE pipelines can mix operators with different states. The visualizations in Figure 1 indicate lifecycle states via colors. A *planned* operator, shown in dark blue, has captured only θ_{topology} or θ_{steps} , but $\theta_{\text{hyperparams}}$ is still latent. Planned operators support auto_configure but not fit or predict. A *trainable* operator, shown in light blue, has also captured $\theta_{\text{hyperparams}}$, leaving \mathcal{D}_{fit} latent. Trainable operators support auto_configure and fit but not predict. A *trained* operator, shown in white, also captures \mathcal{D}_{fit} . Trained operators support auto_configure, fit, and predict. Later states subsume the functionality of earlier states, enabling user control over where automation is applied. The state of a pipeline is the least upper bound of the states of its steps.

Partially captured hyperparameters of an individual operator treat some of its hyperparameters as given while keeping the remaining ones latent. Specifying some hyperparameters by hand lets users control and hand-prune the search space while still searching other hyperparameters automatically. For example, Figure 1 Line 12 shows partially captured hyperparameters for SVM and RFC. The visualization after Line 13 reflects this in a tooltip for RFC. And the pretty-printed code after Line 20 shows that automation respected the given dual hyperparameter of SVM while capturing the latent C, penalty, and tol. Individual operators with partially captured hyperparameters are trainable: fit uses defaults for latents.

Freezing an operator turns future auto_configure or fit operations into an identity. $PCA(n_components=4)$. freeze_trainable() >> SVM freezes all hyperparameters of PCA (using defaults for its latents), so auto_configure on this pipeline tunes only the hyperparameters of SVM. Similarly, on a trained operator, freeze_trained() freezes its learned coefficients, so any subsequent fit call will ignore its new \mathcal{D}_{fit} . Freezing part of a pipeline speeds up (Auto-)ML.

A custom schema derives a variant of an individual operator that differs only in its schema. Custom schemas can modify ranges or distributions for search. As an extreme case, users can attach custom schemas to non-Lale operators to enable hyperparameter tuning on them—the call to wrap_imported_operators in Figure 1 Line 8 implicitly does that. Figure 8 shows how to explicitly customize a schema. Line 2 imports helper functions for expressing JSON Schema in Python. XGBoost implements a forest of boosted trees, so to get a small forest (a Grove), Line 5 restricts the number of trees to [2..6]. Line 6 restricts the booster to a constant, using a singleton enum. Afterwards, Grove is an individual operator like any other. Mathematically, we can view the ability to attach a schema to an individual operator as extending its curried function on the left:

```
indivOp: \theta_{schemas} \rightarrow \theta_{hyperparams} \rightarrow \mathcal{D}_{fit} \rightarrow \mathcal{D}_{in} \rightarrow \mathcal{D}_{out}
```

```
pipeline = make_pipeline(
    MinMaxScaler | StandardScaler | Normalizer
    | RobustScaler | QuantileTransformer,
    AdaBoostClassifier(base_estimator=DecisionTreeClassifier))
```

Figure 9: Example for higher-order operator.

```
g = Grammar()
  g.start = g.est | (g.clean >> g.est) | (g.tfm >> g.est) \
            | (g.clean >> g.tfm >> g.est)
           = (g.clean1 >> g.clean) | g.clean1
  g.tfm
           = (g.tfm1 >> g.tfm) | g.tfm1
  g.clean1 = SimpleImputer | MissingIndicator
  g.tfm1
           = PCA | OrdinalEncoder \
           OneHotEncoder(handle_unknown='ignore')
           = GaussNB | RidgeClassifier | LinearSVC | SGDClassifier
  g.est
  grid = g.unfold(3)
13
pipe = grid.auto_configure(
      train_X, train_y, optimizer=Hyperopt, cv=3, max_evals=100)
```

Figure 10: Example grammar inspired by AlphaD3M.

3.3 Abstractions for Expressive AutoML

A higher-order operator is an operator that takes another operator as an argument. Scikit-learn includes several higher-order operators including RFE, AdaBoostClassifier, and BaggingClassifier. The nested operator is a hyperparameter of the higher-order operator and the nested operator can have hyperparameters of its own. Finding the best predictive performance requires AutoML to search both outside and inside higher-order operators. Figure 9 shows an example higher-order AdaBoostClassifier with a nested DecisionTreeClassifier. On the outside, AutoML should search the operator choice in Lines 2–3 and the hyperparameters of AdaBoostClassifier such as n_estimators. On the inside, AutoML should tune the hyperparameters of DecisionTreeClassifier. LALE searches both jointly, helping solve problem P_3 from Section 2. The JSON schema of the base_estimator hyperparameter of AdaBoostClassifier is:

```
{ description: "Base estimator from which the ensemble is built.",
anyOf: [
typeForOptimizer: "operator"},
enum: [null]}],
default: null}
```

A pipeline grammar is a context-free grammar that describes a possibly unbounded set of pipeline topologies. A grammar describes a search space for the $\theta_{topology}$ and θ_{steps} arguments needed to create planned pipelines and operator choices. Grammars formalize AutoML tools for topology search such as TPOT [15], Recipe [8], and AlphaD3M [9] that capture $\theta_{topology}$ and θ_{steps} automatically. Lale provides a grammar syntax that is a natural extension of concepts described earlier, helping solve problem P_3 from Section 2.

Figure 10 shows a LALE grammar inspired by the AlphaD3M paper [9]. It describes linear pipelines comprising zero or more data cleaning operators, followed by zero or more transformers, followed by exactly one estimator. This is implemented via recursive non-terminals: g.clean on Line 5 is a recursive definition, and so is g.tfm on Line 6, implementing a search space with sub-pipelines of

Figure 11: Example grammar inspired by TPOT.

unbounded length. While AlphaD3M uses reinforcement learning to search over this grammar, Figure 10 does something far less sophisticated. Line 13 unfolds the grammar to depth 3, obtaining a bounded planned pipeline, and Line 14 searches that using hyperopt, with no further modifications required.

Figure 11 shows a Lale grammar inspired by TPOT [15]. It describes possibly *non-linear* pipelines, which use not only >> but also the & combinator. Recall that (x & y) >> Concat applies both x and y to the same data and then concatenates the features from both. Besides transformers, Line 6 also uses estimators with &, turning their predictions into features for downstream operators. This is not supported in scikit-learn pipelines but is supported in Lale.

Progressive disclosure is a design technique that makes things easier to use by only requiring users to learn new features when and as they need them. The starting point for LALE is manual machine learning, and thus, the scikit-learn code in Figure 2 is also valid LALE code. User needs to learn zero new features if they do not use AutoML. To use algorithm selection, users only need to learn about the | combinator and the auto_configure function. To express pipelines more concisely, users can learn about the >> and & combinators, but those are optional syntactic sugar for make_pipeline and make_union from scikit-learn. To use hyperparameter tuning, users only need to learn about wrap_imported_operators. To exercise more control over the search space, users can learn about freeze and custom schemas. While schemas are a non-trivial concept, LALE expresses them in JSON Schema [16], which is a widely-adopted and well-documented standard proposal. To use higher-order operators, users need not learn new syntax, as LALE supports scikit-learn syntax for them. Finally, to use grammars, users need to add 'g.' in front of their pipeline definitions; however, all the other features, such as the | combinator and the auto_configure function, continue to work the same with or without grammars.

4 SEARCH SPACE GENERATION

This section describes how to map the programming model from Section 3 to work directly with three popular AutoML tools: scikit-learn's GridSearchCV [5], hyperopt [4], and SMAC [12], the library behind auto-sklearn [10].

4.1 From Grammars to Planned Pipelines

LALE offers two approaches for using a grammar with GridSearch-CV, hyperopt, and SMAC: unfolding and sampling. Both approaches produce a planned pipeline, which can be directly used as the input for the compiler in Section 4.2. Unfolding and sampling are merely intended as proof-of-concept baseline implementations. In the future, we will also explore integrating LALE grammars directly with AutoML tools that support them, such as AlphaD3M [9].

Unfolding first expands the grammar to a given depth, such as 3 in the example from Figure 10 Line 13. Then, it prunes all disjuncts containing unresolved nonterminals, so that only planned LALE operators (individual, pipeline, or choice) remain.

Sampling traverses the grammar by following each nonterminal, picking a random step in each choice, and unfolding each pipeline. The result is a planned pipeline without any operator choices.

4.2 From Planned Pipelines to Existing Tools

This section sketches how to map a planned pipeline (which includes a topology, steps for operator choices, and schemas for individual operator) to a search space in the format required by Grid-SearchCV, hyperopt, or SMAC. The running example for this section is the pipeline PCA \gg (J48 | LR) with the individual operator schemas in Figure 7.

Lale's search space generator has two phases: normalizer and backend. The normalizer translates the schemas of individual operators separately. The backend combines the schemas for the entire pipeline and finally generates a tool-specific search space.

The *normalizer* processes the schema for an individual operator in a bottom-up pass. The desired end result is a search space in Lale's *normal form*, which is \lor (dict{cat*, cont*}*). At each level, the normalizer simplifies children and hoists disjunctions up.

```
 PCA: \operatorname{dict}\{N: (0..1)\} \vee \operatorname{dict}\{N: [\mathit{mle}]\} \\  348: \operatorname{dict}\{R: [\mathit{false}], C: (0..0.5)\} \vee \operatorname{dict}\{R: [\mathit{true}, \mathit{false}], C: [0.25]\} \\  LR: \operatorname{dict}\{S: [\mathit{linear}], P: [\mathit{l1}, \mathit{l2}]\} \vee \operatorname{dict}\{S: [\mathit{linear}, \mathit{sag}, \mathit{lbfgs}], P: [\mathit{l2}]\}
```

The backend starts by first *combining* the search spaces for all operators in the pipeline. Each pipeline becomes a 'dict' over its steps; each operator choice becomes an ' \lor ' over its steps with added discriminants D to track what was chosen; and each individual operator simply comes from the normalizer. This yields an intermediate representation (IR) whose nesting structure reflects the operator nesting of the original pipeline. For our running example, this is:

$$\det \begin{cases} 0 : \det\{N : \{0..1\}\} \lor \det\{N : [mle]\} \\ \det\{D : [\mathcal{J}48], R : [false], C : \{0..0.5\}\} \lor \\ \det\{D : [\mathcal{J}48], R : [true, false], C : \{0..25\}\} \rbrace \lor \\ \det\{D : [\mathcal{L}R], S : [linear], P : [l1, l2]\} \lor \\ \det\{D : [\mathcal{L}R], S : [linear, sag, lbfgs], P : [l2]\} \end{cases})$$

The remainder of the backend is specific to the targeted AutoML tools, which the following text describes one by one.

The *hyperopt backend* of Lale is the simplest because hyperopt supports nested search space specifications that are conceptually similar to the Lale IR. For instance, an exclusive disjunction 'V' from the IR can be translated into a hyperopt hp.choice, an example for which occurs in Figure 4 Line 5. Similarly, a 'dict' from the IR can be translated into a Python dictionary that hyperopt understands.

For working with higher-order operators, LALE adds additional markers that enable it to reconstruct nested operators later.

The SMAC backend has to flatten Lale's nested IR into a grid of disjuncts with discriminants D. To do this, it internally uses a name mangling encoding that extends the $_$ mangling of scikit-learn, an example for which occurs in Figure 3 Line 7. Each element of the grid needs to be a simple 'dict' with no further nesting. For our running example, the result in mathematical notation is:

```
dict{N: (0..1), D: [J48], R: [false], C: (0..0.5)}

\( \) dict{N: (0..1), D: [J48], R: [true, false], C: [0.25] }

\( \) dict{N: [mle], D: [J48], R: [false], C: (0..0.5)}

\( \) dict{N: [mle], D: [J48], R: [true, false], C: [0.25] }

\( \) dict{N: (0..1), D: [LR], S: [linear], P: [l1, l2] }

\( \) dict{N: (0..1), D: [LR], S: [linear, sag, lbfgs], P: [l2] }

\( \) dict{N: [mle], D: [LR], S: [linear], P: [l1, l2] }

\( \) dict{N: [mle], D: [LR], S: [linear, sag, lbfgs], P: [l2] }
```

Next, the SMAC backend adds conditionals that tell the Bayesian optimizer which variables are relevant for which disjunct, and finally outputs the search space in SMAC's PCS format.

The *GridSearchCV backend* starts from the same flattened grid representation that is also used by the SMAC backend. Then, it discretizes each continuous hyperparameter into a categorical by first including the default and then sampling a user-configurable number of additional values from its range and prior distribution (such as uniform in Figure 7 Line 7). The generated search space in mathematical notation is:

```
\begin{aligned} & \operatorname{dict}\{N:[0.50,0.01], D:[\mathcal{J}48], R:[false], C:[0.25,0.01]\} \\ & \vee \operatorname{dict}\{N:[0.50,0.01], D:[\mathcal{J}48], R:[true,false], C:[0.25]\} \\ & \vee \operatorname{dict}\{N:[mle], D:[\mathcal{J}48], R:[false], C:[0.25,0.01]\} \\ & \vee \operatorname{dict}\{N:[mle], D:[\mathcal{J}48], R:[true,false], C:[0.25]\} \\ & \vee \operatorname{dict}\{N:[0.50,0.01], D:[LR], S:[linear], P:[l1,l2]\} \\ & \vee \operatorname{dict}\{N:[0.50,0.01], D:[LR], S:[linear, sag, lbfgs], P:[l2]\} \\ & \vee \operatorname{dict}\{N:[mle], D:[LR], S:[linear], P:[l1,l2]\} \\ & \vee \operatorname{dict}\{N:[mle], D:[LR], S:[linear, sag, lbfgs], P:[l2]\} \end{aligned}
```

5 IMPLEMENTATION

This section highlights some of the trickier parts of the Lale implementation, which is entirely in Python.

To implement *lifecycle states*, Lale uses Python subclassing. For example, the Trainable is a subclass of Planned, adding a fit method. Subclassing lets users treat an operator as also still belonging to an earlier state, e.g., in a mixed-state pipeline. The Lale implementation adds Python 3 type hints so users can get additional help from tools such as MyPy, PyCharm, or VSCode.

To implement the *combinators* », &, and |, Lale uses Python's overloaded __rshift__, __and__, and __or__ methods. Python only supports overriding these as instance methods. Therefore, unlike in scikit-learn, Lale planned operators are object instances, not classes. This required emulating the scikit-learn __init__ with __call__.

The implementation carefully avoids in-place mutation of operators by methods such as auto_configure, fit, customize_schema, or unfold. This prevents unintended side effects and keeps the implementation consistent with the mathematical function abstractions from Section 3.1. Unfortunately, in scikit-learn, fit does in-place mutation, so for compatibility, LALE supports that but with a deprecation warning.

```
prep = ( NoOp | MinMaxScaler | StandardScaler | Normalizer | RobustScaler )

feat = ( NoOp | PCA | PolynomialFeatures | Nystroem )

clf = ( GaussianNB | GradientBoostingClassifier | SVC | KNeighborsClassifier | RandomForestClassifier | ExtraTreesClassifier | QuadraticDiscriminantAnalysis | PassiveAggressiveClassifier | DecisionTreeClassifier | LogisticRegression | XGBClassifier | LGBMClassifier )

lale_openml_pipeline = prep >> feat >> clf
```

Figure 12: Pipeline for OpenML experiment.

The implementation lets users *import operators directly from* their source packages. For example, see Figure 1 Lines 2–5. However, these operators need to then support the combinators and have attached schemas. Lale supports that via wrap_imported_operators(), which reflects over the symbol table and replaces any known non-Lale operators by an object that points to the non-Lale operator and augments it with Lale operator functionality.

The implementation supports interoperability with PyTorch, Weka, and R operators. This is demonstrated by Lale's operators from PyTorch (BERT, ResNet50), Weka (J48), and R (ARulesCBA). Supporting them requires, first, a class that is scikit-learn compatible. While this is easy for some cases (e.g., XGBoost), it is sometimes non-trivial. For instance, for Weka, Lale uses javabridge. Second, each operator needs a JSON schema for its hyperparameters. This is eased by Lale's customize_schema API.

The implementation of grammars had to overcome the core difficulty that recursive nonterminals require being able to use a name before it is defined. Python does not allow that for local variables. Therefore, Lale grammars implement it with object attributes instead. More specifically, Lale grammars use overloaded __getattr__ and __setattr__ methods.

6 RESULTS

This section evaluates Lale on OpenML classification tasks and on different data modalities. It also experimentally demonstrates the importance of side constraints for the optimization process. For each experiment, we specified a Lale search space and then used auto_configure to run hyperopt on it. The value proposition of Lale is to leverage existing AutoML tools effectively and consistently; in general, we do not expect Lale to outperform them.

6.1 Benchmarks: OpenML Classification

To demonstrate the use of LALE, we designed four experiments that specify different search spaces for OpenML classification tasks.

lale-pipe: The three-step planned lale_openml_pipeline in Figure 12.

lale-ad3m: The AlphaD3M-inspired grammar of Figure 10 unfolded with a maximal depth of 3.

lale-tpot: The TPOT-inspired grammar of Figure 11 unfolded with a maximal depth of 3.

lale-adb: The higher-order operator pipeline of Figure 9.

For comparison, we used auto-sklearn [10] — a popular scikit-learn based AutoML tool that has won two OpenML challenges — with its default setting as a baseline. We chose 15 OpenML datasets for which we could get meaningful results (more than 30 trials)

	Absolute accuracy (mean and standard deviation over 5 runs)					100 * (accuracy/Autoskl - 1)				
Dataset	AUTOSKL	LALE-PIPE	LALE-TPOT	LALE-AD3M	LALE-ADB	ASKL-ADB	LALE-PIPE	LALE-TPOT	LALE-AD3M	LALE-ADB
australian	85.09 (0.44)	85.44 (0.72)	85.88 (0.57)	86.84 (0.00)	86.05 (1.62)	84.74 (3.11)	0.41	0.93	2.06	1.13
blood	77.89 (1.39)	76.28 (5.22)	77.49 (2.46)	74.74 (0.74)	77.09 (0.74)	74.74 (0.84)	-2.08	-0.52	-4.05	-1.04
breast-cancer	73.05 (0.58)	71.16 (1.20)	71.37 (1.15)	69.47 (3.33)	70.95 (2.05)	72.42 (0.47)	-2.59	-2.31	-4.90	-2.88
car	99.37 (0.10)	98.25 (1.16)	99.12 (0.12)	92.71 (0.63)	98.28 (0.26)	98.25 (0.25)	-1.13	-0.25	-6.70	-1.09
credit-g	76.61 (1.20)	74.85 (0.52)	74.12 (0.55)	74.79 (0.40)	76.06 (1.27)	76.24 (1.02)	-2.29	-3.24	-2.37	-0.71
diabetes	77.01 (1.32)	77.48 (1.51)	76.38 (1.11)	77.87 (0.18)	75.98 (0.48)	75.04 (1.03)	0.61	-0.82	1.12	-1.33
hill-valley	99.45 (0.97)	99.25 (1.15)	100.0 (0.00)	96.80 (0.21)	100.00 (0.00)	99.10 (0.52)	-0.20	0.55	-2.66	0.55
jungle-chess	88.06 (0.24)	90.29 (0.00)	88.90 (2.05)	74.14 (2.02)	89.41 (2.29)	86.87 (0.20)	2.54	0.96	-15.80	1.53
kc1	83.79 (0.31)	83.48 (0.75)	83.48 (0.54)	83.62 (0.23)	83.30 (0.36)	84.02 (0.31)	-0.38	-0.38	-0.21	-0.58
kr-vs-kp	99.70 (0.04)	99.34 (0.07)	99.43 (0.00)	96.83 (0.14)	99.51 (0.10)	99.47 (0.16)	-0.36	-0.27	-2.87	-0.19
mfeat-factors	98.70 (0.08)	97.58 (0.28)	97.18 (0.50)	97.55 (0.07)	97.52 (0.40)	97.94 (0.08)	-1.14	-1.54	-1.17	-1.20
phoneme	90.31 (0.39)	89.06 (0.67)	89.56 (0.36)	76.57 (0.00)	90.11 (0.45)	91.36 (0.21)	-1.39	-0.83	-15.20	-0.22
shuttle	87.27 (11.6)	99.94 (0.01)	99.93 (0.04)	99.89 (0.00)	99.98 (0.00)	99.97 (0.01)	14.51	14.50	14.45	14.56
spectf	87.93 (0.86)	87.24 (1.12)	88.45 (2.25)	83.62 (6.92)	88.45 (2.63)	89.66 (2.92)	-0.78	0.59	-4.90	0.59
sylvine	95.42 (0.21)	95.00 (0.61)	94.41 (0.75)	91.31 (0.12)	95.15 (0.20)	95.07 (0.14)	-0.45	-1.07	-4.31	-0.29

Table 1: Accuracy for 15 OpenML classification tasks

using the default settings of Auto-sklearn. The selected datasets comprise 5 simple classification tasks (test accuracy > 90% in all our experiments) and 10 harder tasks (test accuracy < 90%). For each experiment, we used a 66% - 33% validation-test split, and a 5-fold cross validation on the validation split during optimization. Experiments were run on a 32 cores (2.0GHz) virtual machine with 128GB memory, and for each task, the total optimization time was set to 1 hour with a timeout of 6 minutes per trial.

Table 1 presents the results of our experiments. For each experiment, we report the test accuracy of the best pipeline found averaged over 5 runs. Note that for the *shuttle* dataset, 3 out of 5 runs of auto-sklearn resulted in a MyDummyClassifier being returned as the result. Since we were trying to evaluate the default settings, we did not attempt debugging it, but according to the tool's issue log, other users have encountered it before. The column *askl-adb* reports the accuracy of auto-sklearn when the set of classifiers is limited to AdaBoost with only data pre-processing. These results are presented for comparison with the *lale-adb* experiments, as the data preprocessing operators in Figure 9 were chosen to match those of auto-sklearn as much as possible. Also note that the default setting for auto-sklearn uses meta-learning.

The results show that carefully crafted search spaces (e.g., TPOT-inspired grammar, or pipelines with higher-order operators) and off-the-shelf optimizers such as hyperopt can achieve accuracies that are competitive with state-of-the-art tools. These experiments thus validate Lale's controlled approach to AutoML as an alternative to black-box solutions. In addition, these experiments illustrate that Lale is modular enough to easily express and compare multiple search spaces for a given task.

6.2 Case Studies: Other Modalities

While all the examples so far focused on tasks for tabular datasets, the core contribution of LALE is not limited to those. This section demonstrates LALE's versatility on three datasets from different modalities. Table 2 summarizes the results.

Text. We used the Drug Review dataset for predicting a rating given by a patient to a drug. The Drug Review dataset has a text column called review, to which the pipeline applies either TfidfVectorizer

Table 2: Performance of the best pipeline using LALE with hyperopt. The mean and stdev are over 3 runs.

MODALITY	DATASET	MEAN	STDEV	METRIC
Text	Drug Review	1.9237	0.06	test RMSE
Image	CIFAR-10	93.53%	0.11	test accuracy
Time-series	Epilepsy	73.15%	8.2	test accuracy

from scikit-learn or a pretrained BERT embeddings, which is a text embedding based on neural networks. The dataset also has numeric columns, which are concatenated with the result of the embedding.

```
planned_pipeline = (
    Project(columns=['review']) >> (BERT | TfidfVectorizer)
    & Project(columns={'type': 'number'})
    >> Cat >> (LinearRegression | XGBRegressor)
```

Image. We used the CIFAR-10 computer vision dataset. We picked the ResNet50 deep-learning model, since it has been shown to do well on CIFAR-10. Our experiments kept the architecture of ResNet50 fixed and tuned learning-procedure hyperparameters.

Time-series. We used the Epilepsy dataset, a subset of the TUH Seizure Corpus, for classifying seizures by onset location (generalized or focal). We used a three-step pipeline:

We implemented a popular pre-processing method [17] in a Window operator with three hyperparameters W, O, and T. Note that this transformer leads to multiple samples per seizure. Hence, during evaluation, each seizure is classified by taking a vote of the predictions made by each sample generated from it.

6.3 Effect of Side Constraints on Convergence

LALE's search space compiler takes rich hyperparameter schemas including side constraints and translates them into semantically equivalent search spaces for different AutoML tools. This raises the question of how important those side constraints are in practice.

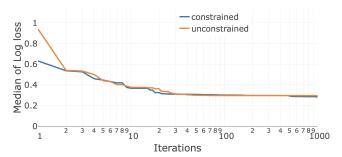


Figure 13: Convergence with planned pipeline LR | KNN.

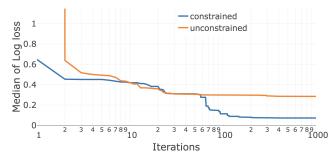


Figure 14: Convergence with planned pipeline J48 | LR | KNN.

To explore this, we did an ablation study where we generated not just the constrained search spaces that are default with LALE but also unconstrained search spaces that drop side constraints. With hyperopt on the unconstrained search space, some iterations are unsuccessful due to exceptions, for which we reported np.float.max loss. Figure 13 plots the convergence for the Car dataset on the planned pipeline LR | KNN. Both of these operators have a few side constraints. Whereas the unconstrained search space causes some invalid points early in the search, the two curves more-or-less coincide after about two dozen iterations. The story looks very different in Figure 14 when adding a third operator J48 | LR | KNN. In the unconstrained case, J48 has many more invalid runs, causing hyperopt to see so many np.float.max loss values from J48 that it gives up on it. In the constrained case, on the other hand, J48 has no invalid runs, and hyperopt eventually realizes that it can configure J48 to obtain substantially better performance.

6.4 Dataset Details

In order to be specific about the exact datasets for reproducibility, Table 3 report the URLs for accessing those.

7 RELATED WORK

There are various search tools, designed around scikit-learn [5], and each usually focused on a particular novel optimization algorithm. Auto-sklearn [10] uses the search space specification and optimization algorithm of SMAC [12]. Hyperopt-sklearn [14] uses its own search space specification scheme and a novel optimizer based on Tree-structured Parzen Estimators (TPE) [3]. Scikit-learn also comes with its own GridSearchCV and RandomizedSearchCV classes. Auto-Weka [18] is a predecessor of auto-sklearn that also uses SMAC but operates on operators from Weka [11] instead of

Table 3: Dataset details for reproducibility.

Dataset	URL
australian	https://www.openml.org/d/40981
blood	https://www.openml.org/d/1464
breast-cancer	https://www.openml.org/d/13
car	https://www.openml.org/d/40975
credit-g	https://www.openml.org/d/31
diabetes	https://www.openml.org/d/37
hill-valley	https://www.openml.org/d/1479
jungle-chess	https://www.openml.org/d/41027
kc1	https://www.openml.org/d/1067
kr-vs-kp	https://www.openml.org/d/3
mfeat-factors	https://www.openml.org/d/12
phoneme	https://www.openml.org/d/1489
shuttle	https://www.openml.org/d/40685
spectf	https://www.openml.org/d/337
sylvine	https://www.openml.org/d/41146
CIFAR-10	https://en.wikipedia.org/wiki/CIFAR-10
Drug Review	https://archive.ics.uci.edu/ml/datasets/Drug+Revi+
	Dataset+%28Drugs.com%29
Epilepsy	https://www.ncbi.nlm.nih.gov/pmc/articles/
	PMC6246677

scikit-learn. TPOT [15] is designed around scikit-learn and uses genetic programming to search for pipeline topologies and operator choices. This usually leads to the generation of many misconfigured pipelines, wasting execution time. RECIPE [8] prunes away the misconfigurations to save execution time by validating generated pipelines with a grammar for linear pipelines. AlphaD3M [9] makes use of a grammar in a generative manner (instead of just for validation) with a deep reinforcement learning based algorithm. In contrast to these tools, the contribution of this paper is not a novel optimization algorithm but rather a more consistent programming model with search space generation targeting existing tools.

8 CONCLUSION

This paper describes Lale, a library for semi-automated data science. Lale contributes a syntax that is consistent with scikit-learn, but extends it to support a broad spectrum of automation including algorithm selection, hyperparameter tuning, and topology search. Lale works by automatically generating search spaces for established AutoML tools, extending their capabilities to grammar-based search and to search inside higher-order operators. The experiments show that search spaces crafted using Lale achieve results that are competitive with state-of-the-art tools while offering more versatility.

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