

In **quantum computing**, we can perform **simple addition using qubits** with **basic quantum gates**, usually with a **quantum ripple-carry adder** approach. For a beginner-friendly example, let's create a circuit to **add two 1-bit numbers**.

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### Simple 1-Bit Addition Using Quantum Gates

**Goal:** Add two numbers  $a$  and  $b$  (each 0 or 1) and get:

- Sum ( $s$ )
- Carry ( $c$ )

**Truth table for 1-bit addition:**

**a b Sum ( $s$ ) Carry ( $c$ )**

|       |   |
|-------|---|
| 0 0 0 | 0 |
| 0 1 1 | 0 |
| 1 0 1 | 0 |
| 1 1 0 | 1 |

### Step 1: Quantum Circuit Setup

We need **3 qubits**:

1.  $a \rightarrow$  first number
2.  $b \rightarrow$  second number
3. carry/sum  $\rightarrow$  output

And **2 classical bits** to read the outputs.

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### Step 2: Gates for 1-Bit Adder

1. **CNOT gate**  $\rightarrow$  calculates **sum modulo 2 (XOR)**
  - sum =  $a \text{ XOR } b$
2. **CCNOT (Toffoli) gate**  $\rightarrow$  calculates **carry**
  - carry =  $a \text{ AND } b$

### 3. Quantum Circuit: Step-by-Step Explanation

#### 4. 1. Qubits and Classical Bits

`qc = QuantumCircuit(3,2)`

**3 qubits:**

1.  $q_0 \rightarrow$  represents input  $a$
2.  $q_1 \rightarrow$  represents input  $b$
3.  $q_2 \rightarrow$  represents **sum/carry output**

**2 classical bits:**

1.  $c_0 \rightarrow$  stores **sum**
2.  $c_1 \rightarrow$  stores **carry**

`qc.x(0) # a=1`

`qc.x(1) # b=1`

X gate flips a qubit from  $|0\rangle \rightarrow |1\rangle$ .

Here, we set  $a=1$  and  $b=1$  for this example.

If inputs were 0, we would not apply X.

#### Compute Sum (XOR)

`qc.cx(0,2)`

- `qc.cx(1,2)`

**CNOT (controlled-NOT) gate:** flips the target qubit if the control qubit is 1.

- **Step explanation:**

1. First CNOT(0,2)  $\rightarrow$  sum qubit flips if  $a=1$
2. Second CNOT(1,2)  $\rightarrow$  sum qubit flips again if  $b=1$

- **Result:** sum =  $a \text{ XOR } b$

### Example:

- $a=1, b=1 \rightarrow$  sum qubit flips twice  $\rightarrow$  ends up as 0  $\rightarrow$  correct sum bit.

Compute Carry (AND)

- qc.ccx(0,1,2)
- **CCX (Toffoli gate):** controlled-controlled-NOT
- Flips the target qubit **only if both control qubits are 1.**
- **Purpose:** compute carry = a AND b

### Example:

- $a=1, b=1 \rightarrow$  both controls are 1  $\rightarrow$  sum/carry qubit flips  $\rightarrow$  represents carry bit.

Measurement

```
qc.measure(2,0) # sum  
qc.measure(1,1) # carry
```

Measures qubits into classical bits.

$q2 \rightarrow c0 \rightarrow$  sum

$q1 \rightarrow c1 \rightarrow$  carry

Now the outputs can be read as classical binary numbers.

### Draw the Circuit

```
qc.draw('text')
```

## 1-Bit Quantum Subtractor Logic

**Inputs:** a (minuend), b (subtrahend)

**Outputs:**

- difference = a XOR b
- borrow = NOT a AND b

### Truth Table:

**a b Difference Borrow**

|       |   |
|-------|---|
| 0 0 0 | 0 |
| 0 1 1 | 1 |
| 1 0 1 | 0 |
| 1 1 0 | 0 |

## Quantum Circuit Steps in Quirk

### Step 1: Qubits

- Use 3 qubits:
  - $q0 \rightarrow a$  (minuend)
  - $q1 \rightarrow b$  (subtrahend)
  - $q2 \rightarrow$  difference/borrow output

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### Step 2: Difference Calculation (XOR)

- Same as adder:

difference = a XOR b

In Quirk:

1. CNOT(a -> q2)
2. CNOT(b -> q2)

### Step 3: Borrow Calculation

- Borrow occurs if  $b = 1$  and  $a = 0$ :

borrow = b AND (NOT a)

- Steps in Quirk:
  1. Apply X gate on a (to create NOT a)

2. Apply CCX (Toffoli) gate:
  - Controls: NOT a (q0) and b (q1)
  - Target: q2 or another qubit for borrow

This flips the target qubit only when borrow is needed.

#### **Step 4: Measurement**

- Measure:
  - Difference qubit → classical bit c0
  - Borrow qubit → classical bit c1