

Title

rdsampsi — Sample size selection based on power calculations for Regression Discontinuity designs using robust bias-corrected local polynomial inference.

Syntax

rdsampsi depvar runvar [if] [in] [, c(#) tau(#) alpha(#) beta(#) nsamples(# # # #)
 samph(# #) all plot graph_range(# #) graph_step(#) graph_options(graph_opt)
 bias(# #) variance(# #) nratio(#) init_cond(#) covs(covars) deriv(#) p(#) q(#)
 h(# #) b(# #) rho(#) fuzzy(fuzzyvar [sharpbw]) kernel(kernelfn)
 bwselect(bwmethod) vce(vcetype [vceopt1 vceopt2]) scalepar(#) scaleregul(#)]

Description

rdsampsi provides sample size selection based on power calculations in Regression
Discontinuity designs using conventional and robust bias-corrected local
polynomial methods. Companion command is: rdpower for power calculations.

A detailed introduction to this command is given in Cattaneo, Titiunik and Gonzalo Vazquez-Bare (2018).

Companion R functions are also available <u>here</u>.

This command employs the Stata (and R) package <u>rdrobust</u> for underlying calculations. See <u>Calonico</u>, <u>Cattaneo and Titiunik</u> (2014) and <u>Calonico</u>, <u>Cattaneo</u>, <u>Farrell and Titiunik</u> (2017) for more details.

Related Stata and R packages useful for inference in RD designs are described in the following website:

https://sites.google.com/site/rdpackages/

Options

- c(#) specifies the RD cutoff for indepvar. Default is c(0).
- tau(#) specifies the treatment effect under the alternative at which the power function is evaluated. The default is half the standard deviation of the outcome for the untreated group.
- alpha(#) specifies the significance level for the power function. Default is alpha(.05).
- beta(#) specifies the desired power. Default is beta(.8).
- nsamples(# # # #) sets the total sample size to the left, sample size to the left
 inside the bandwidth, total sample size to the right and sample size to the
 right of the cutoff inside the bandwidth to calculate the variance when the
 running variable is not specified. When this option is not specified, the
 values are calculated using the running variable.
- samph(# #) sets the bandwidths at each side of the cutoff for power calculation.
 The first number is the bandwidth to the left of the cutoff and the second
 number is the bandwidth to the right. Default values are the bandwidths used
 by rdrobust.
- all displays the power using the conventional variance estimator, in addition to the robust bias corrected one.
- plot plots the power function using the robust bias corrected standard error from rdrobust. If all is specified, the conventional power function is also plotted.
- graph_range(# #) specifies the range of the plot when plot option is used.
 Default range is [-1.5*tau; 1.5*tau].

- graph_step(#) specifies the step increment of the plot when plot option is used.
 Default range is 0.2*range.
- graph_options(#) specifies the graph options (title, axes titles, etc) to be passed to the plot when plot option is used.
- bias(# #) allows the user to set bias to the left and right of the cutoff. If not specified, the biases are estimated using rdrobust.
- variance(# #) allows the user to set variance to the left and right of the cutoff.
 If not specified, the variances are estimated using rdrobust.
- nratio(#) specifies the proportion of treated units in the window. Default is the
 ratio of the standard deviation of the treated to the sum of the standard
 deviations for treated and controls.
- init_cond(#) sets the initial condition for the Newton-Raphson algorithm that
 finds the sample size. Default is the number of observations in the sample
 with non-missing values of the outcome and running variable.
- The following options are passed directly to rdrobust:
- covs(covars) specifies additional covariates to be used for estimation and inference.
- deriv(#) specifies the order of the derivative of the regression functions to be
 estimated. Default is deriv(0). Setting deriv(1) results in estimation of a
 Kink RD design (up to scale).
- p(#) specifies the order of the local polynomial used to construct the point estimator. Default is p(1) (local linear regression).
- q(#) specifies the order of the local polynomial used to construct the bias correction. Default is q(2) (local quadratic regression).
- h(##) specifies the main bandwidth (h) used to construct the RD point estimator. If not specified, bandwidth h is computed by the companion command $\underline{rdbwselect}$. If two bandwidths are specified, the first bandwidth is used for the data below the cutoff and the second bandwidth is used for the data above the cutoff.
- b(# #) specifies the bias bandwidth (b) used to construct the bias-correction
 estimator. If not specified, bandwidth b is computed by the companion command
 rdbwselect. If two bandwidths are specified, the first bandwidth is used for
 the data below the cutoff and the second bandwidth is used for the data above
 the cutoff.
- **rho**(#) specifies the value of *rho*, so that the bias bandwidth b equals b=h/rho. Default is **rho**(1) if h is specified but b is not.
- fuzzy(fuzzyvar [sharpbw]) specifies the treatment status variable used to implement fuzzy RD estimation (or Fuzzy Kink RD if deriv(1) is also specified). Default is Sharp RD design and hence this option is not used. If the option sharpbw is set, the fuzzy RD estimation is performed using a bandwidth selection procedure for the sharp RD model. This option is automatically selected if there is perfect compliance at either side of the threshold.
- kernel(kernelfn) specifies the kernel function used to construct the
 local-polynomial estimator(s). Options are: triangular, epanechnikov, and
 uniform. Default is kernel(triangular).

- **bwselect**(bwmethod) specifies the bandwidth selection procedure to be used. By default it computes both h and b, unless rho is specified, in which case it only computes h and sets b=h/rho. Options are:
 - ${f mserd}$ one common MSE-optimal bandwidth selector for the RD treatment effect estimator.
 - msetwo two different MSE-optimal bandwidth selectors (below and above the cutoff) for the RD treatment effect estimator.
 - msesum one common MSE-optimal bandwidth selector for the sum of regression
 estimates (as opposed to difference thereof).
 - msecomb1 for min(mserd, msesum).
 - msecomb2 for median(msetwo,mserd,msesum), for each side of the cutoff
 separately.
 - cerrd one common CER-optimal bandwidth selector for the RD treatment effect
 estimator.
 - certwo two different CER-optimal bandwidth selectors (below and above the cutoff) for the RD treatment effect estimator.
 - cersum one common CER-optimal bandwidth selector for the sum of regression
 estimates (as opposed to difference thereof).
 - cercomb1 for min(cerrd, cersum).
 - cercomb2 for median(certwo,cerrd,cersum), for each side of the cutoff
 separately.
 - Note: MSE = Mean Square Error; CER = Coverage Error Rate.
 - Default is **bwselect(mserd)**. For details on implementation see <u>Calonico</u>, <u>Cattaneo and Titiunik (2014a)</u>, <u>Calonico</u>, <u>Cattaneo and Farrell (2016a)</u>, and <u>Calonico</u>, <u>Cattaneo</u>, <u>Farrell and Titiunik (2016)</u>, and the companion software articles.
- vce(vcetype [vceopt1 vceopt2]) specifies the procedure used to compute the variance-covariance matrix estimator. Options are:
 - vce(nn [nnmatch]) for heteroskedasticity-robust nearest neighbor variance
 estimator with nnmatch indicating the minimum number of neighbors to be
 used.
 - vce(hc0) for heteroskedasticity-robust plug-in residuals variance estimator
 without weights.
 - vce(hc1) for heteroskedasticity-robust plug-in residuals variance estimator with hc1 weights.
 - vce(hc2) for heteroskedasticity-robust plug-in residuals variance estimator with hc2 weights.
 - vce(hc3) for heteroskedasticity-robust plug-in residuals variance estimator with hc3 weights.
 - vce(nncluster clustervar [nnmatch]) for cluster-robust nearest neighbor
 variance estimation using with clustervar indicating the cluster ID
 variable and nnmatch matches indicating the minimum number of neighbors to
 be used.
 - vce(cluster clustervar) for cluster-robust plug-in residuals variance
 estimation with degrees-of-freedom weights and clustervar indicating the
 cluster ID variable.
 - Default is vce(nn 3).
- scalepar(#) specifies scaling factor for RD parameter of interest. This option is
 useful when the estimator of interest requires a known multiplicative factor
 rescaling (e.g., Sharp Kink RD). Default is scalepar(1) (no rescaling).
- scaleregul(#) specifies scaling factor for the regularization term added to the
 denominator of the bandwidth selectors. Setting scaleregul(0) removes the
 regularization term from the bandwidth selectors. Default is scaleregul(1).

Example: Cattaneo, Frandsen and Titiunik (2015) Incumbency Data

Setup

. use rdpower_senate.dta

Sample size calculation against an alternative hypothesis of tau = 5

. rdsampsi demvoteshfor2 demmv, tau(5)

```
Sample size calculation with covariates
    . rdsampsi demvoteshfor2 demmv, tau(5) covs(population dopen dmidterm)
Sample size calculation with user-specified bandwidths
    . rdsampsi demvoteshfor2 demmv, tau(5) h(16 18) b(18 20)
Sample size calculation with user-specified options
    . rdsampsi demvoteshfor2 demmv, tau(5) beta(.9) all samph(18 19) nratio(.5)
Power function plot with default options
    . rdsampsi demvoteshfor2 demmv, tau(5) plot
Power function plot with user-specified range and step
    . rdsampsi demvoteshfor2 demmv, tau(5) plot graph_range(0 800) graph_step(200)
Power function plot with user-specified options
    . rdsampsi demvoteshfor2 demmv, tau(5) plot graph_range(0 800) graph_step(200)
    graph_options(title(Power function) xtitle(sample size) ytitle(power)
    graphregion(fcolor(white)))
rdsampsi saves the following in r():
Scalars
```

Saved results

```
r(alpha)
                    significance level
                    desired power
r(beta)
r(tau)
                    desired effect
r(samph_1)
                   bandwidth to the left of the cutoff
r(samph_h)
                  bandwidth to the right of the cutoff
                   robust bias corrected variance to the left of the cutoff
r(var_l)
                   robust bias corrected variance to the right of the cutoff
r(var_r)
r(bias_1)
                  bias to the left of the cutoff
                   bias to the right of the cutoff
r(bias_r)
                   sample size in bandwidth to the left of the cutoff for
r(N_h_1)
                     variance calculation
                   sample size in bandwidth to the right of the cutoff for
r(N_h_r)
                     variance calculation
                    sample size to the left of the cutoff for variance
r(N_1)
                      calculation
r(N_r)
                    sample size to the right of the cutoff for variance
                      calculation
r(sampsi_tot)
                    implied total sample size using robust bias corrected s.e.
r(sampsi_h_l)
                    sample size to the left of the cutoff using robust bias
                      corrected s.e.
r(sampsi_h_r)
                    sample size to the right of the cutoff using robust bias
                      corrected s.e.
r(sampsi_h_tot)
                    sample size inside the window using robust bias corrected
                      s.e.
r(var_l_cl)
                    conventional variance to the left of the cutoff
                    conventional variance to the right of the cutoff
r(var_r_cl)
r(sampsi_tot_cl)
                    implied total sample size using conventional s.e.
r(sampsi_h_l_cl)
                    sample size to the left of the cutoff using conventional
                      s.e.
r(sampsi_h_r_cl)
                    sample size to the right of the cutoff using conventional
r(sampsi_h_tot_cl)
                    sample size inside the window using conventional s.e.
r(no_iter)
                    number of iterations until convergence of the
                     Newton-Raphson algorithm
r(init_cond)
                    initial condition of the Newton-Raphson algorithm
```

References

```
Calonico, S., M. D. Cattaneo, M. H. Farrell, and R. Titiunik. 2017. rdrobust:
   Software for Regression Discontinuity Designs.
    Stata Journal 17(2): 372-404.
```

Calonico, S., M. D. Cattaneo, and R. Titiunik. 2014. Robust Data-Driven Inference in the Regression-Discontinuity Design. Stata Journal 14(4): 909-946.

- Cattaneo, M. D., Frandsen, B., and R. Titiunik. 2015. <u>Randomization Inference in the Regression Discontinuity Design: An Application to Party Advantages in the U.S. Senate</u>.

 Journal of Causal Inference 3(1): 1-24.
- Cattaneo, M. D., R. Titiunik, and G. Vazquez-Bare. 2018. <u>Power Calculations for Regression Discontinuity Designs</u>. Forthcoming, *Stata Journal*.

<u>Authors</u>

- Matias D. Cattaneo, University of Michigan, Ann Arbor, MI. cattaneo@umich.edu.
- Rocio Titiunik, University of Michigan, Ann Arbor, MI. titiunik@umich.edu.
- Gonzalo Vazquez-Bare, University of California, Santa Barbara. gvazquez@econ.ucsb.edu.