

```
In[84]:= Charting`$InteractiveHighlighting = False
```

```
Out[84]=
```

False

```
In[85]:= SetOptions[SelectedNotebook[],  
    PrintingStyleEnvironment → "Printout", ShowSyntaxStyles → True]
```

```
In[86]:= n = 15; (* Points to sample along each connection *)
```

```
In[87]:= path = N@With[{ $\mathbf{r} = \{0, 0, 0\}$ ,  $\mathbf{x} = \{0, 1, 0\}$ ,  $\mathbf{w} = \{\frac{1}{2}, 1, 0\}$ ,  $\mathbf{l} = \{\frac{1}{2}, \frac{1}{2}, \frac{1}{2}\}$ ,  
     $\mathbf{k} = \{\frac{3}{4}, \frac{3}{4}, 0\}$ ,  $\mathbf{u} = \{\frac{1}{4}, 1, \frac{1}{4}\}$ }, { $\mathbf{l}, \mathbf{k}, \mathbf{u}, \mathbf{w}, \mathbf{r}, \mathbf{x}, \mathbf{w}, \mathbf{l}, \mathbf{r}, \mathbf{k}, \mathbf{u}, \mathbf{x}$ }];
```

```
(* The list of high-symmetry points *)
```

```
kPts = N@Subdivide[ $\#1$ ,  $\#2$ , n] &@@@ Partition[path, 2, 1] // Flatten[ $\#$ , 1] & //  
    DeleteAdjacentDuplicates; (* List of n points sampled along  
    each line of the path going through the high-symmetry points,  
    it's literally the points generated by traversing the line,  
    although not in equal steps *)
```

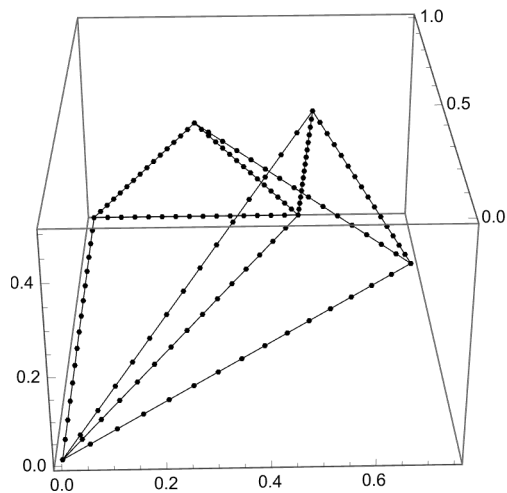
```
Length@kPts (* Total count of the sampling points *)
```

```
Graphics3D[{Point[ $\#$ ] & /@ kPts, Line[path]}, Axes → True]
```

```
Out[89]=
```

166

```
Out[90]=
```



```

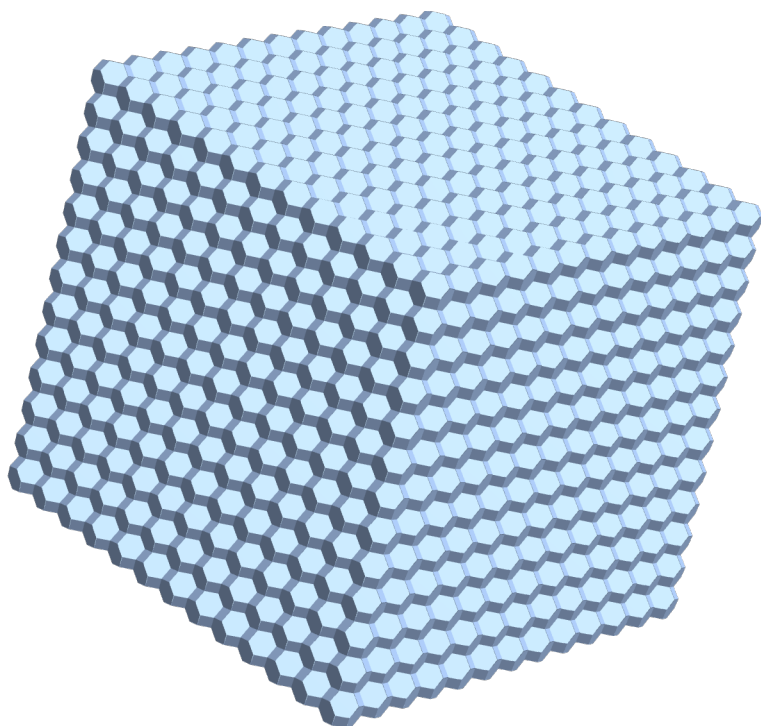
In[91]:= basis = N@{{1, -1, 1}, {1, 1, -1}, {-1, 1, 1}}; (* The basis for the G *)
G = Tuples[N@Range[-7, 7], 3].basis;
(* All possible combinations that give the G points *)
Length@G (* Number of sampled points *)
(* 1BZ represented for a bcc lattice *)
eee = VoronoiMesh[G];
hm = HighlightMesh[eee, Style[2, Directive[Red]]];
eee = MeshRegion[MeshCoordinates[hm], MeshCells[hm, {3, "Interior"}]]

```

Out[93]=

3375

Out[96]=



In[97]:=

```

In[98]:= (*Export["~/Downloads/test3d.stl",
MeshPrimitives[BoundaryMesh[eee], 2] // RegionUnion, "STL"] *)

```

In[99]:=

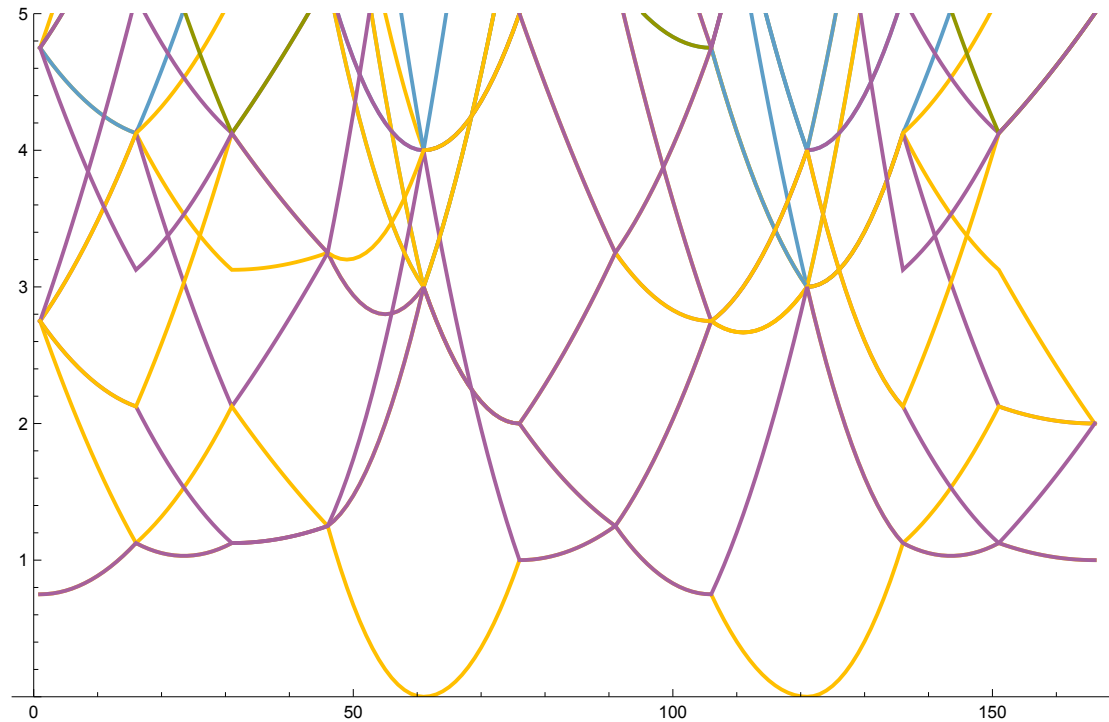
In[100]:=

```

ens = With[{allCombs = Tuples[{kPts, G}] // Partition[#, Length@G] &},
  Norm[#1 - #2]^2 & @@@ # & /@ allCombs] // Transpose;
(* Energy levels calculated along the path traced in the
  first Brillouin zone for a bcc lattice *)
ListLinePlot[ens, ImageSize → Large, PlotRange → {0, 5}]

```

Out[101]=



## 3D DOS (bulk)

In[102]:=

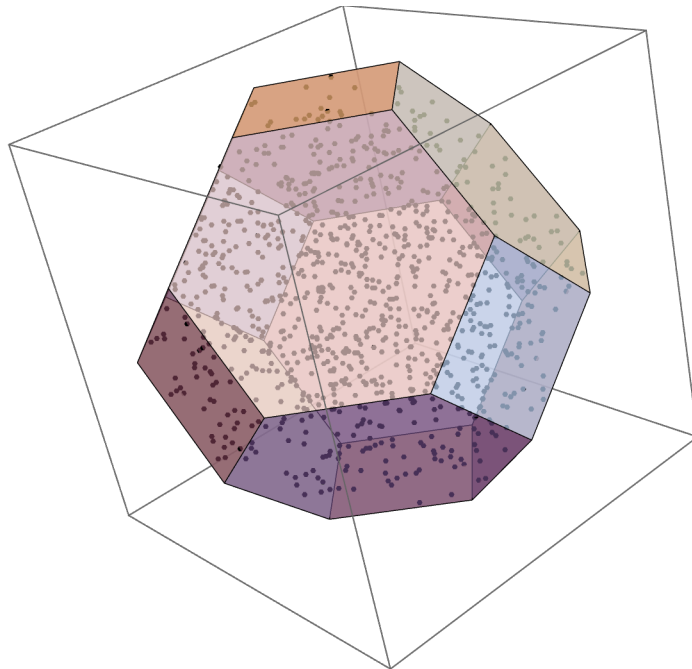
```

firstBz = With[{G = Tuples[Range[-1, 1], 3].basis}, Select[
  MeshPrimitives[VoronoiMesh[G], 3], RegionMember[#, {0, 0, 0}] &] // First];

```

```
In[103]:=
kPts = RandomPoint[firstBz, 103];
Graphics3D[{Style[firstBz, Opacity[0.7]], Point@kPts}]
RegionMeasure[firstBz]
```

Out[104]=



Out[105]=

4.

In[106]:=

```
(*Export["~/Downloads/firstBz.stl",firstBz,"STL"]*)
```

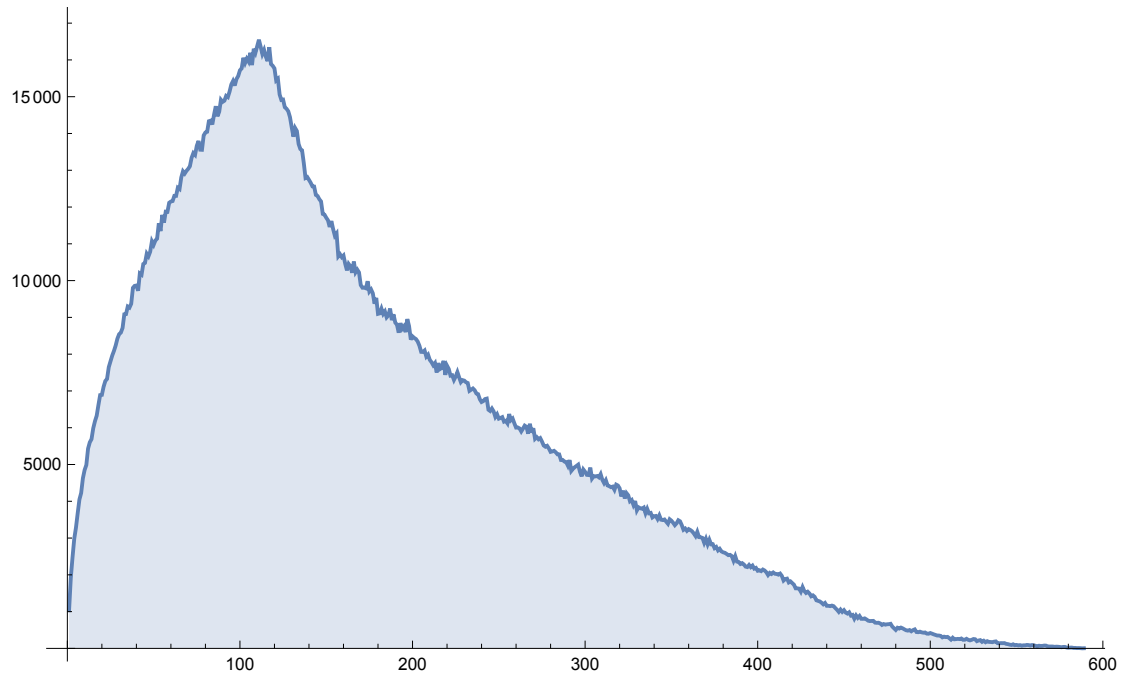
In[107]:=

```
G = Tuples[N@Range[-7, 7], 3].basis;
(* All possible combinations that give the G points *)
allCombs = Tuples[{kPts, G}] // Partition[#, Length@G] &;
eVals = Norm[#1 - #2]2 & @@@ # & /@ allCombs // Transpose;
```

In[110]:=

```
(* Plot of the density of states as a function of energy *)
Show[BinCounts[Flatten@eVals] //
  ListLinePlot[#, ImageSize → Large, Filling → Axis, PlotRange → All] &,
  Plot[dosFit["BestFit"], {x, 0, 130}, PlotStyle → {Dashed, Orange, Thick}],
  PlotRange → All]
```

Out[110]=

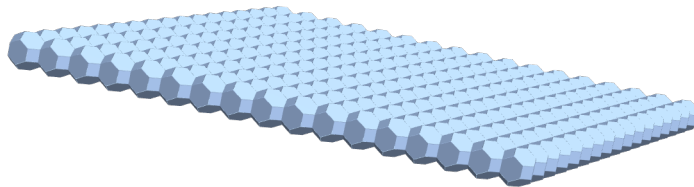


## 2D DOS part (quantum well)

In[111]:=

```
n = 1;
basis2d = {{1, -1, 1}, {1, 1, -1}, {-1, 1, 1}}; (* The basis for the G *)
gen = Select[Tuples[Range[-9, 9], 3], Abs[#[[3]]] ≤ n &];
G2d = gen.basis2d;
vm = VoronoiMesh[G2d];
hm = HighlightMesh[vm, Style[2, Directive[Red]]];
vm = MeshRegion[MeshCoordinates[hm], MeshCells[hm, {3, "Interior"}]]
```

Out[117]=



In[118]:=

```
(*Export["~/Downloads/test2d.stl",
  MeshPrimitives[BoundaryMesh[vm], 2] // RegionUnion, "STL" *)
```

In[119]:=

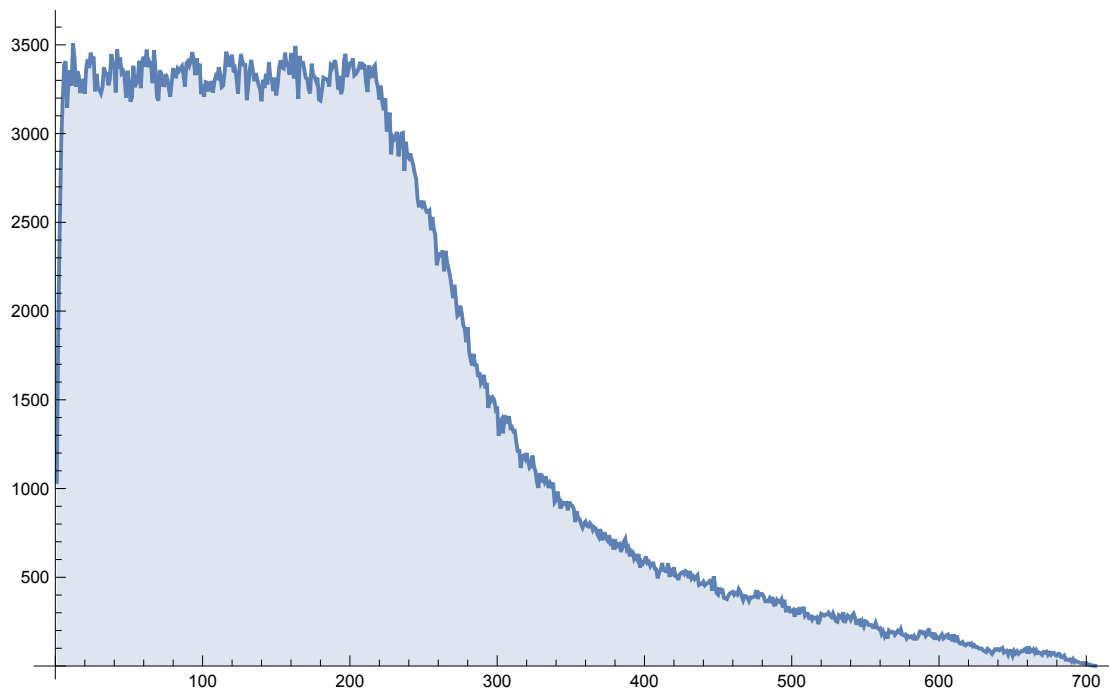
In[120]:=

```
allCombs = Tuples[{kPts, G2d}] // Partition[#, Length@G2d] &;
eVals = Norm[#1 - #2]2 & @@@ # & /@ allCombs // Transpose;
```

In[122]:=

```
(* Plot of the density of states as a function of energy *)
BinCounts[Flatten@eVals] //
  ListLinePlot[#, ImageSize → Large, PlotRange → All, Filling → Axis] &
```

Out[122]=



## 1D DOS part (quantum wire)

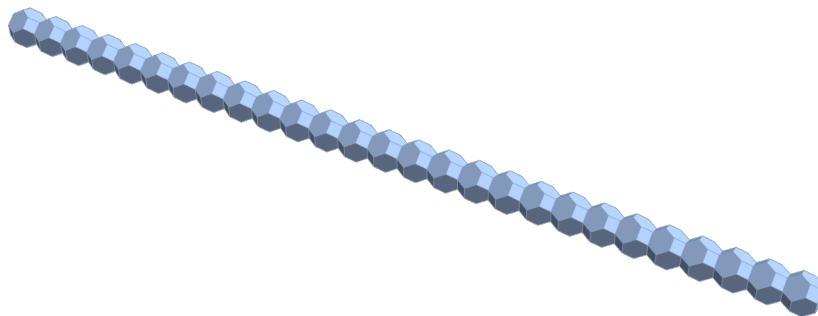
In[123]:=

```
n = 1
basis1d = {{1, -1, 1}, {1, 1, -1}, {-1, 1, 1}}; (* The basis for the G *)
gen1 =
  Select[Tuples[Range[-14, 14], 3], #[[3]] ≤ n && #[[3]] ≥ -n && #[[2]] ≤ n && #[[2]] ≥ -n &];
G1d = gen1.basis1d;
vm1 = VoronoiMesh[G1d];
hm = HighlightMesh[vm1, Style[2, Directive[Red]]];
vm1 = MeshRegion[MeshCoordinates[hm], MeshCells[hm, {3, "Interior"}]]
```

Out[123]=

1

Out[129]=



In[130]:=

```
mp = MeshPrimitives[BoundaryMesh[vm1], 2] // RegionUnion;
```

In[131]:=

```
(*Export["~/Downloads/test1d.stl",mp, "STL"]*)
```

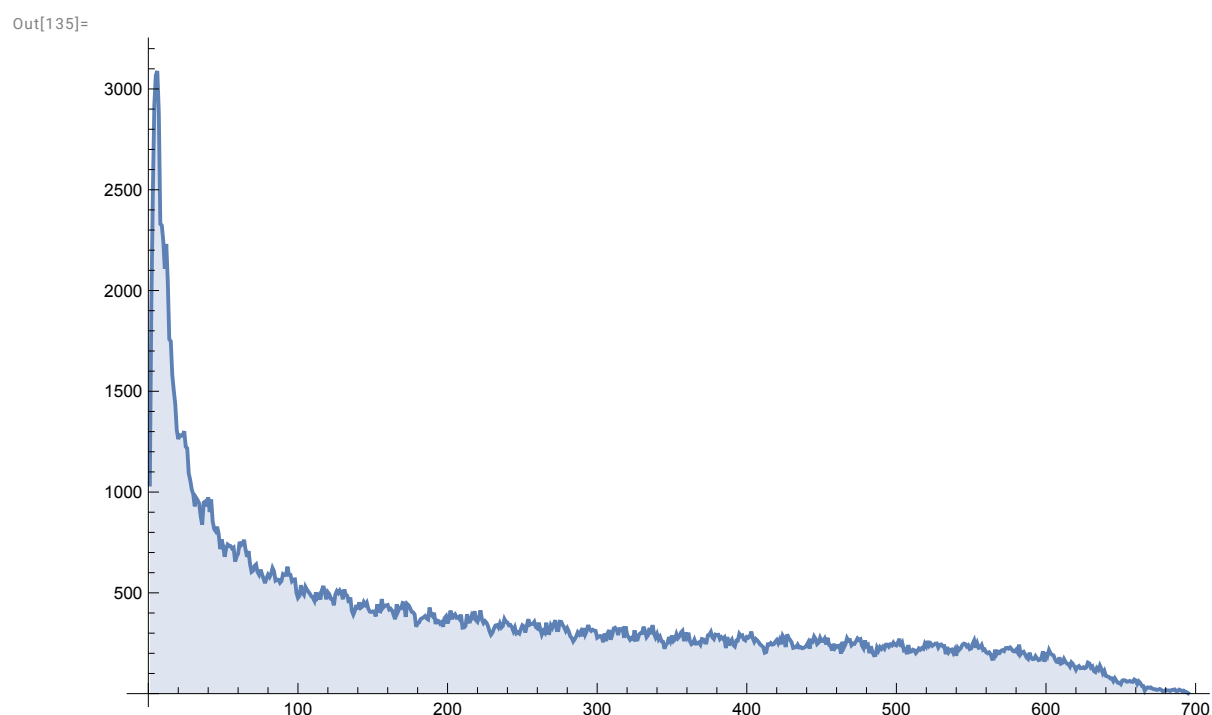
In[132]:=

```
(*Export[
  "/Users/giovannigravili/Library/Mobile Documents/com~apple~CloudDocs/LM
  MANO/Computational material physics /Report for
  the exam/1dlattPlt.pdf",vm1,ImageResolution→800]*)
```

In[133]:=

```
allCombs = Tuples[{kPts, G1d}] // Partition[#, Length@G1d] &;
eVals = Norm[#1 - #2]^2 & @@@ # & /@ allCombs // Transpose;
```

```
In[135]:=
(* Plot of the density of states as a function of energy *)
BinCounts[Flatten@eVals] //
ListLinePlot[#, ImageSize → Large, PlotRange → All, Filling → Axis] &
```



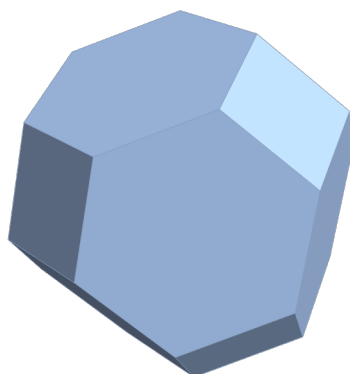
## 0D DOS part (quantum dots)

```
In[136]:=
n = 1
basis1d = {{1, -1, 1}, {1, 1, -1}, {-1, 1, 1}}; (* The basis for the G *)
gen1 = Select[Tuples[Range[-3, 3], 3],
  Abs[#[[3]]] ≤ n && Abs[#[[2]]] ≤ n && Abs[#[[1]]] ≤ n &];
G1d = gen1.basis1d;
vm1 = VoronoiMesh[G1d];
hm = HighlightMesh[vm1, Style[2, Directive[Red]]];
vm1 = MeshRegion[MeshCoordinates[hm], MeshCells[hm, {3, "Interior"}]]
```

Out[136]=

1

Out[142]=





In[143]:=

```
(*Printout3D[vm1] ["FileName"] [[1]] // CopyToClipboard*)
```

In[144]:=

```
allCombs = Tuples[{kPts, G1d}] // Partition[#, Length@G1d] &;
eVals = Norm[#1 - #2]^2 & @@@ # & /@ allCombs // Transpose;
```

In[146]:=

```
(* Plot of the density of states as a function of energy *)
BinCounts[Flatten@eVals] //
ListPlot[#, ImageSize → Large, PlotRange → All, Filling → Axis] &
```

Out[146]=

