

Malte Siemers
 Martin Lundfall
 Henri Bunting

2.1

a

A nonlinear transfer function gives the neural network a universal property: Given enough layers and neurons, the network can model any function within a certain accuracy. In a network with a linear transfer function we can only compute a linear function. A network with a linear transfer function of n layers will always be equivalent to a network with only one layer: linear functions can always be concatenated.

Whenever the function that we are trying to model isn't a linear function, it is useful to use a nonlinear transfer function. Examples include image classification or speech recognition.

b

Consider a simple neural network with two input neurons that can both either be 0 or 1 and one output layer. We want to construct an AND gate with our network, so without bias our quest would be to find $w = (w_1, w_2)$ such that:

$$\begin{aligned} 0 &\leq 0 \\ w_1 &\leq 0 \\ w_2 &\leq 0 \\ w_1 + w_2 &> 0 \end{aligned}$$

w_0							1.5
w_1		0	1	0	1		1
w_2		0	0	1	1		1
0 0	-	-	-	-	-		-
0 1	-	-	-	+	+		-
1 0	-	-	+	-	+		-
1 1	+	-	+	+	+		+

which is impossible. We can easily however create the network with a bias, if we have the weights $w = (1, 1)$ and the bias $\theta = \frac{3}{2}$. Then $\text{sgn}(w^T x - \theta)$ would give us AND.

c

Point and edge filters are for example a connectionist neuron which gets values of a scalar field as input, that represent the color of each pixel or the color gradient or even a higher derivative and has weights in the following form: In the simple case of two colors (0 and 1) this point filter would return

-1	-1	-1
-1	+8	-1
-1	-1	-1

point filter

-1	0	+1
-2	0	+2
-1	0	+1

edge filter (Sobel filter)

+1	+2	+1
0	0	0
-1	-2	-1

zero for no point, 1 or -1 for a point in the outer region and 8 or -8 if the point is in the middle. This goes analogously for the other filter.

d

The first is deterministic and the second has a noise parameter and can return different states for set parameters and a given input.

2.2

a

b

c

Best weight vector is .

d

e

2.3

a

A MLP could decide between a horizontal and a vertical edge, whereas a perceptionist neuron would either be able to differ between vertical edge or no vertical edge OR horizontal edge or no horizontal edge.

b

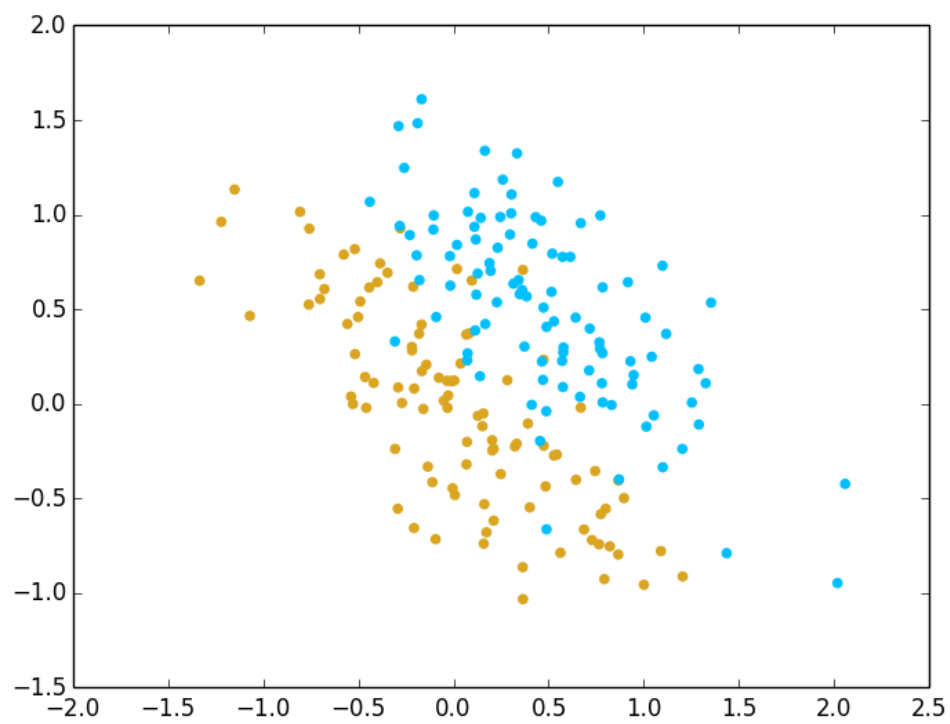


Figure 1: Plot where $Y=1$ (blue) and $Y=0$ (gold).

c + bonus

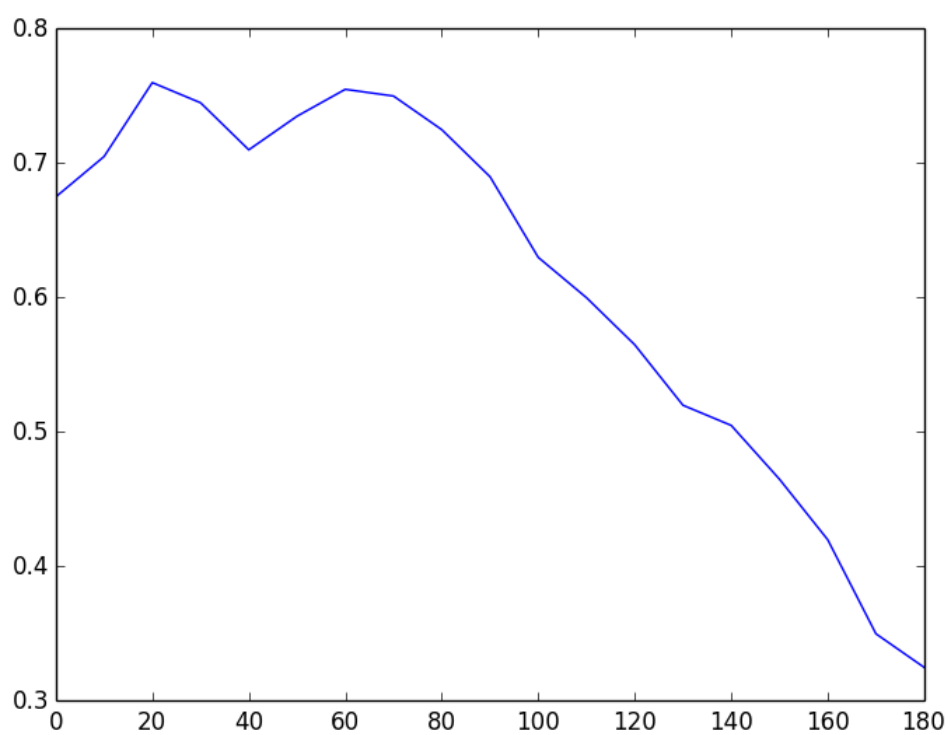


Figure 2: Classification performance for different alphas.

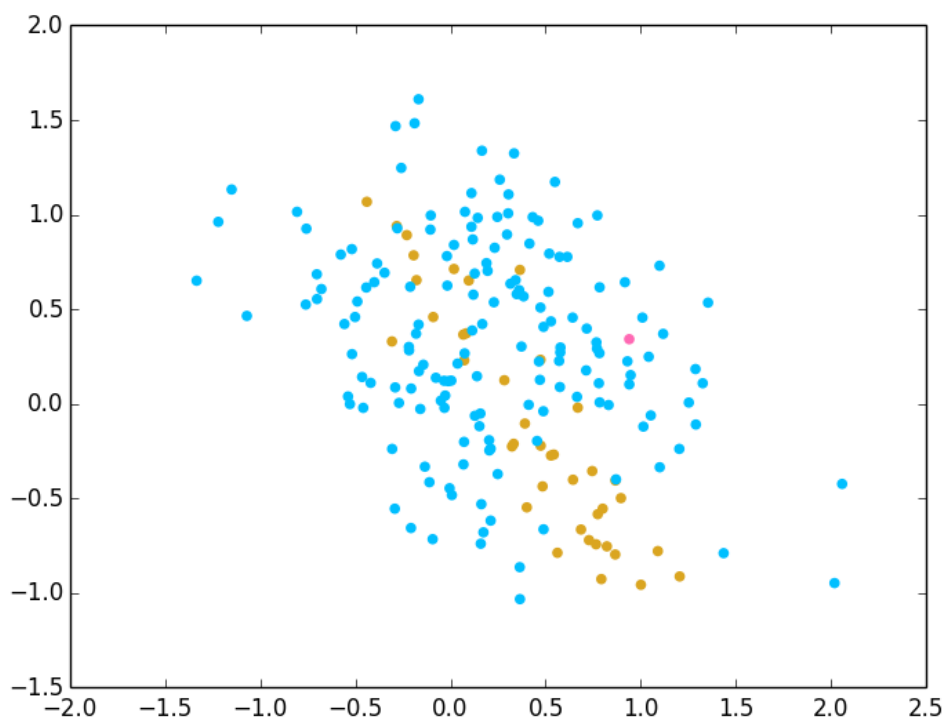


Figure 3: Classified data points. Blue = correctly classified, Gold = other data points, Pink = weight.

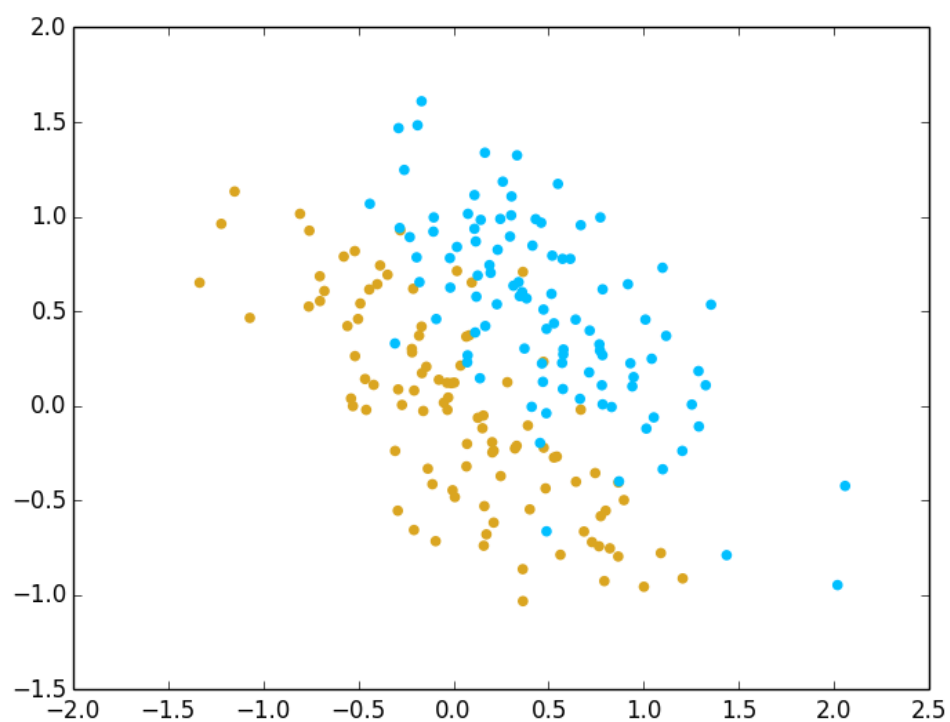


Figure 4: Plot where $Y=1$ (blue) and $Y=0$ (gold).

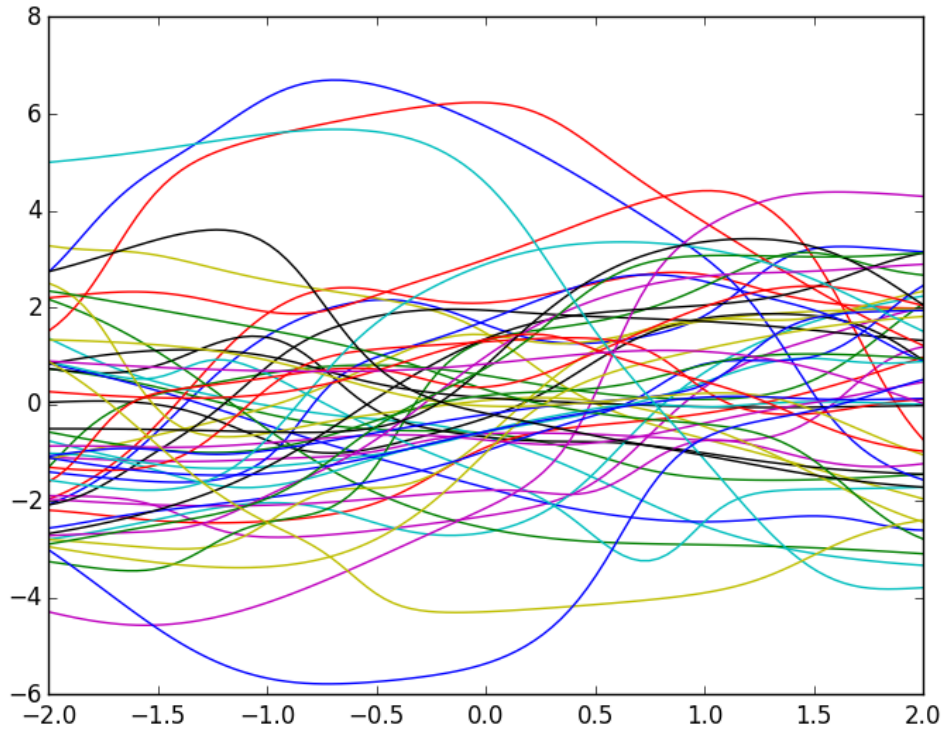


Figure 5: functions computed with normally distributed a_i with a standard deviation of 2

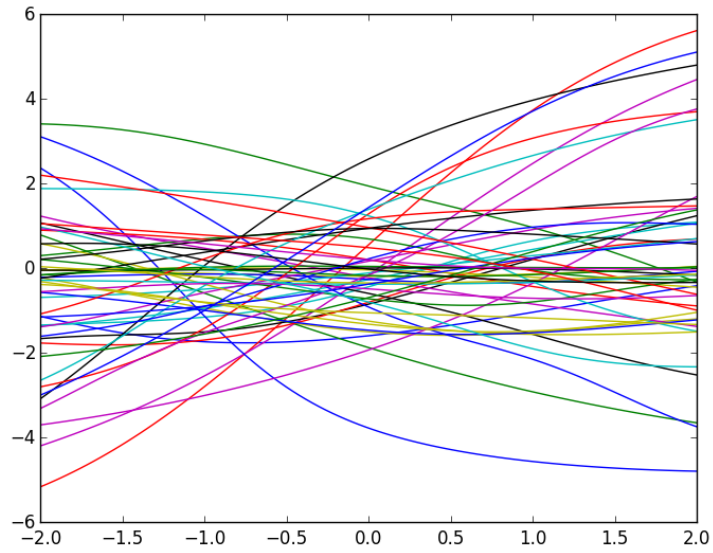


Figure 6: functions computed with normally distributed a_i with a standard deviation of 0.5

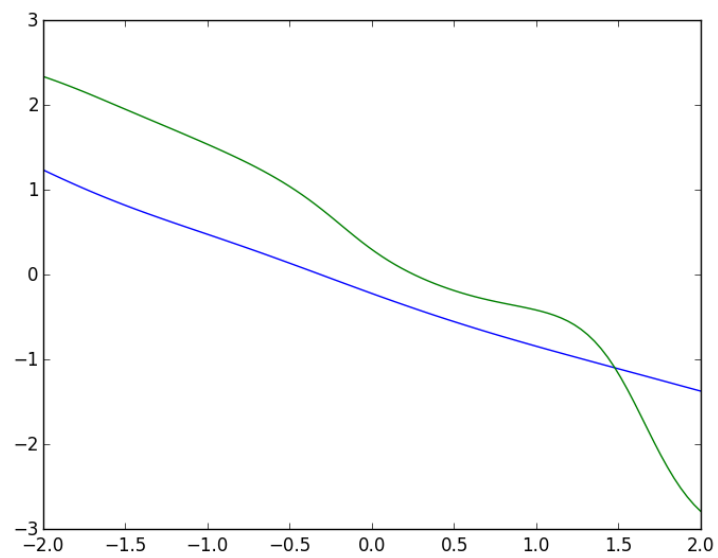


Figure 7: functions with least mean square error from $f(x)=-x$, computed with an std of 2 (green) and 0.5 (blue)