Daily Coding Problem #142

Problem

This problem was asked by Google.

You're given a string consisting solely of (,), and *. * can represent either a (,), or an empty string. Determine whether the parentheses are balanced.

For example, (()* and (*) are balanced.)*(is not balanced.

Solution

The brute force method here would be to keep a count of current open parentheses that gets incremented every time we see (and decremented every time we see). When we encounter a *, we'll recursively try every path (so with `count`, `count - 1`, and `count + 1`) to see if we can get a valid string.

```
def balanced(s, count=0):
    if not s and count == 0:
        return True

    c = count
    for i, char in enumerate(s):
        if char == '(':
            c += 1
        elif char == ')':
            c -= 1
```

```
        elif char == '*':
            return balanced(s[i + 1:], c) or balanced(s[i + 1:], c + 1) or
balanced(s[i + 1:], c - 1)

        if c < 0:
            return False

    return c == 0
```

This takes exponential time though since we're recursively calling `balanced` 3 times on each call.

We can use a faster trick, though. Notice from the brute force solution that * basically means a range from `c - 1` to `c + 1`. We can keep just two variables, `low` and `high`. We'll maintain the following invariants:

- `low` represents the minimum number of unbalanced open parentheses
- `high` represents the maximum number of unbalanced open parentheses

where `low` and `high` will diverge when we encounter an *. We'll keep track of these counts by doing the following:

- If we encounter `(`, then we increment both `low` and `high` - they both contribute to the counts of unbalanced open parentheses.
- If we encounter `)`, then we decrement both `low` and `high` - we have one less unbalanced open parenthesis.
- If we encounter *, then we decrement `low` but increment `high`, since it could mean either a `)` or `(`.

```
def balanced(s):
    low = 0
    high = 0
    for char in s:
        if char == '(':
            low += 1
            high += 1
        elif char == ')':

            low = max(low - 1, 0)
```

```
            high -= 1
        elif char == '*':
            low = max(low - 1, 0)
            high += 1

        if high < 0:
            return False
    return low == 0
```

This will take only O(1) space and O(n) time.