8) Le système à la date
$$t_N$$
 vaut :
$$\alpha_{N-1}(S_{t_{N-1}}^{(N)})(1+h_N)S_{t_{N-1}}^{(N)}+\beta_{N-1}(S_{t_{N-1}}^{(N)})S_{t_N}^0=f((1+h_N)S_{t_{N-1}}^{(N)}) \eqno(1)$$

$$\alpha_{N-1}(S_{t_{N-1}}^{(N)})(1+b_N)S_{t_{N-1}}^{(N)} + \beta_{N-1}(S_{t_{N-1}}^{(N)})S_{t_N}^0 = f((1+b_N)S_{t_{N-1}}^{(N)})$$
 [2]

[1] - [2] donne:

$$\alpha_{N-1}(S_{t_{N-1}}^{(N)}) = \frac{f((1+h_N)S_{t_{N-1}}^{(N)}) - f((1+b_N)S_{t_{N-1}}^{(N)})}{(h_N - b_N)S_{t_{N-1}}^{(N)}}$$

 $(1+h_N)[1]-(1+b_N)[2]$ donne:

$$\beta_{N-1}(S_{t_{N-1}}^{(N)}) = \frac{1}{S_{t_N}^0(h_N - b_N)} (f((1+b_N)S_{t_{N-1}}^{(N)})(1+h_N) - f((1+h_N)S_{t_{N-1}}^{(N)})(1+b_N))$$

9) Le système à la date t_k vaut :

$$\alpha_{k-1}(S_{t_{k-1}}^{(N)})(1+h_N)S_{t_{k-1}} + \beta_{k-1}(S_{t_{k-1}}^{(N)})S_{t_k}^0 = v_k((1+h_N)S_{t_{k-1}}^{(N)})$$
[1]

$$\alpha_{k-1}(S_{t_{k-1}}^{(N)})(1+b_N)S_{t_{k-1}} + \beta_{k-1}(S_{t_{k-1}}^{(N)})S_{t_k}^0 = v_k((1+b_N)S_{t_{k-1}}^{(N)})$$
 [2]

Ce qui donne, par un raisonnement analogue :

$$\alpha_{k-1}\big(S_{t_{k-1}}^{(N)}\big) = \frac{v_k((1+h_N)S_{t_{k-1}}^{(N)}) - v_k((1+b_N)S_{t_{k-1}}^{(N)})}{(h_N - b_N)S_{t_{k-1}}^{(N)}}$$

$$\beta_{k-1}(S_{t_{k-1}}^{(N)}) = \frac{1}{S_{t_k}^0(h_N - b_N)} (v_k((1 + b_N)S_{t_{k-1}}^{(N)}(1 + h_N) - v_k((1 + h_N)S_{t_{k-1}}^{(N)}(1 + b_N)))$$