

Title

kdrobust — Kernel Density Estimation with Robust Bias-Corrected Confidence Intervals and Inference Procedures.

Syntax

kdrobust varname [if] [in] [, eval(gridvar) neval(#) h(#) b(#) rho(#)
 kernel(kernelfn) bwselect(bwmethod) bwcheck(#) imsegrid(#) level(#)
 separator(#) genvars plot graph_options(gphopts)]

Description

- kdrobust implements kernel density point estimators with robust bias-corrected
 confidence intervals and inference procedures developed in <u>Calonico</u>, <u>Cattaneo
 and Farrell (2018a)</u>. It also implements other estimation and inference
 procedures available in the literature. See Wand and Jones (1995) and Fan and
 Gijbels (1996) for background references.
- A detailed introduction to this command is given in <u>Calonico</u>, <u>Cattaneo and Farrell</u> (2018).
- Companion command is: kdbwselect for data-driven bandwidth selection.
- Related Stata and R packages useful for empirical analysis are described in the following website:

https://sites.google.com/site/nppackages/

Options

- eval(gridvar) specifies the grid of evaluation points for xvar. By default it
 uses 30 equally spaced points over to support of xvar.
- neval(#) specifies the number of evaluation points to estimate the regression
 functions. Default is 30 evaluation points.
- $\mathbf{h}(hvar)$ specifies the main bandwidth (h) used to construct the point estimator for each evaluation point. If not specified, it is computed by the companion command kdbwselect.
- $\mathbf{b}(bvar)$ specifies the bias bandwidth (b) used to construct the bias-correction estimator for each evaluation point. If not specified, it is computed by the companion command $\underline{kdbwselect}$.
- ${\bf rho}(\#)$ specifies the value of ${\it rho}$, so that the bias bandwidth b equals b=h/rho. Default is ${\bf rho}(1)$ if h is specified but b is not.
- kernel(kernelfn) specifies the kernel function used to construct the kernel
 density estimator(s). Options are: epanechnikov, and uniform. Default is
 kernel(epanechnikov).
- bwselect(bwmethod) bandwidth selection procedure to be used. By default it computes both h and b, unless rho is specified, in which case it only computes h and sets b=h/rho. Options are:
 - mse-dpi second-generation DPI implementation of MSE-optimal bandwidth. Default choice.
 - mse-rot ROT implementation of MSE-optimal bandwidth.
 - imse-dpi second-generation DPI implementation of IMSE-optimal bandwidth.
 - imse-rot ROT implementation of IMSE-optimal bandwidth.
 - ce-dpi second generation DPI implementation of CE-optimal bandwidth.
 - ce-rot ROT implementation of CE-optimal bandwidth.
- Note: MSE = Mean Square Error; IMSE = Integrated Mean Squared Error; CE = Coverage Error; DPI = Direct Plug-in; ROT = Rule-of-Thumb.
 - Default is **bwselect**(*mse-dpi*). For details on implementation see <u>Calonico</u>, <u>Cattaneo and Farrrell (2018b)</u>.

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bwcheck(#) specifies an optional positive integer so that the selected bandwidth
    is enlarged to have at least # effective observations available for each
    evaluation point.
imsegrid(#) number of evaluations points used to compute the IMSE bandwidth
    selector. Default is 30 points.
level(#) specifies confidence level for confidence intervals. Default is
    level(95).
separator(#) draws separator line after every # variables; default is
    separator(5).
plot generates the local polynomial regression plot.
genvars generates new variables storing the following results.
    kdrobust_eval evaluation points.
    kdrobust_h bandwidth h.
    kdrobust_b bandwidth b.
    kdrobust_nh effective sample size.
    kdrobust_gx_us conventional local polynomial estimate.
    kdrobust_se_us conventional standard error for the local polynomial estimator.
    kdrobust_gx_bc bias-corrected local polynomial regression estimate.
    kdrobust_se_rb robust standard error for the local polynomial estimator.
kdrobust_ci_l_rb lower end value of the robust confidence interval.
    kdrobust_ci_r_rb upper end value of the robust confidence interval.
graph_options(gphopts) specifies graphical options to be passed on to the
    underlying graph command.
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Setup

. sysuse auto

Kernel density estimates for length

. kdrobust length

Saved results

kdrobust saves the following in e():

Scalars

original number of observations e(N)

Macros

name of variable e(varname)

e(bwselect) bandwidth selection choice

kernel choice e(kernel)

Matrices

estimation result e(Result)

References

- Calonico, S., M. D. Cattaneo, and M. H. Farrell. 2018a. On the Effect of Bias Estimation on Coverage Accuracy in Nonparametric Inference. Journal of the American Statistical Association, forthcoming.
- Calonico, S., M. D. Cattaneo, and M. H. Farrell. 2018b. nprobust: Nonparametric Kernel-Based Estimation and Robust Bias-Corrected Inference. Working Paper.
- Fan, J., and Gijbels, I. 1996. Local Polynomial Modelling and Its Applications, London: Chapman and Hall.

Wand, M., and Jones, M. 1995. Kernel Smoothing, Florida: Chapman & Hall/CRC.

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