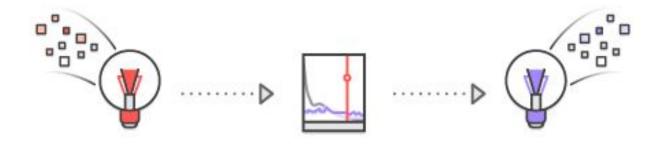
Predict Future Sales

- Kaggle Competition



Stakeholders

-	Upeksha Liyanage	15000771
-	Kshithija Liyanage	15000788
-	Panduka Liyanathanthri	15000796
_	Basuru Amaradiwakara	15000087

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Problem Definition

Challenge Description

This competition consist of challenging time-series dataset consisting of daily sales data, provided by one of the largest Russian software firms - 1C Company. Challenge is to predict total sales for every product a store will sell in the next month.

Data Description

Daily historical sales data of 1C Company is provided as training data. The task is to forecast the total amount of products sold per month in every shop for the test set. List of shops and products slightly changes every month. Data fields

- ID an Id that represents a (Shop, Item) tuple within the test set
- shop_id unique identifier of a shop
- item id unique identifier of a product
- item_category_id unique identifier of item category
- item_cnt_day number of products sold. You are predicting a monthly amount of this measure
- item price current price of an item
- date date in format dd/mm/yyyy
- date_block_num a consecutive month number, used for convenience. January 2013 is 0, February 2013 is 1,..., October 2015 is 33
- item name name of item
- shop name name of shop
- item_category_name name of item category

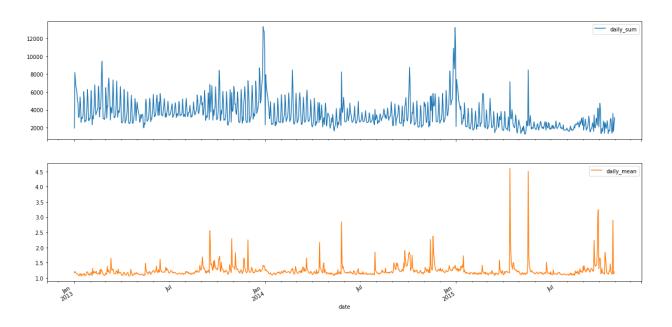
File Descriptions

- sales_train.csv the training set. Daily historical data from January 2013 to October 2015.
- test.csv the test set. need to forecast the sales for these shops and products for November 2015.
- sample submission.csv a sample submission file in the correct format.
- items.csv supplemental information about the items/products.
- item_categories.csv supplemental information about the items categories.
- shops.csv- supplemental information about the shops.
- As we analysed the dataset we found out the following facts
- Item_cnt_data in sales_train.csv file contains both positive and negative values and it
 does not have any zero values. This lead us to conclusion that this file contains only sales
 and returns per day for a particular item at a particular shop. Also we found out that
 shops, items and item categories are not consistent throughout the time period. They
 does not appear for some months.

Data Analysis

Daily Sales Analysis

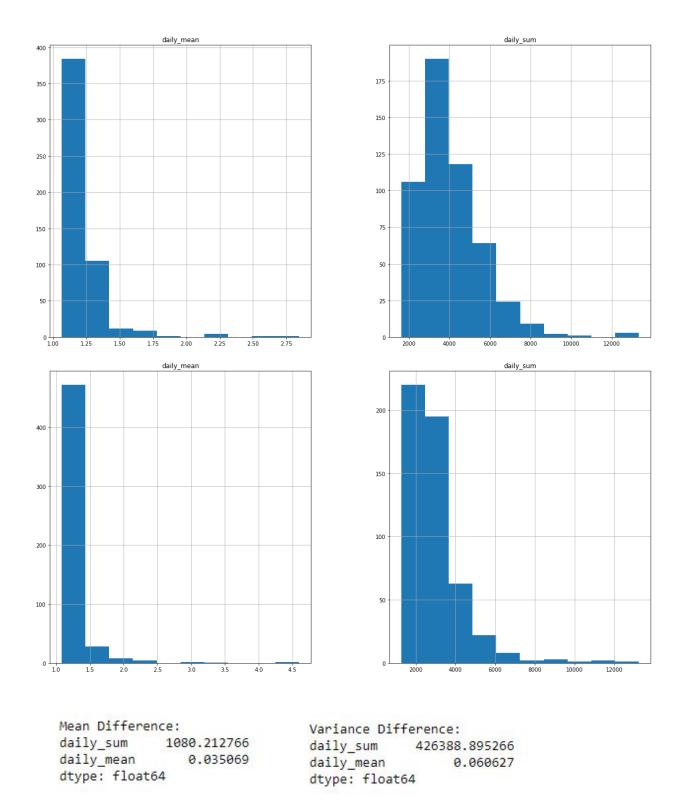
The training set is available as daily sales of the company. Even though the final prediction has to be made in monthly sales, since daily sales data was available data analysis process was carried out on daily sales also in order to identify any increase in demand because of special days such as Valentines Day and Women's Day and to get better insight of the dataset.



Stationarity

Stationarity of a time series is the single most important aspect when considering using statistical models for time series analysis such as ARIMA. Basic meaning of stationarity is when all statistical properties of a time series such as mean, median and variance are constant over time.

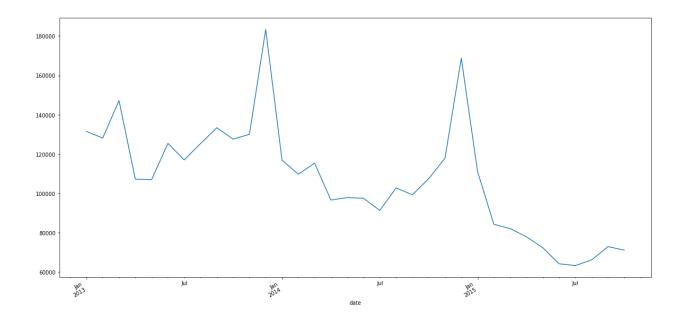
In order to check the stationarity, the data set was split into two sections and the mean and variance was calculated for each section and compared.



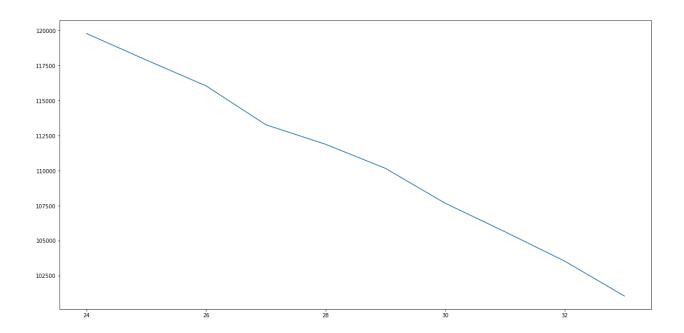
Which provided above results where the conclusion was that the time series is not stationary when looking at daily sales.

Monthly Sales Analysis

The data set was grouped monthly and the sum of item counts per each month was plotted against the number of month in order to identify any seasonality in the data. As seen below, the sales of the company are clearly affected around the November and December months because of the festival season.



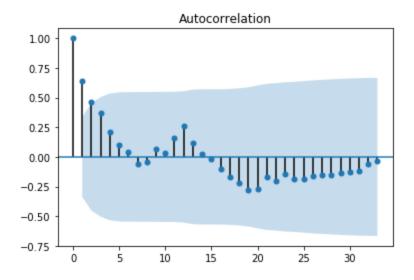
Rolling mean of the monthly sales was plotted against the number of the month in order ro identify the overall trend of sales. The rolling mean window has been set to a higher value in order to produce a smoother curve to remove monthly fluctuations of sales. By analysing the graph, it can be concluded that the sales of the company has a decreasing trend.



Autocorrelation of Monthly Sales

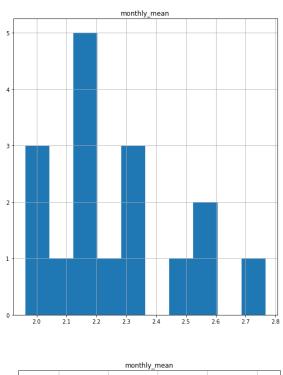
Autocorrelation quantifies internal association of data with fixed time periods apart. For analysing monthly sales, monthly autocorrelation was plotted.

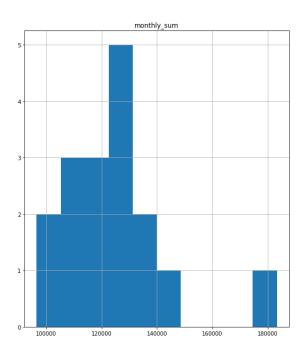
A positive value depicts positive relationship among neighbouring data, a negative value depicts negative relationship and 0 is where no relationship exists among neighbouring data.

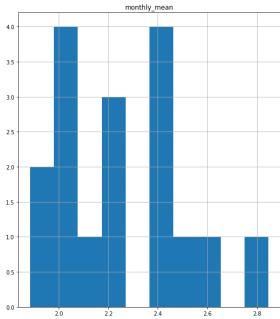


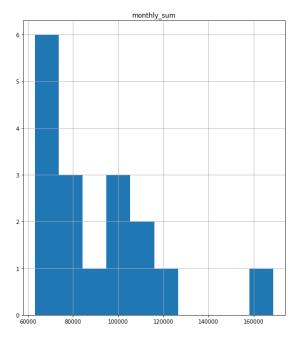
By analysing the plot above, correlation difference of time periods 12 months apart are greater than 0.7, which indicates high correlation of data 12 months apart.

Stationarity









Variance: Mean:

var11:

monthly_sum 123468.352941 monthly_sum 4.160894e+08
monthly_mean 2.258329 monthly_mean dtype: float64 dtype: float64

var2: mean2:

monthly_sum 91132.000000 monthly_mean 2.254215 dtype: float64 monthly_sum 6.985138e+08 monthly_mean 6.892915e-02

dtype: float64

Monthly sales data was also checked for stationarity using the same method as daily sales data. Mean and variance differs significantly between the two time splits considered. Therefore the data is not stationary looking at monthly sales.

Augmented Dicky Fuller test was also carried out to identify the non stationarity of the data.

ADF Statistic: -2.395704

p-value: 0.142953 Critical Values:

1%: -3.646 5%: -2.954 10%: -2.616

The result was obtained after carrying out ADF for the monthly sum of items for each month, where seasonality and trend was present. The p-value of the test is higher than the accepted range of 5%, which means the dataset is non stationary.

Missing Data

Some shops from each each month are missing from the data set inconsistently.

Missing shops for the test set:

{0, 1, 8, 9, 11, 13, 17, 20, 23, 27, 29, 30, 32, 33, 40, 43, 51, 54}

Missing shops per month for the first 33 months:

15 14 14 14 15 14 14 15 15 14 15 14 14 14 14 12 11 11 11 10 9 10 8 10 10 10 13 14 13 16 17 17 18 17 16

Model Selection

Since our dataset is not ordered by the time (has a composite index), we could not directly apply time series models. It was not possible to create our own ensemble model using time series models due to resource and time constraints.

Even most time series models consider the dataset is stationary where it removes seasonality and trend component from the data to predict the next value. By using ANN we could save the time depended components. But it would consume lots of resources.

Because of this we thought of converting the dataset, so that we could apply supervised learning algorithms with gradient boosting models.

Supervised Models

Rolling Windows-Based Regression

Basically in Rolling windows based regression, if we want to predict X(t+1), next value in a time series, we feed not only X(t), but X(t-1), X(t-2) etc to the model and use a regression algorithm to predict the X(t+1) value.

$$y_t = w \Phi(x_t + x[n]_{t-1} + x[n]_{t-2} + x[n]_{t-3} + x[n]_{t-5} + x[n]_{t-12})$$

Time Series models

ARIMA

In statistics and econometrics, and in particular in time series analysis, an autoregressive integrated moving average (ARIMA) model is a generalization of an autoregressive moving average (ARMA) model. Both of these models are fitted to time series data either to better understand the data or to predict future points in the series (forecasting). ARIMA models are applied in some cases where data show evidence of non-stationarity, where an initial differencing step (corresponding to the "integrated" part of the model) can be applied one or more times to eliminate the non-stationarity.

The AR part of ARIMA indicates that the evolving variable of interest is regressed on its own lagged values. The MA part indicates that the regression error is actually a linear combination of error terms whose values occurred contemporaneously and at various times in the past. The I (for "integrated") indicates that the data values have been replaced with the difference between their values and the previous values (and this differencing process may have been performed more than once). The purpose of each of these features is to make the model fit the data as well as possible.

Non-seasonal ARIMA models are generally denoted ARIMA(p,d,q) where parameters p, d, and q are non-negative integers, p is the order (number of time lags) of the autoregressive model, d is the degree of differencing (the number of times the data have had past values subtracted), and q is the order of the moving-average model. Seasonal ARIMA models are usually denoted ARIMA(p,d,q)(P,D,Q)m, where m refers to the number of periods in each season, and the uppercase P,D,Q refer to the autoregressive, differencing, and moving average terms for the seasonal part of the ARIMA model

SARIMA

Seasonal Autoregressive Integrated Moving Average, SARIMA or Seasonal ARIMA, is an extension of ARIMA that explicitly supports univariate time series data with a seasonal component.

It adds three new hyperparameters to specify the autoregression (AR), differencing (I) and moving average (MA) for the seasonal component of the series, as well as an additional parameter for the period of the seasonality.

Models Comparisons

XGBoost vs LightGBM

XGBoost is a pre sort based algorithm and has time complexity of O(data)

- LightGBM uses a histogram based model which has a lower time complexity than XGBoost.
- LGBM also requires less memory compared to XGBoost.
- Since we used standard laptop computers in training the model, LGBM was a better fit than XGB.

Boosting Methods vs Neural Networks

- Model generation using neural networks requires huge amount of data points.
- Requires more time and computing resources compared to boosting methods.
- Even though NNs could provide better precision. Boosting was selected because of ease of use and time efficiency.

Model Development

We have used LightGBM model which is a Tree base gradient boosting algorithm.

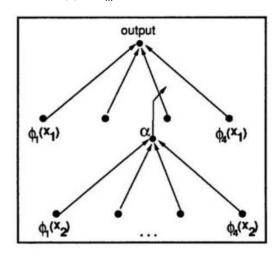
Gradient boosting involves three elements:

1. A loss function to be optimized.

Loss Function: L(y,F_m(x)) =
$$\sqrt{\frac{1}{n} \sum_{i}^{n} (y - Fm(x))^{2}}$$

2. A weak learner to make predictions.

We preprocess the dataset according to Rolling Windows-based Regression, Where, $y_t = w \Phi(x_t + x[n]_{t-1} + x[n]_{t-2} + x[n]_{t-3} + x[n]_{t-5} + x[n]_{t-12})$ $y' = w \Phi(x) = F_m(x)$



3. An additive model to add weak learners to minimize the loss function.

for $m=1 \rightarrow M$

$$F_{m}(x) = F_{m-1}(x) + \alpha h_{m}(x)$$

Data Preprocessing

Feature Engineering

Downcasting Variables

Sales data

95	date	date_block_num	shop_id	item_id	item_price	item_cnt_day
0	2013-01-02	0	59	22154	999.00	1
1	2013-01-03	0	25	2552	899.00	1
2	2013-01-05	0	25	2552	899.00	-1
3	2013-01-06	0	25	2554	1709.05	1
4	2013-01-15	0	25	2555	1099.00	1

- Downcast data (in sales) to manipulate the memory productively.



```
sales.info()
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 2935849 entries, 0 to 2935848
Data columns (total 6 columns):
                  object
date
date_block_num
                  int64
shop_id
                  int64
item id
                  int64
item_price
                  float64
item_cnt_day
                  float64
dtypes: float64(2), int64(3), object(1)
memory usage: 134.4+ MB
```

```
sales.info()
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 2935849 entries, 0 to 2935848
Data columns (total 6 columns):
                 datetime64[ns]
date
date_block_num
                 int8
shop_id
                 int8
item_id
                 int16
item price
                 float64
item_cnt_day
                 int16
dtypes: datetime64[ns](1), float64(1), int16(2), int8(2)
memory usage: 61.6 MB
```

Item Data

	item_name	item_id	item_category_id
0	$! \theta \Box \theta \Box \theta \Box \theta \Box \theta \Box \theta \Box \theta \Box \theta \Box \theta \Box $	0	40
1	IABBYY FineReader 12 Professional Edition Full	1	76
2	*** $D = D = D + D = D = D = D = D = D = D = $	2	40
3	*** Θ = Θ	3	40
4	*** Θ DDDDDDDDDDD (Θ j D ¢ D DDDDDDDDDDDDDDDDDDDDDDDDDDDDDDD	4	40

- Downcast data(in items)



items.info()

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 22170 entries, 0 to 22169
Data columns (total 3 columns):

dtypes: int64(2), object(1)
memory usage: 519.7+ KB

items.info()

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 22170 entries, 0 to 22169
Data columns (total 3 columns):

memory usage: 238.2+ KB

Merging Features

- merging sales data and item data. (training day data set)

	date	date_block_num	shop_id	item_id	item_price	item_cnt_day	item_category_id
0	2013-01-02	0	59	22154	999.00	1	37
1	2013-01-03	0	25	2552	899.00	1	58
2	2013-01-05	0	25	2552	899.00	-1	58
3	2013-01-06	0	25	2554	1709.05	1	58
4	2013-01-15	0	25	2555	1099.00	1	56

Add Window Features

Converting Daily Sales into Monthly sales.

- data group by month

	date	date_block_num	shop_id	item_id	item_price	item_cnt_day	item_category_id
0	2013-01-01	0	59	22154	999.00	1	37
1	2013-01-01	0	25	2552	899.00	1	58
2	2013-01-01	0	25	2552	899.00	-1	58
3	2013-01-01	0	25	2554	1709.05	1	58
4	2013-01-01	0	25	2555	1099.00	1	56

- Groupby data to analyse the item count for a month (training month data set)

	date_block_num	shop_id	item_id	item_price	item_cnt_month
0	0	0	32	221.0	6
1	0	0	33	347.0	3
2	0	0	35	247.0	1
3	0	0	43	221.0	1
4	0	0	51	128.5	2

- merging training day data set with training month data set

	shop_id	item_id	date_block_num	date	item_category_id	item_price	item_cnt_month
0	59	22154	0	2013-01-01	37	999.00	1
1	25	2552	0	2013-01-01	58	899.00	0
2	25	2552	0	2013-01-01	58	899.00	0
3	25	2554	0	2013-01-01	58	1709.05	1
4	25	2555	0	2013-01-01	56	1099.00	1

- drop duplicates on training month data set using month, item and shop fields.

	shop_id	item_id	date_block_num	date	item_category_id	item_price	item_cnt_month
0	59	22154	0	2013-01-01	37	999.00	1
1	25	2552	0	2013-01-01	58	899.00	0
3	25	2554	0	2013-01-01	58	1709.05	1
4	25	2555	0	2013-01-01	56	1099.00	1
5	25	2564	0	2013-01-01	59	349.00	1

- creating zero sales for every item which did not sale

	shop_id	item_id	date_block_num
0	59	22154	0
1	59	2552	0
2	59	2554	0
3	59	2555	0
4	59	2564	0

- merging zero sales with training month data set and dropping category and price fields(all data)

	shop_id	item_id	date_block_num	date	item_cnt_month
0	59	22154	0	2013-01-01 00:00:00	1.0
1	59	2552	0	0	0.0
2	59	2554	0	0	0.0
3	59	2555	0	0	0.0
4	59	2564	0	0	0.0

Add Missing Values

- Assume item price is differed from the date. Add prices to Zero sales. Merging all data with training month data.

	shop_id	item_id	date_block_num	date	item_cnt_month	item_price
0	59	22154	0	2013-01-01	1	999.0
1	59	22154	0	2013-01-01	1	999.0
2	59	22154	0	2013-01-01	1	999.0
3	59	22154	0	2013-01-01	1	999.0
4	59	22154	0	2013-01-01	1	999.0

```
all_data.info()
<class 'pandas.core.frame.DataFrame'>
Int64Index: 75218848 entries, 0 to 75218847
Data columns (total 6 columns):
shop_id
                 int8
item_id
                 int16
date_block_num
                 int8
date
                 datetime64[ns]
item cnt month
                 int16
item price
                 float16
dtypes: datetime64[ns](1), float16(1), int16(2), int8(2)
memory usage: 1.7 GB
```

Add Rolling Window Features (Sum and Mean)

- Get shop wise data for a month by grouping date and shop

	date_block_num	shop_id	shop_block_target_sum	shop_block_target_mean
0	0	0	5578	0.687369
1	0	1	2947	0.363155
2	0	2	1146	0.141220
3	0	3	767	0.094516
4	0	4	2114	0.260505

- Get item wise data for a month by grouping date and item

	date_block_num	item_id	item_block_target_sum	item_block_target_mean
0	0	19	1.0	0.022222
1	0	27	7.0	0.155556
2	0	28	8.0	0.177778
3	0	29	4.0	0.088889
4	0	32	299.0	6.644444

- merging item wise data with all data

	shop_id	item_id	date_block_num	date	item_cnt_month	item_category_id
0	59	22154	0	2013-01-01	1.0	37
1	59	2552	0	2013-01-01	0.0	58
2	59	2554	0	2013-01-01	0.0	58
3	59	2555	0	2013-01-01	0.0	56
4	59	2564	0	2013-01-01	0.0	59

- Get item-category wise data for a month by grouping date and item-category

	date_block_num	item_category_id	item_cat_block_target_sum	item_cat_block_target_mean
0	0	0	1.0	0.022222
1	0	1	1.0	0.022222
2	0	2	1390.0	0.834835
3	0	3	440.0	4.888889
4	0	4	251.0	0.507071

- merging all data with items

	shop_id	item_id	date_block_num	date	item_cnt_month	item_price	item_category_id
0	59	22154	0	2013-01-01	1	999.0	37
1	59	22154	0	2013-01-01	1	999.0	37
2	59	22154	0	2013-01-01	1	999.0	37
3	59	22154	0	2013-01-01	1	999.0	37
4	59	22154	0	2013-01-01	1	999.0	37

- merging all data with item-category

	shop_id	item_id	date_block_num	date	item_cnt_month	item_price	item_category_id	item_cat_block_target_sum	item_cat_block_target_m
0	59	22154	0	2013- 01-01	1	999.0	37	6094.0	0.199738
1	59	22154	0	2013- 01-01	1	999.0	37	6094.0	0.199738
2	59	22154	0	2013- 01-01	1	999.0	37	6094.0	0.199738
3	59	22154	0	2013- 01-01	1	999.0	37	6094.0	0.199738
4	59	22154	0	2013- 01-01	1	999.0	37	6094.0	0.199738

- merging all data with item.

	shop_id	item_id	date_block_num	date	item_cnt_month	item_price	item_category_id	item_cat_block_target_sum	item_cat_block_target_m
0	59	22154	0	2013- 01-01	1	999.0	37	37	0.199707
1	59	22154	0	2013- 01-01	1	999.0	37	37	0.199707
2	59	22154	0	2013- 01-01	1	999.0	37	37	0.199707
3	59	22154	0	2013- 01-01	1	999.0	37	37	0.199707
4	59	22154	0	2013- 01-01	1	999.0	37	37	0.199707

- merging all data with shop data.

	shop_id	item_id	date_block_num	date	item_cnt_month	item_price	item_category_id	item_cat_block_target_sum	item_cat_block_target_m
0	59	22154	0	2013- 01-01	1	999.0	37	37	0.199707
1	59	22154	0	2013- 01-01	1	999.0	37	37	0.199707
2	59	22154	0	2013- 01-01	1	999.0	37	37	0.199707
3	59	22154	0	2013- 01-01	1	999.0	37	37	0.199707
4	59	22154	0	2013- 01-01	1	999.0	37	37	0.199707

Preprocessed Data

```
all_data.info()
<class 'pandas.core.frame.DataFrame'>
Int64Index: 75218848 entries, 0 to 75218847
Data columns (total 13 columns):
shop id
                             int8
                             int16
item_id
date_block_num
                              int8
date
                              datetime64[ns]
item_cnt_month
                              int16
item_price
                              float16
item_category_id
                              int8
item_cat_block_target_sum
                              int8
item_cat_block_target_mean
                             float16
item_block_target_sum
                              int16
item_block_target_mean
                             float16
shop_block_target_sum
                              int16
shop_block_target_mean
                             float16
dtypes: datetime64[ns](1), float16(4), int16(4), int8(4)
memory usage: 2.5 GB
```

	shop_id	item_id	date_block_num	date	item_cnt_month	item_price	item_category_id	item_cat_block_target_sum
0	59	22154	0	2013- 01-01	1	999.0	37	37
1	59	22154	0	2013- 01-01	1	999.0	37	37
2	59	22154	0	2013- 01-01	1	999.0	37	37
3	59	22154	0	2013- 01-01	1	999.0	37	37
4	59	22154	0	2013- 01-01	1	999.0	37	37

item_cat_block_target_mean	item_block_target_sum	item_block_target_mean	shop_block_target_sum	shop_block_target_mean
0.199707	18	0.399902	2017	0.248535
0.199707	18	0.399902	2017	0.248535
0.199707	18	0.399902	2017	0.248535
0.199707	18	0.399902	2017	0.248535
0.199707	18	0.399902	2017	0.248535 Activat

Add Lag Features

1, 2, 3, 5 months was selected in order to reflect the overall decreasing trend of the sales of the company and to reflect the effect of recent events in the most recent quarter to the month being considered.

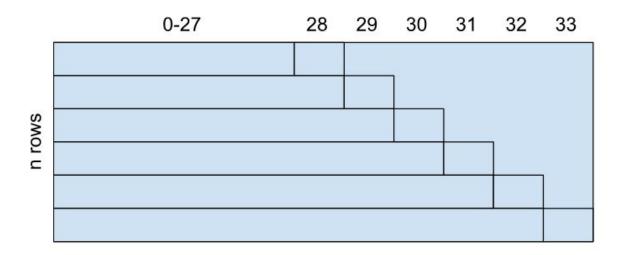
12th month lag feature was selected to reflect the annual seasonality of the sales.

Add Seasonal Components/ Holidays

```
temp=all_data all_data['December'] = temp.date_block_num.apply(lambda x: 1 if x in [23] else 0) all_data['Newyear_Xmas'] = temp.date_block_num.apply(lambda x: 1 if x in [12,24] else 0) all_data['Valentine_MenDay'] = temp.date_block_num.apply(lambda x: 1 if x in [13,25] else 0) all_data['WomenDay'] = temp.date_block_num.apply(lambda x: 1 if x in [14,26] else 0) all_data['Easter_Labor'] = temp.date_block_num.apply(lambda x: 1 if x in [15,27] else 0)
```

Cross Validation and Hyperparameter Tuning

We created 6 folds of validation sets using last 6 months 28 to 33 and calculated the root mean squared error per each fold. We used the mean of all the 6 folds as the metric to improve hyperparameters.



Hyperparameter tuning is done by using hyperopt python library which we tried to tune the following parameter

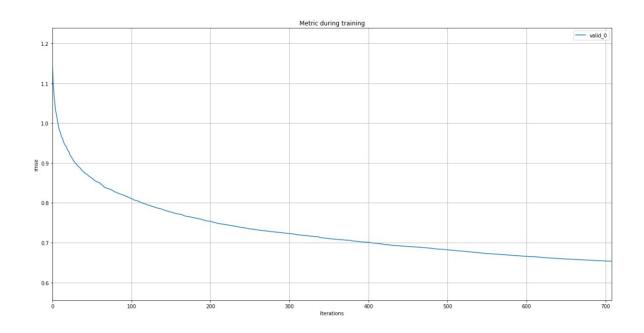
Hyperparameters for LightGBM

- 'colsample_bytree': 0.8
 - Percentage of columns used per iteration.
- 'metric': 'rmse'
 - Evaluation metrics to be monitored through iterations.
- 'min_data_in_leaf': 21
 - It is the minimum number of the records a leaf may have.
- 'subsample': 0.55
 - Subsample ratio of the training instance.
- 'learning rate': 0.225
 - List of learning rates for each boosting round or a customized function that calculates.

- 'objective': 'regression'
 - Final objective of what method used for prediction.
- 'bagging_seed': 128
 - Random seed for bagging.
- 'num leaves': 7
 - Maximum tree leaves for base learners.
- 'max depth': 3
 - It describes the maximum depth of tree. This parameter is used to handle model overfitting. Any time you feel that your model is overfitted.
- 'bagging_freq': 1
 - Turning on bagging.
- 'seed': 1204
 - Seed used to generate the weights

Regularization

We have not used a specific regularization term in the model but we controlled overfitting by tuning hyperparameters such as reducing the depth of the tree, number of leaves, subsampling and choosing set of columns per iteration. Some of these values are taken from recommendations such as number of leaves and depth and some of the values are taken from hyper tuning the parameters such as subsample size. By addressing the overfitting issue we were able to reduce the 'root mean square error' (rmse) of testing dataset from 4.2rmse to 2.1rmse.



Contribution

Member	Index Number	Contribution
Upeksha Liyanage	15000771	Data Analysis, Preprocessing, Model implementation, Model training
Basuru Amaradiwakara	15000087	Preprocessing, Model training
Panduka Liyanathanthri	15000796	Data Analysing, Model training
Kshithija Liyanage	15000788	Model selection, Model training

References

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- [3]T. Sanger, *Basis-Function Trees as a Generalization of Local Variable Selection Methods for Function Approximation*. 2018 [Online]. Available: https://papers.nips.cc/paper/340-basis-function-trees-as-a-generalization-of-local-variable-sele ction-methods-for-function-approximation.pdf. [Accessed: 19- Sep- 2018]
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