

## Daily Coding Problem #13

### Problem

This problem was asked by Amazon.

Given an integer  $k$  and a string  $s$ , find the length of the longest substring that contains at most  $k$  distinct characters.

For example, given  $s = \text{"abcba"}$  and  $k = 2$ , the longest substring with  $k$  distinct characters is  $\text{"bcb"}$ .

### Solution

The most obvious brute force solution here is to simply try every possible substring of the string and check whether it contains at most  $k$  distinct characters. If it does and it is greater than the current longest valid substring, then update the current one. This takes  $O(n^2 * k)$  time, since we use  $n^2$  to generate each possible substring, and then take  $k$  to check each character.

```
def longest_substring_with_k_distinct_characters(s, k):
    current_longest_substring = ''
    for i in range(len(s)):
        for j in range(i + 1, len(s) + 1):
            substring = s[i:j]
            if len(set(substring)) <= k and len(substring) >
len(current_longest_substring):
                current_longest_substring = substring
    return len(current_longest_substring)
```

We can improve this by instead keeping a running window of our longest substring. We'll keep a dictionary that maps characters to the index of their last occurrence. Then, as we iterate over the string, we'll check the size of the dictionary. If it's larger than  $k$ , then it means our window is too big, so we have to pop the smallest item in the dictionary and recompute the bounds. If, when we add a character to the dictionary and it doesn't go over  $k$ , then we're safe -- the dictionary hasn't been filled up yet or it's a character we've seen before.

```
def longest_substring_with_k_distinct_characters(s, k):
    if k == 0:
        return 0

    # Keep a running window
    bounds = (0, 0)
    h = {}
    max_length = 0
    for i, char in enumerate(s):
        h[char] = i
        if len(h) <= k:
            new_lower_bound = bounds[0] # lower bound remains the same
        else:
            # otherwise, pop last occurring char
            key_to_pop = min(h, key=h.get)
            new_lower_bound = h.pop(key_to_pop) + 1

        bounds = (new_lower_bound, bounds[1] + 1)
        max_length = max(max_length, bounds[1] - bounds[0])

    return max_length
```

This takes  $O(n * k)$  time and  $O(k)$  space.

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