

MAX-PLANCK-INSTITUT  
FÜR ASTROPHYSIK



# New standard ingredients in cosmological analyses?

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# Context

- **Inflation:** reconstruct the properties of the initial conditions, and look for gravitational waves  $f_{\text{NL}}$ ,  $n_s$ ,  $r$
- **Dark Energy and Gravity:** the growth of structure depends sensitively on the expansion history of the Universe, and the nature of gravity  $w_0$ ,  $w_a$ ,  $f \propto D'/D$   
Growth equation:  $D'' + aH D' = 4\pi G \bar{\rho} D$
- **Dark Matter/neutrinos:** how “cold” is cold dark matter ? What is the sum of neutrino masses ?  $\sum m_\nu$

# Context

- Inflation: reconstruct the properties of the initial conditions, and look for gravitational waves  $f_{\text{NL}}$ ,  $n_s$ ,  $r$
- Dark Matter: How should we do inference in this space? What to vary, what to keep fixed? f $w_0, w_a, f \propto D'/D$   
gravity
- Growth equation:  $D'' + aH D' = 4\pi G \bar{\rho} D$
- Dark Matter/neutrinos: how “cold” is cold dark matter ? What is the sum of neutrino masses ?  $\sum m_\nu$

# The standard model of cosmology

- (Euclidean)  $\nu\Lambda\text{CDM}$

$$\omega_c, \omega_b, M_\nu, h, A_s, n_s, (\Omega_\Lambda)$$

- not counting astrophysics parameters

- **Assumptions/issues:**

- Assume *simple inflation* prior (Euclidean; scale-invariant  $P_R(k)$ ; purely adiabatic perturbations)
- We don't really know what we are parametrizing with  $\omega_c$
- Assume cosmological constant
- Assume specific neutrino mass ordering

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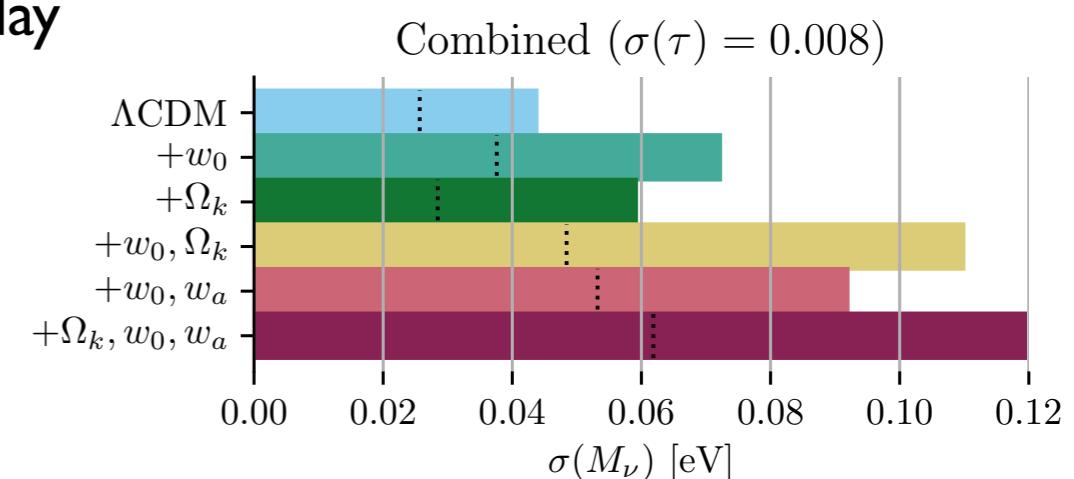
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# Neutrino masses

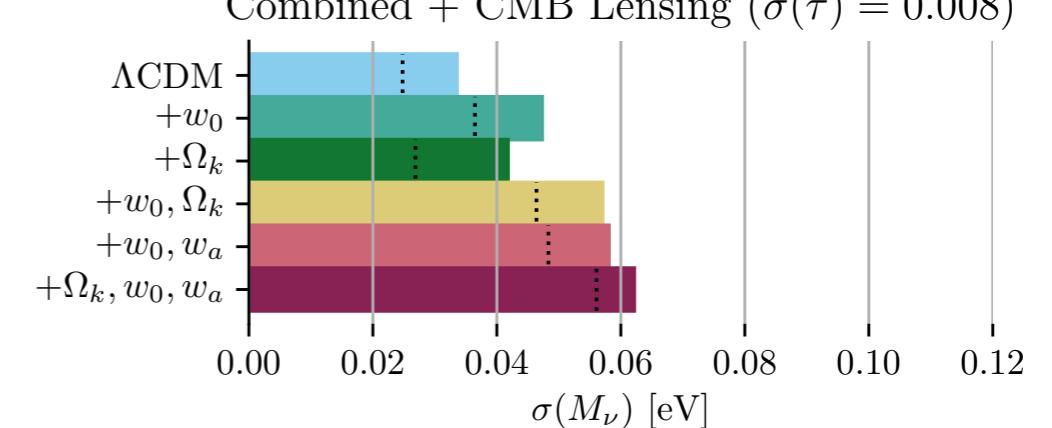
Cf. discussion on Monday

- Part of the standard model — but current  $M_\nu$  constraints sensitive to model extensions
- Model-independent constraints possible using scale-dependent suppression, but these are much weaker and will remain so for some time

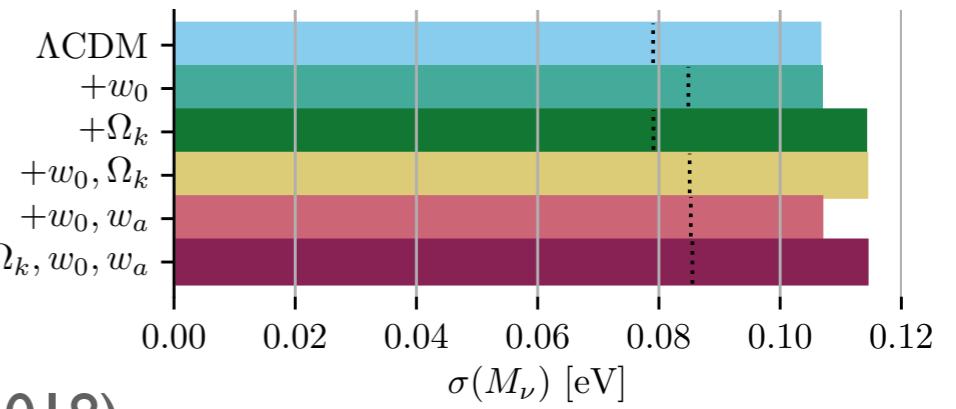
Forecast



Combined ( $\sigma(\tau) = 0.008$ )



Combined + CMB Lensing ( $\sigma(\tau) = 0.008$ )



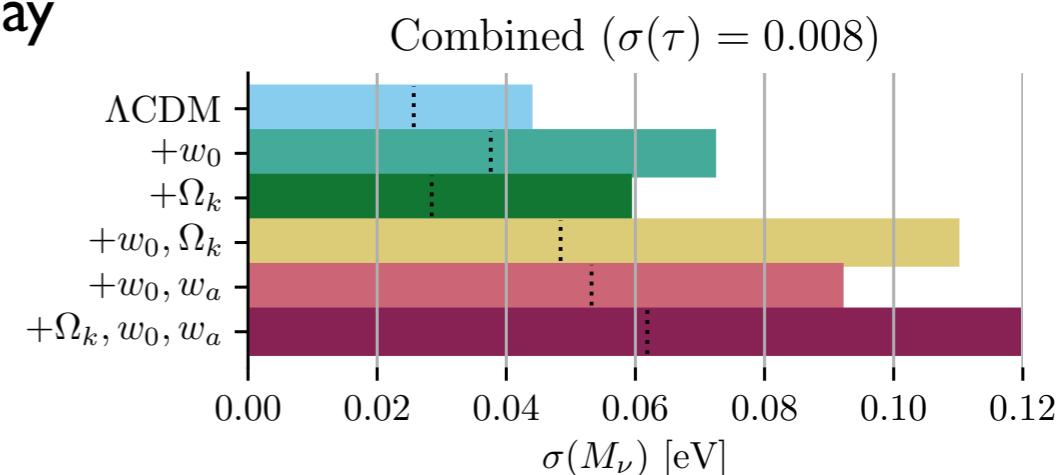
Boyle & FS (2020)  
Boyle (2018)  
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# Neutrino masses

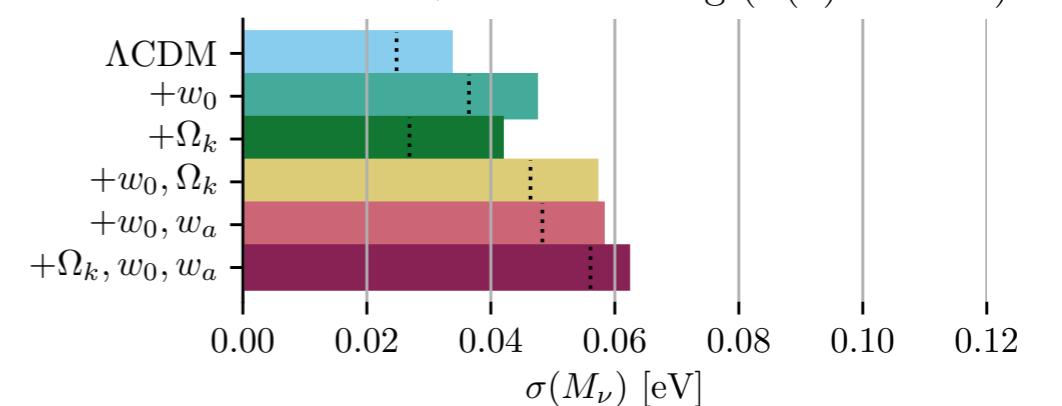
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- Part of the standard model — but current  $M_\nu$  constraints sensitive to model extensions
- Model-independent constraints possible using scale-dependent suppression, but these are much weaker and will remain so for some time
- Sources of constraint depend strongly on details of dataset combination — lots of possibilities for confusion; clear and careful phrasing essential
  - Also prior dependence...

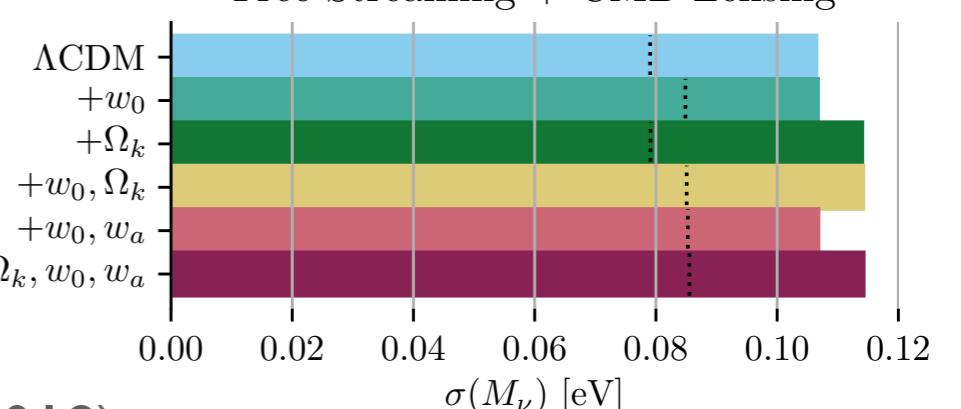
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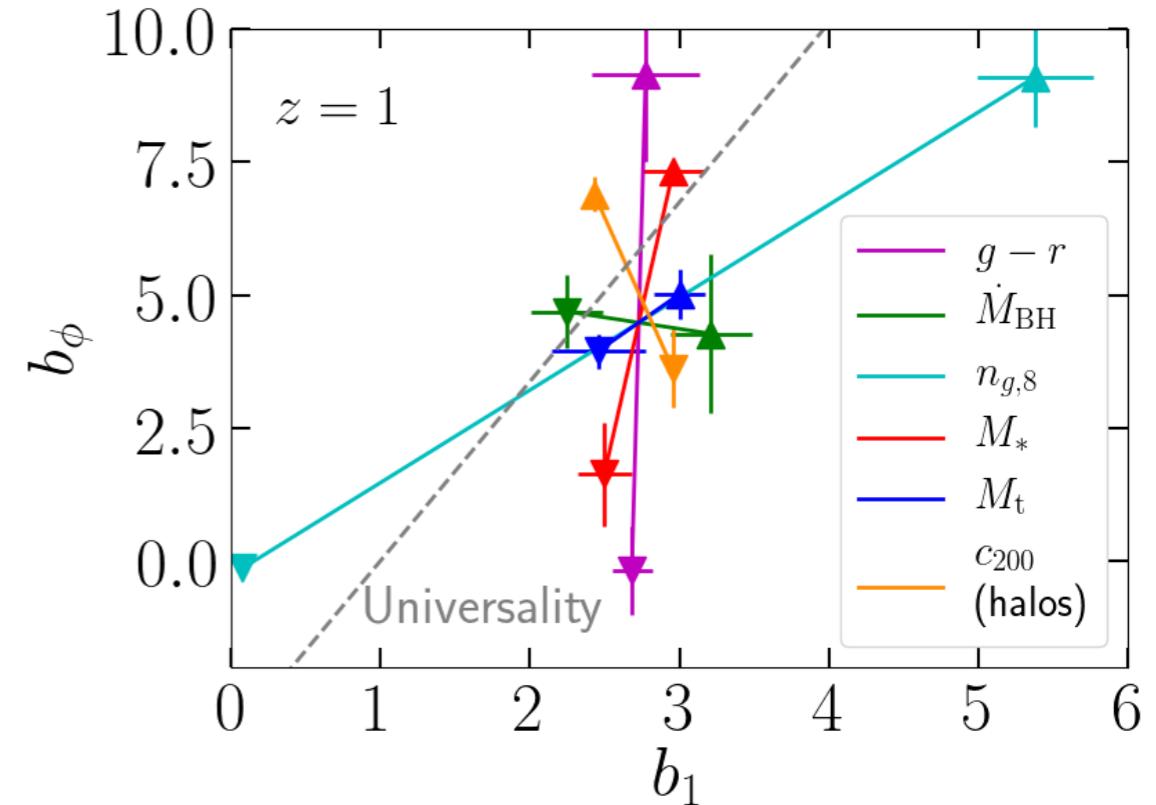
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# Inflation: CMB

- We need to assume some form of prior in model space
- Luckily, inflation scenarios *largely* divide into two classes (*Braglia*):
  - Single dominant d.o.f.:  $r$  potentially detectable;  $f_{NL}^{\text{loc}}=0$
  - $> 1$  light d.o.f. which mix:  $r \sim 0$ ;  $f_{NL}^{\text{loc}}$  detectable
- Fine to ignore  $f_{NL}$  in  $n_s$ - $r$  constraints
- CMB: template correlations in PNG searches need to be considered
  - cf.  $f_{NL}^{\text{ortho}}$  in EFT of single-field inflation
  - quasi-single-field / collider signatures

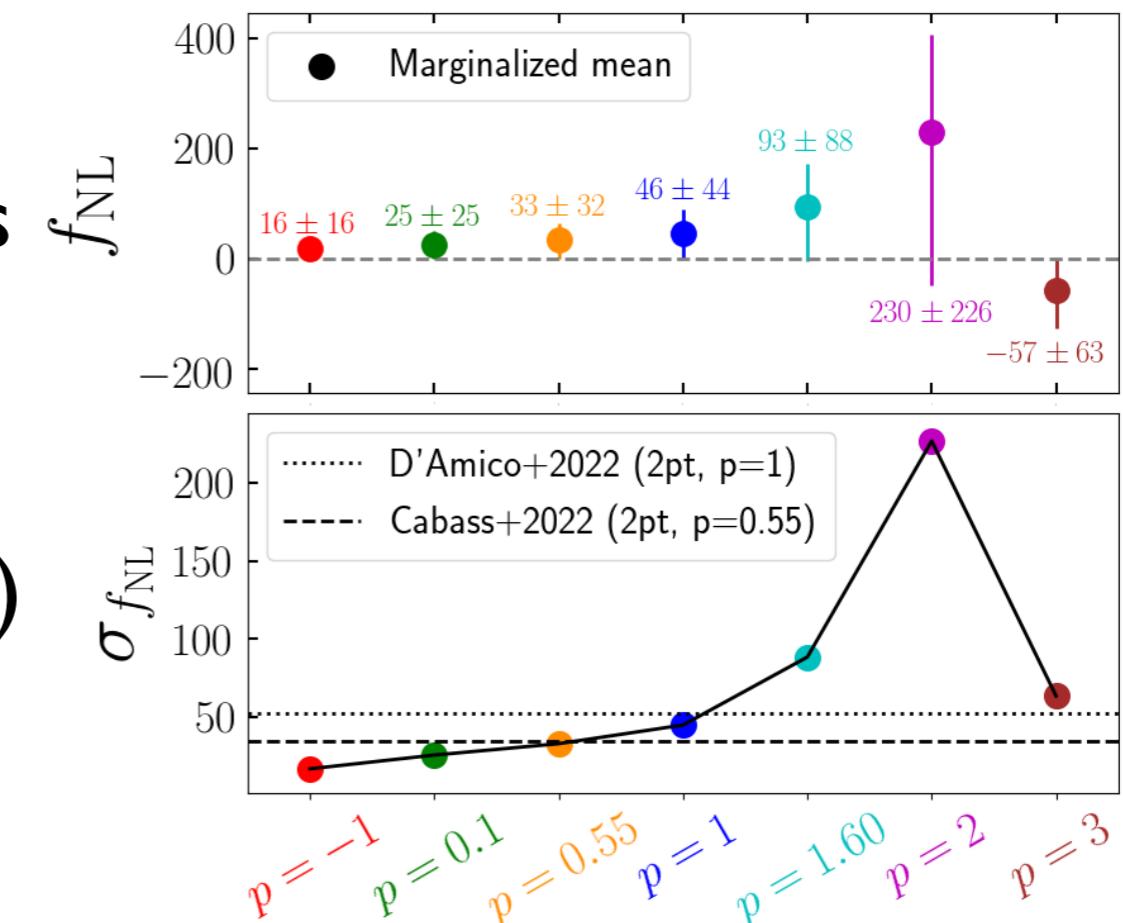
# Inflation: LSS

- Current  $f_{\text{NL}}^{\text{loc}}$  constraints from LSS (scale-dependent bias) fix  $\Lambda\text{CDM}$  parameters and  $b_\phi$ , where the data constrain only  $b_\phi * f_{\text{NL}}^{\text{loc}}$ 
  - This really is no longer ok...
- Of these,  $b_\phi$  is the more difficult problem; we need informative priors to obtain constraints on  $f_{\text{NL}}^{\text{loc}}$ 
  - Issue also in kSZ, measuring momentum of ionized gas (biased)
  - More work needed!



Barreira, Krause (2023)

Barreira (2022), ...

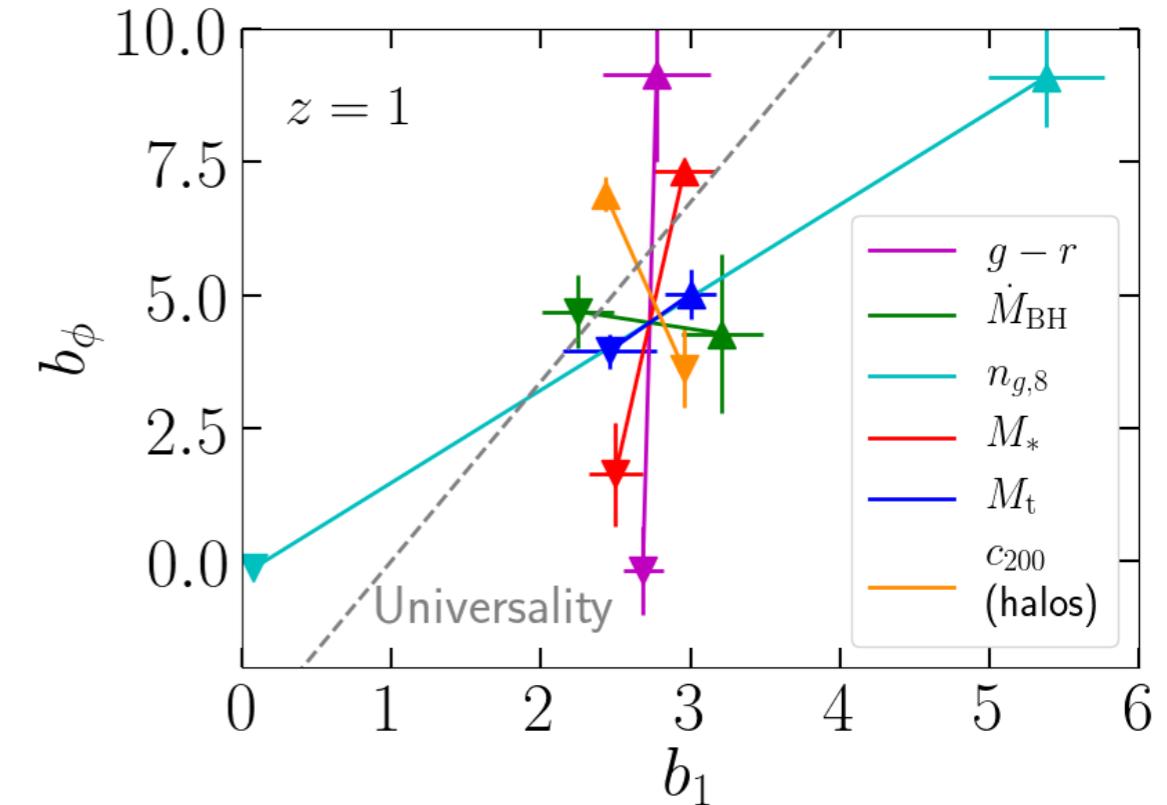


# Inflation: LSS

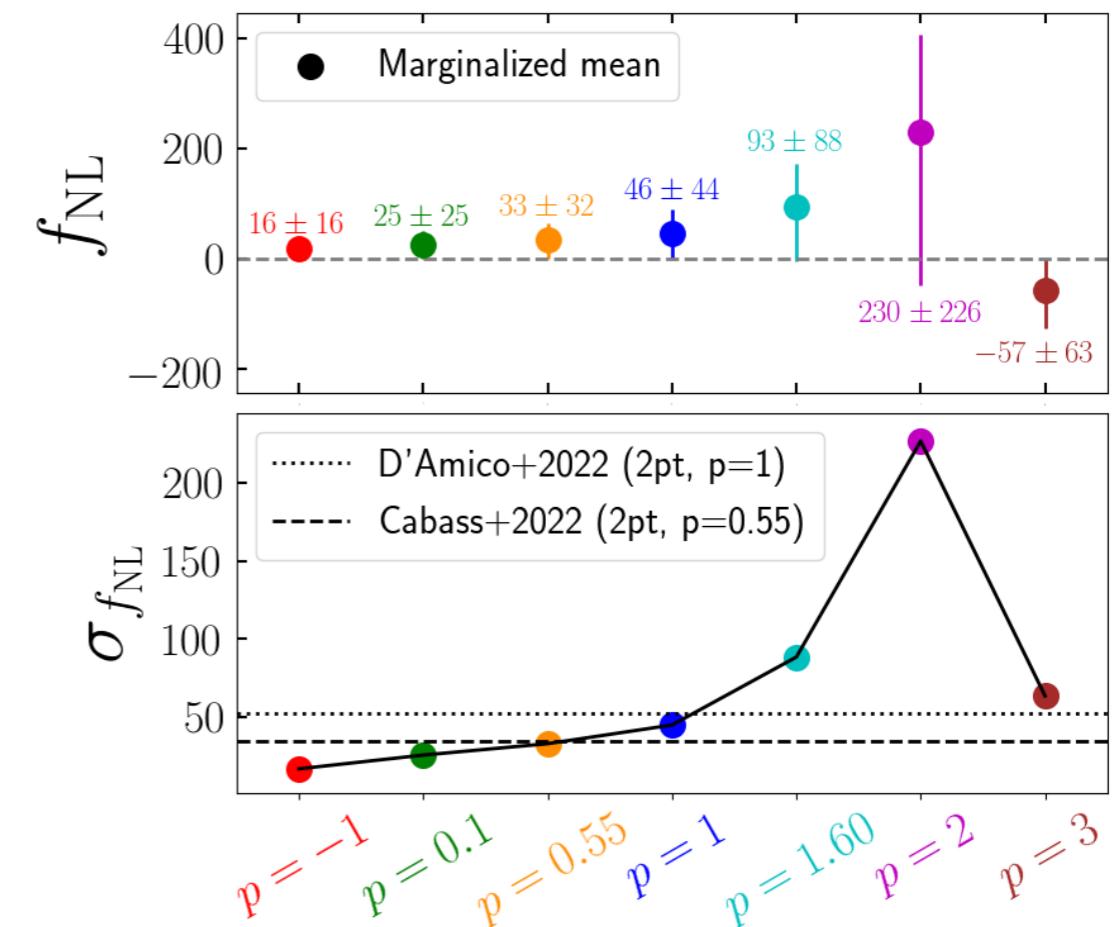
- Moreover,  $f_{NL}^{loc}$  signature exactly degenerate with  $g_{NL}^{loc}$  and compensated isocurvature modes

Desjacques, Ferraro, LoVerde, Smith, ...  
 Barreira, Cabass, FS, ...

- Both expected in general for multifield inflation



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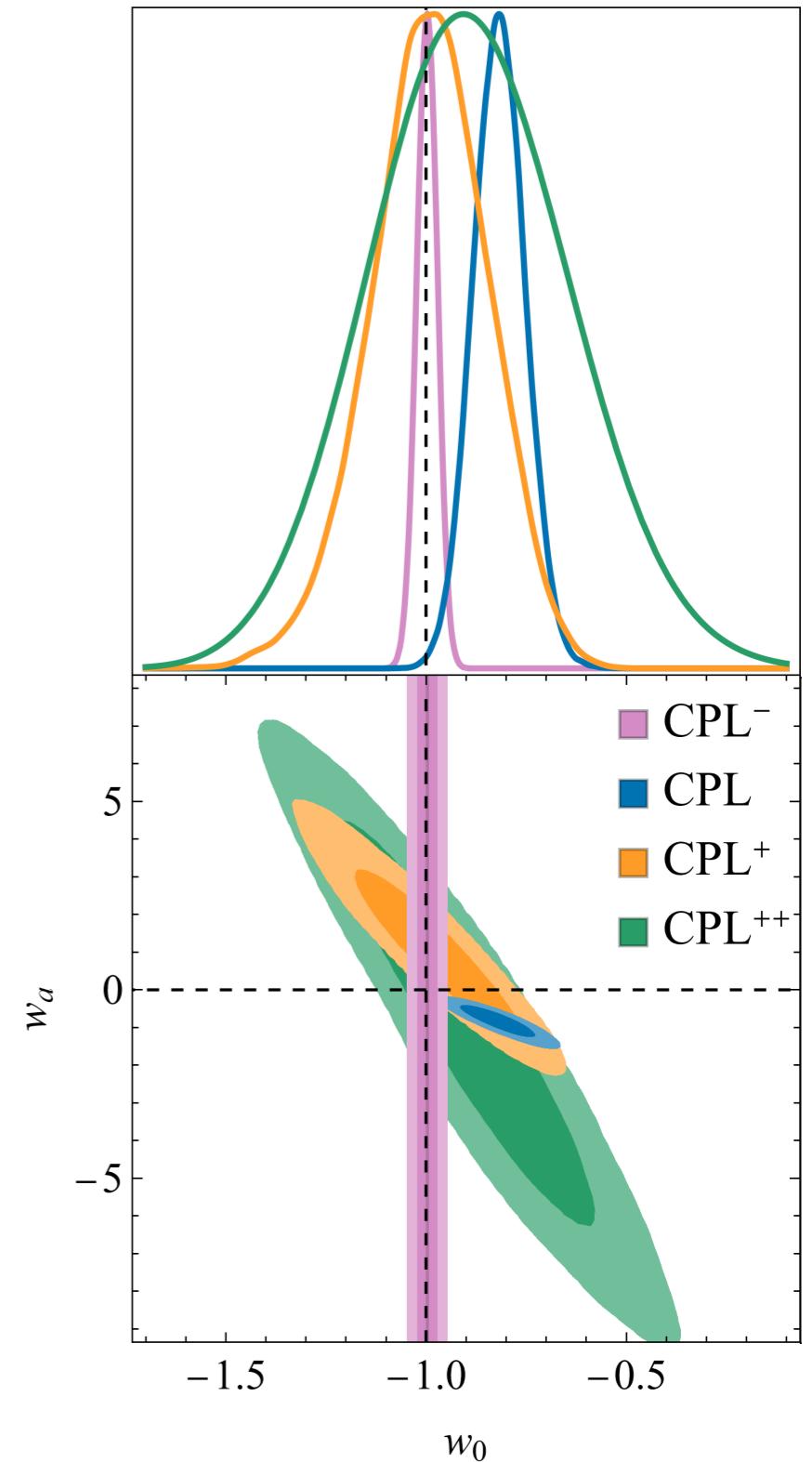


# Dark Energy

- How to parametrize dark energy beyond  $\Lambda$ ?
  - Consider concrete models
  - Parametrize equation of state
- Both have issues:
  - Simple quintessence models possibly too restrictive —> *Baker*; see below
  - Parametrization like  $w_0, w_a$  can only be trusted over limited redshift interval

# On $w_0$ - $w_a$

- Parametrization like  $w_0, w_a$  can only be trusted over limited redshift interval
- Best constraints on DE from  $d_A(z)$ 
  - $w_0 \sim d_A'' ; w_a \sim d_A''' (!)$
  - If  $w_a \sim 1$ , expect  $w_{aa} \sim 1$  as well, but almost all analyses fix it to 0...



$$w_{\text{DE}}(a) = w_0 + w_a(1-a) + w_b(1-a)^2 + w_c(1-a)^3$$

# Dark Energy can cross phantom divide

- If observations indicate  $w$  goes below  $-1$ , have we ruled out “ordinary” dark energy?

- Canonical scalar field: yes

$$p(\phi) = X + V(\phi) \quad \Rightarrow \quad w = \frac{\dot{\phi}^2/2 - V(\phi)}{\dot{\phi}/2 + V(\phi)}$$

$$X \equiv -\frac{1}{2}(\partial_\mu \phi)^2$$

- Not true in general: could have equation of state that varies around  $w=-1$

- *Monodromic k-essence:*  $p(\phi, X) = \tilde{V}(\phi) [-X/M^4 + (X/M^4)^2]$

$$\tilde{V}(\phi) = C \left( \frac{\phi}{\phi_0} \right)^{-\alpha} [1 - A \sin(\nu H_0 \phi + \delta)].$$

# Dark Energy can cross phantom divide

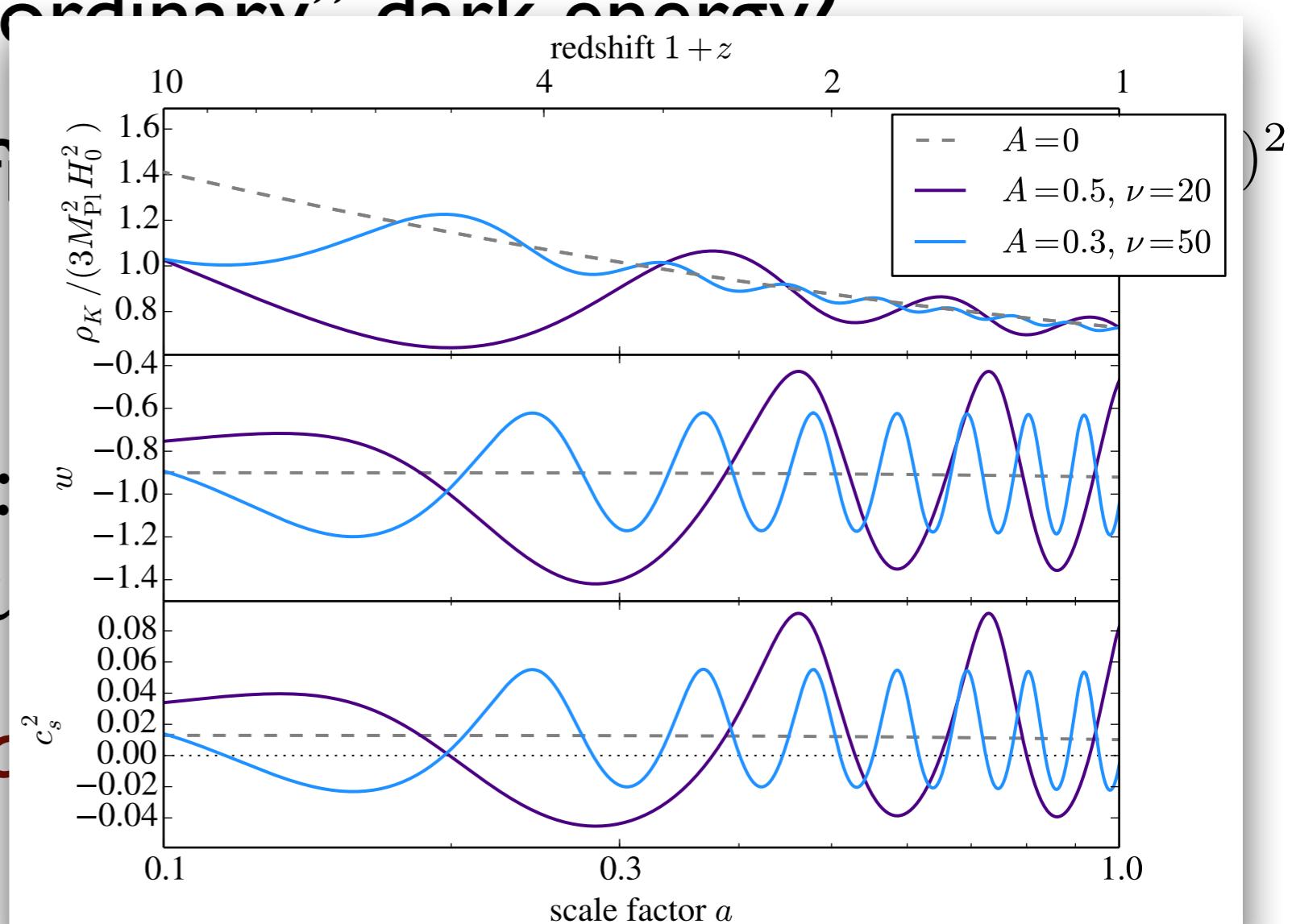
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- *Monodromic k-essence*



# Dark Energy can cross phantom divide

- Fine at the background level, but DE perturbations suffer tachyonic instabilities if  $c_s^2 < 0$
- k-essence case naturally has  $c_s^2 \ll 1$ ; in fact,  $c_s^2 \sim (1+w)$  in  $1+w \rightarrow 0$  limit, leading to tachyonic instabilities as  $1+w < 0$
- These can be dealt with consistently if
  - Higher-derivative contributions are present:  
$$\ddot{\delta\phi} \sim -c_s^2 k^2 \delta\phi + \frac{k^4}{M^2} \delta\phi + \dots$$
e.g., from  
$$\Delta\mathcal{L}_{\text{DE,h.deriv.}} = -\frac{\bar{M}^2}{2} [\square\phi + 3H(\phi)]^2$$
  - $c_s^2$  stays infinitesimally below 0
- Lowers cutoff of the theory, but not ruled out.



# Dark Energy can cross phantom divide

- An example viable model (due to Marco Celoria):

$$p(\phi, X) = \frac{\bar{M}^4}{2}(2X - 1)^2 - F(\phi) + G(\phi)(2X + 1)$$

$$F(\phi) = V_0 \left[ 1 - \tilde{A} \sin(\tilde{\nu} H_0 \phi) \right]$$

$$G(\phi) = V_0 \tilde{A} \tilde{\nu} H_0 \cos(\tilde{\nu} H_0 \phi).$$

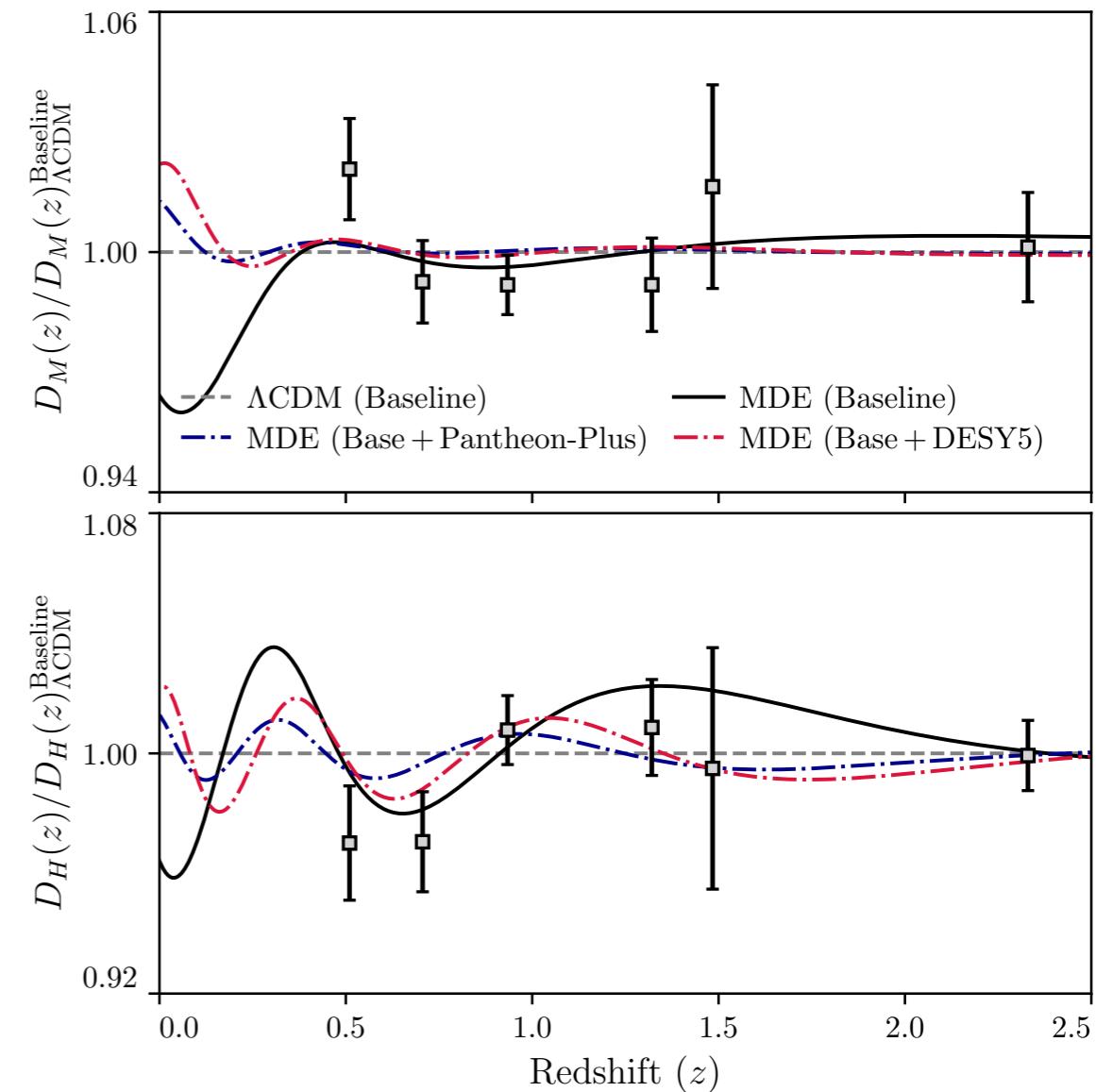
- Oscillations with amplitude  $\Delta w \sim 0.1$  around  $w = -1$  easily possible while satisfying constraints on instabilities and having cutoff > eV scale.



# Monodromic k-essence and DESI

Goldstein, Celoria, FS (2025)

- 3 free parameters (FS 2017 model) in addition to  $\Omega_{de}$ , potential tilt  $a \Leftrightarrow$  mean  $w$ :
  - amplitude, frequency, phase of oscillations
- Exclude all observables sensitive to perturbations here

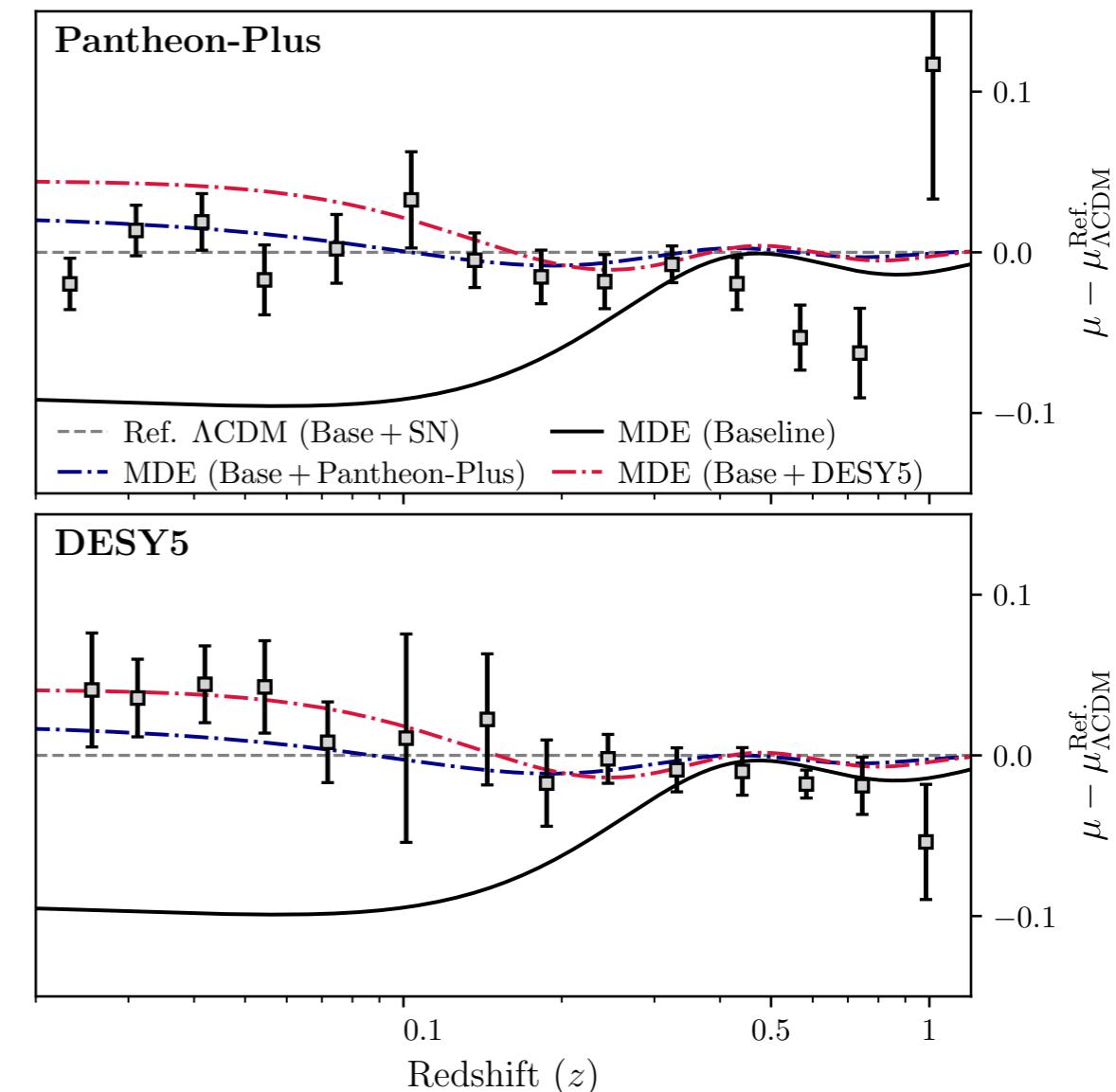




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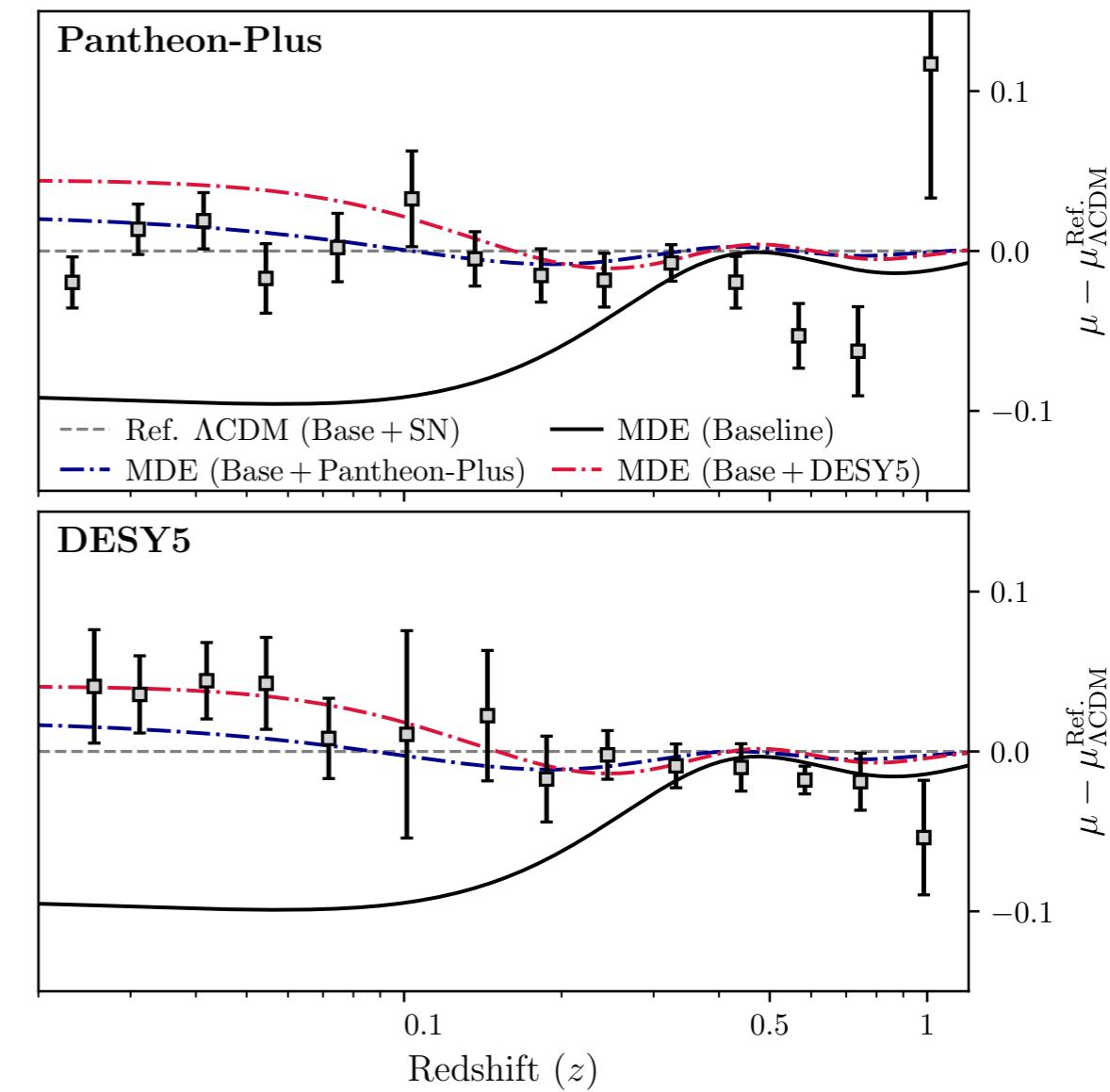




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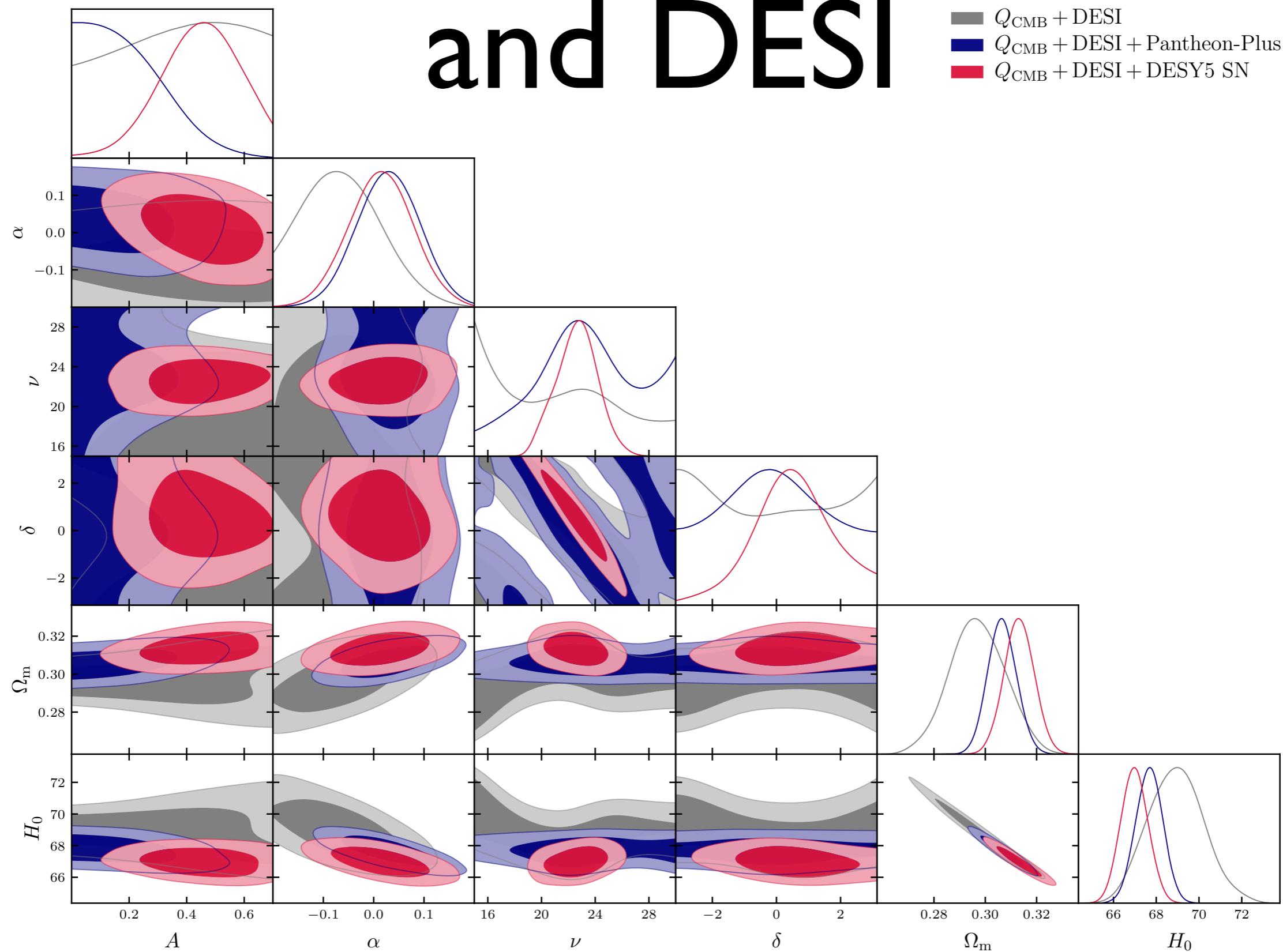
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  - amplitude, frequency, phase of oscillations
- Exclude all observables sensitive to perturbations here
- Similar fit quality to DESI BAO + SN as  $w_0, w_a$
- Mean  $w$  consistent with -1 (motivated by theory as well); then, only 1 more free parameter than  $w_0, w_a$ !



# Monodromic k-essence

## and DESI

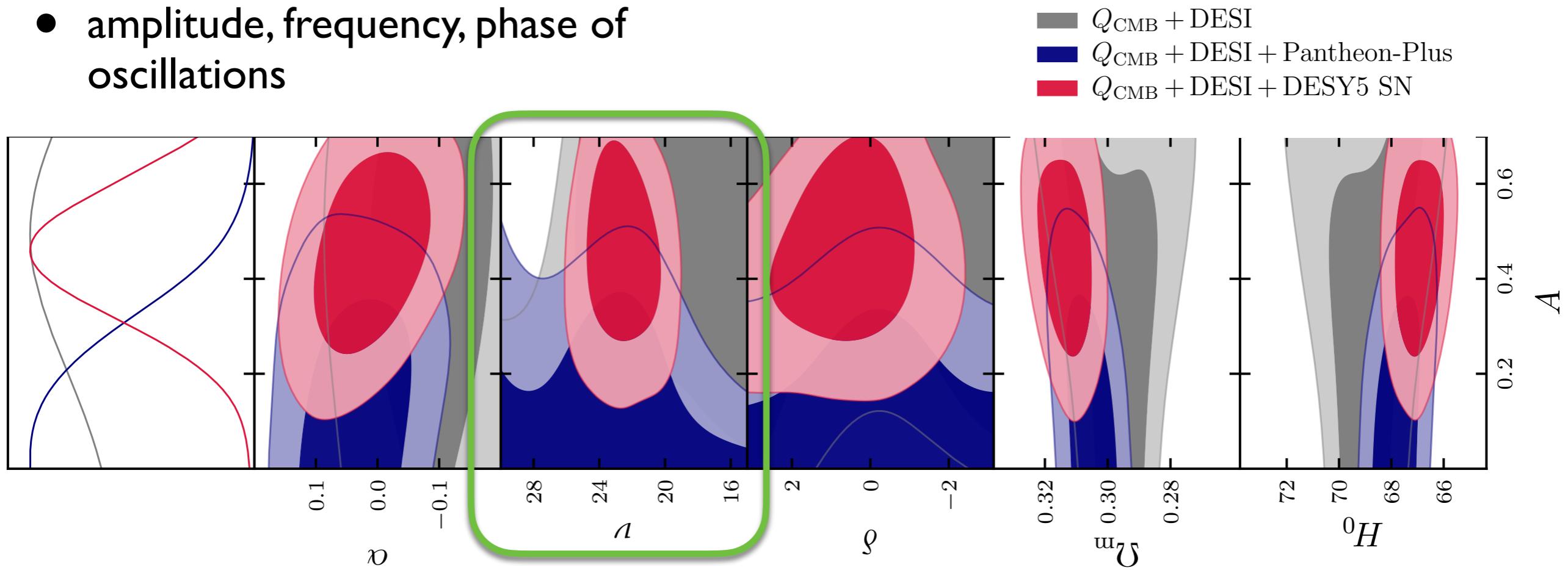




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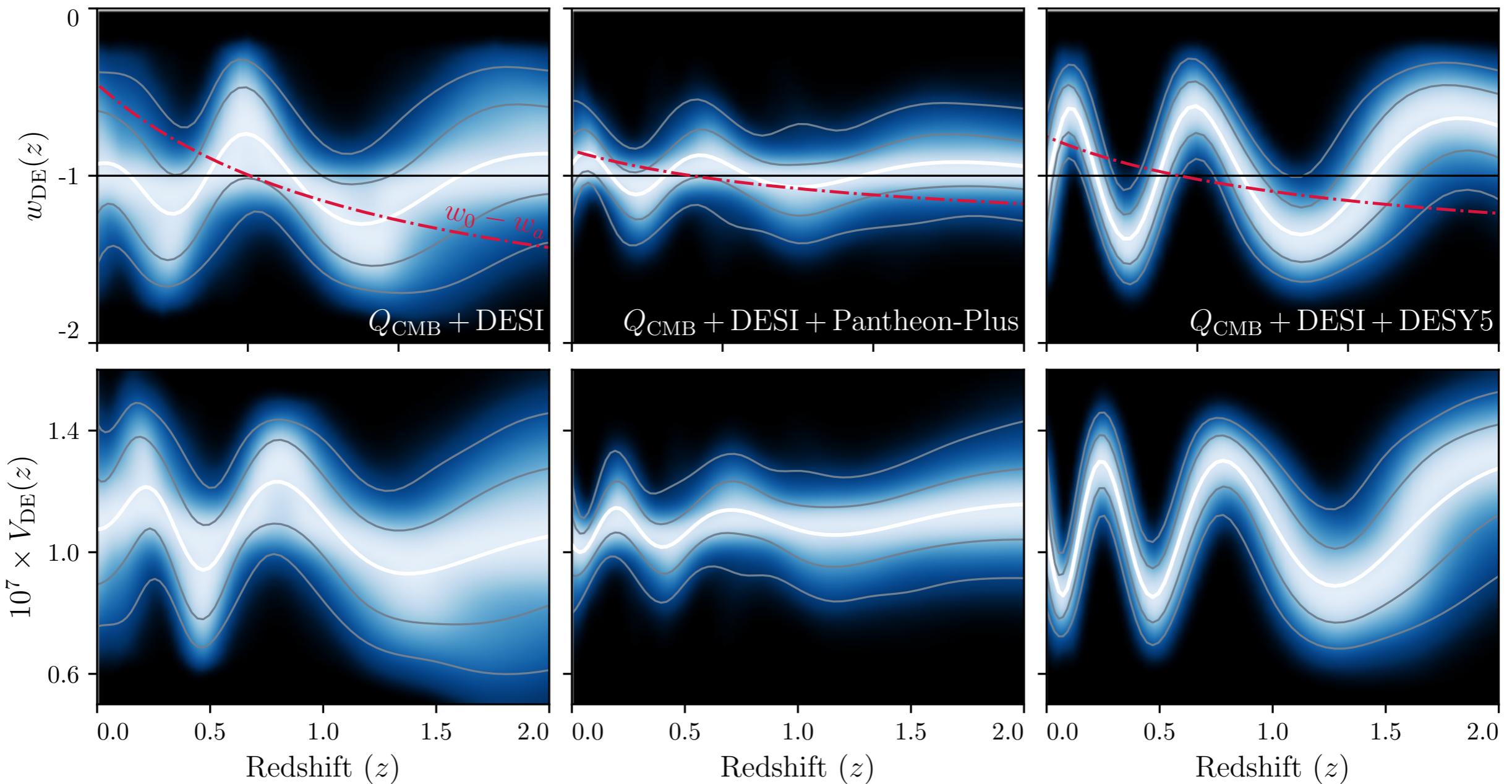




# Monodromic k-essence and DESI

Goldstein, Celoria, FS (2025)

- Reconstruction of  $w(z)$  and k-essence “potential”



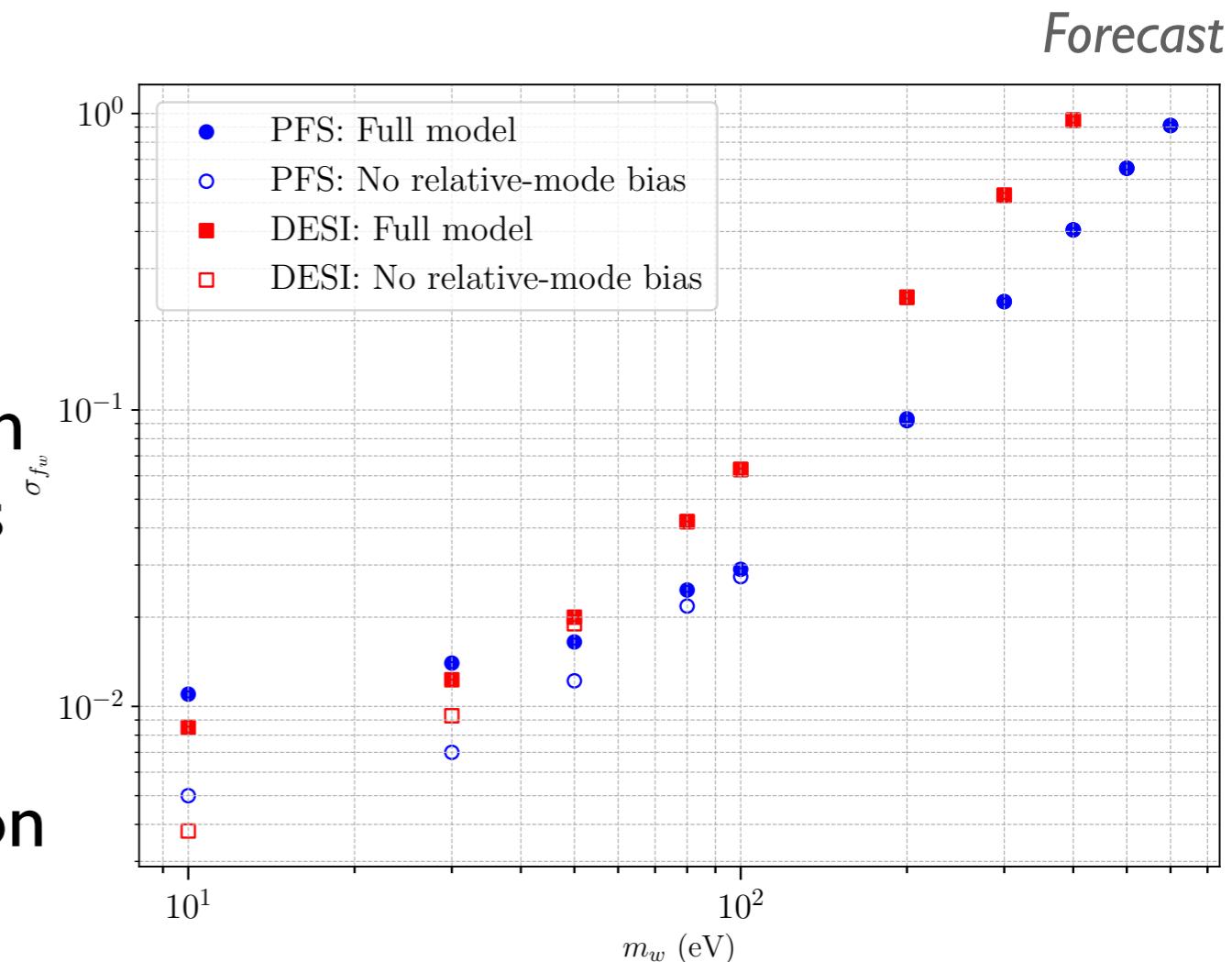
# Dark matter and relics

- Light relic searches are well motivated (*Gerbino, Lattanzi*) — these could also have finite mass
- Smooth transition to warm DM, but *allow for CDM component*
- Current constraints on non-CDM (WDM, FDM, SIDM) usually assume 100% non-CDM
  - PBH searches on the other hand constrain  $f_{\text{PBH}}\dots$
- Should we allow for CDM component when constraining the temperature and/or interactions of DM? → **Mixed DM**



# Mixed dark matter

- Interesting effects in LSS — scale-dependent feature at some  $k_{fs}$  with amplitude controlled by  $f_{\text{relic}}/\text{WDM}$ 
  - Discovery window depending on  $z$  and number density of surveys
- **Relative density & velocity modes** from early universe — need to be taken into account in bias expansion but also have unique signatures
- EFTofLSS and galaxy bias expansion become nontrivial — two complementary approaches pursued



# Summary...

$\omega_c$ ,  $\omega_b$ ,  $M_\nu$ ,  $h$ ,  $A_s$ ,  $n_s$ ,  $(\Omega_\Lambda)$

- ... of my two cents on current constraint analyses:
  - Need to assume some *inflation* prior
  - Neutrino mass constraints are complicated, dataset- and prior-dependent—do not lend themselves to catchy summaries
  - Issues with  $w_0-w_a$ ; use pivot redshift at least, and consider models with more interesting phenomenology
  - Opening up dark matter constraints beyond the 100% single component