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2.1

a

A nonlinear transfer function gives the neural network a universal property: Given enough layers and neurons, the network can model any function within a certain accuracy. In a network with a linear transfer function we can only compute a linear function. A network with a linear transfer function of n layers will always be equivalent to a network with only one layer: linear functions can always be concatenated.
Whenever the function that we are trying to model isn't a linear function, it is useful to use a nonlinear transfer function. Examples include image classification or speech recognition.

b

Consider a simple neural network with two input neurons that can both either be 0 or 1 and one output layer. We want to construct an AND gate with our network, so without bias our quest would be to find $w = (w_1, w_2)$ such that:

$$\begin{aligned} 0 &\leq 0 \\ w_1 &\leq 0 \\ w_2 &\leq 0 \\ w_1 + w_2 &> 0 \end{aligned}$$

which is impossible. We can easily however create the network with a bias, if we have the weights $w = (1,1)$ and the bias $\theta = \frac{3}{2}$. Then $sgn(w^T x - \theta)$ would give us AND.

c

Point and edge filters are for example a connectionist neuron which gets values of a scalar field as input, that represent the color of each pixel or the color gradient or even a higher derivative and has weights in the following form: In the simple case of two colors (0 and 1) this point filter would return zero for no point, 1 or -1 for a point in the outer region and 8 or -8 if the point is in the middle. This goes analogously for the other filter.

-1	-1	-1
-1	+8	-1
-1	-1	-1

point filter

-1	0	+1
−2	0	+2
-1	0	+1

+1	+2	+1
0	0	0
-1	−2	-1

edge filter (Sobel filter)

d

The first is deterministic and the second has a noise parameter and can return different states for set parameters and a given input.

2.2

a

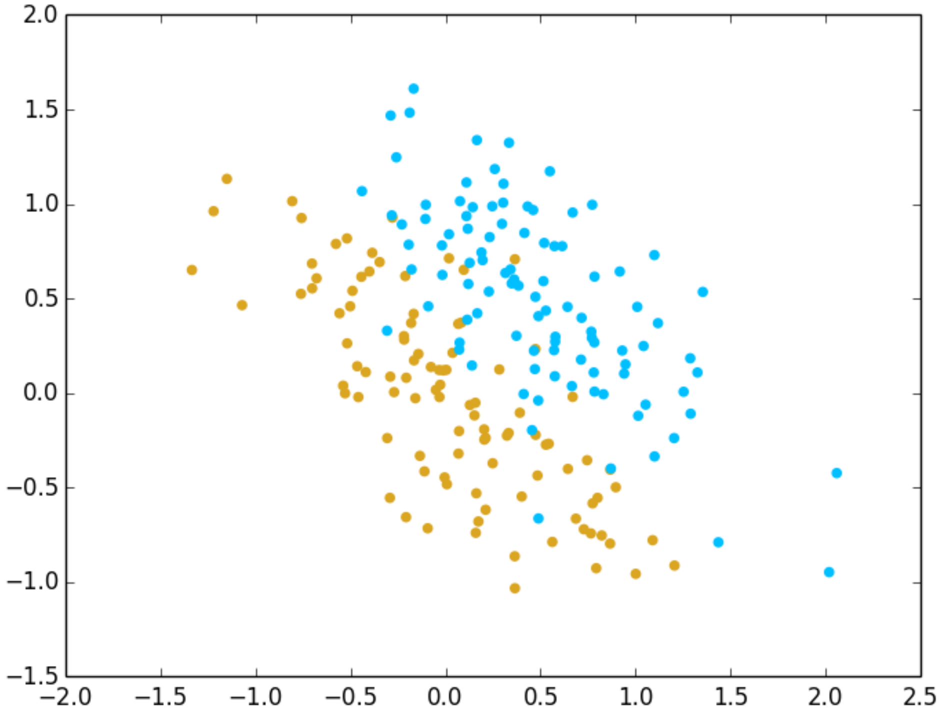

Figure 1: Plot where Y=1 (blue) and Y=0 (gold).

b

c

Best weight vector is .

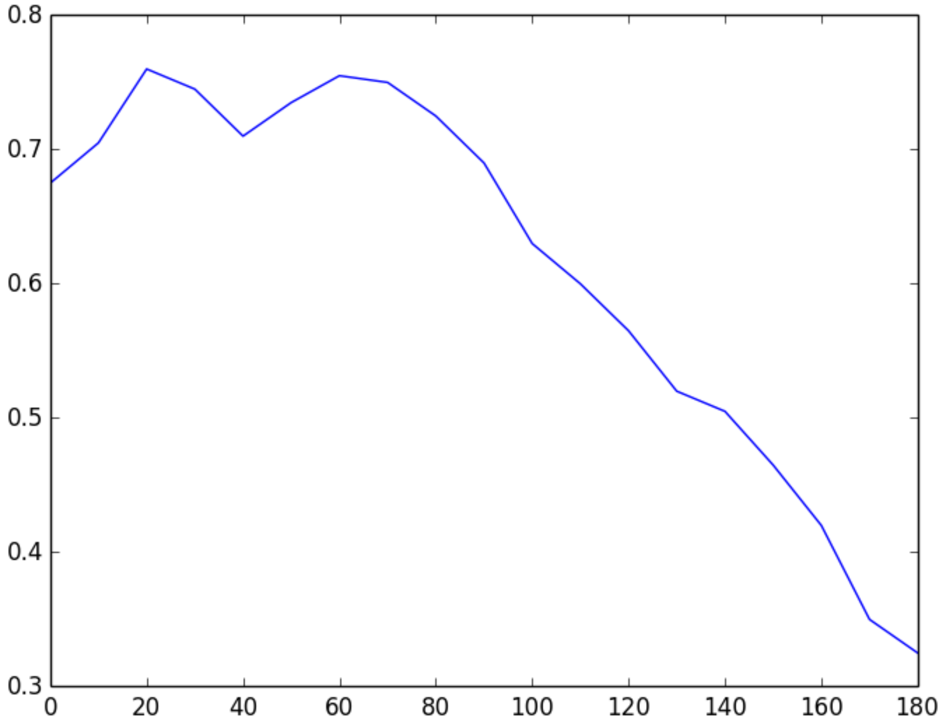

Figure 2: Classification performance for different alphas.

d

e

2.3

a

A MLP could decide between a horizontal and a vertical edge, whereas a perceptionist neuron would either be able to differ between vertical edge or no vertical edge OR horizontal edge or no horizontal edge.

b

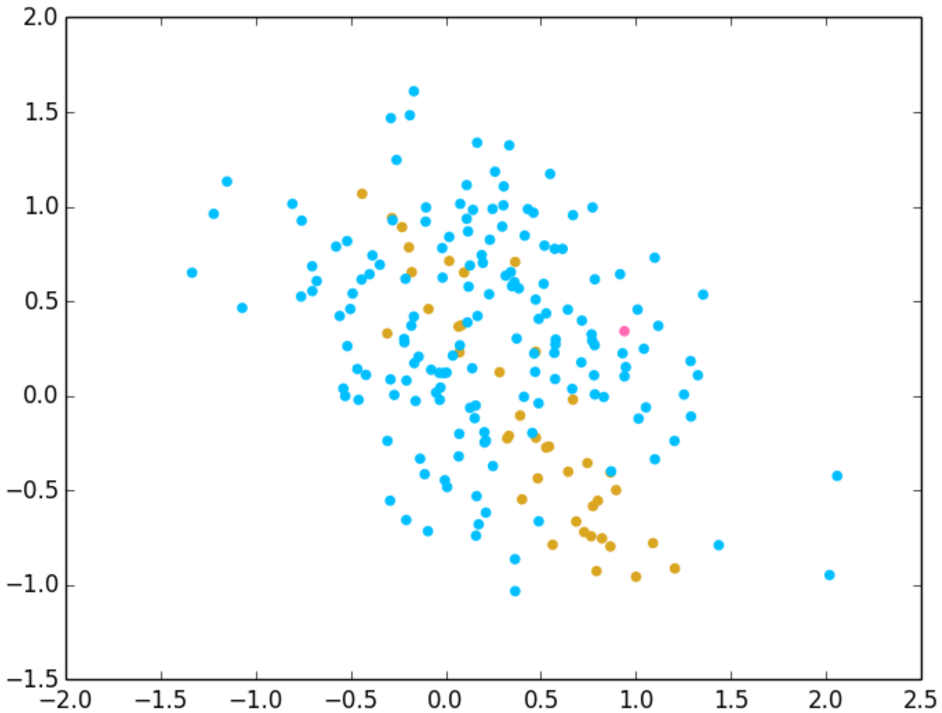

Figure 3: Classified data points. Blue = correctly classified, Gold = other data points, Pink = weight.

c + bonus

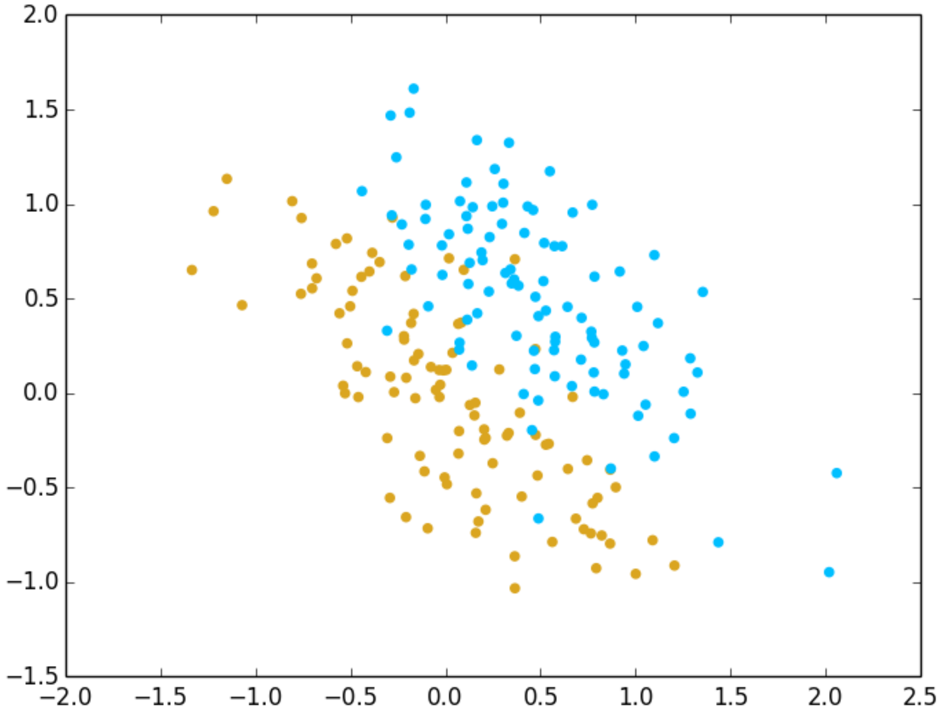

Figure 4: Plot where Y=1 (blue) and Y=0 (gold).

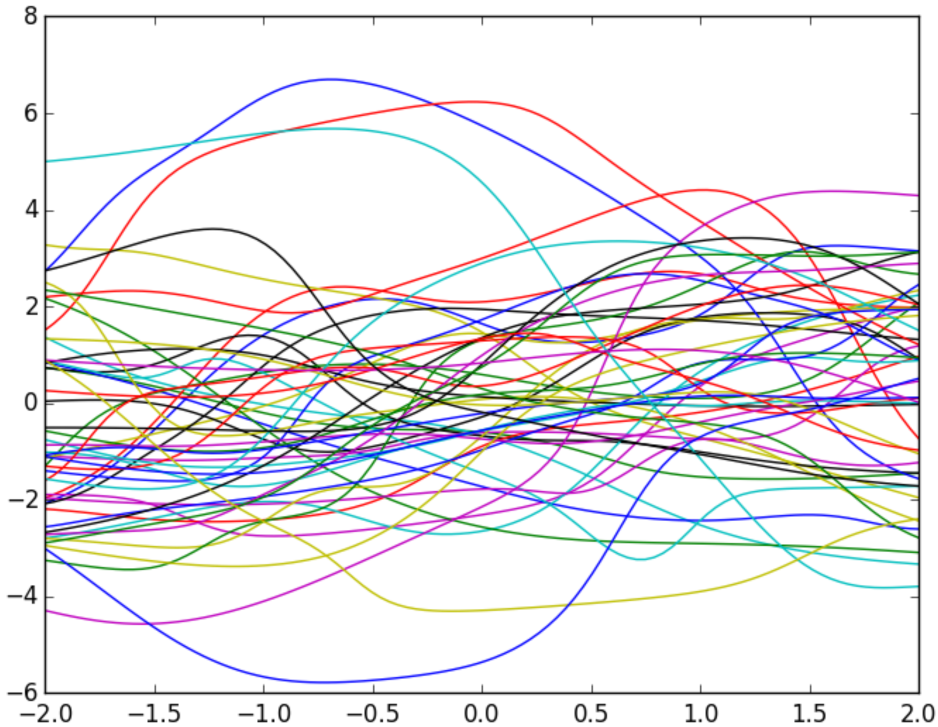

Figure 5: functions computed with normally distributed a_i with a standard deviation of 2

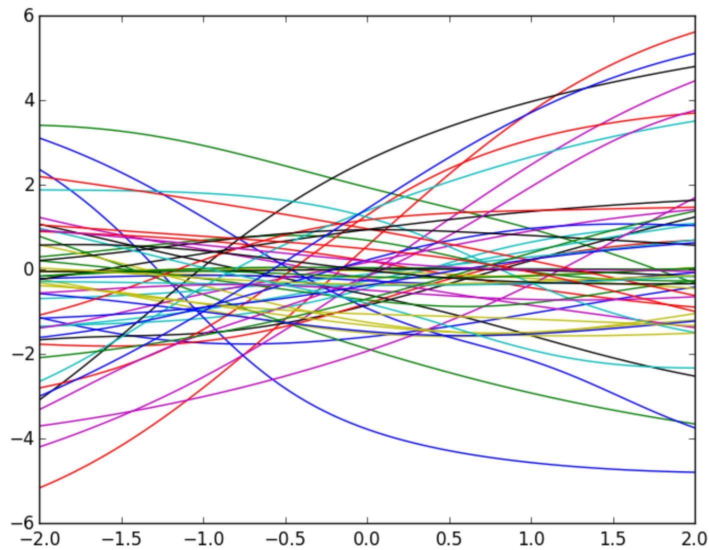

Figure 6: functions computed with normally distributed a_i with a standard deviation of 0.5

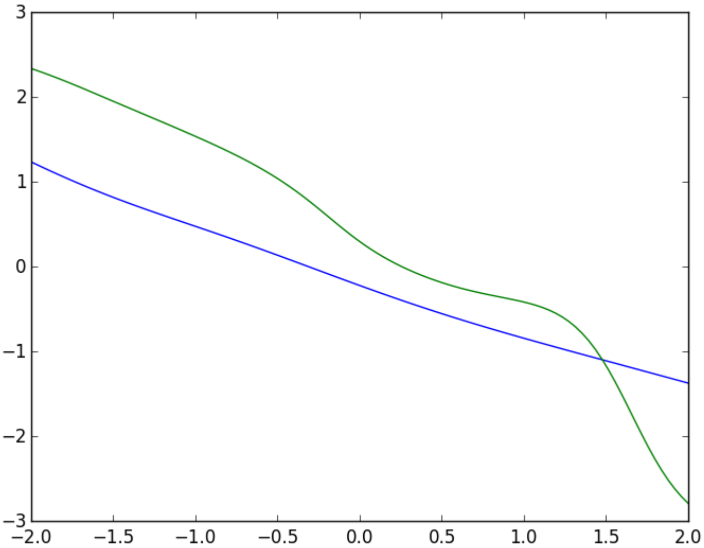

Figure 7: functions with least mean square error from f(x)=-x, computed with an std of 2 (green) and 0.5 (blue)